

Constraining the Hemispherical Structure in the Hidden Layer At the Top of the Earth's Inner Core

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Abstract

Since its discovery in 1936, the Earth's inner core has been well documented by both body wave and normal mode studies. However, one area where properties are not yet well measured is the top of the inner core. The upper region of the inner core is of particular interest as it is thought that as the outer core freezes onto the inner core the variable environment at this boundary is encoded in the properties of the frozen material.

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1 Introduction

The inner core was first discovered by Inge Lehmann in 1936, who used the existence of P wave arrivals within the P wave shadow zone to infer a solid-liquid boundary lying within the core mantle boundary (Lehmann (1936)). Over the following 80 years large progress has been made on measuring the properties of the inner core, but there is much still to learn.

Of particular interest is the velocity and attenuation structure, which can be used to infer the chemical and physical properties of the inner core’s constituent material. The following gives a summary of these properties, and is quoted directly from Deuss (2014):

- The top 60-80 km of the inner core is isotropic, and the deeper parts have 3-4% anisotropy. The anisotropy exists in both velocity and attenuation; waves traveling in the polar direction are faster and more attenuated than waves traveling equatorially.
- There may be an innermost inner core with different anisotropy, though evidence is not compelling.¹
- The inner core displays a hemispherical variation: The western hemisphere is more strongly anisotropic, has a lower isotropic compressional velocity, and is less attenuating than the eastern hemisphere. There are sharp boundaries between the two hemispheres.
- Inner core superrotation is less than 0.5° /yr and may even be as small as $0.1 - 1^\circ$ /Myr.

The upper inner core is of particular interest, as material from the outer core is currently freezing onto it at a rate of around 1mm/year (Labrosse et al. (2001)). Modelling performed by Deguen & Cardin (2009) shows that the velocity structure of the upper inner core should reflect recent processes in the lower upper core. Thus measuring the structure of the upper inner core could in turn give insights into areas such as how the outer core generates the Earth’s magnetic field.

So far only large scale velocity structures have been measured, with the most recent velocity models BEING VERY COARSE GRAINED. In addition the extent to which the methodology used here and elsewhere is not well understood. In this paper we tackle both of these problems.

We do so by taking individual earthquakes that travel to multiple seismic stations and identifying the arrival of distant seismic phases in seismograms. We constrain our analysis to the uppermost inner core as far as is possible, and area not yet investigated in published literature.

Section 2 gives an brief theoretical background, with section 3 describing our data collection and pre-processing. Waveform analysis is discussed in section 4.1 leading to regional velocity model results presented in section ??.

2 Theoretical Background

We use seismic body wave analysis in order to investigate the velocity structure of the upper inner core. These waves elastic waves, caused by earthquakes, that travel through the interior of the Earth.

2.1 Body Wave Theory

Here we summarise the main aspects of seismic body wave theory, taken from Shearer (2009).

¹Research published since Deuss (2014) provides strong evidence for this (Wang et al. (2015)).

Under the assumptions of a continuous, linearly elastic medium, infinitesimal strains and constant medium properties one can derive the elastic wave equation

$$\rho \frac{\partial^2 \vec{u}}{\partial t^2} = (\lambda + \mu) \nabla (\nabla \cdot \vec{u}) + \mu \nabla^2 \vec{u} \quad (1)$$

where \vec{u} is the local displacement vector, ρ the density of the medium and λ and μ Lamé parameters of the medium. A general displacement vector can be decomposed into irrotational scalar and solenoidal vector potentials such that

$$\vec{u} \equiv \nabla \phi + \nabla \times \vec{\psi} \quad (2)$$

Substituting (2) in to (1) yields two independent wave equations, one for ϕ and one for $\vec{\psi}$, which describe P-waves and S-waves respectively. P-waves are compressional with displacements occurring parallel to the wave vector, whereas S-waves are transverse with displacements occurring perpendicular to the wave vector. These wave equations take the form

$$\frac{\partial^2 \phi}{\partial t^2} = c^2(\vec{x}) \nabla^2 \phi \quad (3)$$

where $c(\vec{x})$ is the local wave velocity that depends on position. A velocity model is a full specification of $c(\vec{x})$ in the region of interest.

2.2 Sampling the Inner Core

Because the outer core is liquid with $\mu \approx 0$ and thus does not transmit S-waves, it is P-waves that are used to sample the inner core. Figure PUT FIGURE HERE shows the ray path for the PKiKP and PKIKP phase; they travel almost identical paths through the Crust, Mantle and upper Outer Core, after which PKiKP reflects off the Inner Core boundary, whereas PKIKP travels just underneath the boundary in the Inner Core.

All measurements are compared to the radially symmetric global velocity model from Kennett et al. (1995) (hereafter called AK135), from which we seek to measure perturbations about. The residual travel time CHECK ME is defined after Waszek & Deuss (2011) as

$$\delta t = (t_{PKiKP} - t_{PKIKP})_{observed} - (t_{PKiKP} - t_{PKIKP})_{model} \quad (4)$$

This equation can be reformulated as an integral along the ray paths

$$\delta t = \left(\int \frac{1}{v_{obs}} - \frac{1}{v_{model}} ds \right)_{PKiKP} - \left(\int \frac{1}{v_{obs}} - \frac{1}{v_{model}} ds \right)_{PKIKP} \quad (5)$$

where the path to be integrated along is indicated by the subscript outside the brackets, and in general the velocities vary as a function of position.

As the inner core has a very low viscosity (eg. de Wijs et al. (1998), Zhang & Guo (2000)) we assume that it is unable to sustain any long term non-radial variations in velocity structure. Under this assumption $v_{jobs} = v_{model}$ for the outer core, setting the first integral in (5) to zero.

Taking perturbations about the model of the form $v_{obs} = v_{model} + \delta v$ gives

$$\delta t = \left(\int \frac{\delta v}{v_{model} + \delta v} \frac{1}{v_{model}} ds \right)_{PKIKP} \quad (6)$$

For depths below the Inner Core boundary of less than 50km v_{model} is constant for AK135, and we assume δv is also a constant such that we are measuring only the average velocity

perturbation along the ray path. We are thus left with the equation (to first order in δt) that will allow us to compute δv

$$\delta v = \frac{\delta t}{t} v_{model} \quad (7)$$

where t is the time PKIKP spends in the inner core. A positive residual implies a positive velocity perturbation and vice versa, as expected from equation (4).

If instead we wish to construct a layered model, we simply apply the above results to the uppermost layer, and then take the effect of the new layer into account when calculating the properties of subsequent lower layers.

3 Data Selection

As discussed in section 2.2, we make differential travel time measurements of PKiKP and PKIKP phases. An ideal seismogram would have a clear PKIKP arrival, little noise and no interference from surface reflection phases. As such, data are selected to meet the following criteria:

- Epicentral distance of 115° - 135° from the earthquake covers the majority of North America, where there is the highest worldwide density of seismometers.
- Depth greater than 15km, to minimise possible interference between PKIKP (PKiKP) and pPKIKP (pPKiKP) waves.
- Magnitude greater than 5.3 and less than 6.3 to ensure a large enough earthquake to produce an observable signal, whilst a small enough earthquake such that the rupture is likely to be impulsive.
- A fracture mechanism that is primarily dip slip². As the ray paths are nearly vertical when they reach the seismic stations, we require significant amounts of energy to be focused in the vertical direction at the site of the earthquake.

Individual earthquakes meeting this criteria typically contain 100 to 400 individual seismograms. Each seismogram is filtered between 0.7Hz - 2Hz in order to focus on the expected frequency of ~ 1 Hz whilst removing unwanted noise. Individual seismograms are then checked by hand, and only those showing a clear PKIKP signal near the predicted arrival time are kept for further analysis.

4 Data Analysis

4.1 Waveform analysis

The same analysis was performed on each individual event, allowing construction of a detailed velocity model for several CHANGE ME regions. Each event is listed in table 1. Here we describe the analysis performed using the specific example of the Celebes Sea earthquake.

Synthetic waveforms are computed using the WKBJ ray tracing program (Chapman (1976)) combined with rupture mechanisms from the global Centroid Moment Tensor (CMT) catalogue (Dziewonski et al. (1981), Alboussière & Deguen (2012)). Predicted ray paths and individual ray travel times are computed using the TauP toolkit (Crotwell et al. (1999)). Initial plots are shown for both real and synthetic data in figures 1 and 2 respectively, with zero time occurring at the time of the earthquake, taken from the global CMT catalogue. Overplotted are theoretical

²ie. a large component of motion in the vertical direction

Location	Latitude	Longitude	Date	Time (GMT)	Magnitude	Depth /km
Celebes Sea	4.55	122.82	2014/04/16	4:28:20.0		575.0
Mindanao						

Table 1: Event details. Information is taken directly from the Centroid Moment Tensor catalogue (Ekström et al. (2012)).

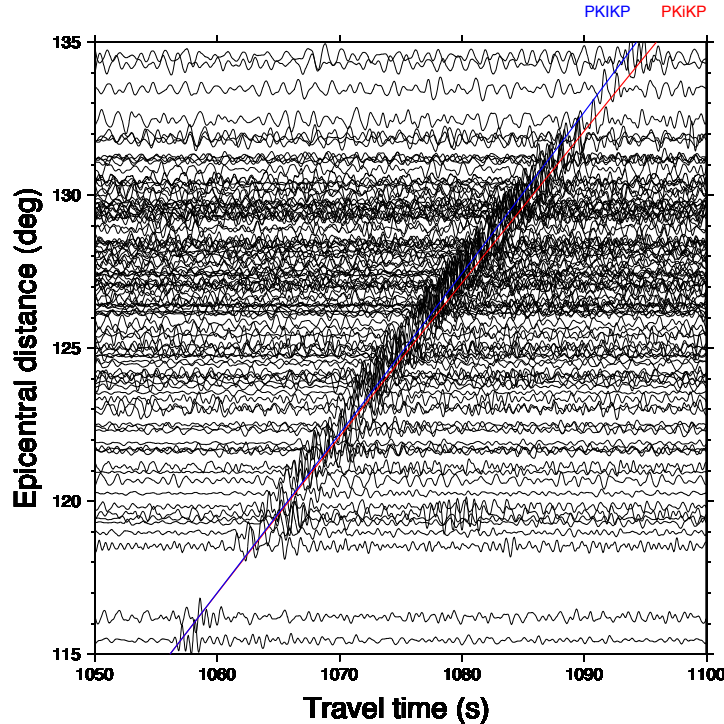


Figure 1: Real seismogram data from the Celebes Sea event after event selection. Each seismogram is zeroed on the earthquake time. Over plotted lines are theoretical phase arrivals computed using the AK135 model. Only data with a clear PKIKP arrival are plotted

PKIKP and PKiKP travel times computed using the AK135 model (Kennett et al. (1995)). The predicted travel times agree well with the data in both cases. For shorter epicentral distances the predicted arrival times become closer, suggesting that eventually there will be a phase separation below which the two distinct phases will not be individually observable.

In order to more easily visualise the two phases we plot individual PKiKP, PKIKP and both combined synthetic seismograms. Each of these is then centred on the final PKiKP upswing, and shown in figure 4. It is now easy to see the PKiKP phase merging with the PKIKP phase at low epicentral distances. In figure 3 we show a similar plot, but for real world data. The PKIKP (leftmost phase) is not moving in as epicentral distance increases here, immediately showing that large positive residuals are expected at low epicentral distances (and hence depths).

4.2 Quantifying minimum resolvable difference

At smaller epicentral distances PKIKP gets weaker and PKiKP develops a large upswing to the left. Both of these features mean that when measuring the peak to peak difference at low distances on the combined seismogram (or equivalently the real data) we are measuring two features of PKiKP and not one feature from each phase. criteria will be met either when

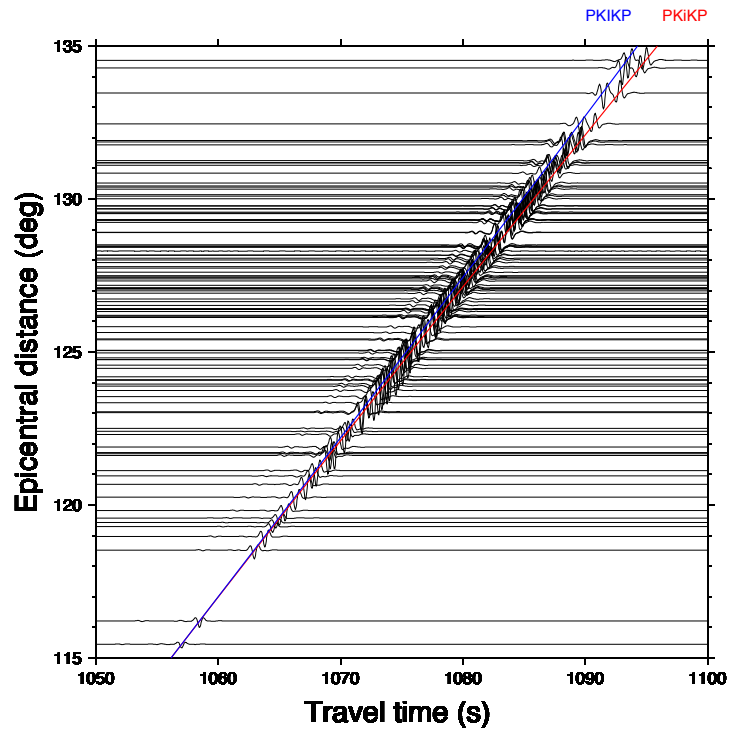


Figure 2: Synthetic seismogram data for the Celebes Sea event.. Each seismogram is zeroed on the earthquake time. Over plotted lines show theoretical phase arrivals computed using the AK135 model.

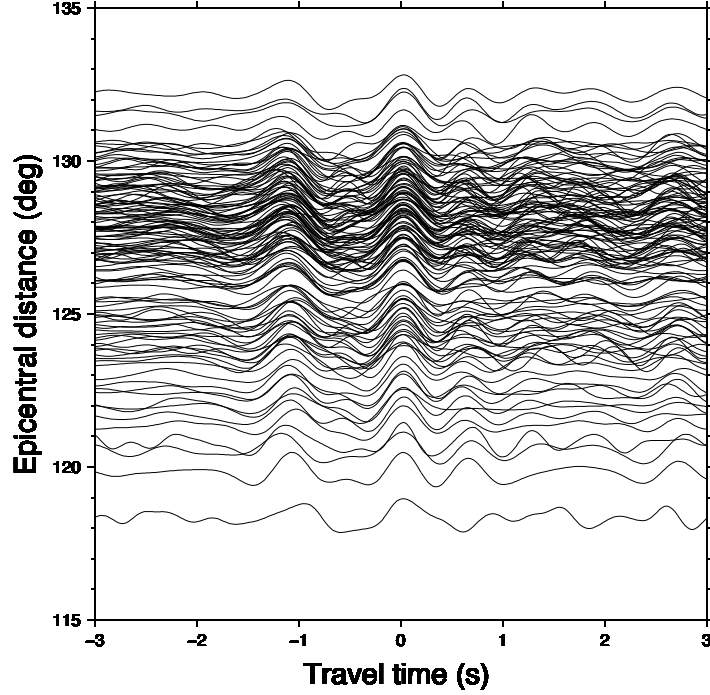


Figure 3: Real seismogram data for the Celebes Sea event. Each seismogram is zeroed on the final PKiKP upswing. Only data with clear PKiKP arrivals and clear PKiKP final upswings are plotted.

PKiKP peak to peak differences are large or equal than combined differences, or when PKiKP and combined differences coincide.

Figure 5 shows measurements of peak to peak differences for PKiKP, PKiKP and combined synthetic waveforms. In each case the upswings furthest to the left and right are measured, and the difference taken between these two peaks. It can be clearly seen that below 0.72 s PKiKP and combined measurements coincide, thus setting 0.72 s as the maximum peak to peak difference at which the two phases can be distinguished for this event.

For other events we complete similar analysis and only present measurements which we know to be greater than the minimum separation.

4.3 Residual travel time analysis

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Figure

A Ray paths

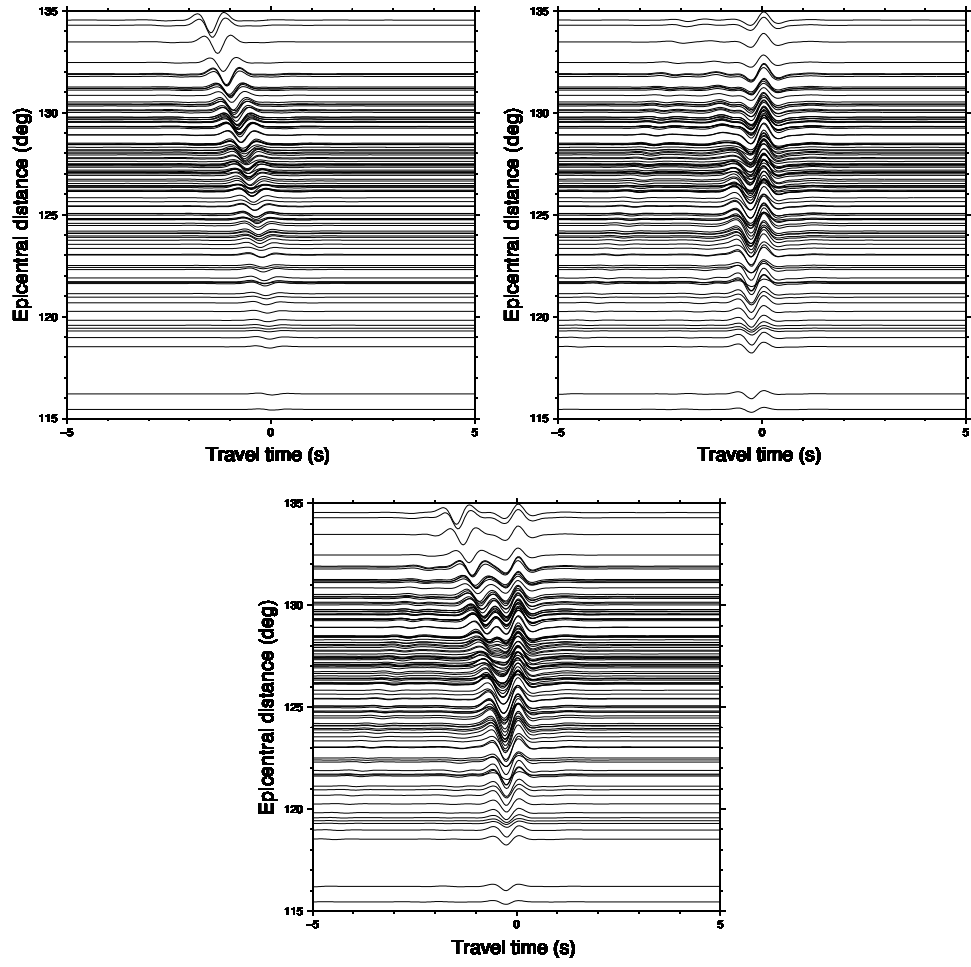


Figure 4: Separated PKIKP (top left) PKiKP (top right), and combined (bottom) synthetic seismograms for the Celebes Sea event.

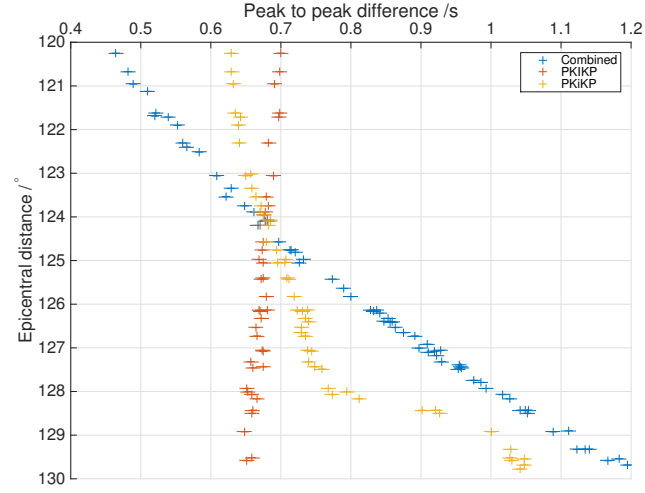


Figure 5: Peak to peak travel times recorded from synthetic data generated for the Celebes Sea earthquake. Differences are measured between the leftmost and rightmost large upswing. Data is shown for combined (blue), PKIKP (red) and PKiKP (yellow) seismograms.

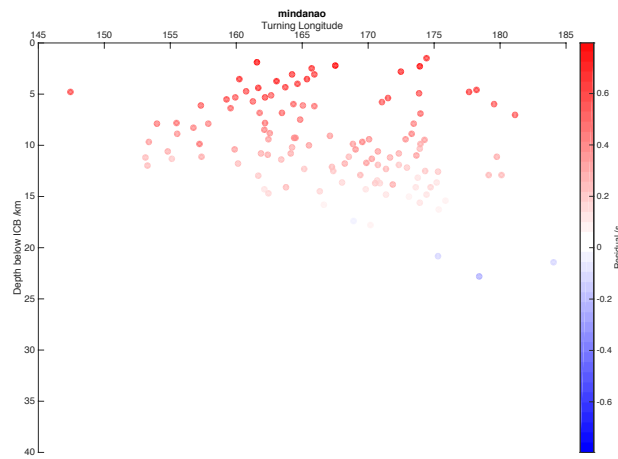


Figure 6: Caption

References

- Alboussière, T., & Deguen, R. 2012, *Journal of Geodynamics*, 61, 172
- Chapman, C. H. 1976, *Geophysical Research Letters*, 3, 153
- Crotwell, H. P., Owens, T. J., & Ritsema, J. 1999, *Seismological Research Letters*, 70, 154
- de Wijs, G. A., Kresse, G., Vocablo, L., et al. 1998, *Nature*, 392, 805
- Deguen, R., & Cardin, P. 2009, *Nature Geoscience*, 2, 419
- Deuss, A. 2014, *Annual Review of Earth and Planetary Sciences*, 42, 103
- Dziewonski, A. M., Chou, T.-A., & Woodhouse, J. H. 1981, *Journal of Geophysical Research*, 86, 2825
- Ekström, G., Nettles, M., & Dziewoski, A. 2012, *Physics of the Earth and Planetary Interiors*, 200-201, 1
- Kennett, B. L. N., Engdahl, E. R., & Buland, R. 1995, *Geophysical Journal International*, 122, 108
- Labrosse, S., Poirier, J.-P., & Le Mouél, J.-L. 2001, *Earth and Planetary Science Letters*, 190, 111
- Lehmann, I. 1936, *Publications du Bureau Central Séismologique International*, 14, 87
- Shearer, P. M. 2009, *Introduction to Seismology*, 2nd edn. (Cambridge University Press)
- Wang, T., Song, X., & Xia, H. H. 2015, *Nature Geoscience*
- Waszek, L., & Deuss, A. 2011, *Journal of Geophysical Research: Solid Earth*, 116, B12313
- Zhang, Y.-G., & Guo, G.-J. 2000, *Physics of the Earth and Planetary Interiors*, 122, 289