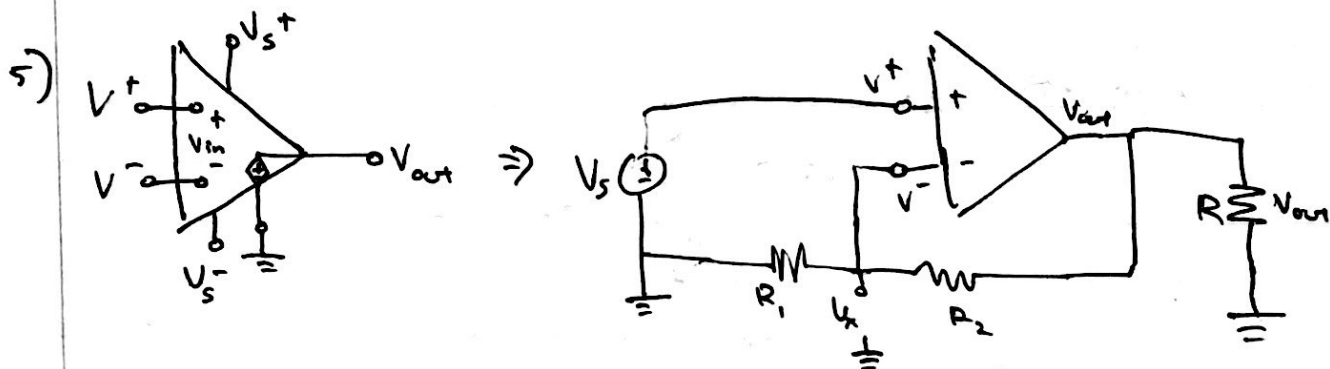


I'M DONE W LATEX



$$\begin{aligned}
 a) \quad V_{out} &= A(V^+ - V^-) \\
 &\quad \hookrightarrow V^+ = V_s \quad V^- = V_x \\
 &= A(V_s - V_x) \\
 &= A\left(V_s - \frac{R_1}{R_1 + R_2} V_{out}\right) \quad V_x = \frac{R_1}{R_1 + R_2} V_{out} \\
 &= AV_s - A\left(\frac{R_1}{R_1 + R_2}\right) V_{out}
 \end{aligned}$$

$I^+ = I^- = 0$

Rearranging,

$$V_{out} \left(1 + A\left(\frac{R_1}{R_1 + R_2}\right)\right) = AV_s$$

$$\therefore V_{out} = \frac{A}{1 + A\left(\frac{R_1}{R_1 + R_2}\right)} V_s$$

$$V_x = \frac{A\left(\frac{R_1}{R_1 + R_2}\right)}{1 + A\left(\frac{R_1}{R_1 + R_2}\right)} V_s$$

* None of these values depend on R .

* This implies that the magnitude of V_x is smaller than that of V_s .

b) As $A \rightarrow \infty$, the ratios $\rightarrow 1$, so

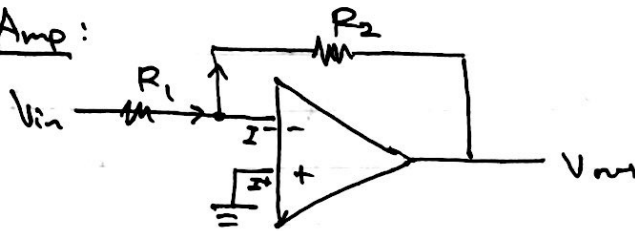
$$\text{both } V_{out} \text{ and } V_x = V_s$$

Yes, we get the same answers $V_+ = V_- = V_s$ when NFB.

$$V_{out} = \left(\frac{R_1 + R_2}{R_1}\right) V_x$$

$$V_{out} = \left(\frac{R_1 + R_2}{R_1}\right) V_s$$

6) a) Inverting Amp:

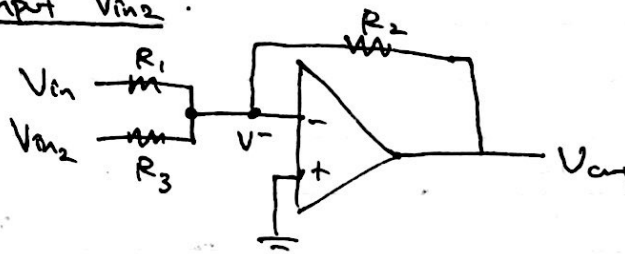


$I^- = I^+ = 0$, so nodal analysis @ V^- node gives
 $V^+ = V^- = 0$

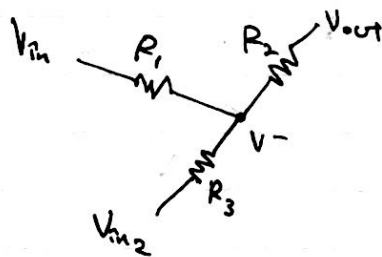
$$\frac{V_{in} - 0}{R_1} = \frac{0 - V_{out}}{R_2}$$

$$\therefore \text{volt. gain} \left| \frac{V_{out}}{V_{in}} = - \frac{R_2}{R_1} \right|$$

b) Second Input V_{in2} :



Nodal analysis @ V^- node:



$$\frac{V^- - V_{in}}{R_1} + \frac{V^- - V_{in2}}{R_3} + \frac{V^- - V_{out}}{R_2} = 0$$

Since $V^- = V^+ = 0$,

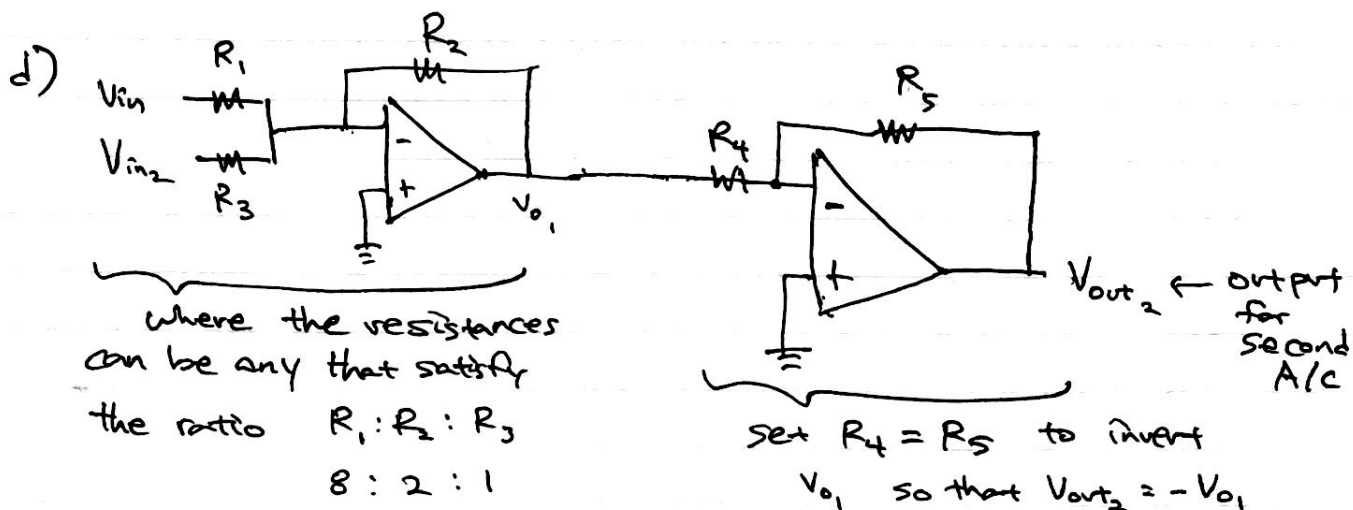
$$\frac{V_{out}}{R_2} = - \frac{V_{in}}{R_1} - \frac{V_{in2}}{R_3}$$

$$\left| V_{out} = - \left(\frac{R_2}{R_1} V_{in} + \frac{R_2}{R_3} V_{in2} \right) \right|$$

c) To get $V_{out} = - \left(\frac{1}{4} V_{s1} + 2 V_{s2} \right)$, we set

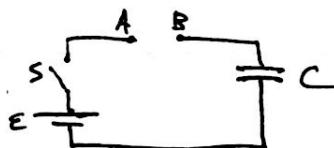
$$\begin{aligned} R_1 &= 8 \text{ k}\Omega \\ R_2 &= 2 \text{ k}\Omega \\ R_3 &= 1 \text{ k}\Omega \end{aligned}$$

$$\text{so that } \frac{R_2}{R_1} = \frac{2 \text{ k}\Omega}{8 \text{ k}\Omega} = \frac{1}{4}, \quad \frac{R_2}{R_3} = \frac{2}{1} = 2$$



7) THINK ABOUT IT!

Question: Consider the following circuit qualitatively:



How will you charge the capacitor?

Answer: Case 1

Attach a wire between A & B, then close S. If we assume resistancelessness of the wires, charge flows into the plates super quick that the ΔV_C across the capacitor "instantly" becomes equal to E across the battery.

$$\text{Thus } Q = C \Delta V_C = \boxed{CE}$$

Case 2

Insert a resistor between A & B, then close S. We know that at any time, $E = \Delta V_R + \Delta V_C$.
 @ $t = 0$, $\Delta V_C = 0$, so the current, initially, can just be described as $I_2 = \Delta V_R / R = E / R$.
 As time goes on, ΔV_C increases while ΔV_R decreases, meaning I decreases, and as $I \rightarrow 0$, $\Delta V_R \rightarrow 0$, $\Delta V_C \rightarrow E$.
 Circuit is now static.