Package 'igraph'

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Description Routines for simple graphs and network analysis. igraph can handle large graphs very well and provides functions for generating random and regular graphs, graph visualization, centrality indices and much more.
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Description

igraph is a library for network analysis.

Introduction

The main goals of the igraph library is to provide a set of data types and functions for 1) pain-free implementation of graph algorithms, 2) fast handling of large graphs, with millions of vertices and edges, 3) allowing rapid prototyping via high level languages like R.

Creating graphs

There are many functions in igraph for creating graphs, both deterministic and stochastic; stochastic graph constructors are called 'games' is igraph.

To create small graphs with a given structure probably the graph.formula function is easiest. It uses R's formula interface, its manual page contains many examples. Another option is graph, which takes numeric vertex ids directly. graph.atlas creates graph from the Graph Atlas, graph.famous can create some special graphs.

To create graphs from field data, graph.edgelist, graph.data.frame and graph.adjacency are probably the best choices.

The igraph include some classic random graphs like the Erdos-Renyi GNP and GNM graphs (erdos.renyi.game) and some recent popular models, like preferential attachment (barabasi.game) and the small-world model (watts.strogatz.game).

Vertex and edge IDs

Vertices and edges have numerical vertex ids in igraph. Vertex ids are always consecutive and they start with zero. I.e. for a graph with 'n' vertices the vertex ids are between '0' and 'n-1'. If some operation changes the number of vertices in the graphs, e.g. a subgraph is created via subgraph, then the vertices are renumbered to satisfty this criteria.

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The same is true for the edges as well, edge ids are always between zero and 'm-1' where 'm' is the total number of edges in the graph.

It is often desirable to follow vertices along a number of graph operations, and vertex ids don't allow this because of the renumbering. The solution is to assign attributes to the vertices. These are kept by all operations, if possible. See more about attributes in the next section.

Attributes

In igraph it is possible to assign attributes to the vertices or edges of a graph, or to the graph itself. igraph provides flexible constructs for selecting a set of vertices or edges based on their attribute values, see get.vertex.attribute and iterators for details.

Some vertex/edge/graph attributes are treated specially. One of them is the 'name' attribute. This is used for printing the graph instead of the numerical ids, if it exists. Vertex names can also be used to specify a vector or set of vertices, in all igraph functions. E.g. degree has a 'v' argument that gives the vertices for which the degree is calculated. This argument can be given as character vector of vertex names as well.

Other attributes define visualization parameters, see igraph.plotting for details.

Attribute values can be set to any R object, but note that storing the graph in some file formats might result the loss of complex attribute values. All attribute values are preserved if you use save and load to store/retrieve your graphs.

Visualization

igraph provides three different ways for visualization. The first is the 'plot.igraph' function. (Actually you don't need to write 'plot.igraph', 'plot' is enough. This function uses base R graphic and can be used with any R device.

The second function is tkplot, which uses a Tk GUI for basic interactive graph manipulation. (Tk is quite resource hungry, so don't try this for very large graphs.)

The third way requires the rgl package and uses OpenGL. See the rglplot function for the details.

Make sure you read igraph.plotting before you start plotting your graphs.

File formats

igraph can handle various graph file formats, usually both for reading and writing. We suggest that you use the GraphML file format for your graphs, except if the graphs are too big. For big graphs a simpler format is recommended. See read.graph and write.graph for details.

Further information

The igraph homepage is at http://cneurocvs.rmki.kfki.hu/igraph. See especially the documentation section. Join the igraph-help mailing list if you have questions or comments.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

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aging.prefatt.game	Generate an evolving random graph with preferential attachment and aging

Description

This function creates a random graph by simulating its evolution. Each time a new vertex is added it creates a number of links to old vertices and the probability that an old vertex is cited depends on its in-degree (preferential attachment) and age.

Usage

```
aging.prefatt.game (n, pa.exp, aging.exp, m = NULL, aging.bin = 300,
   out.dist = NULL, out.seq = NULL, out.pref = FALSE,
   directed = TRUE, zero.deg.appeal = 1, zero.age.appeal = 0,
   deg.coef = 1, age.coef = 1, time.window = NULL)
```

Arguments

	n	The number of vertices in the graph.
	pa.exp	The preferantial attachment exponent, see the details below.
	aging.exp	The exponent of the aging, usually a non-positive number, see details below.
	m	The number of edges each new vertex creates (except the very first vertex). This argument is used only if both the out.dist and out.seq arguments are NULL.
	aging.bin	The number of bins to use for measuring the age of vertices, see details below.
	out.dist	The discrete distribution to generate the number of edges to add in each time step if $\operatorname{out.seq}$ is NULL. See details below.
	out.seq	The number of edges to add in each time step, a vector containing as many elements as the number of vertices. See details below.
	out.pref	Logical constant, whether to include edges not initiated by the vertex as a basis of preferential attachment. See details below.
	directed	Logical constant, whether to generate a directed graph. See details below.
zero.deg.appeal		
		The degree-dependent part of the 'attractiveness' of the vertices with no adjacent edges. See also details below.
zero.age.appeal		
		The age-dependent part of the 'attrativeness' of the vertices with age zero. It is usually zero, see details below.
	deg.coef	The coefficient of the degree-dependent 'attractiveness'. See details below.
	age.coef	The coefficient of the age-dependent part of the 'attractiveness'. See details below.
	time.window	Integer constant, if NULL only adjacent added in the last time.windows time steps are counted as a basis of the preferential attachment. See also details below.

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Details

This is a discrete time step model of a growing graph. We start with a network containing a single vertex (and no edges) in the first time step. Then in each time step (starting with the second) a new vertex is added and it initiates a number of edges to the old vertices in the network. The probability that an old vertex is connected to is proportional to

$$P[i] \sim (c \cdot k_i^{\alpha} + a)(d \cdot l_i^{\beta} + b)$$

Here k_i is the in-degree of vertex i in the current time step and l_i is the age of vertex i. The age is simply defined as the number of time steps passed since the vertex is added, with the extension that vertex age is divided to be in aging.bin bins.

c, α , a, d, β and b are parameters and they can be set via the following arguments: pa.exp (α , mandatory argument), aging.exp (β , mandatory argument), zero.deg.appeal (a, optional, the default value is 1), zero.age.appeal (b, optional, the default is 0), deg.coef (c, optional, the default is 1), and age.coef (d, optional, the default is 1).

The number of edges initiated in each time step is governed by the m, out.seq and out.pref parameters. If out.seq is given then it is interpreted as a vector giving the number of edges to be added in each time step. It should be of length n (the number of vertices), and its first element will be ignored. If out.seq is not given (or NULL) and out.dist is given then it will be used as a discrete probability distribution to generate the number of edges. Its first element gives the probability that zero edges are added at a time step, the second element is the probability that one edge is added, etc. (out.seq should contain non-negative numbers, but if they don't sum up to 1, they will be normalized to sum up to 1. This behavior is similar to the prob argument of the sample command.)

By default a directed graph is generated, but it directed is set to FALSE then an undirected is created. Even if an undirected graph is generated k_i denotes only the adjacent edges not initiated by the vertex itself except if out.pref is set to TRUE.

If the time. window argument is given (and not NULL) then k_i means only the adjacent edges added in the previous time. window time steps.

This function might generate graphs with multiple edges.

Value

A new graph.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

barabasi.game, erdos.renyi.game

```
# The maximum degree for graph with different aging exponents
g1 <- aging.prefatt.game(10000, pa.exp=1, aging.exp=0, aging.bin=1000)
g2 <- aging.prefatt.game(10000, pa.exp=1, aging.exp=-1, aging.bin=1000)</pre>
```

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```
g3 <- aging.prefatt.game(10000, pa.exp=1, aging.exp=-3, aging.bin=1000) \max(\deg(g1)) \max(\deg(g2)) \max(\deg(g3))
```

alpha.centrality

Find Bonacich alpha centrality scores of network positions

Description

alpha.centrality calculates the alpha centrality of some (or all) vertices in a graph.

Usage

Arguments

	graph	The input graph, can be directed or undirected
	nodes	Vertex sequence, the vertices for which the alpha centrality values are returned. (For technical reasons they will be calculated for all vertices first, anyway.)
	alpha	Parameter specifying the relative importance of endogenous versus exogenous factors in the determination of centrality. See details below.
	loops	Whether to eliminate loop edges from the graph before the calculation.
	exo	The exogenous factors, in most cases this is either a constant – the same factor for every node, or a vector giving the factor for every vertex. Note that long vectors will be truncated and short vectors will be replicated.
,	weights	Optional positive weight vector for calculating weighted closeness. If the graph has a weight edge attribute, then this is used by default.
	tol	Tolerance for near-singularities during matrix inversion, see solve.

Details

The alpha centrality measure can be considered as a generalization of eigenvector centerality to directed graphs. It was proposed by Bonacich in 2001 (see reference below).

The alpha centrality of the vertices in a graph is defined as the solution of the following matrix equation:

$$x = \alpha A^T x + e$$
,

where A is the (not neccessarily symmetric) adjacency matrix of the graph, e is the vector of exogenous sources of status of the vertices and α is the relative importance of the endogenous versus exogenous factors.

Value

A numeric vector containing the centrality scores for the selected vertices.

Warning

Singular adjacency matrices cause problems for this algorithm, the routine may fail is certain cases.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>.

References

Bonacich, P. and Paulette, L. (2001). "Eigenvector-like measures of centrality for asymmetric relations" *Social Networks*, 23, 191-201.

See Also

```
evcent and bonpow
```

Examples

```
# The examples from Bonacich's paper
g.1 <- graph( c(1,3,2,3,3,4,4,5)-1 )
g.2 <- graph( c(2,1,3,1,4,1,5,1)-1 )
g.3 <- graph( c(1,2,2,3,3,4,4,1,5,1)-1 )
alpha.centrality(g.1)
alpha.centrality(g.2)
alpha.centrality(g.3,alpha=0.5)</pre>
```

arpack

ARPACK eigenvector calculation

Description

Interface to the ARPACK library for calculating eigenvectors of sparse matrices

Usage

```
arpack(func, extra = NULL, sym = FALSE, options = igraph.arpack.default,
    env = parent.frame(), complex=!sym)
arpack.unpack.complex(vectors, values, nev)
```

Arguments

func	The function to perform the matrix-vector multiplication. ARPACK requires to
	perform these by the user. The function gets the vector x as the first argument,
	and it should return Ax , where A is the "input matrix". (The input matrix is
	never given explicitly.) The second argument is extra.
extra	Extra argument to supply to func.
sym	Logical scalar, whether the input matrix is symmetric. Always supply TRUE here
	if it is, since it can speed up the computation.

options Options to ARPACK, a named list to overwrite some of the default option values.

See details below.

env The environment in which func will be evaluated.

complex Whether to convert the eigenvectors returned by ARPACK into R complex vec-

tors. By default this is not done for symmetric problems (these only have real eigenvectors/values), but only non-symmetric ones. If you have a non-symmetric problem, but you're sure that the results will be real, then supply FALSE here. The conversion is done by calling arpack.unpack.complex.

Eigenvectors, as returned by ARPACK.

values Eigenvalues, as returned by ARPACK

nev The number of eigenvectors/values to extract. This can be less than or equal to

the number of eigenvalues requested in the original ARPACK call.

Details

vectors

ARPACK is a library for solving large scale eigenvalue problems. The package is designed to compute a few eigenvalues and corresponding eigenvectors of a general n by n matrix A. It is most appropriate for large sparse or structured matrices A where structured means that a matrix-vector product w <- Av requires order n rather than the usual order n^2 floating point operations. Please see http://www.caam.rice.edu/software/ARPACK/ for details.

This function is an interface to ARPACK. igraph does not contain all ARPACK routines, only the ones dealing with symmetric and non-symmetric eigenvalue problems using double precision real numbers.

The eigenvalue calculation in ARPACK (in the simplest case) involves the calculation of the Av product where A is the matrix we work with and v is an arbitrary vector. The function supplied in the fun argument is expected to perform this product. If the product can be done efficiently, e.g. if the matrix is sparse, then arpack is usually able to calculate the eigenvalues very quickly.

The options argument specifies what kind of calculation to perform. It is a list with the following members, they correspond directly to ARPACK parameters. On input it has the following fields:

- bmatCharacter constant, possible values: 'I', stadard eigenvalue problem, $Ax = \lambda x$; and 'G', generalized eigenvalue problem, $Ax = \lambda Bx$. Currently only 'I' is supported.
- nNumeric scalar. The dimension of the eigenproblem. You only need to set this if you call arpack directly. (I.e. not needed for evcent, page.rank, etc.)
- whichSpecify which eigenvalues/vectors to compute, character constant with exactly two characters

Possible values for symmetric input matrices:

- 'LA'Compute nev largest (algebraic) eigenvalues.
- 'SA'Compute nev smallest (algebraic) eigenvalues.
- 'LM'Compute nev largest (in magnitude) eigenvalues.
- 'SM'Compute nev smallest (in magnitude) eigenvalues.
- 'BE'Compute nev eigenvalues, half from each end of the spectrum. When nev is odd, compute one more from the high end than from the low end.

Possible values for non-symmetric input matrices:

- 'LM'Compute nev eigenvalues of largest magnitude.
- 'SM'Compute nev eigenvalues of smallest magnitude.
- 'LR'Compute nev eigenvalues of largest real part.
- 'SR'Compute nev eigenvalues of smallest real part.
- 'LI'Compute nev eigenvalues of largest imaginary part.
- 'SI'Compute nev eigenvalues of smallest imaginary part.

This parameter is sometimes overwritten by the various functions, e.g. page.rank always sets 'LM'.

- nevNumeric scalar. The number of eigenvalues to be computed.
- tolNumeric scalar. Stopping criterion: the relative accuracy of the Ritz value is considered acceptable if its error is less than tol times its estimated value. If this is set to zero then machine precision is used.
- ncvNumber of Lanczos vectors to be generated.
- ldvNumberic scalar. It should be set to zero in the current implementation.
- ishiftEither zero or one. If zero then the shifts are provided by the user via reverse communication. If one then exact shifts with respect to the reduced tridiagonal matrix T. Please always set this to one.
- maxiterMaximum number of Arnoldi update iterations allowed.
- nbBlocksize to be used in the recurrence. Please always leave this on the default value, one.
- modeThe type of the eigenproblem to be solved. Possible values if the input matrix is symmetric:
 - $1Ax = \lambda x$, A is symmetric.
 - $2Ax = \lambda Mx$, A is symmetric, M is symmetric positive definite.
 - $3Kx = \lambda Mx$, K is symmetric, M is symmetric positive semi-definite.
 - $4Kx = \lambda KGx$, K is symmetric positive semi-definite, KG is symmetric indefinite.
 - $5Ax = \lambda Mx$, A is symmetric, M is symmetric positive semi-definite. (Cayley transformed mode.)

Please note that only mode==1 was tested and other values might not work properly.

Possible values if the input matrix is not symmetric:

- $1Ax = \lambda x$.
- $2Ax = \lambda Mx$, M is symmetric positive definite.
- $3Ax = \lambda Mx$, M is symmetric semi-definite.
- $4Ax = \lambda Mx$, M is symmetric semi-definite.

Please note that only mode==1 was tested and other values might not work properly.

- startNot used currently. Later it be used to set a starting vector.
- · sigmaNot used currently.
- sigmaiNot use currently.

On output the following additional fields are added:

- infoError flag of ARPACK. Possible values:
 - * 0Normal exit.
 - * 1Maximum number of iterations taken.

* 3No shifts could be applied during a cycle of the Implicitly restarted Arnoldi iteration. One possibility is to increase the size of ncv relative to nev.

ARPACK can return more error conditions than these, but they are converted to regular igraph errors.

- iterNumber of Arnoldi iterations taken.
- nconvNumber of "converged" Ritz values. This represents the number of Ritz values that satisfy the convergence critetion.
- numopTotal number of matrix-vector multiplications.
- numopbNot used currently.
- numreoTotal number of steps of re-orthogonalization.

Please see the ARPACK documentation for additional details.

arpack.unpack.complex is a (semi-)internal function that converts the output of the non-symmetric ARPACK solver to a more readable format. It is called internally by arpack.

Value

A named list with the following members:

values

Numeric vector, the desired eigenvalues.

Numeric matrix, the desired eigenvectors as columns. If complex=TRUE (the default for non-symmetric problems), then the matrix is complex.

A named list with the supplied options and some information about the performed calculation, including an ARPACK exit code. See the details above.

Author(s)

Rich Lehoucq, Kristi Maschhoff, Danny Sorensen, Chao Yang for ARPACK, Gabor Csardi <csardi@rmki.kfki.hu> for the R interface.

References

- D.C. Sorensen, Implicit Application of Polynomial Filters in a k-Step Arnoldi Method. *SIAM J. Matr. Anal. Apps.*, 13 (1992), pp 357-385.
- R.B. Lehoucq, Analysis and Implementation of an Implicitly Restarted Arnoldi Iteration. *Rice University Technical Report* TR95-13, Department of Computational and Applied Mathematics.
- B.N. Parlett & Y. Saad, Complex Shift and Invert Strategies for Real Matrices. *Linear Algebra and its Applications*, vol 88/89, pp 575-595, (1987).

See Also

evcent, page.rank, hub.score, leading.eigenvector.community are some of the functions in igraph which use ARPACK. The ARPACK homepage is at http://www.caam.rice.edu/software/ARPACK/.

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Examples

```
# Identity matrix
f <- function(x, extra=NULL) x
arpack(f, options=list(n=10, nev=2, ncv=4), sym=TRUE)

# Graph laplacian of a star graph (undirected), n>=2
# Note that this is a linear operation
f <- function(x, extra=NULL) {
    y <- x
    y[1] <- (length(x)-1)*x[1] - sum(x[-1])
    for (i in 2:length(x)) {
        y[i] <- x[i] - x[1]
    }
    y
}

arpack(f, options=list(n=10, nev=1, ncv=3), sym=TRUE)

# double check
eigen(graph.laplacian(graph.star(10, mode="undirected")))</pre>
```

articulation.points

Articulation points of a graph

Description

Articuation points or cut vertices are vertices whose removal increases the number of connected components in a graph.

Usage

```
articulation.points(graph)
```

Arguments

graph

The input graph. It is treated as an undirected graph, even if it is directed.

Details

Articuation points or cut vertices are vertices whose removal increases the number of connected components in a graph.

Value

A numeric vector giving the vertex ids of the articulation points of the input graph.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

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See Also

biconnected.components, clusters, is.connected, vertex.connectivity

Examples

```
g <- graph.disjoint.union( graph.full(5), graph.full(5) )
clu <- clusters(g)$membership
g <- add.edges(g, c(which(clu==0), which(clu==1))-1)
articulation.points(g)</pre>
```

as.directed

Convert between directed and undirected graphs

Description

as.directed converts an undirected graph to directed, as.undirected is the opposite, it converts a directed graph to undirected.

Usage

```
as.directed(graph, mode = c("mutual", "arbitrary"))
as.undirected(graph, mode = c("collapse", "each"))
```

Arguments

graph

The graph to convert.

mode

Character constant, defines the conversion algorithm. For as .directed it can

be mutual or arbitrary. For as. undirected it can be each or collapse. See

details below.

Details

Conversion algorithms for as.directed:

- arbitraryThe number of edges in the graph stays the same, an arbitrarily directed edge is created for each undirected edge.
- mutualTwo directed edges are created for each undirected edge, one in each direction.

Conversion algorithms for as.undirected:

- eachThe number of edges remains constant, an undirected edge is created for each directed one, this version might create graphs with multiple edges.
- collapseOne undirected edge will be created for each pair of vertices which are connected with at least one directed edge, no multiple edges will be created.

Value

A new graph object.

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Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

simplify for removing multiple and/or loop edges from a graph.

Examples

```
g <- graph.ring(10)
as.directed(g, "mutual")
g2 <- graph.star(10)
as.undirected(g)</pre>
```

attributes

Graph, vertex and edge attributes

Description

Attributes are associated values belonging to a graph, vertices or edges. These can represent some property, like data about how the graph was constructed, the color of the vertices when the graph is plotted, or simply the weights of the edges in a weighted graph.

Usage

```
get.graph.attribute(graph, name)
set.graph.attribute(graph, name, value)
remove.graph.attribute(graph, name)
get.vertex.attribute(graph, name, index=V(graph))
set.vertex.attribute(graph, name, index=V(graph), value)
remove.vertex.attribute(graph, name)
get.edge.attribute(graph, name, index=E(graph))
set.edge.attribute(graph, name, index=E(graph), value)
remove.edge.attribute(graph, name)
```

Arguments

graph	The graph object to work on. Note that the original graph is never modified, a new graph object is returned instead; if you don't assign it to a variable your modifications will be lost! See examples below.
name	Character constant, the name of the attribute.
index	Numeric vector, the ids of the vertices or edges. It is not recycled, even if value is longer.
value	Numeric vector, the new value(s) of the attributes, it will be recycled if needed.

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Details

There are three types of attributes in igraph: graph, vertex and edge attributes. Graph attributes are associated with graph, vertex attributes with vertices and edge attributes with edges.

Examples for graph attributes are the date when the graph data was collected or other types of memos like the type of the data, or whether the graph is a simple graph, ie. one without loops and multiple edges.

Examples of vertex attributes are vertex properties, like the vertex coordinates for the visualization of the graph, or other visualization parameters, or meta-data associated with the vertices, like the gender and the age of the individuals in a friendship network, the type of the neurons in a graph representing neural circuitry or even some pre-computed structual properties, like the betweenness centrality of the vertices.

Examples of edge attributes are data associated with edges: most commonly edge weights, or visualization parameters.

In recent igraph versions, arbitrary R objects can be assigned as graph, vertex or edge attributes.

Some igraph functions use the values or graph, vertex and edge attributes if they are present but this is not done in the current version very extensively. Expect more in the (near) future.

Graph attributes can be created with the set.graph.attribute function, and removed with remove.graph.attribute. Graph attributes are queried with get.graph.attribute and the assigned graph attributes are listed with list.graph.attributes.

Note that set.graph.attribute and remove.graph.attribute both return a new graph, they do *not* change their argument! If you don't want to lose the results, you have to assign their return value to a variable:

```
G <- set.graph.attribute(G, "name", "My favorite graph")
G <- remove.graph.attribute(G, "name")</pre>
```

There is a simpler notation for using graph attributes: the '\$' operator. It can be used both to query and set graph attributes, see an example below.

The functions for vertex attributes are set.vertex.attribute, get.vertex.attribute, remove.vertex.attribute and list.vertex.attributes and for edge attributes they are set.edge.attribute, get.edge.attribute, remove.edge.attribute and list.edge.attributes.

Note that set.vertex.attribute, remove.vertex.attribute, set.edge.attribute and remove.edge.attribute do *not* change their argument, you have to assign their return value to a variable:

```
G <- set.vertex.attribute(G, "label", value=letters[1:10])
G <- remove.vertex.attribute(G, "label")
G <- set.edge.attribute(G, "weight", value=runif(ecount(G)))
G <- remove.edge.attribute(G, "weight")</pre>
```

There is however a (syntactically) much simpler way to handle vertex and edge attribute by using vertex and edge selectors, it works like this: V(g) selects all vertices in a graph, and V(g)\$name queries the name attribute for all vertices. Similarly is vs is a vertex set vs\$name gives the values of the name attribute for the vertices in the vertex set.

This form can also be used to set the values of the attributes, like the regular R convention:

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```
V(g)$color <- "red"
```

It works for vertex subsets as well:

```
V(g)[0:5]$color <- "green"</pre>
```

The notation for edges is similar: E(g) means all edges E(g) weight is the weight attribute for all edges, etc.

See also the manual page for iterators about how to create various vertex and edge sets.

Value

get.graph.attribute, get.vertex.attribute and get.edge.attribute return an R object, or a list of R objects if attributes of more vertices/edges are requested.

set.graph.attribute, set.vertex.attribute, set.edge.attribute, and also remove.graph.attribute, remove.vertex.attribute and remove.edge.attribute return a new graph object with the updates/removes performed.

list.graph.attributes, list.vertex.attributes and list.edge.attributes return a character vector, the names of the attributes present.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

print.igraph can also print attributes

```
g <- graph.ring(10)
g <- set.graph.attribute(g, "name", "RING")
# It is the same as
g$name <- "RING"
g$name

g <- set.vertex.attribute(g, "color", value=c("red", "green"))
get.vertex.attribute(g, "color")

g <- set.edge.attribute(g, "weight", value=runif(ecount(g)))
get.edge.attribute(g, "weight")

# The following notation is more convenient
g <- graph.star(10)

V(g)$color <- c("red", "green")
V(g)$color</pre>
E(g)$weight <- runif(ecount(g))
```

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```
E(g)$weight
print(g, g=TRUE, v=TRUE, e=TRUE)
```

barabasi.game

Generate scale-free graphs according to the Barabasi-Albert model

Description

The BA-model is a very simple stochastic algorithm for building a graph.

Usage

```
barabasi.game(n, power = 1, m = NULL, out.dist = NULL, out.seq = NULL,
    out.pref = FALSE, zero.appeal = 1, directed = TRUE, time.window = NULL)
```

Arguments

n	Number of vertices.
power	The power of the preferential attachment, the default is one, ie. linear preferential attachment.
m	Numeric constant, the number of edges to add in each time step This argument is only used if both out.dist and out.seq are omitted or NULL.
out.dist	Numeric vector, the distribution of the number of edges to add in each time step. This argument is only used if the out. seq argument is omitted or NULL.
out.seq	Numeric vector giving the number of edges to add in each time step. Its first element is ignored as no edges are added in the first time step.
out.pref	Logical, if true the total degree is used for calculating the citation probability, otherwise the in-degree is used.
zero.appeal	The 'attractiveness' of the vertices with no adjacent edges. See details below.
directed	Whether to create a directed graph.
time.window	Integer constant, if given only edges added in the previous time.window time steps are counted as the basis of preferential attachment.

Details

This is a simple stochastic algorithm to generate a graph. It is a discrete time step model and in each time step a single vertex is added.

We start with a single vertex and no edges in the first time step. Then we add one vertex in each time step and the new vertex initiates some edges to old vertices. The probability that an old vertex is chosen is given by

$$P[i] \sim k_i^{\alpha} + a$$

where k_i is the in-degree of vertex i in the current time step (more precisely the number of adjacent edges of i which were not initiated by i itself) and α and a are parameters given by the power and zero.appeal arguments.

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The number of edges initiated in a time step is given by the m, out.dist and out.seq arguments. If out.seq is given and not NULL then it gives the number of edges to add in a vector, the first element is ignored, the second is the number of edges to add in the second time step and so on. If out.seq is not given or null and out.dist is given and not NULL then it is used as a discrete distribution to generate the number of edges in each time step. Its first element is the probability that no edges will be added, the second is the probability that one edge is added, etc. (out.dist does not need to sum up to one, it normalized automatically.) out.dist should contain non-negative numbers and at east one element should be positive.

If both out.seq and out.dist are omitted or NULL then m will be used, it should be a positive integer constant and m edges will be added in each time step.

barabasi.game generates a directed graph by default, set directed to FALSE to generate an undirected graph. Note that even if an undirected graph is generated k_i denotes the number of adjacent edges not initiated by the vertex itself and not the total (in- + out-) degree of the vertex, unless the out.pref argument is set to TRUE.

If the time.window argument is not NULL then k_i is the number of adjacent edges of i added in the previous time.window time steps.

Note that barabasi.game might generate graphs with multiple edges.

Value

A graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Barabasi, A.-L. and Albert R. 1999. Emergence of scaling in random networks *Science*, 286 509–512.

See Also

```
random.graph.game
```

```
g <- barabasi.game(10000)
degree.distribution(g)</pre>
```

20 betweenness

betweenness	Vertex and edge betweenness centrality	
-------------	--	--

Description

The vertex and edge betweenness are (roughly) defined by the number of geodesics (shortest paths) going through a vertex or an edge.

Usage

Arguments

graph	The graph to analyze.
V	The vertices for which the vertex betweenness will be calculated.
е	The edges for which the edge betweenness will be calculated.
directed	Logical, whether directed paths should be considered while determining the shortest paths.
verbose	Logical, whether to show a progress bar.
vids	The vertices for which the vertex betweenness estimation will be calculated.
cutoff	The maximum path length to consider when calculating the betweenness. If zero or negative then there is no such limit.

Details

The vertex betweenness of vertex v is defined by

$$\sum_{i \neq j, i \neq v, j \neq v} g_{ivj}/g_{ij}$$

The edge betweenness of edge e is defined by

$$\sum_{i \neq j} giej/g_{ij}$$

betweenness calculates vertex betweenness, edge.betweenness calculates edge.betweenness.

betweenness.estimate only considers paths of length cutoff or smaller, this can be run for larger graphs, as the running time is not quadratic (if cutoff is small). If cutoff is zero or negative then the function calculates the exact betweenness scores.

edge.betweenness.estimate is similar, but for edges.

For calculating the betweenness a similar algorithm to the one proposed by Brandes (see References) is used.

Value

A numeric vector with the betweenness score for each vertex in v for betweenness.

A numeric vector with the edge betweenness score for each edge in e for edge. betweenness.

betweenness.estimate returns the estimated betweenness scores for vertices in vids, edge.betweenness.estimate the estimated edge betweenness score for all edges; both in a numeric vector.

Note

edge.betweenness might give false values for graphs with multiple edges.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

References

Freeman, L.C. (1979). Centrality in Social Networks I: Conceptual Clarification. *Social Networks*, 1, 215-239.

Ulrik Brandes, A Faster Algorithm for Betweenness Centrality. *Journal of Mathematical Sociology* 25(2):163-177, 2001.

See Also

```
closeness, degree
```

Examples

```
g <- random.graph.game(10, 3/10)
betweenness(g)
edge.betweenness(g)</pre>
```

biconnected.components

Biconnected components

Description

Finding the biconnected components of a graph

Usage

```
biconnected.components(graph)
```

Arguments

graph

The input graph. It is treated as an undirected graph, even if it is directed.

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Details

A graph is biconnected if the removal of any single vertex (and its adjacent edges) does not disconnect it.

A biconnected component of a graph is a maximal biconnected subgraph of it. The biconnected components of a graph can be given by the partition of its edges: every edge is a member of exactly one biconnected component. Note that this is not true for vertices: the same vertex can be part of many biconnected components.

Value

A named list with three components:

no Numeric scalar, an integer giving the number of biconnected components in the

graph.

components The components themselves, a list of numeric vectors. Each vector is a set of

edge ids giving the edges in a biconnected component.

articulation_points

The articulation points of the graph. See articulation.points.

See examples below on how to extract the vertex ids of the biconnected components from the result.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

See Also

```
articulation.points, clusters, is.connected, vertex.connectivity
```

Examples

```
g <- graph.disjoint.union( graph.full(5), graph.full(5) )
clu <- clusters(g)$membership
g <- add.edges(g, c(which(clu==0), which(clu==1))-1)
bc <- biconnected.components(g)
vertices <- lapply(bc$components, function(x) unique(as.vector(get.edges(g, x))))</pre>
```

bipartite.projection Project a bipartite graph

Description

A bipartite graph is projected into two one-mode networks

Usage

```
bipartite.projection.size(graph, types=NULL)
bipartite.projection (graph, types=NULL, probe1=-1)
```

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Arguments

graph	The input graph. It can be directed, but edge directions are ignored during the computation.
types	An optional vertex type vector to use instead of the 'type' vertex attribute. You must supply this argument if the graph has no 'type' vertex attribute.
probe1	This argument can be used to specify the order of the projections in the resulting list. If given and non-negative, then it is considered as a vertex id; the projection

containing the first one in the result list.

Details

Bipartite graphs have a 'type' vertex attribute in igraph, this is boolean and FALSE for the vertices of the first kind and TRUE for vertices of the second kind.

bipartite.projection.size calculates the number of vertices and edges in the two projections of the bipartite graphs, without calculating the projections themselves. This is useful to check how much memory the projections would need if you have a large bipartite graph.

bipartite.projections calculates the actual projections. You can use the probe1 argument to specify the order of the projections in the result. By default vertex type FALSE is the first and TRUE is the second.

Value

A list of two undirected graphs. See details above.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

Examples

```
## Projection of a full bipartite graph is a full graph
g <- graph.full.bipartite(10,5)
proj <- bipartite.projection(g)
graph.isomorphic(proj[[1]], graph.full(10))
graph.isomorphic(proj[[2]], graph.full(5))</pre>
```

bonpow

Find Bonacich Power Centrality Scores of Network Positions

Description

bonpow takes a graph (dat) and returns the Boncich power centralities of positions (selected by nodes). The decay rate for power contributions is specified by exponent (1 by default).

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Usage

```
bonpow(graph, nodes=V(graph), loops=FALSE, exponent=1,
    rescale=FALSE, tol=1e-7)
```

Arguments

graph the input graph.

nodes vertex sequence indicating which vertices are to be included in the calculation.

By default, all vertices are included.

loops boolean indicating whether or not the diagonal should be treated as valid data.

Set this true if and only if the data can contain loops. loops is FALSE by default.

exponent exponent (decay rate) for the Bonacich power centrality score; can be negative

rescale if true, centrality scores are rescaled such that they sum to 1.

tol tolerance for near-singularities during matrix inversion (see solve)

Details

Bonacich's power centrality measure is defined by $C_{BP}(\alpha,\beta) = \alpha (\mathbf{I} - \beta \mathbf{A})^{-1} \mathbf{A}\mathbf{1}$, where β is an attenuation parameter (set here by exponent) and \mathbf{A} is the graph adjacency matrix. (The coefficient α acts as a scaling parameter, and is set here (following Bonacich (1987)) such that the sum of squared scores is equal to the number of vertices. This allows 1 to be used as a reference value for the "middle" of the centrality range.) When $\beta \to 1/\lambda_{\mathbf{A}1}$ (the reciprocal of the largest eigenvalue of \mathbf{A}), this is to within a constant multiple of the familiar eigenvector centrality score; for other values of β , the behavior of the measure is quite different. In particular, β gives positive and negative weight to even and odd walks, respectively, as can be seen from the series expansion $C_{BP}(\alpha,\beta) = \alpha \sum_{k=0}^{\infty} \beta^k \mathbf{A}^{k+1} \mathbf{1}$ which converges so long as $|\beta| < 1/\lambda_{\mathbf{A}1}$. The magnitude of β controls the influence of distant actors on ego's centrality score, with larger magnitudes indicating slower rates of decay. (High rates, hence, imply a greater sensitivity to edge effects.)

Interpretively, the Bonacich power measure corresponds to the notion that the power of a vertex is recursively defined by the sum of the power of its alters. The nature of the recursion involved is then controlled by the power exponent: positive values imply that vertices become more powerful as their alters become more powerful (as occurs in cooperative relations), while negative values imply that vertices become more powerful only as their alters become *weaker* (as occurs in competitive or antagonistic relations). The magnitude of the exponent indicates the tendency of the effect to decay across long walks; higher magnitudes imply slower decay. One interesting feature of this measure is its relative instability to changes in exponent magnitude (particularly in the negative case). If your theory motivates use of this measure, you should be very careful to choose a decay parameter on a non-ad hoc basis.

Value

A vector, containing the centrality scores.

Warning

Singular adjacency matrices cause no end of headaches for this algorithm; thus, the routine may fail in certain cases. This will be fixed when I get a better algorithm. bonpow will not symmetrize your

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data before extracting eigenvectors; don't send this routine asymmetric matrices unless you really mean to do so.

Note

This function was ported (ie. copied) from the SNA package.

Author(s)

Carter T. Butts <buttsc@uci.edu>, ported to igraph by Gabor Csardi <csardi@rmki.kfki.hu>

References

Bonacich, P. (1972). "Factoring and Weighting Approaches to Status Scores and Clique Identification." *Journal of Mathematical Sociology*, 2, 113-120.

Bonacich, P. (1987). "Power and Centrality: A Family of Measures." *American Journal of Sociology*, 92, 1170-1182.

See Also

evcent and alpha.centrality

```
# Generate some test data from Bonacich, 1987:
g.c <- graph( c(1,2,1,3,2,4,3,5)-1, dir=FALSE)
g.d <- graph( c(1,2,1,3,1,4,2,5,3,6,4,7)-1, dir=FALSE)
g.e <- graph( c(1,2,1,3,1,4,2,5,2,6,3,7,3,8,4,9,4,10)-1, dir=FALSE)
g.f <- graph( c(1,2,1,3,1,4,2,5,2,6,2,7,3,8,3,9,3,10,4,11,4,12,4,13)-1, dir=FALSE)
# Compute Bonpow scores
for (e in seq(-0.5,.5, by=0.1)) {
    print(round(bonpow(g.c, exp=e)[c(1,2,4)], 2))
}

for (e in seq(-0.4,.4, by=0.1)) {
    print(round(bonpow(g.d, exp=e)[c(1,2,5)], 2))
}

for (e in seq(-0.4,.4, by=0.1)) {
    print(round(bonpow(g.e, exp=e)[c(1,2,5)], 2))
}

for (e in seq(-0.4,.4, by=0.1)) {
    print(round(bonpow(g.f, exp=e)[c(1,2,5)], 2))
}</pre>
```

26 canonical.permutation

canonical.permutation Canonical permutation of a graph

Description

The canonical permutation brings every isomorphic graphs into the same (labeled) graphs.

Usage

```
canonical.permutation(graph, sh="fm")
```

Arguments

graph The input graph, treated as undirected.

sh Type of the heuristics to use for the BLISS algorithm. See details for possible

values.

Details

canonical.permutation computes a permutation which brings the graph into canonical form, as defined by the BLISS algorithm. All isomorphic graphs have the same canonical form.

See the paper below for the details about BLISS. This and more information is available at http://www.tcs.hut.fi/Software/bliss/index.html.

The possible values for the sh argument are:

- fFirst non-singleton cell.
- flFirst largest non-singleton cell.
- fsFirst smallest non-singleton cell.
- fmFirst maximally non-trivially connectec non-singleton cell.
- flmLargest maximally non-trivially connected non-singleton cell.
- fsmSmallest maximally non-trivially connected non-singleton cell.

See the paper in references for details about these.

Value

A list with the following members:

labeling The canonical parmutation which takes the input graph into canonical form. A

numeric vector, the first element is the new label of vertex 0, the second element

for vertex 1, etc.

info Some information about the BLISS computation. A named list with the follow-

ing members:

- nof_nodesThe number of nodes in the search tree.
- nof_leaf_nodesThe number of leaf nodes in the search tree.

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- nof_bad_nodesNumber of bad nodes.
- nof_canupdatesNumber of canrep updates.
- max\ levelMaximum level.
- group\sizeThe size of the automorphism group of the input graph, as a string. This number is exact if igraph was compiled with the GMP library, and approximate otherwise.

Author(s)

Tommi Junttila for BLISS, Gabor Csardi csardi@rmki.kfki.hu for the igraph and R interfaces.

References

Tommi Junttila and Petteri Kaski: Engineering an Efficient Canonical Labeling Tool for Large and Sparse Graphs, *Proceedings of the Ninth Workshop on Algorithm Engineering and Experiments and the Fourth Workshop on Analytic Algorithms and Combinatorics*. 2007.

See Also

permute.vertices to apply a permutation to a graph, graph.isomorphic for deciding graph isomorphism, possibly based on canonical labels.

Examples

```
## Calculate the canonical form of a random graph
g1 <- erdos.renyi.game(10, 20, type="gnm")
cp1 <- canonical.permutation(g1)
cf1 <- permute.vertices(g1, cp1$labeling)

## Do the same with a random permutation of it
g2 <- permute.vertices(g1, sample(vcount(g1))-1)
cp2 <- canonical.permutation(g2)
cf2 <- permute.vertices(g2, cp2$labeling)

## Check that they are the same
el1 <- get.edgelist(cf1)
el2 <- get.edgelist(cf2)
el1 <- el1[ order(el1[,1], el1[,2]), ]
el2 <- el2[ order(el2[,1], el2[,2]), ]
all(el1 == el2)</pre>
```

cliques

The functions find cliques, ie. complete subgraphs in a graph

Description

These functions find all, the largest or all the maximal cliques in an undirected graph. The size of the largest clique can also be calculated.

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Usage

```
cliques(graph, min=NULL, max=NULL)
largest.cliques(graph)
maximal.cliques(graph)
clique.number(graph)
```

Arguments

max

min The input graph, directed graphs will be considered as undirected ones, multiple edges and loops are ignored.

Numeric constant, lower limit on the size of the cliques to find. NULL means no limit, ie. it is the same as 0.

Numeric constant, upper limit on the size of the cliques to find. NULL means no

limit.

Details

cliques find all complete subgraphs in the input graph, obeying the size limitations given in the min and max arguments.

largest.cliques finds all largest cliques in the input graph. A clique is largest if there is no other clique including more vertices.

maximal.cliques finds all maximal cliques in the input graph. A clique in maximal if it cannot be extended to a larger clique. The largest cliques are always maximal, but a maximal clique is not neccessarily the largest.

clique.number calculates the size of the largest clique(s).

The current implementation of these functions searches for maximal independent vertex sets (see independent.vertex.sets) in the complementer graph.

Value

cliques, largest.cliques and clique.number return a list containing numeric vectors of vertex ids. Each list element is a clique.

clique.number returns an integer constant.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu> for the R interface and the manual page.

See Also

independent.vertex.sets

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Examples

```
# this usually contains cliques of size six
g <- erdos.renyi.game(100, 0.3)
clique.number(g)
cliques(g, min=6)
largest.cliques(g)
# To have a bit less maximal cliques, about 100-200 usually
g <- erdos.renyi.game(100, 0.03)
maximal.cliques(g)</pre>
```

closeness

Closeness centrality of vertices

Description

Cloness centrality measures how many steps is required to access every other vertex from a given vertex.

Usage

Arguments

graph The graph to analyze.

v,vids The vertices for which closeness will be calculated.

mode Character string, defined the types of the paths used for measuring the distance in directed graphs. "in" measures the paths to a vertex, "out" measures paths from a vertex, all uses undirected paths. This argument is ignored for undirected graphs.

cutoff The maximum path length to consider when calculating the betweenness. If zero

or negative then there is no such limit.

Details

The closeness centrality of a vertex is defined by the inverse of the average length of the shortest paths to/from all the other vertices in the graph:

$$\frac{|V| - 1}{\sum_{i \neq v} d_v i}$$

If there is no (directed) path between vertex v and i then the total number of vertices is used in the formula instead of the path length.

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closeness.estimate only considers paths of length cutoff or smaller, this can be run for larger graphs, as the running time is not quadratic (if cutoff is small). If cutoff is zero or negative then the function calculates the exact closeness scores.

Value

Numeric vector with the closeness values of all the vertices in v.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

References

Freeman, L.C. (1979). Centrality in Social Networks I: Conceptual Clarification. *Social Networks*, 1, 215-239.

See Also

betweenness, degree

Examples

```
g <- graph.ring(10)
g2 <- graph.star(10)
closeness(g)
closeness(g2, mode="in")
closeness(g2, mode="out")
closeness(g2, mode="all")</pre>
```

clusters

Connected components of a graph

Description

Calculate the maximal (weakly or strongly) connected components of a graph

Usage

```
is.connected(graph, mode=c("weak", "strong"))
clusters(graph, mode=c("weak", "strong"))
no.clusters(graph, mode=c("weak", "strong"))
cluster.distribution(graph, cumulative = FALSE, mul.size = FALSE, ...)
```

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Arguments

graph The graph to analyze.

mode Character string, either "weak" or "strong". For directed graphs "weak" implies

weakly, "strong" strongly connected components to search. It is ignored for

undirected graphs.

 $\label{eq:cumulative} \textbf{Logical, if TRUE the cumulative distirubution (relative frequency) is calculated.}$

mul.size Logical. If TRUE the relative frequencies will be multiplied by the cluster sizes.

... Additional attributes to pass to cluster, right now only mode makes sense.

Details

is. connected decides whether the graph is weakly or strongly connected.

clusters finds the maximal (weakly or strongly) connected components of a graph.

no.clusters does almost the same as clusters but returns only the number of clusters found instead of returning the actual clusters.

cluster.distribution creates a histogram for the maximal connected component sizes.

Breadth-first search is conducted from each not-yet visited vertex.

Value

For is. connected a logical constant.

For clusters a named list with three components:

membership numeric vector giving the cluster id to which each vertex belongs.

numeric vector giving the sizes of the clusters.

numeric constant, the number of clusters.

For no. clusters an integer constant is returned.

For cluster distribution a numeric vector with the relative frequencies. The length of the vector is the size of the largest component plus one. Note that (for currently unknown reasons) the first element of the vector is the number of clusters of size zero, so this is always zero.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

See Also

subcomponent

```
g <- erdos.renyi.game(20, 1/20)
clusters(g)</pre>
```

32 cocitation

cocitation

Cocitation coupling

Description

Two vertices are cocited if there is another vertex citing both of them. cocitation siply counts how many types two vertices are cocited. The bibliographic coupling of two vertices is the number of other vertices they both cite, bibcoupling calculates this.

Usage

```
cocitation(graph, v=V(graph))
bibcoupling(graph, v=V(graph))
```

Arguments

graph The graph object to analyze

v Vertex sequence or numeric vector, the vertex ids for which the cocitation or

bibliographic coupling values we want to calculate. The default is all vertices.

Details

cocitation calculates the cocitation counts for the vertices in the v argument and all vertices in the graph.

bibcoupling calculates the bibliographic coupling for vertices in v and all vertices in the graph.

Calculating the cocitation or bibliographic coupling for only one vertex costs the same amount of computation as for all vertices. This might change in the future.

Value

A numeric matrix with length(v) lines and vcount(graph) columns. Element (i,j) contains the cocitation or bibliographic coupling for vertices v[i] and j.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

```
g <- graph.ring(10)
cocitation(g)
bibcoupling(g)</pre>
```

cohesive.blocks 33

cohesive.blocks Calculate Cohesive Blocks

Description

Calculates cohesive blocks for objects of class igraph.

Usage

Arguments

graph A graph object of class igraph.

db An optional RSQLite connection to an existing SQLite database (see details).

Ignored if NULL.

useDB Logical. Whether to use an external SQLite database instead of internal R datas-

tructures (see details). By default an SQLite database is used if the graph has

more than 400 vertices and the RSQLite package is installed.

cutsetHeuristic

Logical scalar. TODO

verbose Level of console output. Supply TRUE here to follow the progress of the compu-

tation.

Details

Cohesive blocking is a method of determining hierarchical subsets of graph vertices based on their structural cohesion (or vertex connectivity). For a given graph G, a subset of its vertices $S \subset V(G)$ is said to be maximally k-cohesive if there is no superset of S with vertex connectivity greater than or equal to k. Cohesive blocking is a process through which, given a k-cohesive set of vertices, maximally l-cohesive subsets are recursively identified with l > k. Thus a hiearchy of vertex subsets is found, whith the entire graph G at its root.

For certain larger graphs this algorithm can be quite memory-intensive due to the number of vertex subsets that are examined. In these cases it is worthwhile to use a database to keep track of this data, specified by the useDB argument. If useDB is TRUE, then either a temporary SQLite database is created, or the RSQLite connection specified in db is used. In either case the package RSQLite will be required.

structurally.cohesive.blocks is an alias to cohesive.blocks.

is.bgraph decides whether its argument is a bgraph object.

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Value

cohesive.blocks returns a graph of class c(bgraph, igraph), with four (new) graph attributes:

blocks A list with one element for each cohesive block found. The elements are numeric

vectors listing the indices of the nodes within that block.

block.cohesion A numeric vector with length equal to the number of cohesive blocks found,

listing the cohesion of those blocks.

tree The hierarchical tree of the cohesive blocks. Each node of this graph represents

a cohesive block, and directed edges represent inclusion as proper subset.

data A list containing supplementary data from the calculation.

is.bgraph returns a logical scalar.

Author(s)

Peter McMahan <peter.mcmahan@gmail.com>

References

- A. Kanevsky. On the number of minimum size separating vertex sets in a graph and how to find all of them *Proceedings of the first annual ACM-SIAM symposium on Discrete algorithms* San Francisco, California, United States. 411–421, 1990.
- J. Moody and D. R. White. Structural cohesion and embeddedness: A hierarchical concept of social groups. *American Sociological Review*, 68(1):103–127, Feb 2003.

See Also

graph.cohesion, plot.bgraph for plotting graphs together with their block hierarchy, write.pajek.bgraph for a writing graphs and cohesive blocks information to Pajek files. See attributes for handling graph attributes.

```
## Create a graph with an interesting structure:
g <- graph.disjoint.union(graph.full(4), graph.empty(2,directed=FALSE))
g <- add.edges(g,c(3,4,4,5,4,2))
g <- graph.disjoint.union(g,g,g)
g <- add.edges(g,c(0,6,1,7,0,12,4,0,4,1))

## Find cohesive blocks:
gBlocks <- cohesive.blocks(g)

## Examine block membership and cohesion:
gBlocks$blocks
gBlocks$blocks
gBlocks$block.cohesion

## Plot the resulting graph with its block hierarchy:
## Not run:
plot(gBlocks, vertex.size=7, layout=layout.kamada.kawai)</pre>
```

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```
## End(Not run)

## Save the results as Pajek ".net" and ".clu" files:
## Not run:
write.pajek.bgraph(gBlocks,file="gBlocks")

## End(Not run)

## An example that works better with the "kanevsky" cutset algorithm
## Not run:
g <- read.graph(file="http://intersci.ss.uci.edu/wiki/Vlado/SanJuanSur.net", format="pajek")
gBlocks <- cohesive.blocks(g, cutsetAlgorithm="kanevsky")

## End(Not run)</pre>
```

communities

Common functions supporting community detection algorithms

Description

community.to.membership takes a merge matrix, a typical result of community structure detection algorithms and creates a membership vector by performing a given number of merges in the merge matrix.

Usage

```
community.to.membership(graph, merges, steps, membership=TRUE, csize=TRUE)
```

Arguments

graph The graph to which the merge matrix belongs.

merges The merge matrix, see e.g. walktrap.community for the exact format.

steps The number of steps, ie. merges to be performed.

membership Logical scalar, whether to include the membership vector in the result.

csize Logical scalar, whether to include the sizes of the communities in the result.

Value

A named list with two members:

membership The membership vector.

csize A numeric vector giving the sizes of the communities.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

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See Also

walktrap.community, edge.betweenness.community, fastgreedy.community, spinglass.community for various community detection methods.

Examples

```
g <- graph.full(5) %du% graph.full(5) %du% graph.full(5)
g <- add.edges(g, c(0,5, 0,10, 5, 10))
wtc <- walktrap.community(g)
community.to.membership(g, wtc$merges, steps=12)</pre>
```

components

In- or out- component of a vertex

Description

Finds all vertices reachable from a given vertex, or the opposite: all vertices from which a given vertex is reachable via a directed path.

Usage

```
subcomponent(graph, v, mode = c("all", "out", "in"))
```

Arguments

graph The graph to analyze.

v The vertex to start the search from.

mode Character string, either "in", "out" or "all". If "in" all vertices from which v is

reachable are listed. If "out" all vertices reachable from v are returned. If "all"

returns the union of these. It is ignored for undirected graphs.

Details

A breadh-first search is conducted starting from vertex v.

Value

Numeric vector, the ids of the vertices in the same component as v.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

clusters

constraint 37

Examples

```
g <- erdos.renyi.game(100, 1/200)
subcomponent(g, 1, "in")
subcomponent(g, 1, "out")
subcomponent(g, 1, "all")</pre>
```

constraint

Burt's constraint

Description

Given a graph, constraint calculates Burt's constraint for each vertex.

Usage

```
constraint(graph, nodes=V(graph), weights=NULL)
```

Arguments

graph A graph object, the input graph.

nodes The vertices for which the constraint will be calculated. Defaults to all vertices.

weights The weights of the edges. If this is NULL and there is a weight edge attribute this is used. If there is no such edge attribute all edges will have the same weight.

Details

Burt's constraint is higher if ego has less, or mutually stronger related (i.e. more redundant) contacts. Burt's measure of constraint, C_i , of vertex i's ego network V_i , is defined for directed and valued graphs,

$$C_i = \sum_{j \in V_i \setminus \{i\}} (p_{ij} + \sum_{q \in V_i \setminus \{i,j\}} p_{iq} p_{qj})^2$$

for a graph of order (ie. number of vertices) N, where proportional tie strengths are defined as

$$p_{ij} = \frac{a_{ij} + a_{ji}}{\sum_{k \in V_i \setminus \{i\}} (a_{ik} + a_{ki})},$$

 a_{ij} are elements of A and the latter being the graph adjacency matrix. For isolated vertices, constraint is undefined.

Value

A numeric vector of constraint scores

Author(s)

Jeroen Bruggeman < j.p.bruggeman@uva.nl> and Gabor Csardi <csardi@rmki.kfki.hu>

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References

Burt, R.S. (2004). Structural holes and good ideas. American Journal of Sociology 110, 349-399.

Examples

```
g <- erdos.renyi.game(20, 5/20)
constraint(g)</pre>
```

conversion

Convert a graph to an adjacency matrix or an edge list

Description

Sometimes it is useful to have a standard representation of a graph, like an adjacency matrix or an edge list.

Usage

Arguments

graph	The graph to convert.
type	Gives how to create the adjacency matrix for undirected graphs. It is ignored for directed graphs. Possible values: upper: the upper right triangle of the matrix is used, lower: the lower left triangle of the matrix is used. both: the whole matrix is used, a symmetric matrix is returned.
attr	Either NULL or a character string giving an edge attribute name. If NULL a traditional adjacency matrix is returned. If not NULL then the values of the given edge attribute are included in the adjacency matrix. If the graph has multiple edges, the edge attribute of an arbitrarily chosen edge (for the multiple edges) is included.
names	Logical constant.
	For graph.adjacenct it gives whether to assign row and column names to the matrix. These are only assigned if the name vertex attribute is present in the graph.
	for get.edgelist it gives whether to return a character matrix containing vertex names (ie. the name vertex attribute) if they exist or numeric vertex ids.
binary	Logical, whether to return a binary matrix. This argument is ignored if attr is not NULL.
sparse	Logical scalar, whether to create a sparse matrix. The 'Matrix' package must be installed for creating sparse matrices.

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Details

get.adjacency returns the adjacency matrix of a graph, a regular R matrix if sparse is FALSE, or a sparse matrix, as defined in the 'Matrix' package, if sparse if TRUE.

get.edgelist returns the list of edges in a graph.

Value

A vcount(graph) by vcount(graph) (usually) numeric matrix for get.adjacency. (This can be huge!) Note that a non-numeric matrix might be returned if attr is a non-numeric edge attribute.

A ecount(graph) by 2 numeric matrix for get.edgelist.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

See Also

```
graph.adjacency, read.graph
```

Examples

```
g <- erdos.renyi.game(10, 2/10)
get.edgelist(g)
get.adjacency(g)
V(g)$name <- letters[1:vcount(g)]
get.adjacency(g)
E(g)$weight <- runif(ecount(g))
get.adjacency(g, attr="weight")</pre>
```

decompose.graph

Decompose a graph into components

Description

Creates a separate graph for each component of a graph.

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Arguments

graph	The original graph.
mode	Character constant giving the type of the components, wither weak for weakly connected components or strong for strongly connected components.
max.comps	The maximum number of components to return. The first max.comps components will be returned (which hold at least min.vertices vertices, see the next parameter), the others will be ignored. Supply NA here if you don't want to limit the number of components.
min.vertices	The minimum number of vertices a component should contain in order to place it in the result list. Eg. supply 2 here to ignore isolate vertices.

Value

A list of graph objects.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

See Also

is.connected to decide whether a graph is connected, clusters to calculate the connected components of a graph.

Examples

```
# the diameter of each component in a random graph
g <- erdos.renyi.game(1000, 1/1000)
comps <- decompose.graph(g, min.vertices=2)
sapply(comps, diameter)</pre>
```

degree

Degree and degree distribution of the vertices

Description

The degree of a vertex is its most basic structural property, the number of its adjacent edges.

```
\label{eq:continuous} \begin{split} &\text{degree(graph, v=V(graph), mode = c("all", "out", "in", "total"), loops = TRUE)} \\ &\text{degree.distribution(graph, cumulative = FALSE, ...)} \end{split}
```

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Arguments

v The ids of vertices of which the degree will be calculated.

mode Character string, "out" for out-degree, "in" for in-degree or "total" for the sum

of the two. For undirected graphs this argument is ignored.

loops Logical; whether the loop edges are also counted.

cumulative Logical; whether the cumulative degree distribution is to be calculated.

... Additional arguments to pass to degree, eg. mode is useful but also v and loops

make sense.

Value

For degree a numeric vector of the same length as argument v.

For degree.distribution a numeric vector of the same length as the maximum degree plus one. The first element is the relative frequency zero degree vertices, the second vertices with degree one, etc.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
g <- graph.ring(10)
degree(g)
g2 <- erdos.renyi.game(1000, 10/1000)
degree.distribution(g2)</pre>
```

degree.sequence.game Generate random graphs with a given degree sequence

Description

It is often useful to create a graph with given vertex degrees. This is exactly what degree. sequence. game does.

```
degree.sequence.game(out.deg, in.deg = numeric(0),
    method = c("simple", "v1"), ...)
```

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Arguments

out.deg	Numeric vector, the sequence of degrees (for undirected graphs) or out-degrees (for directed graphs). For undirected graphs its sum should be even. For directed graphs its sum should be the same as the sum of in.deg.
in.deg	For directed graph, the in-degree sequence.
method	Character, the method for generating the graph. Right now the "simple" and "vl" methods are implemented.
	Additional arguments, these are used as graph attributes.

Details

The "simple" method connects the out-stubs of the edges (undirected graphs) or the out-stubs and in-stubs (directed graphs) together. This way loop edges and also multiple edges may be generated.

This method is not adequate if one needs to generate simple graphs with a given degree sequence. The multiple and loop edges can be deleted, but then the degree sequence is distorted and there is nothing to ensure that the graphs are sampled uniformly.

The "vl" method is a more sophisticated generator. The algorithm and the implementation was done by Fabien Viger and Matthieu Latapy. This generator always generates undirected, connected simple graphs, it is an error to pass the in. deg argument to it. The algorithm relies on first creating an initial (possibly unconnected) simple undirected graph with the given degree sequence (if this is possible at all). Then some rewiring is done to make the graph connected. Finally a Monte-Carlo algorithm is used to randomize the graph. The "vl" samples from the undirected, connected simple graphs unformly. See http://www-rp.lip6.fr/~latapy/FV/generation.html for details.

Value

The new graph object.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

See Also

erdos.renyi.game, barabasi.game, simplify to get rid of the multiple and/or loops edges.

Examples

```
## The simple generator
g <- degree.sequence.game(rep(2,100))
degree(g)
is.simple(g)  # sometimes TRUE, but can be FALSE
g2 <- degree.sequence.game(1:10, 10:1)
degree(g2, mode="out")
degree(g2, mode="in")

## The vl generator
g3 <- degree.sequence.game(rep(2,100), method="vl")</pre>
```

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```
degree(g3)
is.simple(g3) # always TRUE

## Exponential degree distribution
## Note, that we correct the degree sequence if its sum is odd
degs <- sample(1:100, 100, replace=TRUE, prob=exp(-0.5*(1:100)))
if (sum(degs) %% 2 != 0) { degs[1] <- degs[1] + 1 }
g4 <- degree.sequence.game(degs, method="v1")
all(degree(g4) == degs)

## Power-law degree distribution
## Note, that we correct the degree sequence if its sum is odd
degs <- sample(1:100, 100, replace=TRUE, prob=(1:100)^-2)
if (sum(degs) %% 2 != 0) { degs[1] <- degs[1] + 1 }
g5 <- degree.sequence.game(degs, method="v1")
all(degree(g5) == degs)</pre>
```

diameter

Diameter of a graph

Description

The diameter of a graph is the length of the longest geodesic.

Usage

```
diameter(graph, directed = TRUE, unconnected = TRUE, weights = NULL)
get.diameter (graph, directed = TRUE, unconnected = TRUE, weights = NULL)
farthest.nodes (graph, directed = TRUE, unconnected = TRUE, weights = NULL)
```

Arguments

directed Logical, whether directed or undirected paths are to be considered. This is ignored for undirected graphs.

Unconnected Logical, what to do if the graph is unconnected. If FALSE, the function will return the largest possible diameter which is the number of vertices. If TRUE, the diameters of the connected components will be calculated and the largest one will be returned.

Weights Optional positive weight vector for calculating weighted distances. If the graph

has a weight edge attribute, then this is used by default.

Details

The diameter is calculated by using a breadth-first search like method.

get. diameter returns a path with the actual diameter. If there are many shortest paths of the length of the diameter, then it returns the first one found.

farthest.points returns two vertex ids, the vertices which are connected by the diameter path.

Value

A numeric constant for diameter, a numeric vector for get.diameter and a numeric vector of length two for farthest.nodes.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
shortest.paths
```

Examples

```
g <- graph.ring(10)
g2 <- delete.edges(g, c(0,1,0,9))
diameter(g2, unconnected=TRUE)
diameter(g2, unconnected=FALSE)

## Weighted diameter
set.seed(1)
g <- graph.ring(10)
E(g)$weight <- sample(seq_len(ecount(g)))
diameter(g)
get.diameter(g)
diameter(g, weights=NA)
get.diameter(g, weights=NA)</pre>
```

Drawing graphs

Drawing graphs

Description

The common bits of the three plotting functions plot.igraph, tkplot and rglplot are discussed in this manual page

Details

There are currently three different functions in the igraph package which can draw graph in various ways:

plot.igraph does simple non-interactive 2D plotting to R devices. Actually it is an implementation of the plot generic function, so you can write plot(graph) instead of plot.igraph(graph). As it used the standard R devices it supports every output format for which R has an output device. The list is quite impressing: PostScript, PDF files, XFig files, SVG files, JPG, PNG and of course you can plot to the screen as well using the default devices, or the good-looking anti-aliased Cairo device. See plot.igraph for some more information.

tkplot does interactive 2D plotting using the tcltk package. It can only handle graphs of moderate size, a thousend vertices is probably already too many. Some parameters of the plotted graph can be

changed interactively after issuing the tkplot command: the position, color and size of the vertices and the color and width of the edges. See tkplot for details.

rglplot is an experimental function to draw graphs in 3D using OpenGL. See rglplot for some more information.

Please also check the examples below.

How to specify graphical parameters

There are three ways to give values to the parameters described below, in section 'Parameters'. We give these three ways here in the order of their precedence.

The first method is to supply named arguments to the plotting commands: plot.igraph, tkplot or rglplot. Parameters for vertices start with prefix 'vertex.', parameters for edges have prefix 'edge.', and global parameters have now prefix. Eg. the color of the vertices can be given via argument vertex.color, whereas edge.color sets the color of the edges. layout gives the layout of the graphs.

The second way is to assign vertex, edge and graph attributes to the graph. These attributes have now prefix, ie. the color of the vertices is taken from the color vertex attribute and the color of the edges from the color edge attribute. The layout of the graph is given by the layout graph attribute. (Always assuming that the corresponding command argument is not present.) Setting vertex and edge attributes are handy if you want to assign a given 'look' to a graph, attributes are saved with the graph is you save it with save or in GraphML format with write.graph, so the graph will have the same look after loading it again.

If a parameter is not given in the command line, and the corresponding vertex/edge/graph attribute is also missing then the general igraph parameters handled by <code>igraph.par</code> are also checked. Vertex parameters have prefix 'vertex.', edge parameters are prefixed with 'edge.', general parameters like layout are prefixed with 'plot'. These parameters are useful if you want all or most of your graphs to have the same look, vertex size, vertex color, etc. Then you don't need to set these at every plotting, and you also don't need to assign vertex/edge attributes to every graph.

If the value of a parameter is not specified by any of the three ways described here, its default valued is used, as given in the source code.

Different parameters can have different type, eg. vertex colors can be given as a character vector with color names, or as an integer vector with the color numbers from the current palette. Different types are valid for different parameters, this is discussed in detail in the next section. It is however always true that the parameter can always be a function object in which it will be called with the graph as its single argument to get the "proper" value of the parameter. (If the function returns another function object that will *not* be called again...)

The list of parameters

Vertex parameters first, note that the 'vertex.' prefix needs to be added if they are used as an argument or when setting via <code>igraph.par</code>. The value of the parameter may be scalar valid for every vertex or a vector with a separate value for each vertex. (Shorter vectors are recycled.)

• sizeThe size of the vertex, a numeric scalar or vector, in the latter case each vertex sizes may differ. This vertex sizes are scaled in order have about the same size of vertices for a given value for all three plotting commands. It does not need to be an integer number.

The default value is 15. This is big enough to place short labels on vertices.

• size2The "other" size of the vertex, for some vertex shapes. For the various rectangle shapes this gives the height of the vertices, whereas size gives the width. It is ignored by shapes for which the size can be specified with a single number.

The default is 15.

• colorThe fill color of the vertex. If it is numeric then the current palette is used, see palette. If it is a character vector then it may either contain named colors or RGB specified colors with three or four bytes. All strings starting with '#' are assumed to be RGB color specifications. It is possible to mix named color and RGB colors. Note that tkplot ignores the fourth byte (alpha channel) in the RGB color specification.

The default value is "SkyBlue2".

• frame.colorThe color of the frame of the vertices, the same formats are allowed as for the fill color.

By default it is "black".

• shapeThe shape of the vertex, currently "circle", "square", "csquare", "rectangle", "crectangle", "vrectangle" and "none" are supported, and only by the plot.igraph command. "none" does not draw the vertices at all, although vertex label are plotted (if given). See igraph.vertex.shapes for details about vertex shapes.

By default vertices are drawn as circles.

- labelThe vertex labels. They will be converted to character. Specify NA to omit vertex labels. The default vertex labels are the vertex ids.
- label.familyThe font family to be used for vertex labels. As different plotting commands can used different fonts, they interpret this parameter different ways. The basic notation is, however, understood by both plot.igraph and tkplot. rglplot does not support fonts at all right now, it ignores this parameter completely.

For plot.igraph this parameter is simply passed to text as argument family.

For tkplot some conversion is performed. If this parameter is the name of an exixting Tk font, then that font is used and the label.font and label.cex parameters are ignored complerely. If it is one of the base families (serif, sans, mono) then Times, Helvetica or Courier fonts are used, there are guaranteed to exist on all systems. For the 'symbol' base family we used the symbol font is available, otherwise the first font which has 'symbol' in its name. If the parameter is not a name of the base families and it is also not a named Tk font then we pass it to tkfont.create and hope the user knows what she is doing. The label.font and label.cex parameters are also passed to tkfont.create in this case.

The default value is 'serif'.

• label.fontThe font within the font family to use for the vertex labels. It is interpreted the same way as the font graphical parameter: 1 is plain text, 2 is bold face, 3 is italic, 4 is bold and italic and 5 specifies the symbol font.

For plot. igraph this parameter is simply passed to text.

For tkplot, if the label.family parameter is not the name of a Tk font then this parameter is used to set whether the newly created font should be italic and/or boldface. Otherwise it is ignored.

For rglplot it is ignored.

The default value is 1.

• label.cexThe font size for vertex labels. It is interpreted as a multiplication factor of some device-dependent base font size.

For plot. igraph it is simply passed to text as argument cex.

For tkplot it is multiplied by 12 and then used as the size argument for tkfont.create. The base font is thus 12 for tkplot.

For rglplot it is ignored.

The default value is 1.

• label.dist The distance of the label from the center of the vertex. If it is 0 then the label is centered on the vertex. If it is 1 then the label is displayed beside the vertex.

The default value is 0.

• label.degree It defines the position of the vertex labels, relative to the center of the vertices. It is interpreted as an angle in radian, zero means 'to the right', and 'pi' means to the left, up is -pi/2 and down is pi/2.

The default value is -pi/4.

label.colorThe color of the labels, see the color vertex parameter discussed earlier for the
possible values.

The default value is black.

Edge parameters require to add the 'edge.' prefix when used as arguments or set by igraph.par. The edge parameters:

- colorThe color of the edges, see the color vertex parameter for the possible values. By default this parameter is darkgrey.
- widthThe width of the edges.

The default value is 1.

• arrow.sizeThe size of the arrows. Currently this is a constant, so it is the same for every edge. If a vector is submitted then only the first element is used, ie. if this is taken from an edge attribute then only the attribute of the first edge is used for all arrows. This will likely change in the future.

The default value is 1.

• arrow.widthThe width of the arrows. Currently this is a constant, so it is the same for every edge. If a vector is submitted then only the first element is used, ie. if this is taken from an edge attribute then only the attribute of the first edge is used for all arrows. This will likely change in the future.

This argument is currently only used by plot.igraph.

The default value is 1, which gives the same width as before this option appeared in igraph.

• ItyThe line type for the edges. Almost the same format is accepted as for the standard graphics par, 0 and "blank" mean no edges, 1 and "solid" are for solid lines, the other possible values are: 2 ("dashed"), 3 ("dotted"), 4 ("dotdash"), 5 ("longdash"), 6 ("twodash").

tkplot also accepts standard Tk line type strings, it does not however support "blank" lines, instead of type '0' type '1', ie. solid lines will be drawn.

This argument is ignored for rglplot.

The default value is type 1, a solid line.

- labelThe edge labels. They will be converted to character. Specify NA to omit edge labels. Edge labels are omitted by default.
- label.familyFont family of the edge labels. See the vertex parameter with the same name for the details.

- label.fontThe font for the edge labels. See the corresponding vertex parameter discussed earlier for details.
- label.cexThe font size for the edge labels, see the corresponding vertex parameter for details.
- label.colorThe color of the edge labels, see the color vertex parameters on how to specify colors.
- curvedSpecifies whether to draw curved edges, or not. This can be a logical or a numeric vector or scalar.

First the vector is replicated to have the same length as the number of edges in the graph. Then it is interpreted for each edge separately. A numeric value specifies the curvature of the edge; zero curvature means straight edges, negative values means the edge bends clockwise, positive values the opposite. TRUE means curvature 0.5, FALSE means curvature zero.

This parameter is ignored for loop edges.

The default value is FALSE.

This parameter is currently ignored by rglplot.

• arrow.modeThis parameter can be used to specify for which edges should arrows be drawn. If this parameter is given by the user (in either of the three ways) then it specifies which edges will have forward, backward arrows, or both, or no arrows at all. As usual, this parameter can be a vector or a scalar value. It can be an integer or character type. If it is integer then 0 means no arrows, 1 means backward arrows, 2 is for forward arrows and 3 for both. If it is a character vector then "<" and "<-" specify backward, ">" and "->" forward arrows and "<>" and "<->" and "<->" or "-" to specify no arrows.

Hint: this parameter can be used as a 'cheap' solution for drawing "mixed" graphs: graphs in which some edges are directed some are not. If you want do this, then please create a *directed* graph, because as of version 0.4 the vertex pairs in the edge lists can be swapped in undirected graphs.

By default, no arrows will be drawn for undirected graphs, and for directed graphs, an arrow will be drawn for each edge, according to its direction. This is not very surprising, it is the expected behavior.

• loop.angleGives the angle in radian for plotting loop edges. See the label.dist vertex parameter to see how this is interpreted.

The default value is 0.

• loop.angle2Gives the second angle in radian for plotting loop edges. This is only used in 3D, loop.angle is enough in 2D.

The default value is 0.

Other parameters:

• layout Either a function or a numeric matrix. It specifies how the vertices will be placed on the plot.

If it is a numeric matrix, then the matrix has to have one line for each vertex, specifying its coordinates. The matrix should have at least two columns, for the x and y coordinates, and it can also have third column, this will be the z coordinate for 3D plots and it is ignored for 2D plots.

If a two column matrix is given for the 3D plotting function rglplot then the third column is assumed to be 1 for each vertex.

If layout is a function, this function will be called with the graph as the single parameter to determine the actual coordinates. The function should return a matrix with two or three columns. For the 2D plots the third column is ignored.

The default value is layout.random, ie. a function returning with 2D random placement.

• marginThe amount of empty space below, over, at the left and right of the plot, it is a numeric vector of length four. Usually values between 0 and 0.5 are meaningful, but negative values are also possible, that will make the plot zoom in to a part of the graph. If it is shorter than four then it is recycled.

rglplot does not support this parameter, as it can zoom in and out the graph in a more flexible way.

Its default value is 0.

- rescaleLogical constant, whether to rescale the coordinates to the [-1,1]x[-1,1](x[-1,1]) interval. This parameter is not implemented for tkplot.
 - Defaults to TRUE, the layout will be rescaled.
- aspA numeric constant, it gives the asp parameter for plot, the aspect ratio. Supply 0 here if you don't want to give an aspect ratio. It is ignored by tkplot and rglplot.

 Defaults to 1.
- frameBoolean, whether to plot a frame around the graph. It is ignored by tkplot and rglplot. Defaults to FALSE.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

See Also

```
plot.igraph, tkplot, rglplot, igraph.par
```

Examples

```
## Not run:
# plotting a simple ring graph, all default parameters, except the layout
g <- graph.ring(10)</pre>
g$layout <- layout.circle
plot(g)
tkplot(g)
rglplot(g)
# plotting a random graph, set the parameters in the command arguments
g <- barabasi.game(100)</pre>
plot(g, layout=layout.fruchterman.reingold, vertex.size=4,
     vertex.label.dist=0.5, vertex.color="red", edge.arrow.size=0.5)
# plot a random graph, different color for each component
g <- erdos.renyi.game(100, 1/100)</pre>
comps <- clusters(g)$membership</pre>
colbar <- rainbow(max(comps)+1)</pre>
V(g)$color <- colbar[comps+1]</pre>
```

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```
plot(g, layout=layout.fruchterman.reingold, vertex.size=5, vertex.label=NA)

# plot communities in a graph
g <- graph.full(5) %du% graph.full(5) %du% graph.full(5)
g <- add.edges(g, c(0,5, 0,10, 5,10))
com <- spinglass.community(g, spins=5)
V(g)$color <- com$membership+1
g <- set.graph.attribute(g, "layout", layout.kamada.kawai(g))
plot(g, vertex.label.dist=1.5)

# draw a bunch of trees, fix layout
igraph.par("plot.layout", layout.reingold.tilford)
plot(graph.tree(20, 2))
plot(graph.tree(50, 3), vertex.size=3, vertex.label=NA)
tkplot(graph.tree(50, 2, mode="undirected"), vertex.size=10, vertex.color="green")
## End(Not run)</pre>
```

dyad.census

Dyad census of a graph

Description

Classify dyads in a directed graphs. The relationship between each pair of vertices is measured. It can be in three states: mutual, asymmetric or non-existent.

Usage

```
dyad.census(graph)
```

Arguments

graph

The input graph. A warning is given if it is not directed.

Value

A named numeric vector with three elements:

mut The number of pairs with mutual connections.

asym The number of pairs with non-mutual connections.

null The number of pairs with no connection between them.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Holland, P.W. and Leinhardt, S. A Method for Detecting Structure in Sociometric Data. *American Journal of Sociology*, 76, 492–513. 1970.

Wasserman, S., and Faust, K. *Social Network Analysis: Methods and Applications*. Cambridge: Cambridge University Press. 1994.

See Also

triad.census for the same classification, but with triples.

Examples

```
g <- ba.game(100)
dyad.census(g)</pre>
```

edge.betweenness.community

Community structure detection based on edge betweenness

Description

Many networks consist of modules which are densely connected themselves but sparsely connected to other modules.

Usage

```
edge.betweenness.community (graph, directed = TRUE,
    edge.betweenness = TRUE, merges = TRUE, bridges = TRUE,
    labels = TRUE)
edge.betweenness.community.merges (graph, edges)
```

Arguments

graph The graph to analyze.

directed Logical constant, whether to calculate directed edge betweenness for directed

graphs. It is ignored for undirected graphs.

edge.betweenness

Logical constant, whether to return the edge betweenness of the edges at the

time of their removal.

merges Logical constant, whether to return the merge matrix representing the hierarchi-

cal community structure of the network. This argument is called merges, even if the community structure algorithm itself is divisive and not agglomerative: it builds the tree from top to bottom. There is one line for each merge (ie. split) in matrix, the first line is the first merge (last split). The communities are identified by integer number starting from zero. Community ids smaller than 'N', the number of vertices in the graph, belong to singleton communities, ie. individual

vertices. Before the first merge we have 'N' communities numbered from zero to 'N-1'. The first merge, the first line of the matrix creates community 'N', the second merge creates community 'N+1', etc.

Logical constant, whether to return a list the edge removals which actually split-

ted a component of the graph.

labels Logical constant, whether to contain the labels of the vertices in the result. More

precisely, if the graph has a vertex attribute valled 'name', it will be part of the

result object.

edges Numeric vector, the ids of the edges to be removed from a graph, all edges

should be present in the vector, their order specifies the order of removal.

Details

bridges

The edge betweenness score of an edge measures the number of shortest paths through it, see edge.betweenness for details. The idea of the edge betweenness based community structure detection is that it is likely that edges connecting separate modules have high edge betweenness as all the shortest paths from one module to another must traverse through them. So if we gradually remove the edge with the highest edge betweenness score we will get a hierarchical map, a rooted tree, called a dendrogram of the graph. The leafs of the tree are the individual vertices and the root of the tree represents the whole graph.

edge.betweenness.community performs this algorithm by calculating the edge betweenness of the graph, removing the edge with the highest edge betweenness score, then recalculating edge betweenness of the edges and again removing the one with the highest score, etc.

edge.betweeness.community returns various information collected throught the run of the algorithm. See the return value down here.

edge.betweenness.community.merges gets a list of edges and by gradually removes them from the graph it creates a merge matrix similar to the one returned by edge.betweenness.community.

Value

A named list is returned by edge.betweenness.community, with the following components:

removed.edges Numeric vector, the edges of the graph, in the order of their removal. edge.betweenness

Numeric vector, the edge betweenness value of the removed edges, the order is

the same as in removed.edges.

merges Matrix containing the merges (ie. divisions) the algorithm performed, see the

merges argument for the format.

bridges Numeric vector, the steps (ie. edge removals) which resulted a split of a compo-

nent in the graph.

labels The name argument of the vertices.

Note that some components may be missing or NULL if you do not request them, see the parameters.

A numeric matrix is returned by edge.betweenness.community.merges. The matrix has two column and its format is the same as the merges slot of the result of edge.betweenness.community.

edge.connectivity 53

Author(s)

Gabor Csardi < csardi @rmki.kfki.hu>

References

M Newman and M Girvan: Finding and evaluating community structure in networks, *Physical Review E* 69, 026113 (2004)

See Also

edge.betweenness for the definition and calculation of the edge betweenness, walktrap.community, fastgreedy.community, leading.eigenvector.community for other community detection methods. as.dendrogram in package stats for creating an R dendrogram object from the result of the clustering. See community.to.membership to create the actual communities after a number of edges removed from the network.

Examples

```
g <- barabasi.game(100,m=2)
eb <- edge.betweenness.community(g)

g <- graph.full(10) %du% graph.full(10)
g <- add.edges(g, c(0,10))
eb <- edge.betweenness.community(g)
E(g) [ eb$removed.edges[1] ]</pre>
```

edge.connectivity

Edge connectivity.

Description

The edge connectivity of a graph or two vertices, this is recently also called group adhesion.

Usage

```
edge.connectivity(graph, source=NULL, target=NULL, checks=TRUE)
edge.disjoint.paths(graph, source, target)
graph.adhesion(graph, checks=TRUE)
```

Arguments

graph	The input graph.
source	The id of the source vertex, for edge.connectivity it can be NULL, see details below.
target	The id of the target vertex, for edge.connectivity it can be NULL, see details below.

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checks

Logical constant. Whether to check that the graph is connected and also the degree of the vertices. If the graph is not (strongly) connected then the connectivity is obviously zero. Otherwise if the minimum degree is one then the edge connectivity is also one. It is a good idea to perform these checks, as they can be done quickly compared to the connectivity calculation itself. They were suggested by Peter McMahan, thanks Peter.

Details

The edge connectivity of a pair of vertices (source and target) is the minimum number of edges needed to remove to eliminate all (directed) paths from source to target. edge.connectivity calculates this quantity if both the source and target arguments are given (and not NULL).

The edge connectivity of a graph is the minimum of the edge connectivity of every (ordered) pair of vertices in the graph. edge.connectivity calculates this quantity if neither the source nor the target arguments are given (ie. they are both NULL).

A set of edge disjoint paths between two vertices is a set of paths between them containing no common edges. The maximum number of edge disjoint paths between two vertices is the same as their edge connectivity.

The adhesion of a graph is the minimum number of edges needed to remove to obtain a graph which is not strongly connected. This is the same as the edge connectivity of the graph.

The three functions documented on this page calculate similar properties, more precisely the most general is edge.connectivity, the others are included only for having more descriptive function names.

Value

A scalar real value.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

References

Douglas R. White and Frank Harary: The cohesiveness of blocks in social networks: node connectivity and conditional density, TODO: citation

See Also

```
graph.maxflow, vertex.connectivity, vertex.disjoint.paths, graph.cohesion
```

Examples

```
g <- barabasi.game(100, m=1)
g2 <- barabasi.game(100, m=5)
edge.connectivity(g, 99, 0)
edge.connectivity(g2, 99, 0)
edge.disjoint.paths(g2, 99, 0)
```

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```
g <- erdos.renyi.game(50, 5/50)
g <- as.directed(g)
g <- subgraph(g, subcomponent(g, 1))
graph.adhesion(g)</pre>
```

erdos.renyi.game

Generate random graphs according to the Erdos-Renyi model

Description

This model is very simple, every possible edge is created with the same constant probability.

Usage

Arguments

n	The number of vertices in the graph.
p.or.m	Either the probability for drawing an edge between two arbitrary vertices ($G(n,p)$ graph), or the number of edges in the graph (for $G(n,m)$ graphs).
type	The type of the random graph to create, either gnp $(G(n,p)\ graph)$ or gnm $(G(n,m)\ graph)$.
directed	Logical, whether the graph will be directed, defaults to FALSE.
loops	Logical, whether to add loop edges, defaults to FALSE.
	Additional arguments, ignored.

Details

In G(n,p) graphs, the graph has 'n' vertices and for each edge the probability that it is present in the graph is 'p'.

In G(n,m) graphs, the graph has 'n' vertices and 'm' edges, and the 'm' edges are chosen uniformly randomly from the set of all possible edges. This set includes loop edges as well if the loops parameter is TRUE.

random.graph.game is an alias to this function.

Value

A graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

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References

Erdos, P. and Renyi, A., On random graphs, *Publicationes Mathematicae* 6, 290–297 (1959).

See Also

```
barabasi.game
```

Examples

```
g <- erdos.renyi.game(1000, 1/1000)
degree.distribution(g)</pre>
```

evcent

Find Eigenvector Centrality Scores of Network Positions

Description

evcent takes a graph (graph) and returns the eigenvector centralities of positions v within it

Usage

```
evcent (graph, scale = TRUE, weights = NULL, options = igraph.arpack.default)
```

Arguments

graph Graph to be analyzed.

scale Logical scalar, whether to scale the result to have a maximum score of one. If

no scaling is used then the result vector has unit length in the Euclidean norm.

weights A numerical vector or NULL. This argument can be used to give edge weights

for calculating the weighted eigenvector centrality of vertices. If this is NULL and the graph has a weight edge attribute then that is used. If weights is a numerical vector then it used, even if the graph has a weights edge attribute. If this is NA, then no edge weights are used (even if the graph has a weight edge

attribute.

options A named list, to override some ARPACK options. See arpack for details.

Details

Eigenvector centrality scores correspond to the values of the first eigenvector of the graph adjacency matrix; these scores may, in turn, be interpreted as arising from a reciprocal process in which the centrality of each actor is proportional to the sum of the centralities of those actors to whom he or she is connected. In general, vertices with high eigenvector centralities are those which are connected to many other vertices which are, in turn, connected to many others (and so on). (The perceptive may realize that this implies that the largest values will be obtained by individuals in large cliques (or high-density substructures). This is also intelligible from an algebraic point of view, with the first eigenvector being closely related to the best rank-1 approximation of the adjacency matrix (a

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relationship which is easy to see in the special case of a diagonalizable symmetric real matrix via the SLS^{-1} decomposition).)

From igraph version 0.5 this function uses ARPACK for the underlying computation, see arpack for more about ARPACK in igraph.

Value

A named list with components:

vector A vector containing the centrality scores.

value The eigenvalue corresponding to the calculated eigenvector, i.e. the centrality

scores.

options A named list, information about the underlying ARPACK computation. See

arpack for the details.

WARNING

evcent will not symmetrize your data before extracting eigenvectors; don't send this routine asymmetric matrices unless you really mean to do so.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu> and Carter T. Butts <buttsc@uci.edu> for the manual page

References

Bonacich, P. (1987). Power and Centrality: A Family of Measures. *American Journal of Sociology*, 92, 1170-1182.

Katz, L. (1953). A New Status Index Derived from Sociometric Analysis. *Psychometrika*, 18, 39-43.

Examples

```
#Generate some test data
g <- graph.ring(10, directed=FALSE)
#Compute eigenvector centrality scores
evcent(g)</pre>
```

fastgreedy.community Community structure via greedy optimization of modularity

Description

This function tries to find dense subgraph, also called communities in graphs via directly optimizing a modularity score.

Usage

Arguments

graph The input graph

merges Logical scalar, whether to return the merge matrix.

modularity Logcal scalar, whether to return a vector containing the modularity after each

merge.

weights If not NULL, then a numeric vector of edge weights. The length must match the

number of edges in the graph. By default the 'weight' edge attribute is used as weights. If it is not present, then all edges are considered to have the same

weight.

Details

This function implements the fast greedy modularity optimization algorithm for finding community structure, see A Clauset, MEJ Newman, C Moore: Finding community structure in very large networks, http://www.arxiv.org/abs/cond-mat/0408187 for the details.

Value

A named list with the following members:

merges A matrix with two column, this represents a dendogram and contains all the

merges the algorithm performed. Each line is one merge and it is given by the ids of the two communities merged. The community ids are integer numbers starting from zero and the communities between zero and the number of vertices (N) minus one belong to individual vertices. The first line of the matrix gives the first merge, this merge creates community N, the number of vertices, the second

merge creates community N+1, etc.

modularity A numeric vector containing the modularity value of the community structure

after performing every merge.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu> for the R interface.

References

A Clauset, MEJ Newman, C Moore: Finding community structure in very large networks, http://www.arxiv.org/abs/cond-mat/0408187

See Also

walktrap.community, spinglass.community, leading.eigenvector.community, edge.betweenness.community

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Examples

```
g <- graph.full(5) %du% graph.full(5) %du% graph.full(5)
g <- add.edges(g, c(0,5, 0,10, 5, 10))
fastgreedy.community(g)
# The highest value of modularity is before performing the last two
# merges. So this network naturally has three communities.</pre>
```

forest.fire.game

Forest Fire Network Model

Description

This is a growing network model, which resembles of how the forest fire spreads by igniting trees close by.

Usage

```
forest.fire.game (nodes, fw.prob, bw.factor = 1, ambs = 1, directed = TRUE,
    verbose = igraph.par("verbose"))
```

Arguments

nodes The number of vertices in the graph.

fw.prob The forward burning probability, see details below.

bw. factor The backward burning ratio. The backward burning probability is calculated as

bw.factor*fw.prob.

ambs The number of ambassador vertices.

directed Logical scalar, whether to create a directed graph.

verbose Logical scalar, whether to "draw" a progress bar.

Details

The forest fire model intends to reproduce the following network characteristics, observed in real networks:

- Heavy-tailed in-degree distribution.
- Heavy-tailed out-degree distribution.
- Communities.
- Densification power-law. The network is densifying in time, according to a power-law rule.
- Shrinking diameter. The diameter of the network decreases in time.

The network is generated in the following way. One vertex is added at a time. This vertex connects to (cites) ambs vertices already present in the network, chosen uniformly random. Now, for each cited vertex v we do the following procedure:

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1. We generate two random number, x and y, that are geometrically distributed with means p/(1-p) and rp(1-rp). (p is fw.prob, r is bw.factor.) The new vertex cites x outgoing neighbors and y incoming neighbors of v, from those which are not yet cited by the new vertex. If there are less than x or y such vertices available then we cite all of them.

2. The same procedure is applied to all the newly cited vertices.

Value

A simple graph, possibly directed if the directed argument is TRUE.

Note

The version of the model in the published paper is incorrect in the sense that it cannot generate the kind of graphs the authors claim. A corrected version is available from http://www.cs.cmu.edu/~ijure/pubs/powergrowth-tkdd.pdf, our implementation is based on this.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

References

Jure Leskovec, Jon Kleinberg and Christos Faloutsos. Graphs over time: densification laws, shrinking diameters and possible explanations. *KDD '05: Proceeding of the eleventh ACM SIGKDD international conference on Knowledge discovery in data mining*, 177–187, 2005.

See Also

barabasi. game for the basic preferential attachment model.

Examples

```
g <- forest.fire.game(10000, fw.prob=0.37, bw.factor=0.32/0.37)
dd1 <- degree.distribution(g, mode="in")
dd2 <- degree.distribution(g, mode="out")
if (interactive()) {
  plot(seq(along=dd1)-1, dd1, log="xy")
  points(seq(along=dd2)-1, dd2, col=2, pch=2)
}</pre>
```

get.adjlist

Adjacency lists

Description

Create adjacency lists from a graph, either for adjacent edges or for neighboring vertices

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Usage

```
get.adjlist(graph, mode = c("all", "out", "in", "total"))
get.adjedgelist(graph, mode = c("all", "out", "in", "total"))
```

Arguments

graph The input graph.

mode Character scalar, it gives what kind of adjacent edges/vertices to include in the

lists. 'out' is for outgoing edges/vertices, 'in' is for incoming edges/vertices,

'all' is for both. This argument is ignored for undirected graphs.

Details

get.adjlist returns a list of numeric vectors, which include the ids of neighbor vertices (according to the mode argument) of all vertices.

get.adjedgelist returns a list of numeric vectors, which include the ids of adjacent edgs (according to the mode argument) of all vertices.

Value

A list of numeric vectors.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
get.edgelist, get.adjacency
```

Examples

```
g <- graph.ring(10)
get.adjlist(g)
get.adjedgelist(g)</pre>
```

get.incidence

Incidence matrix of a bipartite graph

Description

This function can return a sparse of dense incidence matrix of a bipartite network. The incidence matrix is an n times m matrix, n and m are the number of vertices of the two kinds.x

```
get.incidence(graph, types=NULL, attr=NULL, names=TRUE, sparse=FALSE)
```

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Arguments

graph	The input graph. The direction of the edges is ignored in directed graphs.
types	An optional vertex type vector to use instead of the 'type' vertex attribute. You must supply this argument if the graph has no 'type' vertex attribute.
attr	Either NULL or a character string giving an edge attribute name. If NULL a traditional incidence matrix is returned. If not NULL then the values of the given edge attribute are included in the incidence matrix. If the graph has multiple edges, the edge attribute of an arbitrarily chosen edge (for the multiple edges) is included.
names	Logical scalar, if TRUE and the vertices in the graph are named (i.e. the graph has a vertex attribute called 'name'), then vertex names will be added to the result as row and column names. Otherwise the ids of the vertices are used as row and column names.
sparse	Logical scalar, if it is TRUE then a sparse matrix is created, you will need the Matrix package for this.

Details

Bipartite graphs have a 'type' vertex attribute in igraph, this is boolean and FALSE for the vertices of the first kind and TRUE for vertices of the second kind.

The vertex ids corresponding to rows and columns in the incidence matrix are returned as row/column names.

Value

A sparse or dense matrix.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
graph.incidence for the opposite operation.
```

Examples

```
g \leftarrow graph.bipartite(c(0,1,0,1,0,0),c(0,1,1,2,2,3)) get.incidence(g)
```

girth 63

|--|

Description

The girth of a graph is the length of the shortest circle in it.

Usage

```
girth(graph, circle=TRUE)
```

Arguments

graph The input graph. It may be directed, but the algorithm searches for undirected

circles anyway.

circle Logical scalar, whether to return the shortest circle itself.

Details

The current implementation works for undirected graphs only, directed graphs are treated as undirected graphs. Loop edges and multiple edges are ignored. If the graph is a forest (ie. acyclic), then zero is returned.

This implementation is based on Alon Itai and Michael Rodeh: Finding a minimum circuit in a graph *Proceedings of the ninth annual ACM symposium on Theory of computing*, 1-10, 1977. The first implementation of this function was done by Keith Briggs, thanks Keith.

Value

A named list with two components:

girth Integer constant, the girth of the graph, or 0 if the graph is acyclic.

circle Numeric vector with the vertex ids in the shortest circle.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

References

Alon Itai and Michael Rodeh: Finding a minimum circuit in a graph *Proceedings of the ninth annual ACM symposium on Theory of computing*, 1-10, 1977

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Examples

```
# No circle in a tree
g <- graph.tree(1000, 3)
girth(g)

# The worst case running time is for a ring
g <- graph.ring(100)
girth(g)

# What about a random graph?
g <- erdos.renyi.game(1000, 1/1000)
girth(g)</pre>
```

graph-isomorphism

Graph Isomorphism

Description

These functions deal with graph isomorphism.

Usage

```
graph.isomorphic(graph1, graph2)
graph.isomorphic.34(graph1, graph2)
graph.isomorphic.bliss(graph1, graph2, sh1="fm", sh2="fm")
graph.isomorphic.vf2(graph1, graph2)
graph.count.isomorphisms.vf2(graph1, graph2)
graph.get.isomorphisms.vf2(graph1, graph2)
graph.subisomorphic.vf2(graph1, graph2)
graph.count.subisomorphisms.vf2(graph1, graph2)
graph.get.subisomorphisms.vf2(graph1, graph2)
graph.get.subisomorphisms.vf2(graph1, graph2)
graph.isoclass(graph)
graph.isoclass.subgraph(graph, vids)
graph.isocreate(size, number, directed=TRUE)
```

Arguments

graph A graph object. graph1,graph2 Graph objects

size A numeric integer giving the number of vertices in the graph to create. Only

three or four are supported right now.

number The number of the isomorphism class of the graph to be created.

directed Whether to create a directed graph.

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sh1	Character constant, the heuristics to use in the BLISS algorithm, for graph1. See the sh argument of canonical.permutation for possible values.
sh2	Character constant, the heuristics to use in the BLISS algorithm, for graph2. See the sh argument of canonical.permutation for possible values.
vids	Numeric vector, the vertex ids of vertices to form the induced subgraph for determining the isomorphism class.

Details

graph.isomorphic decides whether two graphs are isomorphic. The input graphs must be both directed or both undirected. This function is a higher level interface to the other graph isomorphism decision functions. Currently it does the following:

- If the two graphs do not agree in the number of vertices and the number of edges then FALSE is returned.
- 2. Otherwise if the graphs have 3 or 4 vertices, then igraph.isomorphic.34 is called.
- 3. Otherwise if the graphs are directed, then igraph.isomorphic.vf2 is called.
- 4. Otherwise igraph.isomorphic.bliss is called.

igraph.isomorphic.34 decides whether two graphs, both of which contains only 3 or 4 vertices, are isomorphic. It works based on a precalculated and stored table.

igraph.isomorphic.bliss uses the BLISS algorithm by Junttila and Kaski, and it works for undirected graphs. For both graphs the canonical.permutation and then the permute.vertices function is called to transfer them into canonical form; finally the canonical forms are compared.

graph.isomorphic.vf2 decides whethe two graphs are isomorphic, it implements the VF2 algorithm, by Cordella, Foggia et al., see references.

graph.count.isomorphisms.vf2 counts the different isomorphic mappings between graph1 and graph2. (To count automorphisms you can supply the same graph twice, but it is better to call graph.automorphisms.) It uses the VF2 algorithm.

graph.get.isomorphisms.vf2 calculates all isomorphic mappings between graph1 and graph2. It uses the VF2 algorithm.

graph.subisomorphic.vf2 decides whether graph2 is isomorphic to some subgraph of graph1. It uses the VF2 algorithm.

graph.count.subisomorphisms.vf2 counts the different isomorphic mappings between graph2 and the subgraphs of graph1. It uses the VF2 algorithm.

graph.get.subisomorphisms.vf2 calculates all isomorphic mappings between graph2 and the subgraphs of graph1. It uses the VF2 algorithm.

graph.isoclass returns the isomorphism class of a graph, a non-negative integer number. Graphs (with the same number of vertices) having the same isomorphism class are isomorphic and isomorphic graphs always have the same isomorphism class. Currently it can handle only graphs with 3 or 4 vertices.

graph.isoclass.subgraph calculates the isomorphism class of a subgraph of the input graph. Currently it only works for subgraphs with 3 or 4 vertices.

graph.isocreate create a graph from the given isomorphic class. Currently it can handle only graphs with 3 or 4 vertices.

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Value

graph.isomorphic and graph.isomorphic.34 return a logical scalar, TRUE if the input graphs are isomorphic, FALSE otherwise.

graph.isomorphic.bliss returns a named list with elements:

iso	A logical scalar, whether the two graphs are isomorphic.
map12	A numeric vector, an mapping from graph1 to graph2 if iso is TRUE, an empty numeric vector otherwise.
map21	A numeric vector, an mapping from graph2 to graph1 if iso is TRUE, an empty numeric vector otherwise.
info1	Some information about the canonical form calculation for graph1. A named list, see the return value of canonical.permutation for details.
info2	Some information about the canonical form calculation for graph2. A named

list, see the return value of canonical permutation for details.

graph.isomorphic.vf2 returns a names list with three elements:

iso A logical scalar, whether the two graphs are isomorphic.

map12 A numeric vector, an mapping from graph1 to graph2 if iso is TRUE, an empty

numeric vector otherwise.

map21 A numeric vector, an mapping from graph2 to graph1 if iso is TRUE, an empty

numeric vector otherwise.

graph.count.isomorphisms.vf2 returns a numeric scalar, an integer, the number of isomorphic mappings between the two input graphs.

graph.get.isomorphisms.vf2 returns a list of numeric vectors. Every numeric vector is a permutation which takes graph2 into graph1.

graph.subisomorphic.vf2 returns a named list with three elements:

iso Logical scalar, TRUE if a subgraph of graph1 is isomorphic to graph2.

map12 Numeric vector, empty if iso is FALSE. Otherwise a mapping from a subgraph

of graph1 to graph2. -1 denotes the vertices which are not part of the mapping.

map21 Numeric vector, empty if iso is FALSE. Otherwise a mapping from graph2 into

graph1.

graph.count.subisomorphisms.vf2 returns a numeric scalar, an integer.

graph.get.subisomorphisms.vf2 returns a list of numeric vectors, each numeric vector is an isomorphic mapping from graph2 to a subgraph of graph1.

graph.isoclass and graph.isoclass.subgraph return a non-negative integer number.

graph.isocreate returns a graph object.

Note

Functions graph.isoclass, graph.isoclass.subgraph and graph.isocreate are considered experimental and might be reorganized/rewritten later.

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Author(s)

Gabor Csardi < csardi @rmki.kfki.hu>

References

Tommi Junttila and Petteri Kaski: Engineering an Efficient Canonical Labeling Tool for Large and Sparse Graphs, *Proceedings of the Ninth Workshop on Algorithm Engineering and Experiments and the Fourth Workshop on Analytic Algorithms and Combinatorics.* 2007.

LP Cordella, P Foggia, C Sansone, and M Vento: An improved algorithm for matching large graphs, *Proc. of the 3rd IAPR TC-15 Workshop on Graphbased Representations in Pattern Recognition*, 149–159, 2001.

See Also

```
graph.motifs
```

Examples

```
# create some non-isomorphic graphs
g1 <- graph.isocreate(3, 10)
g2 <- graph.isocreate(3, 11)
graph.isoclass(g1)
graph.isoclass(g2)
graph.isomorphic(g1, g2)

# create two isomorphic graphs, by
# permuting the vertices of the first
g1 <- simplify(barabasi.game(30, m=2, directed=FALSE))
g2 <- permute.vertices(g1, sample(vcount(g1))-1)
# should be TRUE
graph.isomorphic(g1, g2)
graph.isomorphic.bliss(g1, g2)
graph.isomorphic.vf2(g1, g2)</pre>
```

graph-motifs

Graph motifs

Description

Graph motifs are small subgraphs with a well-defined strucure. These functions search a graph for various motifs.

```
graph.motifs(graph, size = 3, cut.prob = rep(0, size))
graph.motifs.no(graph, size = 3, cut.prob = rep(0, size))
graph.motifs.est(graph, size = 3, cut.prob = rep(0, size), sample.size =
    vcount(graph)/10, sample = NULL)
```

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Arguments

graph	Graph object, the input graph.
size	The size of the motif, currently 3 and 4 are supported only.
cut.prob	Numeric vector giving the probabilities that the search graph is cut at a certain level. Its length should be the same as the size of the motif (the size argument). By default no cuts are made.
sample.size	The number of vertices to use as a starting point for finding motifs. Only used if the sample argument is NULL.
sample	If not NULL then it specifies the vertices to use as a starting point for finding motifs.

Details

graph.motifs searches a graph for motifs of a given size and returns a numeric vector containing the number of different motifs. The order of the motifs is defined by their isomorphism class, see graph.isoclass.

graph.motifs.no calculates the total number of motifs of a given size in graph.

graph.motifs.est estimates the total number of motifs of a given size in a graph based on a sample.

Value

```
graph.motifs returns a numeric vector.
graph.motifs.no and graph.motifs.est return a numeric constant.
```

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
graph.isoclass
```

Examples

```
g <- barabasi.game(100)
graph.motifs(g, 3)
graph.motifs.no(g, 3)
graph.motifs.est(g, 3)</pre>
```

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graph-operators

Graph operators

Description

Graph operators handle graphs in terms of set theory.

Usage

```
graph.union(...)
graph.disjoint.union(...)
graph.intersection(...)
graph.compose(g1, g2)
graph.difference(big, small)
graph.complementer(graph, loops=FALSE)
x %c% y
x %du% y
x %m% y
x %s% y
x %u% y
```

Arguments

```
... Graph objects or lists of graph objects.

g1,g2,big,small,graph,x,y

Graph objects.

loops Logical constant, whether to generate loop edges.
```

Details

A graph is homogenous binary relation over the set 0, ..., |V|-1, |V| is the number of vertices in the graph. A homogenous binary relation is a set of ordered (directed graphs) or unordered (undirected graphs) pairs taken from 0, ..., |V|-1. The functions documented here handle graphs as relations.

graph.union creates the union of two or more graphs. Ie. only edges which are included in at least one graph will be part of the new graph.

graph.disjoint.union creates a union of two or more disjoint graphs. Thus first the vertices in the second, third, etc. graphs are relabeled to have completely disjoint graphs. Then a simple union is created.

graph.intersection creates the intersection of two or more graphs: only edges present in all graphs will be included.

graph.difference creates the difference of two graphs. Only edges present in the first graph but not in the second will be be included in the new graph.

graph.complementer creates the complementer of a graph. Only edges which are *not* present in the original graph will be included in the new graph.

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graph.compose creates the composition of two graphs. The new graph will contain an (a,b) edge only if there is a vertex c, such that edge (a,c) is included in the first graph and (c,b) is included in the second graph.

These functions do not handle vertex and edge attributes, the new graph will have no attributes at all. Yes, this is considered to be a bug, so will likely change in the near future.

Value

A new graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
g1 <- graph.ring(10)
g2 <- graph.star(10, mode="undirected")
graph.union(g1, g2)
graph.disjoint.union(g1, g2)
graph.intersection(g1, g2)
graph.difference(g1, g2)
graph.complementer(g2)
graph.compose(g1, g2)</pre>
```

graph.adjacency

Create graphs from adjacency matrices

Description

graph.adjacency is a flexible function for creating igraph graphs from adjacency matrices.

Usage

Arguments

adjmatrix

A square adjacency matrix. From igraph version 0.5.1 this can be a sparse matrix created with the Matrix package.

mode

Character scalar, specifies how igraph should interpret the supplied matrix. See also the weighted argument, the interpretation depends on that too. Possible values are: directed, undirected, upper, lower, max, min, plus. See details below.

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weighted This argument specifies whether to create a weighted graph from an adjacency

matrix. If it is NULL then an unweighted graph is created and the elements of the adjacency matrix gives the number of edges between the vertices. If it is a character constant then for every non-zero matrix entry an edge is created and the value of the entry is added as an edge attribute named by the weighted argument. If it is TRUE then a weighted graph is created and the name of the

edge attribute will be weight. See also details below.

diag Logical scalar, whether to include the diagonal of the matrix in the calculation.

If this is FALSE then the diagonal is zero-d out first.

add.colnames Character scalar, whether to add the column names as vertex attributes. If it is

'NULL' (the default) then, if present, column names are added as vertex attribute 'name'. If 'NA' then they will not be added. If a character constant, then it gives

the name of the vertex attribute to add.

add.rownames Character scalar, whether to add the row names as vertex attributes. Possible

values the same as the previous argument. By default row names are not added. If 'add.rownames' and 'add.colnames' specify the same vertex attribute, then

the former is ignored.

Details

graph.adjacency creates a graph from an adjacency matrix.

The order of the vertices are preserved, i.e. the vertex corresponding to the first row will be vertex 0 in the graph, etc.

graph.adjacency operates in two main modes, depending on the weighted argument.

If this argument is NULL then an unweighted graph is created and an element of the adjacency matrix gives the number of edges to create between the two corresponding vertices. The details depend on the value of the mode argument:

- directedThe graph will be directed and a matrix element gives the number of edges between two vertices.
- undirectedThis is exactly the same as max, for convenience. Note that it is *not* checked whether the matrix is symmetric.
- maxAn undirected graph will be created and max(A(i,j), A(j,i)) gives the number of edges.
- upperAn undirected graph will be created, only the upper right triangle (including the diagonal) is used for the number of edges.
- lowerAn undirected graph will be created, only the lower left triangle (including the diagonal) is used for creating the edges.
- minundirected graph will be created with min(A(i,j), A(j,i)) edges between vertex i and j.
- plus undirected graph will be created with A(i,j)+A(j,i) edges between vertex i and j.

If the weighted argument is not NULL then the elements of the matrix give the weights of the edges (if they are not zero). The details depend on the value of the mode argument:

• directedThe graph will be directed and a matrix element gives the edge weights.

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• undirectedFirst we check that the matrix is symmetric. It is an error if not. Then only the upper triangle is used to create a weighted undirected graph.

- maxAn undirected graph will be created and max(A(i,j), A(j,i)) gives the edge weights.
- upperAn undirected graph will be created, only the upper right triangle (including the diagonal) is used (for the edge weights).
- lowerAn undirected graph will be created, only the lower left triangle (including the diagonal) is used for creating the edges.
- minAn undirected graph will be created, min(A(i,j), A(j,i)) gives the edge weights.
- plus An undirected graph will be created, A(i,j)+A(j,i) gives the edge weights.

Value

An igraph graph object.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

See Also

graph and graph. formula for other ways to create graphs.

Examples

```
adjm <- matrix(sample(0:1, 100, replace=TRUE, prob=c(0.9,0.1)), nc=10)
g1 <- graph.adjacency( adjm )</pre>
adjm <- matrix(sample(0:5, 100, replace=TRUE,</pre>
                       prob=c(0.9,0.02,0.02,0.02,0.02,0.02)), nc=10)
g2 <- graph.adjacency(adjm, weighted=TRUE)</pre>
E(g2)$weight
## various modes for weighted graphs, with some tests
nzs <- function(x) sort(x [x!=0])</pre>
adjm <- matrix(runif(100), 10)</pre>
adjm[adjm<0.5]<-0
g3 <- graph.adjacency((adjm + t(adjm))/2, weighted=TRUE,
                       mode="undirected")
g4 <- graph.adjacency(adjm, weighted=TRUE, mode="max")</pre>
all(nzs(pmax(adjm, t(adjm))[upper.tri(adjm)]) == sort(E(g4)$weight))
g5 <- graph.adjacency(adjm, weighted=TRUE, mode="min")</pre>
all(nzs(pmin(adjm, t(adjm))[upper.tri(adjm)]) == sort(E(g5)$weight))
g6 <- graph.adjacency(adjm, weighted=TRUE, mode="upper")</pre>
all(nzs(adjm[upper.tri(adjm)]) == sort(E(g6)$weight))
g7 <- graph.adjacency(adjm, weighted=TRUE, mode="lower")
all(nzs(adjm[lower.tri(adjm)]) == sort(E(g7)$weight))
```

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```
g8 <- graph.adjacency(adjm, weighted=TRUE, mode="plus")</pre>
d2 \leftarrow function(x) \{ diag(x) \leftarrow diag(x)/2; x \}
all(nzs((d2(adjm+t(adjm)))[lower.tri(adjm)]) == sort(E(g8)$weight))
g9 <- graph.adjacency(adjm, weighted=TRUE, mode="plus", diag=FALSE)
d0 \leftarrow function(x) \{ diag(x) \leftarrow 0 \}
all(nzs((d0(adjm+t(adjm)))[lower.tri(adjm)]) == sort(E(g9)$weight))
## row/column names
rownames(adjm) <- sample(letters, nrow(adjm))</pre>
colnames(adjm) <- seq(ncol(adjm))</pre>
g10 <- graph.adjacency(adjm, weighted=TRUE, add.rownames="code")</pre>
summary(g10)
```

graph.automorphisms

Number of automorphisms

Description

Calculate the number of automorphisms of a graph, i.e. the number of isomorphisms to itself.

Usage

```
graph.automorphisms(graph, sh="fm")
```

Arguments

graph

The input graph, it is treated as undirected.

sh

The splitting heuristics for the BLISS algorithm. Possible values are: 'f': first non-singleton cell, 'f1': first largest non-singleton cell, 'fs': first smallest nonsingleton cell, 'fm': first maximally non-trivially connected non-singleton cell, 'flm': first largest maximally non-trivially connected non-singleton cell, 'fsm':

first smallest maximally non-trivially connected non-singleton cell.

Details

An automorphism of a graph is a permutation of its vertices which brings the graph into itself.

This function calculates the number of automorphism of a graph using the BLISS algorithm. See also the BLISS homepage at http://www.tcs.hut.fi/Software/bliss/index.html.

Value

A named list with the following members:

The size of the automorphism group of the input graph, as a string. This number group_size

is exact if igraph was compiled with the GMP library, and approximate other-

wise.

The number of nodes in the search tree. nof_nodes

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```
nof_leaf_nodes The number of leaf nodes in the search tree.

nof_bad_nodes Number of bad nodes.

nof_canupdates Number of canrep updates.

max_level Maximum level.
```

Author(s)

Tommi Juntilla <google@for.it> for BLISS and Gabor Csardi <csardi@rmki.kfki.hu> for the igraph glue code and this manual page.

References

Tommi Junttila and Petteri Kaski: Engineering an Efficient Canonical Labeling Tool for Large and Sparse Graphs, *Proceedings of the Ninth Workshop on Algorithm Engineering and Experiments and the Fourth Workshop on Analytic Algorithms and Combinatorics*. 2007.

See Also

```
canonical.permutation, permute.vertices
```

Examples

```
## A ring has n*2 automorphisms, you can "turn" it by 0-9 vertices
## and each of these graphs can be "flipped"
g <- graph.ring(10)
graph.automorphisms(g)</pre>
```

graph.bipartite

Create a bipartite graph

Description

A bipartite graph has two kinds of vertices and connections are only allowed between different kinds.

Usage

```
graph.bipartite(types, edges, directed=FALSE)
```

Arguments

types	A vector giving the vertex types. It will be coerced into boolean. The length of the vector gives the number of vertices in the graph.
edges	A vector giving the edges of the graph, the same way as for the regular graph function. It is checked that the edges indeed connect vertices of different kind, according to the supplied types vector.
directed	Whether to create a directed graph, boolean constant. Note that by default undirected graphs are created, as this is more common for bipartite graphs.

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Details

Bipartite graphs have a 'type' vertex attribute in igraph, this is boolean and FALSE for the vertices of the first kind and TRUE for vertices of the second kind.

graph.bipartite basically does three things. First it checks tha edges vector against the vertex types. Then it creates a graph using the edges vector and finally it adds the types vector as a vertex attribute called type.

Value

A bipartite igraph graph. In other words, an igraph graph that has a vertex attribute type.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
graph to create one-mode networks
```

Examples

```
g <- graph.bipartite( rep(0:1,length=10), c(0:9))
print(g, v=TRUE)</pre>
```

graph.constructors

Various methods for creating graphs

Description

These method can create various (mostly regular) graphs: empty graphs, graphs with the given edges, graphs from adjacency matrices, star graphs, lattices, rings, trees.

Usage

Usage

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```
graph.ring(n, directed = FALSE, mutual = FALSE, circular=TRUE)
graph.tree(n, children = 2, mode="out")
graph.full(n, directed = FALSE, loops = FALSE)
graph.full.citation(n, directed = TRUE)
graph.atlas(n)
graph.edgelist(el, directed=TRUE)
graph.extended.chordal.ring(n, w)
```

Arguments

edges Numeric vector defining the edges, the first edge points from the first element to

the second, the second edge from the third to the fourth, etc.

directed Logical, if TRUE a directed graph will be created. Note that for while most con-

structors the default is TRUE, for graph.lattice and graph.ring it is FALSE. For graph.star the mode argument should be used for creating an undirected

graph.

n The number of vertices in the graph for most functions.

For graph this parameter is ignored if there is a bigger vertex id in edges. This means that for this function it is safe to supply zero here if the vertex with the

largest id is not an isolate.

For graph. atlas this is the number (id) of the graph to create.

mode For graph.star it defines the direction of the edges, in: the edges point to

the center, out: the edges point from the center, undirected: the edges are

undirected.

For igraph, tree this parameter defines the direction of the edges, out indicates that the edges point from the parent to the children, in indicates that they point from the children to their parents, while undirected creates an undirected

graph.

center For graph. star the center vertex of the graph, by default the first vertex.

dimvector A vector giving the size of the lattice in each dimension, for graph.lattice.

nei The distance within which (inclusive) the neighbors on the lattice will be con-

nected. This parameter is not used right now.

mutual Logical, if TRUE directed lattices will be mutually connected.

circular Logical, if TRUE the lattice or ring will be circular.

length Integer constant, for regular lattices, the size of the lattice in each dimension.

dim Integer constant, the dimension of the lattice.

children Integer constant, the number of children of a vertex (except for leafs) for graph. tree.

loops If TRUE also loops edges (self edges) are added.

graph An object.

el An edge list, a two column matrix, character or numeric. See details below.

w A matrix which specifies the extended chordal ring. See details below.

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Details

All these functions create graphs in a deterministic way.

graph. empty is the simplest one, this creates an empty graph.

graph creates a graph with the given edges.

graph.star creates a star graph, in this every single vertex is connected to the center vertex and nobody else.

graph.lattice is a flexible function, it can create lattices of arbitrary dimensions, periodic or unperiodic ones.

graph.ring is actually a special case of graph.lattice, it creates a one dimensional circular lattice.

graph. tree creates regular trees.

graph. full simply creates full graphs.

graph.full.citation creates a full citation graph. This is a directed graph, where every i->j edge is present if and only if j<i. If directed=FALSE then the graph is just a full graph.

graph.atlas creates graphs from the book An Atlas of Graphs by Roland C. Read and Robin J. Wilson. The atlas contains all undirected graphs with up to seven vertices, numbered from 0 up to 1252. The graphs are listed:

- 1. in increasing order of number of nodes;
- 2. for a fixed number of nodes, in increasing order of the number of edges;
- 3. for fixed numbers of nodes and edges, in increasing order of the degree sequence, for example 111223 < 112222;
- 4. for fixed degree sequence, in increasing number of automorphisms.

graph.edgelist creates a graph from an edge list. Its argument is a two-column matrix, each row defines one edge. If it is a numeric matrix then its elements are interpreted as vertex ids. If it is a character matrix then it is interpreted as symbolic vertex names and a vertex id will be assigned to each name, and also a name vertex attribute will be added.

graph.extended.chordal.ring creates an extended chordal ring. An extended chordal ring is regular graph, each node has the same degree. It can be obtained from a simple ring by adding some extra edges specified by a matrix. Let p denote the number of columns in the 'W' matrix. The extra edges of vertex i are added according to column i mod p in 'W'. The number of extra edges is the number of rows in 'W': for each row j an edge i->i+w[ij] is added if i+w[ij] is less than the number of total nodes. See also Kotsis, G: Interconnection Topologies for Parallel Processing Systems, PARS Mitteilungen 11, 1-6, 1993.

Value

Every function documented here returns a graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

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See Also

graph.adjacency to create graphs from adjacency matrices, graph.formula for a handy way to create small graphs, graph.data.frame for an easy way to create graphs with many edge/vertex attributes.

Examples

```
g1 <- graph.empty()
g2 <- graph( c(1,2,2,3,3,4,5,6), directed=FALSE )
g5 <- graph.star(10, mode="out")
g6 <- graph.lattice(c(5,5,5))
g7 <- graph.lattice(length=5, dim=3)
g8 <- graph.ring(10)
g9 <- graph.tree(10, 2)
g10 <- graph.full(5, loops=TRUE)
g11 <- graph.full.citation(10)
g12 <- graph.atlas(sample(0:1252, 1))
e1 <- matrix( c("foo", "bar", "bar", "foobar"), nc=2, byrow=TRUE)
g13 <- graph.extended.chordal.ring(15, matrix(c(3,12,4,7,8,11), nr=2))</pre>
```

graph.coreness

K-core decomposition of graphs

Description

The k-core of graph is a maximal subgraph in which each vertex has at least degree k. The coreness of a vertex is k if it belongs to the k-core but not to the (k+1)-core.

Usage

```
graph.coreness(graph, mode=c("all", "out", "in"))
```

Arguments

graph The input graph, it can be directed or undirected

mode The type of the core in directed graphs. Character constant, possible values: in:

in-cores are computed, out: out-cores are computed, all: the corresponding undirected graph is considered. This argument is ignored for undirected graphs.

Details

The k-core of a graph is the maximal subgraph in which every vertex has at least degree k. The cores of a graph form layers: the (k+1)-core is always a subgraph of the k-core.

This function calculates the coreness for each vertex.

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Value

Numeric vector of integer numbers giving the coreness of each vertex.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

References

Vladimir Batagelj, Matjaz Zaversnik: An O(m) Algorithm for Cores Decomposition of Networks, 2002

Seidman S. B. (1983) Network structure and minimum degree, *Social Networks*, 5, 269–287.

See Also

degree

Examples

```
g <- graph.ring(10)
g <- add.edges(g, c(0,1, 1,2, 0,2))
graph.coreness(g)</pre>
```

graph.data.frame

Creating igraph graphs from data frames

Description

This function creates an igraph graph from one or two data frames containing the (symbolic) edge list and edge/vertex attributes.

Usage

```
graph.data.frame(d, directed=TRUE, vertices=NULL)
```

Arguments

d	A data frame containing a symbolic edge list in the first two columns. Additional
	columns are considered as edge attributes.
directed	Logical scalar, whether or not to create a directed graph.

vertices A data frame with vertex metadata, or NULL. See details below.

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Details

graph.data.frame creates igraph graphs from one or two data frames. It has two modes of operatation, depending whether the vertices argument is NULL or not.

If vertices is NULL, then the first two columns of d are used as a symbolic edge list and additional columns as edge attributes. The names of the attributes are taken from the names of the columns.

If vertices is not NULL, then it must be a data frame giving vertex metadata. The first column of vertices is assumed to contain symbolic vertex names, this will be added to the graphs as the 'name' vertex attribute. Other columns will be added as additional vertex attributes. If vertices is not NULL then the symbolic edge list given in d is checked to contain only vertex names listed in vertices.

Typically, the data frames are exported from some speadsheat software like Excel and are imported into R via read.table, read.delimor read.csv.

Value

An igraph graph object.

Note

NA elements in the first two columns 'd' are replaced by the string "NA" before creating the graph. This means that all NAs will correspond to a single vertex.

NA elements in the first column of 'vertices' are also replaced by the string "NA", but the rest of 'vertices' is not touched. In other words, vertex names (=the first column) cannot be NA, but other vertex attributes can.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

graph.constructors and graph.formula for other ways to create graphs, read.table to read in tables from files.

graph.de.bruijn 81

graph.de.bruijn

De Bruijn graphs.

Description

De Bruijn graphs are labeled graphs representing the overlap of strings.

Usage

```
graph.de.bruijn(m,n)
```

Arguments

m Integer scalar, the size of the alphabet. See details below.

n Integer scalar, the length of the labels. See details below.

Details

A de Bruijn graph represents relationships between strings. An alphabet of m letters are used and strings of length n are considered. A vertex corresponds to every possible string and there is a directed edge from vertex v to vertex w if the string of v can be transformed into the string of w by removing its first letter and appending a letter to it.

Please note that the graph will have m to the power n vertices and even more edges, so probably you don't want to supply too big numbers for m and n.

De Bruijn graphs have some interesting properties, please see another source, eg. Wikipedia for details.

Value

A graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

```
graph.kautz,line.graph
```

```
# de Bruijn graphs can be created recursively by line graphs as well
g <- graph.de.bruijn(2,1)
graph.de.bruijn(2,2)
line.graph(g)</pre>
```

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graph.density	Graph density
graph.density	Grapn aensity

Description

The density of a graph is the ratio of the number of edges and the number of possible edges.

Usage

```
graph.density(graph, loops=FALSE)
```

Arguments

graph The input graph.

loops Logical constant, whether to allow loop edges in the graph. If this is TRUE then

self loops are considered to be possible. If this is FALSE then we assume that the graph does not contain any loop edges and that loop edges are not meaningful.

Details

Note that this function may return strange results for graph with multiple edges, density is ill-defined for graphs with multiple edges.

Value

A real constant. This function returns NaN (=0.0/0.0) for an empty graph with zero vertices.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

References

Wasserman, S., and Faust, K. (1994). Social Network Analysis: Methods and Applications. Cambridge: Cambridge University Press.

See Also

vcount, ecount, simplify to get rid of the multiple and/or loop edges.

```
g1 <- graph.empty(n=10)
g2 <- graph.full(n=10)
g3 <- erdos.renyi.game(n=10, 0.4)
# loop edges
g <- graph( c(0,1, 1,1, 1,2) )</pre>
```

graph.famous 83

graph.famous

Creating named graphs

Description

There are some famous, named graphs, sometimes counterexamples to some conjecture or unique graphs with given features. These can be created with this function

Usage

```
graph.famous(name)
```

Arguments

name

Character constant giving the name of the graph. It is case insensitive.

Details

graph. famous knows the following graphs:

- BullThe bull graph, 5 vertices, 5 edges, resembles to the head of a bull if drawn properly.
- ChvatalThis is the smallest triangle-free graph that is both 4-chromatic and 4-regular. According to the Grunbaum conjecture there exists an m-regular, m-chromatic graph with n vertices for every m>1 and n>2. The Chvatal graph is an example for m=4 and n=12. It has 24 edges.
- CoxeterA non-Hamiltonian cubic symmetric graph with 28 vertices and 42 edges.
- CubicalThe Platonic graph of the cube. A convex regular polyhedron with 8 vertices and 12 edges.
- DiamondA graph with 4 vertices and 5 edges, resembles to a schematic diamond if drawn properly.
- Dodecahedral, DodecahedronAnother Platonic solid with 20 vertices and 30 edges.
- FolkmanThe semisymmetric graph with minimum number of vertices, 20 and 40 edges. A semisymmetric graph is regular, edge transitive and not vertex transitive.
- FranklinThis is a graph whose embedding to the Klein bottle can be colored with six colors, it is a counterexample to the neccessity of the Heawood conjecture on a Klein bottle. It has 12 vertices and 18 edges.
- FruchtThe Frucht Graph is the smallest cubical graph whose automorphism group consists only of the identity element. It has 12 vertices and 18 edges.
- GrotzschThe Grötzsch graph is a triangle-free graph with 11 vertices, 20 edges, and chromatic number 4. It is named after German mathematician Herbert Grötzsch, and its existence demonstrates that the assumption of planarity is necessary in Grötzsch's theorem that every triangle-free planar graph is 3-colorable.

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• HeawoodThe Heawood graph is an undirected graph with 14 vertices and 21 edges. The graph is cubic, and all cycles in the graph have six or more edges. Every smaller cubic graph has shorter cycles, so this graph is the 6-cage, the smallest cubic graph of girth 6.

- HerschelThe Herschel graph is the smallest nonhamiltonian polyhedral graph. It is the unique such graph on 11 nodes, and has 18 edges.
- HouseThe house graph is a 5-vertex, 6-edge graph, the schematic draw of a house if drawn properly, basicly a triangle of the top of a square.
- HouseXThe same as the house graph with an X in the square. 5 vertices and 8 edges.
- Icosahedral, Icosahedron A Platonic solid with 12 vertices and 30 edges.
- Krackhardt_KiteA social network with 10 vertices and 18 edges. Krackhardt, D. Assessing the Political Landscape: Structure, Cognition, and Power in Organizations. Admin. Sci. Quart. 35, 342-369, 1990.
- LeviThe graph is a 4-arc transitive cubic graph, it has 30 vertices and 45 edges.
- McGeeThe McGee graph is the unique 3-regular 7-cage graph, it has 24 vertices and 36 edges.
- MeredithThe Meredith graph is a quartic graph on 70 nodes and 140 edges that is a counterexample to the conjecture that every 4-regular 4-connected graph is Hamiltonian.
- Noperfectmatching A connected graph with 16 vertices and 27 edges containing no perfect matching. A matching in a graph is a set of pairwise non-adjacent edges; that is, no two edges share a common vertex. A perfect matching is a matching which covers all vertices of the graph.
- NonlineA graph whose connected components are the 9 graphs whose presence as a vertex-induced subgraph in a graph makes a nonline graph. It has 50 vertices and 72 edges.
- Octahedral, OctahedronPlatonic solid with 6 vertices and 12 edges.
- PetersenA 3-regular graph with 10 vertices and 15 edges. It is the smallest hypohamiltonian graph, ie. it is non-hamiltonian but removing any single vertex from it makes it Hamiltonian.
- RobertsonThe unique (4,5)-cage graph, ie. a 4-regular graph of girth 5. It has 19 vertices and 38 edges.
- SmallestcyclicgroupA smallest nontrivial graph whose automorphism group is cyclic. It has 9 vertices and 15 edges.
- Tetrahedral, TetrahedronPlatonic solid with 4 vertices and 6 edges.
- ThomassenThe smallest hypotraceable graph, on 34 vertices and 52 edges. A hypotracable graph does not contain a Hamiltonian path but after removing any single vertex from it the remainder always contains a Hamiltonian path. A graph containing a Hamiltonian path is called tracable.
- TutteTait's Hamiltonian graph conjecture states that every 3-connected 3-regular planar graph is Hamiltonian. This graph is a counterexample. It has 46 vertices and 69 edges.
- Uniquely3colorableReturns a 12-vertex, triangle-free graph with chromatic number 3 that is uniquely 3-colorable.
- WaltherAn identity graph with 25 vertices and 31 edges. An identity graph has a single graph automorphism, the trivial one.

Value

A graph object.

graph.formula 85

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

graph can create arbitrary graphs, see also the other functions on the its manual page for creating special graphs.

Examples

graph.formula

Creating (small) graphs via a simple interface

Description

This function is useful if you want to create a small (named) graph quickly, it works for both directed and undirected graphs.

Usage

```
graph.formula(...)
```

Arguments

... The formulae giving the structure of the graph, see details below.

Details

graph. formula is very handy for creating small graphs quickly. You need to supply one or more R expressions giving the structure of the graph. The expressions consist of vertex names and edge operators. An edge operator is a sequence of '-' and '+' characters, the former is for the edges and the latter is used for arrow heads. The edges can be arbitrarily long, ie. you may use as many '-' characters to "draw" them as you like.

If all edge operators consist of only '-' characters then the graph will be undirected, whereas a single '+' character implies a directed graph.

Let us see some simple examples. Without arguments the function creates an empty graph:

```
graph.formula()
```

A simple undirected graph with two vertices called 'A' and 'B' and one edge only:

86 graph.formula

```
graph.formula(A-B)
```

Remember that the length of the edges does not matter, so we could have written the following, this creates the same graph:

```
graph.formula( A----B )
```

If you have many disconnected components in the graph, separate them with commas. You can also give isolate vertices.

```
graph.formula( A--B, C--D, E--F, G--H, I, J, K )
```

The ':' operator can be used to define vertex sets. If an edge operator connects two vertex sets then every edge from the first set will be connected to every edge in the second set. The following form creates a full graph, including loop edges:

```
graph.formula( A:B:C:D -- A:B:C:D )
```

In directed graphs, edges will be created only if the edge operator includes a arrow head ('+') at the end of the edge:

```
graph.formula( A -+ B -+ C )
graph.formula( A +- B -+ C )
graph.formula( A +- B -- C )
```

Thus in the third example no edge is created between vertices B and C.

Mutual edges can be also created with a simple edge operator:

```
graph.formula( A +-+ B +---+ C ++ D + E)
```

Note again that the length of the edge operators is arbitrary, '+', '++' and '+----+' have exactly the same meaning.

If the vertex names include spaces or other special characters then you need to quote them:

```
graph.formula( "this is" +- "a silly" -+ "graph here" )
```

You can include any character in the vertex names this way, even '+' and '-' characters. See more examples below.

Value

A new graph object.

graph.full.bipartite 87

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

graph for more general graph creation methods.

Examples

```
# A simple undirected graph
g <- graph.formula( Alice-Bob-Cecil-Alice, Daniel-Cecil-Eugene, Cecil-Gordon )</pre>
# Another undirected graph, ":" notation
g2 <- graph.formula( Alice-Bob:Cecil:Daniel, Cecil:Daniel-Eugene:Gordon )</pre>
g2
# A directed graph
g3 <- graph.formula( Alice +-+ Bob --+ Cecil +-- Daniel,
                     Eugene --+ Gordon:Helen )
g3
# A graph with isolate vertices
g4 <- graph.formula( Alice -- Bob -- Daniel, Cecil:Gordon, Helen )
g4
V(g4)$name
# "Arrows" can be arbitrarily long
g5 <- graph.formula( Alice +----+ Bob )
g5
# Special vertex names
g6 <- graph.formula( "+" -- "-", "*" -- "/", "%%" -- "%/%" )
g6
```

graph.full.bipartite Create a full bipartite graph

Description

Bipartite graphs are also called two-mode by some. This function creates a bipartite graph in which every possible edge is present.

Usage

```
graph.full.bipartite (n1, n2, directed = FALSE, mode = c("all", "out", "in"))
```

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Arguments

n1	The number of vertices of the first kind.
n2	The number of vertices of the second kind.
directed	Logical scalar, whether the graphs is directed.
mode	Scalar giving the kind of edges to create for di

Scalar giving the kind of edges to create for directed graphs. If this is 'out' then all vertices of the first kind are connected to the others; 'in' specifies the opposite direction; 'all' creates mutual edges. This argument is ignored for

undirected graphs.x

Details

Bipartite graphs have a 'type' vertex attribute in igraph, this is boolean and FALSE for the vertices of the first kind and TRUE for vertices of the second kind.

Value

An igraph graph, with the 'type' vertex attribute set.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

See Also

```
graph. full for creating one-mode full graphs
```

Examples

```
g <- graph.full.bipartite(2, 3)
g2 <- graph.full.bipartite(2, 3, dir=TRUE)
g3 <- graph.full.bipartite(2, 3, dir=TRUE, mode="in")
g4 <- graph.full.bipartite(2, 3, dir=TRUE, mode="all")</pre>
```

graph.graphdb

Load a graph from the graph database for testing graph isomorphism.

Description

This function downloads a graph from a database created for the evaluation of graph isomorphism testing algorithms.

Usage

```
graph.graphdb (url = NULL, prefix = "iso", type = "r001", nodes = NULL,
    pair = "A", which = 0, base = "http://cneurocvs.rmki.kfki.hu/graphdb/gzip",
    compressed = TRUE, directed = TRUE)
```

graph.graphdb 89

Arguments

url If not NULL it is a complete URL with the file to import.

prefix Gives the prefix. See details below. Possible values: iso, i2, si4, si6, mcs10,

mcs30, mcs50, mcs70, mcs90.

type Gives the graph type identifier. See details below. Possible values: r001, r005,

r01, r02, m2D, m2Dr2, m2Dr4, m2Dr6 m3D, m3Dr2, m3Dr4, m3Dr6, m4D, m4Dr2,

m4Dr4, m4Dr6, b03, b03m, b06, b06m, b09, b09m.

nodes The number of vertices in the graph.

pair Specifies which graph of the pair to read. Possible values: A and B.

which Gives the number of the graph to read. For every graph type there are a number

of actual graphs in the database. This argument specifies which one to read.

The base address of the database. See details below.

compressed Logical constant, if TRUE than the file is expected to be compressed by gzip. If

url is NULL then a '.gz' suffix is added to the filename.

directed Logical constant, whether to create a directed graph.

Details

graph. graphdb reads a graph from the graph database from an FTP or HTTP server or from a local copy. It has two modes of operation:

If the url argument is specified then it should the complete path to a local or remote graph database file. In this case we simply call read.graph with the proper arguments to read the file.

If url is NULL, and this is the default, then the filename is assembled from the base, prefix, type, nodes, pair and which arguments.

See the documentation for the graph database at http://amalfi.dis.unina.it/graph/db/doc/graphdbat.html for the actual format of a graph database file and other information.

Value

A new graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

M. De Santo, P. Foggia, C. Sansone, M. Vento: A large database of graphs and its use for benchmarking graph isomorphism algorithms, *Pattern Recognition Letters*, Volume 24, Issue 8 (May 2003)

See Also

read.graph, graph.isomorphic.vf2

90 graph.incidence

Examples

```
## Not run:
g <- graph.graphdb(prefix="iso", type="r001", nodes=20, pair="A",
  which=10, compressed=TRUE)
g2 <- graph.graphdb(prefix="iso", type="r001", nodes=20, pair="B",
  which=10, compressed=TRUE)
graph.isomorphic.vf2(g, g2)
g3 <- graph.graphdb(url="http://cneurocvs.rmki.kfki.hu/graphdb/gzip/iso/bvg/b06m/iso_b06m_m200.A09.gz")
## End(Not run)
```

graph.incidence

Create graphs from an incidence matrix

Description

graph.incidence creates a bipartite igraph graph from an incidence matrix.

Usage

```
graph.incidence(incidence, directed = FALSE, mode = c("all", "out",
    "in", "total"), multiple = FALSE, weighted = NULL, add.names = NULL)
```

Arguments

incidence The input incidence matrix. It can also be a sparse matrix from the Matrix

package.

directed Logical scalar, whether to create a directed graph.

mode A character constant, defines the direction of the edges in directed graphs, ig-

> nored for undirected graphs. If 'out', then edges go from vertices of the first kind (corresponding to rows in the incidence matrix) to vertices of the second kind (columns in the incidence matrix). If 'in', then the opposite direction is

used. If 'all' or 'total', then mutual edges are created.

multiple Logical scalar, specifies how to interpret the matrix elements. See details below.

weighted This argument specifies whether to create a weighted graph from the incidence

> matrix. If it is NULL then an unweighted graph is created and the multiple argument is used to determine the edges of the graph. If it is a character constant then for every non-zero matrix entry an edge is created and the value of the entry is added as an edge attribute named by the weighted argument. If it is TRUE then a weighted graph is created and the name of the edge attribute will be 'weight'.

add.names A character constant, NA or NULL. graph.incidence can add the row and col-

umn names of the incidence matrix as vertex attributes. If this argument is NULL (the default) and the incidence matrix has both row and column names, then these are added as the 'name' vertex attribute. If you want a different vertex attribute for this, then give the name of the attributes as a character string. If this

argument is NA, then no vertex attributes (other than type) will be added.

graph.kautz 91

Details

Bipartite graphs have a 'type' vertex attribute in igraph, this is boolean and FALSE for the vertices of the first kind and TRUE for vertices of the second kind.

graph.incidence can operate in two modes, depending on the multiple argument. If it is FALSE then a single edge is created for every non-zero element in the incidence matrix. If multiple is TRUE, then the matrix elements are rounded up to the closest non-negative integer to get the number of edges to create between a pair of vertices.

Value

A bipartite igraph graph. In other words, an igraph graph that has a vertex attribute type.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
graph.bipartite for another way to create bipartite graphs
```

Examples

```
inc <- matrix(sample(0:1, 15, repl=TRUE), 3, 5)
colnames(inc) <- letters[1:5]
rownames(inc) <- LETTERS[1:3]
graph.incidence(inc)</pre>
```

graph.kautz

Kautz graphs

Description

Kautz graphs are labeled graphs representing the overlap of strings.

Usage

```
graph.kautz(m,n)
```

Arguments

- m Integer scalar, the size of the alphabet. See details below.
- n Integer scalar, the length of the labels. See details below.

92 graph.knn

Details

A Kautz graph is a labeled graph, vertices are labeled by strings of length n+1 above an alphabet with m+1 letters, with the restriction that every two consecutive letters in the string must be different. There is a directed edge from a vertex v to another vertex w if it is possible to transform the string of v into the string of w by removing the first letter and appending a letter to it.

Kautz graphs have some interesting properties, see eg. Wikipedia for details.

Value

A graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>, the first version in R was written by Vincent Matossian.

See Also

```
graph.de.bruijn, line.graph
```

Examples

```
line.graph(graph.kautz(2,1))
graph.kautz(2,2)
```

graph.knn

Average nearest neighbor degree

Description

Calculate the average nearest neighbor degree of the given vertices and the same quantity in the function of vertex degree

Usage

```
graph.knn(graph, vids=V(graph), weights=NULL)
```

Arguments

graph	The input graph. It can be directed, but it will be treated as undirected, i.e. the direction of the edges is ignored.
vids	The vertices for which the calculation is performed. Normally it includes all vertices. Note, that if not all vertices are given here, then both 'knn' and 'knnk' will be calculated based on the given vertices only.
weights	Weight vector. If the graph has a weight edge attribute, then this is used by default. If this argument is given, then vertex strength (see graph.strength) is

used instead of vertex degree. But note that knnk is still given in the function of the normal vertex degree.

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Details

Note that for zero degree vertices the answer in 'knn' is NaN (zero divided by zero), the same is true for 'knnk' if a given degree never appears in the network.

Value

A list with two members:

knn A numeric vector giving the average nearest neighbor degree for all vertices in

vids.

knnk A numeric vector, its length is the maximum (total) vertex degree in the graph.

The first element is the average nearest neighbor degree of vertices with degree

one, etc.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Alain Barrat, Marc Barthelemy, Romualdo Pastor-Satorras, Alessandro Vespignani: The architecture of complex weighted networks, Proc. Natl. Acad. Sci. USA 101, 3747 (2004)

```
# Some trivial ones
g <- graph.ring(10)
graph.knn(g)
g2 <- graph.star(10)
graph.knn(g2)

# A scale-free one, try to plot 'knnk'
g3 <- simplify(ba.game(1000, m=5))
graph.knn(g3)

# A random graph
g4 <- random.graph.game(1000, p=5/1000)
graph.knn(g4)

# A weighted graph
g5 <- graph.star(10)
E(g5)$weight <- seq(ecount(g5))
graph.knn(g5)</pre>
```

94 graph.laplacian

graph.	l an l	lacian

Graph Laplacian

Description

The Laplacian of a graph.

Usage

```
graph.laplacian(graph, normalized=FALSE)
```

Arguments

graph The input graph.

normalized Whether to calculate the normalized Laplacian. See definitions below.

Details

The Laplacian Matrix of a graph is a symmetric matrix having the same number of rows and columns as the number of vertices in the graph and element (i,j) is d[i], the degree of vertex i if i=j, -1 if i!=j and there is an edge between vertices i and j and 0 otherwise.

A normalized version of the Laplacian Matrix is similar: element (i,j) is 1 if i==j, -1/sqrt(d[i] d[j]) if i!=j and there is an edge between vertices i and j and 0 otherwise.

Value

A square matrix with as many rows as the number of vertices in the input graph.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

```
g <- graph.ring(10)
graph.laplacian(g)
graph.laplacian(g, norm=TRUE)</pre>
```

graph.lcf 95

graph.lcf

Creating a graph from LCF notation

Description

LCF is short for Lederberg-Coxeter-Frucht, it is a concise notation for 3-regular Hamiltonian graphs. It constists of three parameters, the number of vertices in the graph, a list of shifts giving additional edges to a cycle backbone and another integer giving how many times the shifts should be performed. See http://mathworld.wolfram.com/LCFNotation.html for details.

Usage

```
graph.lcf(n, shifts, repeats)
```

Arguments

n Integer, the number of vertices in the graph.

shifts Integer vector, the shifts.

repeats Integer constant, how many times to repeat the shifts.

Value

A graph object.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

See Also

graph can create arbitrary graphs, see also the other functions on the its manual page for creating special graphs.

```
# This is the Franklin graph:
g1 <- graph.lcf(12, c(5,-5), 6)
g2 <- graph.famous("Franklin")
graph.isomorphic.vf2(g1, g2)</pre>
```

96 graph.maxflow

graph.maxflow	Maximum flow in a network	
---------------	---------------------------	--

Description

In a graph where each edge has a given flow capacity the maximal flow between two vertices is calculated.

Usage

Arguments

graph The input graph.

source The id of the source vertex.

target The id of the target vertex (sometimes also called sink).

capacity Vector giving the capacity of the edges. If this is NULL (the default) then the

capacity edge attribute is used.

value.only Logical scalar, if TRUE only the minumum cut value is returned, if FALSE the

edges in the cut and a the two (or more) partitions are also returned. This cur-

rently only works for undirected graphs.

Details

graph.maxflow calculates the maximum flow between two vertices in a weighted (ie. valued) graph. A flow from source to target is an assignment of non-negative real numbers to the edges of the graph, satisfying two properties: (1) for each edge the flow (ie. the assigned number) is not more than the capacity of the edge (the capacity parameter or edge attribute), (2) for every vertex, except the source and the target the incoming flow is the same as the outgoing flow. The value of the flow is the incoming flow of the target vertex. The maximum flow is the flow of maximum value.

graph.mincut calculates the minimum st-cut between two vertices in a graph (if the source and target arguments are given) or the minimum cut of the graph (if both source and target are NULL).

The minimum st-cut between source and target is the minimum total weight of edges needed to remove to eliminate all paths from source to target.

The minimum cut of a graph is the minimum total weight of the edges needed to remove to separate the graph into (at least) two components. (Which is to make the graph *not* strongly connected in the directed case.)

The maximum flow between two vertices in a graph is the same as the minimum st-cut, so graph.maxflow and graph.mincut essentially calculate the same quantity, the only difference is that graph.mincut

graph.strength 97

can be invoked without giving the source and target arguments and then minimum of all possible minimum cuts is calculated.

Starting from version 0.5 igraph can return the edges in the minimum cut for undirected graphs.

Value

A numeric constant, the maximum flow, or the minimum cut, except if value.only=FALSE for graph.mincut. In this case a named list with components:

value Numeric scalar, the cut value.
cut Numeric vector, the edges in the cut.

partition1 The vertices in the first partition after the cut edges are removed. Note that

these vertices might be actually in different components (after the cut edges are

removed), as the graph may fall apart into more than two components.

partition2 The vertices in the second partition after the cut edges are removed. Note that

these vertices might be actually in different components (after the cut edges are

removed), as the graph may fall apart into more than two components.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

References

A. V. Goldberg and R. E. Tarjan: "A New Approach to the Maximum Flow Problem" Journal of the ACM 35:921-940, 1988.

See Also

```
shortest.paths, edge.connectivity, vertex.connectivity
```

Examples

```
g <- graph.ring(100)
graph.mincut(g, capacity=rep(1,vcount(g)))
graph.mincut(g, value.only=FALSE, capacity=rep(1,vcount(g)))</pre>
```

graph.strength

Strength or weighted vertex degree

Description

Summing up the edge weights of the adjacent edges for each vertex.

Usage

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Arguments

graph	The input graph.
vids	The vertices for which the strength will be calculated.
mode	Character string, "out" for out-degree, "in" for in-degree or "all" for the sum of the two. For undirected graphs this argument is ignored.
loops	Logical; whether the loop edges are also counted.
weights	Weight vector. If the graph has a weight edge attribute, then this is used by default. If the graph does not have a weight edge attribute and this argument is NULL, then a warning is given and degree is called.

Value

A numeric vector giving the strength of the vertices.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Alain Barrat, Marc Barthelemy, Romualdo Pastor-Satorras, Alessandro Vespignani: The architecture of complex weighted networks, Proc. Natl. Acad. Sci. USA 101, 3747 (2004)

See Also

degree for the unweighted version.

```
g <- graph.star(10)
E(g)$weight <- seq(ecount(g))
graph.strength(g)
graph.strength(g, mode="out")
graph.strength(g, mode="in")

# No weights, a warning is given
g <- graph.ring(10)
graph.strength(g)</pre>
```

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graph.structure	Method for structural manipulation of graphs

Description

These are the methods for simple manipulation of graphs: adding and deleting edges and vertices.

Usage

```
add.edges(graph, edges, ..., attr=list())
add.vertices(graph, nv, ..., attr=list())
delete.edges(graph, edges)
delete.vertices(graph, v)
```

Arguments

graph	The graph to work on.
edges	Edge sequence, the edges to remove.
•••	Additional parameters will be added as edge/vertex attributes. Note that these arguments have to be named.
attr	Additional edge/vertex attributes to add. This will be concatenated to the other supplied attributes.
nv	Numeric constant, the number of vertices to add.
V	Vector sequence, the vertices to remove.

Details

add. edges adds the specified edges to the graph. The ids of the vertices are preserved. The additionally supplied named arguments will be added as edge attributes for the new edges. If an attribute was not present in the original graph, its value for the original edges will be NA.

add.vertices adds the specified number of isolate vertices to the graph. The ids of the old vertices are preserved. The additionally supplied named arguments will be added as vertex attributes for the new vertices. If an attribute was not present in the original graph, its value is set to NA for the original vertices.

delete.edges removes the specified edges from the graph. If a specified edge is not present, the function gives an error message, and the original graph remains unchanged. The ids of the vertices are preserved.

delete.vertices removes the specified vertices from the graph together with their adjacent edges. The ids of the vertices are *not* preserved.

Value

The new graph.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
g <- graph.ring(10)
add.edges(g, c(1,5,2,6) )
delete.edges(g, E(g, P=c(0,9, 1,2)) )
delete.vertices(g, c(1,6,7) )</pre>
```

Graphs from adjacency lists

Create graphs from adjacency lists

Description

An adjacency list is a list of numeric vectors, containing the neighbor vertices for each vertex. This function creates an igraph graph object from such a list.

Usage

```
graph.adjlist(adjlist, directed = TRUE, duplicate = TRUE)
```

Arguments

adjlist	The adjacency list. It should be consistent, i.e. the maximum throughout all vectors in the list must be less than the number of vectors (=the number of vertices in the graph). Note that the list is expected to be 0-indexed.
directed	Logical scalar, whether or not to create a directed graph.
duplicate	Logical scalar. For undirected graphs it gives whether edges are included in the list twice. E.g. if it is TRUE then for an undirected {A,B} edge graph.adjlist expects A included in the neighbors of B and B to be included in the neighbors of

This argument is ignored if directed is TRUE.

Details

Adjacency lists are handy if you intend to do many (small) modifications to a graph. In this case adjacency lists are more efficient than igraph graphs.

The idea is that you convert your graph to an adjacency list by get.adjlist, do your modifications to the graphs and finally create again an igraph graph by calling graph.adjlist.

Value

An igraph graph object.

grg.game 101

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
get.edgelist
```

Examples

```
## Directed
g <- graph.ring(10, dir=TRUE)
al <- get.adjlist(g, mode="out")
g2 <- graph.adjlist(al)
graph.isomorphic(g, g2)

## Undirected
g <- graph.ring(10)
al <- get.adjlist(g)
g2 <- graph.adjlist(al, dir=FALSE)
graph.isomorphic(g, g2)
ecount(g2)
g3 <- graph.adjlist(al, dir=FALSE, duplicate=FALSE)
ecount(g3)
is.multiple(g3)</pre>
```

grg.game

Geometric random graphs

Description

Generate a random graph based on the distance of random point on a unit square

Usage

```
grg.game(nodes, radius, torus=FALSE, coords=FALSE)
```

Arguments

nodes	The number of vertices in the graph.
radius	The radius within which the vertices will be connected by an edge.
torus	Logical constant, whether to use a torus instead of a square.
coords	Logical scalar, whether to add the positions of the vertices as vertex attributes

called 'x' and 'y'.

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Details

First a number of points are dropped on a unit square, these points correspond to the vertices of the graph to create. Two points will be connected with an undirected edge if they are closer to each other in Euclidean norm than a given radius. If the torus argument is TRUE then a unit area torus is used instead of a square.

Value

A graph object. If coords is TRUE then with vertex attributes 'x' and 'y'.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>, first version was written by Keith Briggs <keith.briggs@bt.com>

See Also

```
random.graph.game
```

Examples

```
g <- grg.game(1000, 0.05, torus=FALSE)
g2 <- grg.game(1000, 0.05, torus=TRUE)</pre>
```

growing.random.game

Growing random graph generation

Description

This function creates a random graph by simulating its stochastic evolution.

Usage

```
growing.random.game(n, m=1, directed=TRUE, citation=FALSE)
```

Arguments

n Numeric constant, number of vertices in the graph.

m Numeric constant, number of edges added in each time step.

directed Logical, whether to create a directed graph.

citation Logical. If TRUE a citation graph is created, ie. in each time step the added edges

are originating from the new vertex.

Details

This is discrete time step model, in each time step a new vertex is added to the graph and m new edges are created. If citation is FALSE these edges are connecting two uniformly randomly chosen vertices, otherwise the edges are connecting new vertex to uniformly randomly chosen old vertices.

Value

A new graph object.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

See Also

```
barabasi.game, erdos.renyi.game
```

Examples

```
g <- growing.random.game(500, citation=FALSE)
g2 <- growing.random.game(500, citation=TRUE)</pre>
```

```
igraph from/to graphNEL conversion
```

Convert igraph graphs to graphNEL objects or back

Description

The graphNEL class is defined in the graph package, it is another way to represent graphs. These functions are provided to convert between the igraph and the graphNEL objects.

Usage

Arguments

graphNEL	The graphNEL graph.
name	Logical scalar, whether to add graphNEL vertex names as an igraph vertex attribute called 'name'.
weight	Logical scalar, whether to add graphNEL edge weights as an igraph edge attribute called 'weight'. (graphNEL graphs are always weighted.)
unlist.attrs	Logical scalar. graphNEL attribute query functions return the values of the attributes in R lists, if this argument is TRUE (the default) these will be converted to atomic vectors, whenever possible, before adding them to the igraph graph.
graph	An igraph graph object.

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Details

igraph.from.graphNEL takes a graphNEL graph and converts it to an igraph graph. It handles all graph/vertex/edge attributes. If the graphNEL graph has a vertex attribute called 'name' it will be used as igraph vertex attribute 'name' and the graphNEL vertex names will be ignored.

Because graphNEL graphs poorly support multiple edges, the edge attributes of the multiple edges are lost: they are all replaced by the attributes of the first of the multiple edges.

igraph. to.graphNEL converts and igraph graph to a graphNEL graph. It converts all graph/vertex/edge attributes. If the igraph graph has a vertex attribute 'name', then it will be used to assign vertex names in the graphNEL graph. Otherwise igraph vertex ids will be used for this purpose.

Value

```
igraph.from.graphNEL returns an igraph graph object.
igraph.to.graphNEL returns a graphNEL graph object.
```

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

See Also

```
get.adjacency, graph.adjacency, get.adjlist and graph.adjlist.
```

Examples

```
g <- graph.ring(10)
V(g)$name <- letters[1:10]
GNEL <- igraph.to.graphNEL(g)
g2 <- igraph.from.graphNEL(GNEL)
g2</pre>
```

igraph-parameters

Parameters for the igraph package

Description

igraph has some parameters which (usually) affect the behavior of many functions. These can be set for the whole session via igraph.par.

Usage

```
igraph.par(parid, parvalue = NULL)
```

Arguments

parid The name of the parameter. See the currently used parameters below.

parvalue The new value of the parameter. If NULL then the current value of the parameter

is listed.

igraph.sample 105

Details

The currently used parameters in alphabetical order:

• print.edge.attributesLogical constant, whether to print edge attributes when printing graphs. Defaults to FALSE.

- print.graph.attributesLogical constant, whether to print graph attributes when printing graphs. Defaults to FALSE.
- print.vertex.attriubutesLogical constant, whether to print vertex attributes when printing graphs. Defaults to FALSE.
- verboseLogical constant, whether igraph functions should talk more than minimal. Eg. if TRUE thne some functions will use progress bars while computing. Defaults to FALSE.

Value

If parvalue is NULL then the current value of the parameter is returned. Otherwise the new value of the parameter is returned invisibly.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

Examples

```
igraph.par("verbose", FALSE)
layout.kamada.kawai( graph.ring(10) )
igraph.par("verbose", TRUE)
```

igraph.sample

Sampling a random integer sequence

Description

This function provides a very efficient way to pull an integer random sample sequence from an integer interval.

Usage

```
igraph.sample(low, high, length)
```

Arguments

The lower limit of the interval (inclusive).highThe higher limit of the interval (inclusive).

length The length of the sample.

Details

The algorithm runs in O(length) expected time, even if high-low is big. It is much faster (but of course less general) than the builtin sample function of R.

Value

An increasing numeric vector containing integers, the sample.

Author(s)

```
Gabor Csardi < csardi@rmki.kfki.hu>
```

References

Jeffrey Scott Vitter: An Efficient Algorithm for Sequential Random Sampling, ACM Transactions on Mathematical Software, 13/1, 58–67.

Examples

```
rs <- igraph.sample(1, 100000000, 10)
rs
```

independent.vertex.sets

Independent vertex sets

Description

A vertex set is called independent if there no edges between any two vertices in it. These functions find independent vertex sets in undirected graphs

Usage

```
independent.vertex.sets(graph, min=NULL, max=NULL)
largest.independent.vertex.sets(graph)
maximal.independent.vertex.sets(graph)
independence.number(graph)
```

Arguments

graph	The input graph, directed graphs are considered as undirected, loop edges and multiple edges are ignored.
min	Numeric constant, limit for the minimum size of the independent vertex sets to find. NULL means no limit.
max	Numeric constant, limit for the maximum size of the independent vertex sets to find. NULL means no limit.

independent.vertex.sets 107

Details

independent.vertex.sets finds all independent vertex sets in the network, obeying the size limitations given in the min and max arguments.

largest.independent.vertex.sets finds the largest independent vertex sets in the graph. An independent vertex set is largest if there is no independent vertex set with more vertices.

maximal.independent.vertex.sets finds the maximal independent vertex sets in the graph. An independent vertex set is maximal if it cannot be extended to a larger independent vertex set. The largest independent vertex sets are maximal, but the opposite is not always true.

independece.number calculate the size of the largest independent vertex set(s).

These functions use the algorithm described by Tsukiyama et al., see reference below.

Value

independent.vertex.sets, largest.independent.vertex.sets and maximal.independent.vertex.sets return a list containing numeric vertex ids, each list element is an independent vertex set.

independence. number returns an integer constant.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> ported it from the Very Nauty Graph Library by Keith Briggs <google@for.it> and Gabor Csardi <csardi@rmki.kfki.hu> wrote the R interface and this manual page.

References

S. Tsukiyama, M. Ide, H. Ariyoshi and I. Shirawaka. A new algorithm for generating all the maximal independent sets. *SIAM J Computing*, 6:505–517, 1977.

See Also

cliques

```
# A quite dense graph
g <- erdos.renyi.game(100, 0.8)
independence.number(g)
independent.vertex.sets(g, min=independence.number(g))
largest.independent.vertex.sets(g)
# Empty graph
subgraph(g, largest.independent.vertex.sets(g)[[1]])
length(maximal.independent.vertex.sets(g))</pre>
```

is.bipartite

is.bipartite

Decide whether a graph is bipartite

Description

This function decides whether the vertices of a network can be mapped to two vertex types in a way that no vertices of the same type are connected.

Usage

```
is.bipartite(graph)
```

Arguments

graph

The input graph.

Details

A bipartite graph in igraph has a 'type' vertex attribute giving the two vertex types.

This function simply checks whether a graph *could* be bipartite. It tries to find a mapping that gives a possible division of the vertices into two classes, such that no two vertices of the same class are connected by an edge.

The existence of such a mapping is equivalent of having no circuits of odd length in the graph. A graph with loop edges cannot bipartite.

Note that the mapping is not necessarily unique, e.g. if the graph has at least two components, then the vertices in the separate components can be mapped independently.

Value

A named list with two elements:

res A logical scalar, TRUE if the can be bipartite, FALSE otherwise.

type A possibly vertex type mapping, a logical vector. If no such mapping exists,

then an empty vector.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

```
## A ring has just one loop, so it is fine
g <- graph.ring(10)
is.bipartite(g)

## A star is fine, too
g2 <- graph.star(10)</pre>
```

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```
is.bipartite(g2)
## A graph containing a triangle is not fine
g3 <- graph.ring(10)
g3 <- add.edges(g3, c(0,2))
is.bipartite(g3)</pre>
```

is.igraph

Is this object a graph?

Description

is.graph makes its decision based on the class attribute of the object.

Usage

```
is.igraph(graph)
```

Arguments

graph

An R object.

Value

A logical constant, TRUE if argument graph is a graph object.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

Examples

```
g <- graph.ring(10)
is.igraph(g)
is.igraph(numeric(10))</pre>
```

is.multiple

is.multiple

Find the multiple or loop edges in a graph

Description

A loop edge is an edge from a vertex to itself. An edge is a multiple edge if it has exactly the same head and tail vertices as another edge. A graph without multiple and loop edges is called a simple graph.

Usage

```
is.loop(graph, eids=E(graph))
is.multiple(graph, eids=E(graph))
count.multiple(graph, eids=E(graph))
```

Arguments

graph The input graph.

eids The edges to which the query is restricted. By default this is all edges in the

graph.

Details

Note that the semantics for is.multiple and count.multiple is different. is.multiple gives TRUE for all occurences of a multiple edge except for one. Ie. if there are three i-j edges in the graph then is.multiple returns TRUE for only two of them while count.multiple returns '3' for all three.

See the examples for getting rid of multiple edges while keeping their original multiplicity as an edge attribute.

Value

is.loop and is.multiple return a logical vector. count.multiple returns a numeric vector.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

simplify to eliminate loop and multiple edges.

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Examples

```
# Loops
g \leftarrow graph(c(0,0,1,1,2,2,3,4))
is.loop(g)
# Multiple edges
g <- barabasi.game(10, m=3)
is.multiple(g)
count.multiple(g)
is.multiple(simplify(g))
all(count.multiple(simplify(g)) == 1)
# Direction of the edge is important
is.multiple(graph(c(0,1,1,0)))
is.multiple(graph( c(0,1, 1,0), dir=FALSE ))
# Remove multiple edges but keep multiplicity
g <- barabasi.game(10, m=3)</pre>
E(g)$weight <- count.multiple(g)</pre>
g <- simplify(g)
any(is.multiple(g))
E(g)$weight
```

is.mutual

Find mutual edges in a directed graph

Description

This function checks the reciproc pair of the supplied edges.

Usage

```
is.mutual(graph, es = E(graph))
```

Arguments

graph The input graph.

es Edge sequence, the edges that will be probed. By default is includes all edges in

the order of their ids.

Details

In a directed graph an (A,B) edge is mutual if the graph also includes a (B,A) directed edge.

Note that multi-graphs are not handled properly, i.e. if the graph contains two copies of (A,B) and one copy of (B,A), then these three edges are considered to be mutual.

Undirected graphs contain only mutual edges by definition.

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Value

A logical vector of the same length as the number of edges supplied.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

reciprocity, dyad. census if you just want some statistics about mutual edges.

Examples

```
g <- erdos.renyi.game(10,50,type="gnm",directed=TRUE)
reciprocity(g)
dyad.census(g)
is.mutual(g)
sum(is.mutual(g))/2 == dyad.census(g)$mut</pre>
```

iterators

Vertex and edge sequences and iterators

Description

Vertex and edge sequences are central concepts of igraph.

Usage

```
V(graph)
E(graph, P=NULL, path=NULL, directed=TRUE)
```

Arguments

graph	A graph object.	
Р	Numeric vector for selecting edges by giving their end points. See details below	
path	Numeric vector, this is for selecting all edges along a path. See also details below.	
directed	Logcal constant, can be supplied only if either P or path is also present and	

gives whether the pairs or the path are directed or not.

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Details

It is often needed to perform an operation on a subset of vertices of edges in a graph.

A vertex sequence is simply a vector containing vertex ids, but it has a special class attribute which makes it possible to perform graph specific operations on it, like selecting a subset of the vertices based on some vertex attributes.

A vertex sequence is created by V(g) this selects are vertices in increasing vertex id order. A vertex sequence can be indexed by a numeric vector, and a subset of all vertices can be selected.

Vertex sequences provide powerful operations for dealing with vertex attributes. A vertex sequence can be indexed with the '\$' operator to select (or modify) the attributes of a subset of vertices. A vertex sequence can be indexed by a logical expression, and this expression may contain the names of the vertex attributes and ordinary variables as well. The return value of such a construct (ie. a vertex sequence indexed by a logical expression) is another vertex sequence containing only vertices from the original sequence for which the expression evaluates to TRUE.

Let us see an example to make everything clear. We assign random numbers between 1 and 100 to the vertices, and select those vertices for which the number is less than 50. We set the color of these vertices to red.

There is a similar notation for edges. E(g) selects all edges from the 'g' graph. Edge sequences can be also indexed with logical expressions containing edge attributes:

```
g <- graph.ring(10)
E(g)$weight <- runif(ecount(g))
E(g)$width <- 1
E(g)[ weight >= 0.5 ]$width <- 3
plot(g, layout=layout.circle, edge.width=E(g)$width, edge.color="black")</pre>
```

It is important to note that, whenever we use iterators to assign new attribute values, the new values are recycled. So in the following example half of the vertices will be black, the other half red, in an alternated way.

```
g <- graph.ring(10)
V(g)$color <- c("black", "red")
plot(g, layout=layout.circle)</pre>
```

For the recycling, the standard R rules apply and a warning is given if the number of items to replace is not a multiple of the replacement length. E.g. the following code gives a warning, because we set the attribute for three vertices, but supply only two values:

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```
g <- graph.tree(10)
V(g)$color <- "grey"
V(g)[0:2]$color <- c("green", "blue")</pre>
```

If a new vertex/edge attribute is created with an assignment, but only a subset of of vertices are specified, then the rest is set to NA if the new values are in a vector and to NULL if they are a list. Try the following:

```
V(g)[5]$foo <- "foo"
V(g)$foo
V(g)[5]$bar <- list(bar="bar")
V(g)$bar</pre>
```

There are some special functions which are only defined in the indexing expressions of vertex and edge sequences. For vertex sequences these are: nei, adj, from and to, innei and outnei.

nei has a mandatory and an optional argument, the first is another vertex sequence, the second is a mode argument similar to that of the neighbors function. nei returns a logical vector of the same length as the indexed vertex sequence and evaluates to TRUE for those vertices only which have a neighbor vertex in the vertex sequence supplied as a parameter. Thus for selecting all neighbors of vertices 0 and 1 one can write:

```
V(g) [ nei( 0:1 ) ]
```

The mode argument (just like for neighbors) gives the type of the neighbors to be included, it is interpreted only in directed graphs, and defaults to all types of neighbors. See the example below. innei(v) is a shorthand for the 'incoming' neighbors (nei(v, mode="in")), and outnei(v) is a shorthand for the 'outgoing' neighbors (nei(v, mode="out")).

adj takes an edge sequence as an argument and returns TRUE for vertices which have at least one adjacent edge in it.

from and to are similar to adj but only edges originated at (from) or pointing to (to) are taken into account.

For edge sequences the special functions are: adj, from, to, %--%, %->% and %<-%.

adj takes a vertex sequence as an argument and returns NULL for edges which have an adjacent vertex in it.

from and to are similar to adj, but only vertices at the source (from) or target (to) of the edge.

The %--% operator selects edges connecting two vertex sequences, the direction of the edges is ignored. The %->% is different only for directed graphs and only edges pointing from the left hand side argument to the right hand side argument are selected. %<-% is exactly the opposite, it selects edges pointing from the right hand side to the left hand side.

E has two optional arguments: P and path. If given P can be used to select edges based on their end points, eg. E(g, P=c(0,1)) selects edge 0->1.

path can be used to select all edges along a path. The path should be given with the visited vertex ids in the appropriate order.

See also the examples below.

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Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
# mean degree of vertices in the largest cluster in a random graph
g <- erdos.renyi.game(100, 2/100)</pre>
c <- clusters(g)</pre>
vsl <- which(which.max(c$csize)-1==c$membership)-1</pre>
mean(degree(g, vsl))
# set the color of these vertices to red, others greens
V(g)$color <- "green"
V(g)[vsl]$color <- "red"
## Not run: plot(g, vertex.size=3, labels=NA, vertex.color="a:color",
              layout=layout.fruchterman.reingold)
## End(Not run)
# the longest geodesic within the largest cluster
long <- numeric()</pre>
for (v in vsl) {
  paths <- get.shortest.paths(g, from=v, to=vsl)</pre>
  fl <- paths[[ which.max(sapply(paths, length)) ]]</pre>
  if (length(fl) > length(long)) {
    long <- fl
}
\# the mode argument of the nei() function
g \leftarrow graph(c(0,1, 1,2, 1,3, 3,1))
V(g)[ nei( c(1,3) ) ]
V(g)[ nei( c(1,3), "in") ]
V(g)[ nei( c(1,3), "out") ]
# operators for edge sequences
g <- barabasi.game(100, power=0.3)</pre>
E(g) [ 0:2 %--% 1:5 ]
E(g) [ 0:2 %->% 1:5 ]
E(g) [ 0:2 %<-% 1:5 ]
# the edges along the diameter
g <- barabasi.game(100, directed=FALSE)</pre>
d <- get.diameter(g)</pre>
E(g, path=d)
```

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Description

Kleinberg's hub and authority scores.

Usage

```
authority.score (graph, scale = TRUE, options = igraph.arpack.default)
hub.score (graph, scale = TRUE, options = igraph.arpack.default)
```

Arguments

graph The input graph.

scale Logical scalar, whether to scale the result to have a maximum score of one. If

no scaling is used then the result vector has unit length in the Euclidean norm.

options A named list, to override some ARPACK options. See arpack for details.

Details

The authority scores of the vertices are defined as the principal eigenvector of $A^T A$, where A is the adjacency matrix of the graph.

The hub scores of the vertices are defined as the principal eigenvector of AA^T , where A is the adjacency matrix of the graph.

Obviously, for undirected matrices the adjacency matrix is symmetric and the two scores are the same.

Value

A named list with members:

vector The authority/hub scores of the vertices.

value The corresponding eigenvalue of the calculated principal eigenvector.

options Some information about the ARPACK computation, it has the same members as

the options member returned by arpack, see that for documentation.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

J. Kleinberg. Authoritative sources in a hyperlinked environment. *Proc. 9th ACM-SIAM Symposium on Discrete Algorithms*, 1998. Extended version in *Journal of the ACM* 46(1999). Also appears as IBM Research Report RJ 10076, May 1997.

See Also

evcent for eigenvector centrality, page.rank for the Page Rank scores. arpack for the underlining machinery of the computation.

Examples

```
## An in-star
g <- graph.star(10)
hub.score(g)$vector
authority.score(g)$vector

## A ring
g2 <- graph.ring(10)
hub.score(g2)$vector
authority.score(g2)$vector</pre>
```

label.propagation.community

Finding communities based on propagating labels

Description

This is a fast, nearly linear time algorithm for detecting community structure in networks. In works by labeling the vertices with unique labels and then updating the labels by majority voting in the neighborhood of the vertex.

Usage

Arguments

graph	The input graph, should be undirected to make sense.
weights	An optional weight vector. It should contain a positive weight for all the edges. The 'weight' edge attribute is used if present. Supply 'NA' here if you want to ignore the 'weight' edge attribute.
initial	The initial state. If NULL, every vertex will have a different label at the beginning. Otherwise it must be a vector with an entry for each vertex. Non-negative values denote different labels, negative entries denote vertices without labels.
fixed	Logical vector denoting which labels are fixed. Of course this makes sense only if you provided an initial state, otherwise this element will be ignored. Also note that vertices without labels cannot be fixed.

Details

This function implements the community detection method described in: Raghavan, U.N. and Albert, R. and Kumara, S.: Near linear time algorithm to detect community structures in large-scale networks. Phys Rev E 76, 036106. (2007). This version extends the original method by the ability to take edge weights into consideration and also by allowing some labels to be fixed.

From the abstract of the paper: "In our algorithm every node is initialized with a unique label and at every step each node adopts the label that most of its neighbors currently have. In this

iterative process densely connected groups of nodes form a consensus on a unique label to form communities."

Value

A numeric vector giving the final label (=community) of each vertex.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> for the C implementation, Gabor Csardi <Gabor.Csardi@unil.ch> for this manual page.

References

Raghavan, U.N. and Albert, R. and Kumara, S.: Near linear time algorithm to detect community structures in large-scale networks. *Phys Rev E* 76, 036106. (2007)

See Also

fastgreedy.community, walktrap.community and spinglass.community for other community detection methods.

Examples

```
g <- erdos.renyi.game(10, 5/10) %du% erdos.renyi.game(9, 5/9)
g <- add.edges(g, c(0, 11))
label.propagation.community(g)</pre>
```

layout

Generate coordinates for plotting graphs

Description

Some simple and not so simple functions determining the placement of the vertices for drawing a graph.

Usage

Arguments

graph	The graph to place.
params	The list of function dependent parameters.
dim	Numeric constant, either 2 or 3. Some functions are able to generate 2d and 3d layouts as well, supply this argument to change the default behavior.
•••	Function dependent parameters, this is an alternative notation to the params argument.
verbose	Logial constant, whether to show a progress bar while calculating the layout.
d	The matrix used for multidimansional scaling. By default it is the distance matrix of the graph.
layout	A matrix with two or three columns, the layout to normalize.
xmin,xmax	The limits for the first coordinate, if one of them or both are NULL then no normalization is performed along this direction.
ymin,ymax	The limits for the second coordinate, if one of them or both are NULL then no normalization is performed along this direction.
zmin,zmax	The limits for the third coordinate, if one of them or both are NULL then no normalization is performed along this direction.

Details

These functions calculate the coordinates of the vertices for a graph usually based on some optimality criterion.

layout.random simply places the vertices randomly on a square. It has no parameters.

layout.circle places the vertices on a unit circle equidistantly. It has no paramaters.

layout.sphere places the vertices (approximately) uniformly on the surface of a sphere, this is thus a 3d layout. It is not clear however what "uniformly on a sphere" means.

layout.fruchterman.reingold uses a force-based algorithm proposed by Fruchterman and Reingold, see references. Parameters and their default values:

- niterNumeric, the number of iterations to perform (500).
- coolexpNumeric, the cooling exponent for the simulated annealing (3).
- maxdeltaMaximum change (vcount(graph)).
- areaArea parameter (vcount(graph)^2).
- repulseradCancellation radius (area*vcount(graph)).

• weights A vector giving edge weights or NULL. If not NULL then the attraction along the edges will be multiplied by the given edge weights (NULL).

This function was ported from the SNA package.

layout.kamada.kawai is another force based algorithm. Parameters and default values:

- niterNumber of iterations to perform (1000).
- sigmaSets the base standard deviation of position change proposals (vcount(graph)/4).
- initempThe initial temperature (10).
- coolexpThe cooling exponent (0.99).
- kkconstSets the Kamada-Kawai vertex attraction constant (vcount(graph)**2).

This function performs very well for connected graphs, but it gives poor results for unconnected ones. This function was ported from the SNA package.

layout.spring is a spring embedder algorithm. Parameters and default values:

- massThe vertex mass (in 'quasi-kilograms'). (Defaults to 0.1.)
- equilThe equilibrium spring extension (in 'quasi-meters'). (Defaults to 1.)
- kThe spring coefficient (in 'quasi-Newtons per quasi-meter'). (Defaults to 0.001.)
- repequisThe point at which repulsion (if employed) balances out the spring extension force (in 'quasi-meters'). (Defaults to 0.1.)
- kfrThe base coefficient of kinetic friction (in 'quasi-Newton quasi-kilograms'). (Defaults to 0.01.)
- repulseShould repulsion be used? (Defaults to FALSE.)

This function was ported from the SNA package.

layout.reingold.tilford generates a tree-like layout, so it is mainly for trees. Parameters and default values:

- rootThe id of the root vertex, defaults to 0.
- circularLogical scalar, whether to plot the tree in a circular fashion, defaults to FALSE.

layout.fruchterman.reingold.grid is similar to layout.fruchterman.reingold but repelling force is calculated only between vertices that are closer to each other than a limit, so it is faster. Patameters and default values:

- niterNumeric, the number of iterations to perform (500).
- maxdeltaMaximum change for one vertex in one iteration. (The number of vertices in the graph.)
- areaThe area of the surface on which the vertices are placed. (The square of the number of vertices.)
- coolexpThe cooling exponent of the simulated annealing (1.5).
- repulseradCancellation radius for the repulsion (the area times the number of vertices).
- cellsizeThe size of the cells for the grid. When calculating the repulsion forces between vertices only vertices in the same or neighboring grid cells are taken into account (the fourth root of the number of area.

layout.lgl is for large connected graphs, it is similar to the layout generator of the Large Graph Layout software (http://bioinformatics.icmb.utexas.edu/lgl). Parameters and default values:

- maxiterThe maximum number of iterations to perform (150).
- maxdeltaThe maximum change for a vertex during an iteration (the number of vertices).
- areaThe area of the surface on which the vertices are placed (square of the number of vertices).
- coolexpThe cooling exponent of the simulated annealing (1.5).
- repulseradCancellation radius for the repulsion (the area times the number of vertices).
- cellsizeThe size of the cells for the grid. When calculating the repulsion forces between vertices only vertices in the same or neighboring grid cells are taken into account (the fourth root of the number of area.
- rootThe id of the vertex to place at the middle of the layout. The default value is -1 which means that a random vertex is selected.

layout graphopt is a port of the graphopt layout algorithm by Michael Schmuhl. graphopt version 0.4.1 was rewritten in C and the support for layers was removed (might be added later) and a code was a bit reorganized to avoid some unnecessary steps is the node charge (see below) is zero.

graphopt uses physical analogies for defining attracting and repelling forces among the vertices and then the physical system is simulated until it reaches an equilibrium. (There is no simulated annealing or anything like that, so a stable fixed point is not guaranteed.)

See also http://www.schmuhl.org/graphopt/ for the original graphopt.

Parameters and default values:

- niterInteger scalar, the number of iterations to perform. Should be a couple of hundred in general. If you have a large graph then you might want to only do a few iterations and then check the result. If it is not good enough you can feed it in again in the start argument. The default value is 500.
- charge The charge of the vertices, used to calculate electric repulsion. The default is 0.001.
- massThe mass of the vertices, used for the spring forces. The default is 30.
- spring.lengthThe length of the springs, an integer number. The default value is zero.
- spring.constantThe spring constant, the default value is one.
- max.sa.movementReal constant, it gives the maximum amount of movement allowed in a single step along a single axis. The default value is 5.
- startIf given, then it should be a matrix with two columns and one line for each vertex. This matrix will be used as starting positions for the algorithm. If not given, then a random starting matrix is used.

layout.mds uses metric multidimensional scaling for generating the coordinates. This function does not have the usual params argument. It can just take a single argument, the distance matrix used for multidimensional scaling. This function generates the layout separately for each graph component and then merges them via layout.merge. layout.mds is an *experimental* function currently.

layout.svd is a currently *experimental* layout function based on singular value decomposition. It does not have the usual params argument, but take a single argument, the distance matrix of the

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graph. This function generates the layout separately for each graph component and then merges them via layout.merge.

layout.norm normalizes a layout, it linearly transforms each coordinate separately to fit into the given limits.

layout.drl is another force-driven layout generator, it is suitable for quite large graphs. See layout.drl for details.

Value

All these functions return a numeric matrix with at least two columns and the same number of lines as the number of vertices.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Fruchterman, T.M.J. and Reingold, E.M. (1991). Graph Drawing by Force-directed Placement. *Software - Practice and Experience*, 21(11):1129-1164.

Kamada, T. and Kawai, S. (1989). An Algorithm for Drawing General Undirected Graphs. *Information Processing Letters*, 31(1):7-15.

Reingold, E and Tilford, J (1981). Tidier drawing of trees. *IEEE Trans. on Softw. Eng.*, SE-7(2):223–228.

See Also

```
layout.drl, plot.igraph, tkplot
```

Examples

```
g <- graph.ring(10)
layout.random(g)
layout.kamada.kawai(g)</pre>
```

layout.drl

The DrL graph layout generator

Description

DrL is a force-directed graph layout toolbox focused on real-world large-scale graphs, developed by Shawn Martin and colleagues at Sandia National Laboratories.

Usage

```
layout.drl (graph, use.seed = FALSE, seed = matrix(runif(vcount(graph) *
    2), nc = 2), options = igraph.drl.default, weights = E(graph)$weight,
    fixed = NULL, dim = 2)
```

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Arguments

graph	The input graph, in can be directed or undirected.	
use.seed	Logical scalar, whether to use the coordinates given in the seed argument as a starting point.	
seed	A matrix with two columns, the starting coordinates for the vertices is use. seed is TRUE. It is ignored otherwise.	
options	Options for the layout generator, a named list. See details below.	
weights	Optional edge weights. Supply NULL here if you want to weight edges equally. By default the weight edge attribute is used if the graph has one.	
fixed	Logical vector, it can be used to fix some vertices. All vertices for which it is TRUE are kept at the coordinates supplied in the seed matrix. It is ignored it NULL or if use. seed is FALSE.	
dim	Either '2' or '3', it specifies whether we want a two dimensional or a three dimensional layout. Note that because of the nature of the DrL algorithm, the three dimensional layout takes significantly longer to compute.	

Details

This function implements the force-directed DrL layout generator.

The generator has the following parameters:

- edge.cutEdge cutting is done in the late stages of the algorithm in order to achieve less dense layouts. Edges are cut if there is a lot of stress on them (a large value in the objective function sum). The edge cutting parameter is a value between 0 and 1 with 0 representing no edge cutting and 1 representing maximal edge cutting.
- init.iterationsNumber of iterations in the first phase.
- init.temperatureStart temperature, first phase.
- init.attractionAttraction, first phase.
- init.damping.multDamping, first phase.
- liquid.iterationsNumber of iterations, liquid phase.
- liquid.temperatureStart temperature, liquid phase.
- liquid.attractionAttraction, liquid phase.
- liquid.damping.multDamping, liquid phase.
- expansion.iterationsNumber of iterations, expansion phase.
- expansion.temperatureStart temperature, expansion phase.
- expansion.attractionAttraction, expansion phase.
- expansion.damping.multDamping, expansion phase.
- cooldown.iterationsNumber of iterations, cooldown phase.
- cooldown.temperatureStart temperature, cooldown phase.
- cooldown.attractionAttraction, cooldown phase.
- cooldown.damping.multDamping, cooldown phase.

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- crunch.iterationsNumber of iterations, crunch phase.
- crunch.temperatureStart temperature, crunch phase.
- crunch.attractionAttraction, crunch phase.
- crunch.damping.multDamping, crunch phase.
- simmer.iterationsNumber of iterations, simmer phase.
- simmer.temperatureStart temperature, simmer phase.
- simmer.attractionAttraction, simmer phase.
- simmer.damping.multDamping, simmer phase.

There are five pre-defined parameter settings as well, these are called igraph.drl.default, igraph.drl.coarsen, igraph.drl.coarsest, igraph.drl.refine and igraph.drl.final.

Value

A numeric matrix with two columns.

Author(s)

Shawn Martin <google@for.it> and Gabor Csardi <csardi@rmki.kfki.hu> for the R/igraph interface and the three dimensional version.

References

```
http://www.cs.sandia.gov/~smartin/software.html
```

See Also

layout for other layout generators.

Examples

```
g <- as.undirected(ba.game(100, m=1))
l <- layout.drl(g, options=list(simmer.attraction=0))
## Not run:
plot(g, layout=l, vertex.size=3, vertex.label=NA)
## End(Not run)</pre>
```

layout.merge

Merging graph layouts

Description

Place several graphs on the same layout

layout.merge 125

Usage

Arguments

graphs A list of graph objects.

layouts A list of two-column matrices.

method Character constant giving the method to use. Right now only dla is imple-

mented.

verbose Logical constant, whether to show a progress bar while doing the calculation.

graph The input graph.

layout A function object, the layout function to use.

... Additional arguments to pass to the layout layout function.

Details

layout.merge takes a list of graphs and a list of coordinates and places the graphs in a common layout. The method to use is chosen via the method parameter, although right now only the dla method is implemented.

The dla method covers the graph with circles. Then it sorts the graphs based on the number of vertices first and places the largest graph at the center of the layout. Then the other graphs are placed in decreasing order via a DLA (diffision limited aggregation) algorithm: the graph is placed randomly on a circle far away from the center and a random walk is conducted until the graph walks into the larger graphs already placed or walks too far from the center of the layout.

The piecewise.layout function disassembles the graph first into maximal connected components and calls the supplied layout function for each component separately. Finally it merges the layouts via calling layout.merge.

Value

A matrix with two columns and as many lines as the total number of vertices in the graphs.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

```
plot.igraph, tkplot, layout, graph.disjoint.union
```

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Examples

layout.star

Generate coordinates to place the vertices of a graph in a star-shape

Description

A simple layout generator, that places one vertex in the center of a circle and the rest of the vertices equidistantly on the perimeter.

Usage

```
layout.star(graph, center = V(graph)[0], order = NULL)
```

Arguments

graph The graph to layout.

center The id of the vertex to put in the center. By default it is the first vertex.

order Numeric vector, the order of the vertices along the perimeter. The default order-

ing is given by the vertex ids.

Details

It is possible to choose the vertex that will be in the center, and the order of the vertices can be also given.

Value

A matrix with two columns and as many rows as the number of vertices in the input graph.

Author(s)

```
Gabor Csardi Gabor . Csardi@unil . ch>
```

See Also

layout and layout.drl for other layout algorithms, plot.igraph and tkplot on how to plot graphs and graph.star on how to create ring graphs.

Examples

```
g <- graph.star(10)
layout.star(g)</pre>
```

leading.eigenvector.community

Community structure detecting based on the leading eigenvector of the community matrix

Description

These functions try to find densely connected subgraphs in a graph by calculating the leading non-negative eigenvector of the modularity matrix of the graph.

Usage

NULL.

Arguments

graph	The input graph. Should be undirected as the method needs a symmetric matrix.
steps	The number of steps to take, this is actually the number of tries to make a step. It is not a particularly useful parameter.
	For community.le.to.membership the number of merges to produce from the supplied membership vector.
naive	Logical constant, it defines how the algorithm tries to find more divisions after the first division was made. If TRUE then it simply considers both communities as separate graphs and then creates modularity matrices for both communities, etc. This method however does not maximize modularity, see the paper in the references section below. If it is FALSE then the proper method is used which maximizes modularity.
fromhere	An object returned by a previous call to leading.eigenvector.community.step. This will serve as a starting point to take another step. This argument is ignored if it is NULL.
membership	The starting community structure. It is a numeric vector defining the member- ship of every vertex in the graph with a number between 0 and the total number of communities at this level minus one. By default we start with a single com- munity containing all vertices. This argument is ignored if fromhere is not

For community.le.to.memberhip the starting community structure on which

steps merges are performed.

community The id of the community which the algorithm will try to split.

options A named list to override some ARPACK options.

merges The merge matrix, possible from the result of leading.eigenvector.community.

Details

The functions documented in these section implement the 'leading eigenvector' method developed by Mark Newman and published in MEJ Newman: Finding community structure using the eigenvectors of matrices, arXiv:physics/0605087. TODO: proper citation.

The heart of the method is the definition of the modularity matrix, B, which is B=A-P, A being the adjacency matrix of the (undirected) network, and P contains the probability that certain edges are present according to the 'configuration model'. In other words, a P[i,j] element of P is the probability that there is an edge between vertices i and j in a random network in which the degrees of all vertices are the same as in the input graph.

The leading eigenvector method works by calculating the eigenvector of the modularity matrix for the largest positive eigenvalue and then separating vertices into two community based on the sign of the corresponding element in the eigenvector. If all elements in the eigenvector are of the same sign that means that the network has no underlying community structure. Check Newman's paper to understand why this is a good method for detecting community structure.

leading.eigenvector.community is the proper implementation of the proposed algorithm. leading.eigenvector.commu is considered worse, in this implementation a community found after a division is considered as a separate graph for further divisions. leading.eigenvector.community.step is the proper implementation, but makes only one step, by trying to split the specified community.

From igraph 0.5 these functions use ARPACK to calculate the eigenvectors. See arpack for details.

community.le.to.memberhip creates a membership vector from the result of leading.eigenvector.community or leading.eigenvector.community.naive. It takes membership and permformes steps merges, according to the supplied merges matrix.

Value

leading.eigenvector.community and leading.eigenvector.community.naive return a named list with the following members:

membership The membership vector at the end of the algorithm, when no more splits are

possible.

merges The merges matrix starting from the state described by the membership member.

This is a two-column matrix and each line describes a merge of two communities, the first line is the first merge and it creates community 'N', N is the number of initial communities in the graph, the second line creates community N+1, etc.

options Information about the underlying ARPACK computation, see arpack for details.

leading.eigenvector.community.step returns a named list with the following members:

membership The new membership vector after the split. If no split was done then this is the

same as the input membership vector.

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split Logical scalar, if TRUE that means that the community was successfully splitted.

eigenvector The eigenvector of the community matrix, or NULL if the eigenvector argument was FALSE.

eigenvalue The largest positive eigenvalue of the modularity matrix.

options Information about the underlying ARPACK computation, see arpack for details.

community.le.to.membership returns a named list with two components:

membership A membership vector, a numerical vector indication which vertex belongs to

which community. The communities are always numbered from zero.

csize A numeric vector giving the sizes of the communities.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

MEJ Newman: Finding community structure using the eigenvectors of matrices, arXiv:physics/0605087

See Also

modularity, walktrap.community, edge.betweenness.community, fastgreedy.community, as.dendrogram in package stats.

Examples

```
g <- graph.full(5) %du% graph.full(5) %du% graph.full(5)
g <- add.edges(g, c(0,5, 0,10, 5, 10))
leading.eigenvector.community(g)

lec <- leading.eigenvector.community.step(g)
lec$membership
# Try one more split
leading.eigenvector.community.step(g, fromhere=lec, community=0)
leading.eigenvector.community.step(g, fromhere=lec, community=1)</pre>
```

line.graph Line graph of a graph

Description

This function calculates the line graph of another graph.

Usage

```
line.graph(graph)
```

Arguments

graph

The input graph, it can be directed or undirected.

Details

The line graph L(G) of a G undirected graph is defined as follows. L(G) has one vertex for each edge in G and two vertices in L(G) are connected by an edge if their corresponding edges share an end point.

The line graph L(G) of a G directed graph is slightly different, L(G) has one vertex for each edge in G and two vertices in L(G) are connected by a directed edge if the target of the first vertex's corresponding edge is the same as the source of the second vertex's corresponding edge.

Value

A new graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>, the first version of the C code was written by Vincent Matossian.

Examples

```
# generate the first De-Bruijn graphs
g <- graph.full(2, directed=TRUE, loops=TRUE)
line.graph(g)
line.graph(line.graph(g))
line.graph(line.graph(line.graph(g)))</pre>
```

 ${\tt minimum.spanning.tree}$ ${\tt \it Minimum.spanning.tree}$

Description

A subgraph of a connected graph is a *minimum spanning tree* if it is tree, and the sum of its edge weights are the minimal among all tree subgraphs of the graph. A minimum spanning forest of a graph is the graph consisting of the minimum spanning trees of its components.

Usage

```
minimum.spanning.tree(graph, weights=NULL, algorithm=NULL, ...)
```

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Arguments

graph	The graph object to analyze.	
weights	Numeric algorithm giving the weights of the edges in the graph. The order i determined by the edge ids. This is ignored if the unweighted algorithm i chosen	
algorithm	The algorithm to use for calculation. unweighted can be used for unwieghted graphs, and prim runs Prim's algorithm for weighted graphs. If this is NULL then igraph tries to select the algorithm automatically: if the graph has an edge attribute called weight of the weights argument is not NULL then Prim's algorithm is chosen, otherwise the unwweighted algorithm is performed.	

... Additional arguments, unused.

Details

If the graph is unconnected a minimum spanning forest is returned.

Value

A graph object with the minimum spanning forest. (To check that it is a tree check that the number of its edges is vcount(graph)-1.) The edge and vertex attributes of the original graph are preserved in the result.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Prim, R.C. 1957. Shortest connection networks and some generalizations *Bell System Technical Journal*, 37 1389–1401.

See Also

clusters

Examples

```
g <- erdos.renyi.game(100, 3/100)
mst <- minimum.spanning.tree(g)</pre>
```

modularity modularity

modularity

Modularity of a community structure of a graph

Description

This function calculates how modular is a given division of a graph into subgraphs.

Usage

modularity(graph, membership, weights = NULL)

Arguments

graph The input graph.

membership Numeric vector, for each vertex it gives its community. The communities are

numbered from zero.

weights If not NULL then a numeric vector giving edge weights.

Details

The modularity of a graph with respect to some division (or vertex types) measures how good the division is, or how separated are the different vertex types from each other. It defined as

$$Q = \frac{1}{2m} \sum_{i,j} A_{ij} - \frac{k_i k_j}{2m} \delta(c_i, c_j),$$

here m is the number of edges, A_{ij} is the element of the A adjacency matrix in row i and column j, k_i is the degree of i, k_j is the degree of j, c_i is the type (or component) of i, c_j that of j, the sum goes over all i and j pairs of vertices, and $\delta(x, y)$ is 1 if x = y and 0 otherwise.

If edge weights are given, then these are considered as the element of the A adjacency matrix, and k_i is the sum of weights of adjacent edges for vertex i.

Value

A numeric scalar, the modularity score of the given configuration.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

MEJ Newman and M Girvan: Finding and evaluating community structure in networks. Physical Review E 69 026113, 2004.

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See Also

walktrap.community, edge.betweenness.community, fastgreedy.community, spinglass.community for various community detection methods.

Examples

```
g <- graph.full(5) %du% graph.full(5) %du% graph.full(5)
g <- add.edges(g, c(0,5, 0,10, 5, 10))
wtc <- walktrap.community(g)
memb <- community.to.membership(g, wtc$merges, steps=12)
modularity(g, memb$membership)</pre>
```

neighborhood

Neighborhood of graph vertices

Description

These functions find the vertices not farther than a given limit from another fixed vertex, these are called the neighborhood of the vertex.

Usage

```
neighborhood.size(graph, order, nodes=V(graph), mode=c("all", "out", "in"))
neighborhood(graph, order, nodes=V(graph), mode=c("all", "out", "in"))
graph.neighborhood(graph, order, nodes=V(graph), mode=c("all", "out", "in"))
connect.neighborhood(graph, order, mode=c("all", "out", "in", "total"))
```

Arguments

graph The input graph.

order Integer giving the order of the neighborhood.

nodes The vertices for which the calculation is performed.

mode Character constatnt, it specifies how to use the direction of the edges if a directed

graph is analyzed. For 'out' only the outgoing edges are followed, so all vertices reachable from the source vertex in at most order steps are counted. For '"in" all vertices from which the source vertex is reachable in at most order steps are counted. "all" ignores the direction of the edges. This argument is ignored for

undirected graphs.

Details

The neighborhood of a given order o of a vertex v includes all vertices which are closer to v than the order. Ie. order 0 is always v itself, order 1 is v plus its immediate neighbors, order 2 is order 1 plus the immediate neighbors of the vertices in order 1, etc.

neighborhood.size calculates the size of the neighborhoods for the given vertices with the given order.

page.rank

neighborhood calculates the neighborhoods of the given vertices with the given order parameter. graph.neighborhood is creates (sub)graphs from all neighborhoods of the given vertices with the given order parameter. This function preserves the vertex, edge and graph attributes.

connect.neighborhood creates a new graph by connecting each vertex to all other vertices in its neighborhood.

Value

```
neighborhood.size returns with an integer vector.
neighborhood returns with a list of integer vectors.
graph.neighborhood returns with a list of graphs.
connect.neighborhood returns with a new graph object.
```

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>, the first version was done by Vincent Matossian

Examples

```
g <- graph.ring(10)
neighborhood.size(g, 0, 1:3)
neighborhood.size(g, 1, 1:3)
neighborhood(size(g, 2, 1:3)
neighborhood(g, 0, 1:3)
neighborhood(g, 1, 1:3)
neighborhood(g, 2, 1:3)

# attributes are preserved
V(g)$name <- c("a", "b", "c", "d", "e", "f", "g", "h", "i", "j")
graph.neighborhood(g, 2, 1:3)

# connecting to the neighborhood
g <- graph.ring(10)
g <- connect.neighborhood(g, 2)</pre>
```

page.rank

The Page Rank algorithm

Description

Calculates the Google PageRank for the specified vertices.

Usage

```
page.rank (graph, vids = V(graph), directed = TRUE, damping = 0.85,
    weights = NULL, options = igraph.arpack.default)
page.rank.old (graph, vids = V(graph), directed = TRUE, niter = 1000,
    eps = 0.001, damping = 0.85, old = FALSE)
```

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Arguments

graph The graph object.

vids The vertices of interest.

directed Logical, if true directed paths will be considered for directed graphs. It is ig-

nored for undirected graphs.

damping The damping factor ('d' in the original paper).

weights A numerical vector or NULL. This argument can be used to give edge weights for

calculating the weighted PageRank of vertices. If this is NULL and the graph has a weight edge attribute then that is used. If weights is a numerical vector then it used, even if the graph has a weights edge attribute. If this is NA, then no edge

weights are used (even if the graph has a weight edge attribute.

options A named list, to override some ARPACK options. See arpack for details.

niter The maximum number of iterations to perform.

eps The algorithm will consider the calculation as complete if the difference of

PageRank values between iterations change less than this value for every node.

old A logical scalar, whether the old style (pre igraph 0.5) normalization to use. See

details below.

Details

For the explanation of the PageRank algorithm, see the following webpage: http://www-db.stanford.edu/~backrub/google.html, or the following reference:

Sergey Brin and Larry Page: The Anatomy of a Large-Scale Hypertextual Web Search Engine. Proceedings of the 7th World-Wide Web Conference, Brisbane, Australia, April 1998.

igraph 0.5 (and later) contains two PageRank calculation implementations. The page.rank function uses ARPACK to perform the calculation, see also arpack.

The page.rank.old function performs a simple power method, this is the implementation that was available under the name page.rank in pre 0.5 igraph versions. Note that page.rank.old has an argument called old. If this argument is FALSE (the default), then the proper PageRank algorithm is used, i.e. (1-d)/n is added to the weighted PageRank of vertices to calculate the next iteration. If this argument is TRUE then (1-d) is added, just like in the PageRank paper; d is the damping factor, and n is the total number of vertices. A further difference is that the old implementation does not renormalize the page rank vector after each iteration. Note that the old=FALSE method is not stable, is does not necessarily converge to a fixed point. It should be avoided for new code, it is only included for compatibility with old igraph versions.

Please note that the PageRank of a given vertex depends on the PageRank of all other vertices, so even if you want to calculate the PageRank for only some of the vertices, all of them must be calculated. Requesting the PageRank for only some of the vertices does not result in any performance increase at all.

Since the calculation is an iterative process, the algorithm is stopped after a given count of iterations or if the PageRank value differences between iterations are less than a predefined value.

permute.vertices

Value

For page.rank a named list with entries:

vector A numeric vector with the PageRank scores.

value The eigenvalue corresponding to the eigenvector with the page rank scores. It

should be always exactly one.

options Some information about the underlying ARPACK calculation. See arpack for

details.

For page.rank.old a numeric vector of Page Rank scores.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu>

References

Sergey Brin and Larry Page: The Anatomy of a Large-Scale Hypertextual Web Search Engine. Proceedings of the 7th World-Wide Web Conference, Brisbane, Australia, April 1998.

See Also

Other centrality scores: closeness, betweenness, degree

Examples

```
g <- random.graph.game(20, 5/20, directed=TRUE)
page.rank(g)$vector
g2 <- graph.star(10)
page.rank(g2)$vector</pre>
```

permute.vertices

Permute the vertices of a graph

Description

Create a new graph, by permuting vertex ids.

Usage

```
permute.vertices(graph, permutation)
```

Arguments

graph The input graph, it can directed or undirected.

permutation A numeric vector giving the permutation to apply. The first element is the new

id of vertex 0, etc. Every number between zero and vcount(graph)-1 must

appear exactly once.

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Details

This function creates a new graph from the input graph by permuting its vertices according to the specified mapping. Call this function with the output of canonical.permutation to create the canonical form of a graph.

Value

A new graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

```
canonical.permutation
```

Examples

```
# Random permutation of a random graph
g <- random.graph.game(20, 50, type="gnm")
g2 <- permute.vertices(g, sample(vcount(g))-1)
graph.isomorphic(g, g2)</pre>
```

plot.bgraph

Plot graphs and their cohesive block hierarchy

Description

This function plots bgraph objects as output by cohesive.blocks. It produces a two-panel plot with the graph itself on the left and a tree representing the block hierarchy on the right.

Usage

```
## S3 method for class 'bgraph'
plot(x, mc = NULL, vertex.size = 3, colpal = NULL, emph = NULL, ...)
```

Arguments

x	The bgraph object to be plotted
mc	A numeric vector listing the vertex connectivity of the maximally cohesive subgraph of each vertex. Automatically calculated if NULL (leaving default is usually preferable).
vertex.size	The size of the vertices in the plot. Applies only to the graph, and not to the block-hierarchy tree.
colpal	The color palette to use to distinguish block cohesion. Defaults to rainbow spectrum.

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emph	A numeric vector of blocks to emphasize. Useful for distinguishing specific blocks when it is unclear which higher-cohesion vertices belong to which block. (see details)
•••	Other arguments to be passed on to plot.igraph for the calculation of the graph (but not the hierarchy).

Details

Two plots are used to represent the cohesive blocks in a graph visually. The first is a standard plot with vertices colored according to their maximally-cohesive containing block. The second is a tree representing the hierarchical structure of the blocks, with edges representing a strict superset relationship.

The emph argument should be a numeric vector corresponding to the indices of blocks in x\$blocks and x\$block.cohesion (1-based indexing). The vertices of the specified blocks are emphasized by enlarging them and using a white border.

The intended usage of this function is the quick plotting of a graph together with its block structure. If you need more flexibility then please plot the graph and the hierarchy (the tree graph attribute) separately by using plot.igraph.

Author(s)

Peter McMahan <peter.mcmahan@gmail.com>

See Also

cohesive.blocks for the cohesive blocks computation, graph.cohesion, plot.igraph and igraph.plotting for regular igraph plotting, write.pajek.bgraph.

Examples

```
## Create a graph with an interesting structure:
g <- graph.disjoint.union(graph.full(4),graph.empty(2,directed=FALSE))
g <- add.edges(g,c(3,4,4,5,4,2))
g <- graph.disjoint.union(g,g,g)
g <- add.edges(g,c(0,6,1,7,0,12,4,0,4,1))

## Find cohesive blocks:
gBlocks <- cohesive.blocks(g)

## Plot:
## Not run:
plot.bgraph(gBlocks,layout=layout.kamada.kawai)

## End(Not run)

## There are two two-cohesive blocks. To differentiate the block
## that contains both the three- and four-cohesive sub-blocks use:
## Not run:
plot(gBlocks,emph=3,layout=layout.kamada.kawai)</pre>
```

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```
## End(Not run)
```

plot.igraph

Plotting of graphs

Description

plot.graph is able to plot graphs to any R device. It is the non-interactive companion of the tkplot function.

Usage

Arguments

х	The graph to plot.
axes	Logical, whether to plot axes, defaults to FALSE.
xlab	The label of the horizontal axis. Defaults to the empty string.
ylab	The label of the vertical axis. Defaults to the empty string.
add	Logical scalar, whether to add the plot to the current device, or delete the device's current contents first.
xlim	The limits for the horizontal axis, it is unlikely that you want to modify this.
ylim	The limits for the vertical axis, it is unlikely that you want to modify this.
main	Main title.
sub	Subtitle.
	Additional arguments, passed to plot.

Details

One convenient way to plot graphs is to plot with tkplot first, handtune the placement of the vertices, query the coordinates by the tkplot.getcoords function and use them with plot to plot the graph to any R device.

Value

```
Returns NULL, invisibly.
```

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

power.law.fit

See Also

layout for different layouts, igraph.plotting for the detailed description of the plotting parameters and tkplot and rglplot for other graph plotting functions.

Examples

```
g <- graph.ring(10)
## Not run: plot(g, layout=layout.kamada.kawai, vertex.color="green")</pre>
```

power.law.fit

Fitting a power-law distribution function to discrete data

Description

power.law.fit fits a power-law distribution to a data set.

Usage

```
power.law.fit(x, xmin = NULL, start = 2, ...)
```

Arguments

X	The data to fit, a numeric vector containing integer values.
xmin	The lower bound for fitting the power-law. If NULL, the smallest value in x will be used. This argument makes it possible to fit only the tail of the distribution.
start	The initial value of the exponent for the minimizing function. Ususally it is safe to leave this untouched.
	Additional arguments, passed to the maximum likelyhood optimizing function, mle.

Details

A power-law distribution is fitted with maximum likelyhood methods as recommended by Newman and (by default) the BFGS optimization (see mle) algorithm is applied.

The additional arguments are passed to the mle function, so it is possible to change the optimization method and/or its parameters.

Value

An object with class 'mle'. It can be used to calculate confidence intervals and log-likelihood. See mle-class for details.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

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References

Power laws, Pareto distributions and Zipf's law, M. E. J. Newman, Contemporary Physics, in press.

See Also

mle

Examples

preference.game

Trait-based random generation

Description

Generation of random graphs based on different vertex types.

Usage

```
preference.game(nodes, types, type.dist=rep(1, types),
    pref.matrix=matrix(1, types, types), directed=FALSE, loops=FALSE)
asymmetric.preference.game(nodes, types,
    type.dist.matrix=matrix(1,types,types),
    pref.matrix = matrix(1, types, types), loops=FALSE)
```

Arguments

nodes The number of vertices in the graphs.

types The number of different vertex types.

type.dist The distribution of the vertex types, a

The distribution of the vertex types, a numeric vector of length 'types' contain-

ing non-negative numbers. The vector will be normed to obtain probabilities.

type.dist.matrix

The joint distribution of the in- and out-vertex types.

pref.matrix A square matrix giving the preferences of the vertex types. The matrix has

'types' rows and columns.

directed Logical constant, whether to create a directed graph.

loops Logical constant, whether self-loops are allowed in the graph.

print.igraph

Details

Both models generate random graphs with given vertex types. For preference.game the probability that two vertices will be connected depends on their type and is given by the 'pref.matrix' argument. This matrix should be symmetric to make sense but this is not checked. The distribution of the different vertes types is given by the 'type.dist' vector.

For asymmetric.preference.game each vertex has an in-type and an out-type and a directed graph is created. The probability that a directed edge is realized from a vertex with a given out-type to a vertex with a given in-type is given in the 'pref.matrix' argument, which can be asymmetric. The joint distribution for the in- and out-types is given in the 'type.dist.matrix' argument.

Value

An igraph graph.

Author(s)

 $Tamas\ Nepusz\ \verb|\colore| ruki.kfki.hu>\ and\ Gabor\ Csardi\ \verb|\colore| csardi\ \verb|\colore| ruki.kfki.hu>\ for\ the\ R$ interface

See Also

```
establishment.game.callaway.traits.game
```

Examples

```
pf <- matrix( c(1, 0, 0, 1), nr=2)
g <- preference.game(20, 2, pref.matrix=pf)
## Not run: tkplot(g, layout=layout.fruchterman.reingold)
pf <- matrix( c(0, 1, 0, 0), nr=2)
g <- asymmetric.preference.game(20, 2, pref.matrix=pf)
## Not run: tkplot(g, layout=layout.circle)</pre>
```

print.igraph

Print graphs to the terminal

Description

These functions attempt to print a graph to the terminal in a human readable form.

Usage

```
## S3 method for class 'igraph'
print(x,
    graph.attributes=igraph.par("print.graph.attributes"),
    vertex.attributes=igraph.par("print.vertex.attributes"),
    edge.attributes=igraph.par("print.edge.attributes"),
```

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```
names=TRUE, quote.names=TRUE,
...)
## S3 method for class 'bgraph'
print(x,
...)
## S3 method for class 'igraph'
summary(object, ...)
```

Arguments

x The graph to print.

graph.attributes

Logical constant, whether to print graph attributes.

vertex.attributes

Logical constant, whether to print vertex attributes.

edge.attributes

Logical constant, whether to print edge attributes.

names Logical constant, whether to print symbolic vertex names (ie. the name vertex

attribute) or vertex ids.

quote.names Logical scalar, whether to quote symbolic vertex names.

object The graph of which the summary will be printed.

... Additional agruments, print.bgraph passes these to print.igraph.

Details

summary.igraph prints the number of vertices, edges and whether the graph is directed. print.igraph prints the same information, and also lists the edges, and optionally graph, vertex and/or edge attributes.

As of igraph 0.4 print.igraph uses the max.print option, see options for details.

print.bgraph prints a bgraph object, a graph together with its cohesive block hierarchy, see cohesive.blocks for details.

Value

All these functions return the graph invisibly.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
g <- graph.ring(10)
g
summary(g)</pre>
```

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read	. g	ra	D	h

Reading foreign file formats

Description

The read graph function is able to read graphs in various representations from a file, or from a http connection. Currently some simple formats are supported.

Usage

Arguments

file The connection to read from. This can be a local file, or a http or ftp connection. It can also be a character string with the file name or URI.

Character constant giving the file format. Right now edgelist, pajek, graphml, gml, ncol, lgl, dimacs and graphdb are supported, the default is edgelist. As of igraph 0.4 this argument is case insensitive.

.. Additional arguments, see below.

Details

The read graph function may have additional arguments depending on the file format (the format argument).

• edgelist

This format is a simple text file with numeric vertex ids defining the edges. There is no need to have newline characters between the edges, a simple space will also do.

Additional arguments:

- nThe number of vertices in the graph. If it is smaller than or equal to the largest integer in the file, then it is ignored; so it is safe to set it to zero (the default).
- directedLogical scalar, whether to create a directed graph. The default value is TRUE.
- pajek Pajek it a popular network analysis program for Windows. (See the Pajek homepage at http://vlado.fmf.uni-lj.si/pub/networks/pajek/.) It has a quite flexible but not very well documented file format, see the Pajek manual on the Pajek homepage for some information about the file format.

igraph implements only a subset of the Pajek format:

- Only .net files are supported, Pajek project files (which can contain many graph and also other type of data) are not. Poject files might be supported in a forthcoming igraph release if they turned out to be needed.
- Time events networks are not supported.
- Hypergraphs (graphs with non-binary edges) are not supported as igraph cannot handle them.

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 Graphs containing both directed and undirected edges are not supported as igraph cannot represent them.

- Bipartite (also called affiliation) networks are not supported. The surrent igraph version imports the network structure correctly but vertex type information is omitted.
- Graph with multiple edge sets are not supported.

Vertex and edge attributes defined in the Pajek file will be also read and assigned to the graph object to be created. These are mainly parameters for graph visualization, but not exclusively, eg. the file might contain edge weights as well.

The following vertex attributes might be added:

igraph name description, Pajek attribute

id Vertex id

x, y, z The 'x', 'y' and 'z' coordinate of the vertex

vertexsize The size of the vertex when plotted (size in Pajek).

shape The shape of the vertex when plotted.

color Vertex color (ic in Pajek) if given with symbolic name

color-red,

color-green,

color-blue Vertex color (ic in Pajek) if given in RGB notation framecolor Border color (bc in Pajek) if given with symbolic name

framecolor-red, framecolor-green,

framecolor-blue Border color (bc in Pajek) if given in RGB notation labelcolor Label color (1c in Pajek) if given with symbolic name

labelcolor-red, labelcolor-green,

labelcolor-blue Label color (1c in Pajek) if given in RGB notation

xfact, yfact The x_fact and y_fact Pajek attributes.

labeldist The distance of the label from the vertex. (1r in Pajek.)

labeldegree,

labeldegree2
framewidth
fontsize
rotation
radius

The 1a and 1phi Pajek attributes
The width of the border (bw in Pajek).
Size of the label font (fos in Pajek.)
The rotation of the vertex (phi in Pajek).
Radius, for some vertex shapes (r in Pajek).

diamondratio For the diamond shape (q in Pajek).

These igraph attributes are only created if there is at least one vertex in the Pajek file which has the corresponding associated information. Eg. if there are vertex coordinates for at least one vertex then the 'x', 'y' and possibly also 'z' vertex attributes will be created. For those vertices for which the attribute is not defined, NaN is assigned.

The following edge attributes might be added:

igraph name description, Pajek attribute

weight Edge weights. label 1 in Pajek.

color Edge color, if the color is given with a symbolic name, c in Pajek.

read.graph

color-red, color-green,

color-blue Edge color if it was given in RGB notation, c in Pajek.

edgewidth w in Pajek.
arrowsize s in Pajek.

hook1, hook2 h1 and h2 in Pajek.

angle1, angle2 a1 and a2 in Pajek, Bezier curve parameters.

velocity1,

velocity2 k1 and k2 in Pajek, Bezier curve parameter.

arrowpos ap in Pajek. labelpos lp in Pajek.

labelangle,

labelangle2 1r and 1phi in Pajek.

labeldegree 1a in Pajek.
fontsize fos in Pajek.
arrowtype a in Pajek.
linepattern p in Pajek.
labelcolor 1c in Pajek.

There are no additional arguments for this format.

- graphml GraphML is an XML-based file format (an XML application in the XML terminology) to describe graphs. It is a modern format, and can store graphs with an extensible set of vertex and edge attributes, and generalized graphs which igraph cannot handle. Thus igraph supports only a subset of the GraphML language:
 - Hypergraphs are not supported.
 - Nested graphs are not supported.
 - Mixed graphs, ie. graphs with both directed and undirected edges are not supported. read.graph() sets the graph directed if this is the default in the GraphML file, even if all the edges are in fact undirected.

See the GraphML homepage at http://graphml.graphdrawing.org for more information about the GraphML format.

Additional arguments:

- indexIf the GraphML file contains more than one graphs, this argument can be used to select the graph to read. By default the first graph is read (index 0).
- GML GML is a simple textual format, see http://www.infosun.fim.uni-passau.de/Graphlet/ GML/ for details.

Although all syntactically correct GML can be parsed, we implement only a subset of this format, some attributes might be ignored. Here is a list of all the differences:

- Only node and edge attributes are used, and only if they have a simple type: integer, real
 or string. So if an attribute is an array or a record, then it is ignored. This is also true if
 only some values of the attribute are complex.
- Top level attributes except for Version and the first graph attribute are completely ignored.
- Graph attributes except for node and edge are completely ignored.

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- There is no maximum line length.
- There is no maximum keyword length.
- Character entities in strings are not interpreted.
- We allow inf (infinity) and nan (not a number) as a real number. This is case insensitive, so nan, NaN and NAN are equal.

Please contact us if you cannot live with these limitations of the GML parser.

There are not additional argument for this format.

• ncol This format is used by the Large Graph Layout program (http://bioinformatics.icmb.utexas.edu/lgl), and it is simply a symbolic weighted edge list. It is a simple text file with one edge per line. An edge is defined by two symbolic vertex names separated by whitespace. (The symbolic vertex names themselves cannot contain whitespace. They might followed by an optional number, this will be the weight of the edge; the number can be negative and can be in scientific notation. If there is no weight specified to an edge it is assumed to be zero.

The resulting graph is always undirected. LGL cannot deal with files which contain multiple or loop edges, this is however not checked here, as igraph is happy with these.

Additional arguments:

- namesLogical constant, whether to add the symbolic names as vertex attributes to the graph. If TRUE the name of the vertex attribute will be 'name'.
- weightsLogical constant, whether to add the weights of the edges as edge attribute 'weight'.
- directedLogical constant, whether to create a directed graph. The default is undirected.
- lglThe lgl format is used by the Large Graph Layout visualization software (http://bioinformatics.icmb.utexas.edu/lgl), it can describe undirected optionally weighted graphs. From the LGL manual:

The second format is the LGL file format (.lgl file suffix). This is yet another graph file format that tries to be as stingy as possible with space, yet keeping the edge file in a human readable (not binary) format. The format itself is like the following:

```
# vertex1name
vertex2name [optionalWeight]
vertex3name [optionalWeight]
```

Here, the first vertex of an edge is preceded with a pound sign '#'. Then each vertex that shares an edge with that vertex is listed one per line on subsequent lines.

LGL cannot handle loop and multiple edges or directed graphs, but in igraph it is not an error to have multiple and loop edges.

Additional arguments:

- namesLogical constant, whether to add the symbolic names as vertex attributes to the graph. If TRUE the name of the vertex attribute will be 'name'.
- weightsLogical constant, whether to add the weights of the edges as edge attribute 'weight'.
- dimacs The DIMACS file format, more specifically the version for network flow problems, see the files at ftp://dimacs.rutgers.edu/pub/netflow/general-info/

This is a line-oriented text file (ASCII) format. The first character of each line defines the type of the line. If the first character is c the line is a comment line and it is ignored. There is one problem line (p) in the file, it must appear before any node and arc descriptor lines.

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The problem line has three fields separated by spaces: the problem type (min, max or asn), the number of vertices and number of edges in the graph. Exactly two node identification lines are expected (n), one for the source, one for the target vertex. These have two fields: the id of the vertex and the type of the vertex, either s (=source) or t (=target). Arc lines start with a and have three fields: the source vertex, the target vertex and the edge capacity.

Vertex ids are numbered from 1.

The source vertex is assigned to the source, the target vertex to the target graph attribute. The edge capacities are assigned to the capacity edge attribute.

Additional arguments:

- directedLogical scalar, whether to create a directed graph. By default a directed graph is created.
- graphdbThis is a binary format, used in the graph database for isomorphism testing (http://amalfi.dis.unina.it/graph/) From the graph database homepage (http://amalfi.dis.unina.it/graph/db/doc/graphdbat-2.html):

The graphs are stored in a compact binary format, one graph per file. The file is composed of 16 bit words, which are represented using the so-called little-endian convention, i.e. the least significant byte of the word is stored first.

Then, for each node, the file contains the list of edges coming out of the node itself. The list is represented by a word encoding its length, followed by a word for each edge, representing the destination node of the edge. Node numeration is 0-based, so the first node of the graph has index 0.

See also graph.graphdb.

Only unlabelled graphs are implemented.

Additional attributes:

- directedLogical scalar. Whether to create a directed graph.

Value

A graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

write.graph

reciprocity

Reciprocity of graphs

Description

Calculates the reciprocity of a directed graph.

rewire 149

Usage

```
reciprocity(graph, ignore.loops = TRUE)
```

Arguments

graph The graph object.

ignore.loops Logical constant, whether to ignore loop edges.

Details

A vertex pair (A, B) is said to be reciprocal if there are edges between them in both directions. The reciprocity of a directed graph is the proportion of all possible (A, B) pairs which are reciprocal, provided there is at least one edge between A and B. The reciprocity of an empty graph is undefined (results in an error code). Undirected graphs always have a reciprocity of 1.0 unless they are empty.

Value

A numeric constaint between zero and one.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
g <- random.graph.game(20, 5/20, directed=TRUE)
reciprocity(g)</pre>
```

rewire

Graph rewiring

Description

Randomly rewires a graph while preserving the degree distribution.

Usage

```
rewire(graph, mode = "simple", niter = 100)
```

Arguments

graph The graph to be rewired.

mode The rewiring algorithm to be used. It can be one of the following: simple: sim-

ple rewiring algorithm which chooses two arbitrary edges in each step (namely (a,b) and (c,d)) and substitutes them with (a,d) and (c,b) if they don't yet exist.

niter Number of rewiring trials to perform.

rewire.edges

Details

This function generates a new graph based on the original one by randomly rewiring edges while preserving the original graph's degree distribution.

Value

A new graph object.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu>

See Also

```
degree.sequence.game
```

Examples

```
g <- graph.ring(20)
g2 <- rewire(g, niter=3)</pre>
```

rewire.edges

Rewires the endpoints of the edges of a graph randomly

Description

This function rewires the endpoints of the edges with a constant probability uniformly randomly to a new vertex in a graph.

Usage

```
rewire.edges(graph, prob)
```

Arguments

graph The input graph

prob The rewiring probability, a real number between zero and one.

Details

Note that this function might create graphs with multiple and/or loop edges.

Value

A new graph object.

rglplot 151

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
# Some random shortcuts shorten the distances on a lattice g <- graph.lattice( length=100, dim=1, nei=5 ) average.path.length(g) g <- rewire.edges( g, prob=0.05 ) average.path.length(g)
```

rglplot

3D plotting of graphs with OpenGL

Description

Using the rgl package, rglplot plots a graph in 3D. The plot can be zoomed, rotated, shifted, etc. but the coordinates of the vertices is fixed.

Usage

```
rglplot(x, ...)
```

Arguments

x The graph to plot.

... Additional arguments, see igraph.plotting fo the details

Details

Note that rglplot is considered to be highly experimental. It is not very useful either. See igraph.plotting for the possible arguments.

Value

```
NULL, invisibly.
```

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

See Also

igraph.plotting, plot.igraph for the 2D version, tkplot for interactive graph drawing in 2D.

running.mean

Examples

```
## Not run:
g <- graph.lattice( c(5,5,5) )
coords <- layout.fruchterman.reingold(g, dim=3)
rglplot(g, layout=coords)
## End(Not run)</pre>
```

running.mean

Running mean of a time series

Description

running.mean calculates the running mean in a vector with the given bin width.

Usage

```
running.mean(v, binwidth)
```

Arguments

v The numeric vector.

binwidth Numeric constant, the size of the bin, should be meaningful, ie. smaller than the

length of v.

Details

The running mean of v is a w vector of length length(v)-binwidth+1. The first element of w id the average of the first binwidth elements of v, the second element of w is the average of elements 2:(binwidth+1), etc.

Value

A numeric vector of length length(v)-binwidth+1

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

Examples

```
running.mean(1:100, 10)
```

shortest.paths 153

shortest.paths

Shortest (directed or undirected) paths between vertices

Description

shortest.paths calculates the length of all the shortest paths from or to the vertices in the network. get.shortest.paths calculates one shortest path (the path itself, and not just its length) from or to the given vertex.

Usage

Arguments

Summers.		
graph	The graph to work on.	
V	Numeric vector, the vertices from or to which the shortest paths will be calculated.	
mode	Character constant, gives whether the shortest paths to or from the given vertices should be calculated for directed graphs. If out then the shortest paths <i>from</i> the vertex, if in then <i>to</i> it will be considered. If all, the default, then the corresponding undirected graph will be used, ie. not directed paths are searched. This argument is ignored for undirected graphs.	
weights	Possibly a numeric vector giving edge weights. If this is NULL and the graph has a weight edge attribute, then the attribute is used. If this is NA then no weights are used (even if the graph has a weight attribute).	
algorithm	Which algorithm to use for the calculation. By default igraph tries to select the fastest suitable algorithm. If there are no weights, then an unweighted breadth-first search is used, otherwise if all weights are positive, then Dijkstra's algorithm is used. If there are negative weights and we do the calculation for more than 100 sources, then Johnson's algorithm is used. Otherwise the Bellman-Ford algorithm is used. You can override igraph's choice by explicitly giving this parameter. Note that the igraph C core might still override your choice in obvious cases, i.e. if there are no edge weights, then the unweighted algorithm will be used, regardless of this argument.	
from	Numeric constant, the vertex from or to the shortest paths will be calculated.	

Note that right now this is not a vector of vertex ids, but only a single vertex.

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to Numeric vector, only the shortest paths to these vertices will be calculated. De-

faults to all vertices.

directed Whether to consider directed paths in directed graphs, this argument is ignored

for undirected graphs.

unconnected What to do if the graph is unconnected (not strongly connected if directed paths

are considered). If TRUE only the lengths of the existing paths are considered and averaged; if FALSE the length of the missing paths are counted having length vcount(graph), one longer than the longest possible geodesic in the

network.

verbose Logical scalar, whether to draw a progress meter while the calculation is run-

ning.

Details

The shortest paths (also called geodesics) are calculated by using breath-first search in the graph. If no edge weights were specified, then a breadth-first search is used to calculate the shortest paths. If edge weights are given and all of them are non-zero, then Dijkstra's algorithm is used. Otherwise the Bellman-Ford algorithm is used for shortest.paths.

Please do NOT call get.shortest.paths and get.all.shortest.paths with negative edge weights, it will not work, these functions do not use the Belmann-Ford algorithm.

Note that shortest.paths is able to calculate the path length from or to many vertices at the same time, but get.shortest.paths works from one source only. This might change in the future.

Also note that get.shortest.paths gives only one shortest path, however, more than one might exist between two vertices.

get.all.shortest.paths calculates all shortest paths from a vertex to other vertices given in the to argument.

path.length.hist calculates a histogram, by calculating the shortest path length between each pair of vertices. For directed graphs both directions are considered, so every pair of vertices appears twice in the histogram.

Value

For shortest.paths a numeric matrix with vcount(graph) columns and length(v) rows. The shortest path length from a vertex to itself is always zero. For unreachable vertices Inf is included.

For get.shortest.paths a list of length vcount(graph). List element i contains the vertex ids on the path from vertex from to vertex i (or the other way for directed graphs depending on the mode argument). The vector also contains from and i as the first and last elements. If from is the same as i then it is only included once. If there is no path between two vertices then a numeric vector of length zero is returned as the list element.

For get.all.shortest.paths a list is returned, each list element contains a shortest path from from to a vertex in to. The shortest paths to the same vertex are collected into consecutive elements of the list.

For average.path.length a single number is returned.

path.length.hist returns a named list with two entries: res is a numeric vector, the histogram of distances, unconnected is a numeric scalar, the number of pairs for which the first vertex is not

similarity 155

reachable from the second. The sum of the two entries is always n(n-1) for directed graphs and n(n-1)/2 for undirected graphs.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

West, D.B. (1996). Introduction to Graph Theory. Upper Saddle River, N.J.: Prentice Hall.

Examples

similarity

Similarity measures of two vertices

Description

These functions calculates similarity scores for vertices based on their connection patterns.

Usage

Arguments

graph	The input graph.
vids	The vertex ids for which the similarity is calculated.
mode	The type of neighboring vertices to use for the calculation, possible values: 'out', 'in', 'all'.
loops	Whether to include vertices themselves in the neighbor sets.

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Details

The Jaccard similarity coefficient of two vertices is the number of common neighbors divided by the number of vertices that are neighbors of at least one of the two vertices being considered. similarity.jaccard calculates the pairwise Jaccard similarities for some (or all) of the vertices.

The Dice similarity coefficient of two vertices is twice the number of common neighbors divided by the sum of the degrees of the vertices. similarity.dice calculates the pairwise Dice similarities for some (or all) of the vertices.

The inverse log-weighted similarity of two vertices is the number of their common neighbors, weighted by the inverse logarithm of their degrees. It is based on the assumption that two vertices should be considered more similar if they share a low-degree common neighbor, since high-degree common neighbors are more likely to appear even by pure chance. Isolated vertices will have zero similarity to any other vertex. Self-similarities are not calculated. See the following paper for more details: Lada A. Adamic and Eytan Adar: Friends and neighbors on the Web. Social Networks, 25(3):211-230, 2003.

Value

A length(vids) by length(vids) numeric matrix containing the similarity scores.

Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu> for the manual page.

References

Lada A. Adamic and Eytan Adar: Friends and neighbors on the Web. *Social Networks*, 25(3):211-230, 2003.

See Also

cocitation and bibcoupling

Examples

```
g <- graph.ring(5)
similarity.dice(g)
similarity.jaccard(g)</pre>
```

simplify

Simple graphs

Description

Simple graphs are graphs which do not contain loop and multiple edges.

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Usage

```
simplify(graph, remove.multiple = TRUE, remove.loops = TRUE)
is.simple(graph)
```

Arguments

graph The graph to work on.

remove.loops Logical, whether the loop edges are to be removed.

remove.multiple

Logical, whether the multiple edges are to be removed.

Details

A loop edge is an edge for which the two endpoints are the same vertex. Two edges are multiple edges if they have exactly the same two endpoints (for directed graphs order does matter). A graph is simple is it does not contain loop edges and multiple edges.

is. simple checks whether a graph is simple.

simplify removes the loop and/or multiple edges from a graph. If both remove.loops and remove.multiple are TRUE the function returns a simple graph.

Value

A new graph object with the edges deleted.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

See Also

```
is.loop, is.multiple and count.multiple, delete.edges, delete.vertices
```

Examples

```
g <- graph( c(1,2,1,2,3,3) )
is.simple(g)
is.simple(simplify(g, remove.loops=FALSE))
is.simple(simplify(g, remove.multiple=FALSE))
is.simple(simplify(g))</pre>
```

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spinglass.community

Finding communities in graphs based on statistical meachanics

Description

This function tries to find communities in graphs via a spin-glass model and simulated annealing.

Usage

Usage

Arguments

graph	The input graph, can be directed but the direction of the edges is neglected.
weights	The weights of the edges. Either a numeric vector or NULL. If it is null and the input graph has a 'weight' edge attribute then that will be used. If NULL and no such attribute is present then the edges will have equal weights.
spins	Integer constant, the number of spins to use. This is the upper limit for the number of communities. It is not a problem to supply a (reasonably) big number here, in which case some spin states will be unpopulated.
parupdate	Logical constant, whether to update the spins of the vertices in parallel (synchronously) or not. This argument is ignored if the second form of the function is used (ie. the 'vertex' argument is present).
start.temp	Real constant, the start temperature. This argument is ignored if the second form of the function is used (ie. the 'vertex' argument is present).
stop.temp	Real constant, the stop temperature. The simulation terminates if the temperature lowers below this level. This argument is ignored if the second form of the function is used (ie. the 'vertex' argument is present).
cool.fact	Cooling factor for the simulated annealing. This argument is ignored if the second form of the function is used (ie. the 'vertex' argument is present).
update.rule	Character constant giving the 'null-model' of the simulation. Possible values: "simple" and "config". "simple" uses a random graph with the same number of edges as the baseline probability and "config" uses a random graph with the same vertex degrees as the input graph.

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gamma Real constant, the gamma argument of the algorithm. This specifies the bal-

ance between the importance of present and non-present edges in a community. Roughly, a comunity is a set of vertices having many edges inside the community and few edges outside the community. The default 1.0 value makes existing and non-existing links equally important. Smaller values make the existing

links, greater values the missing links more important.

vertex This parameter can be used to calculate the community of a given vertex without

calculating all communities. Note that if this argument is present then some

other arguments are ignored.

Details

This function tries to find communities in a graph. A community is a set of nodes with many edges inside the community and few edges between outside it (ie. between the community itself and the rest of the graph.

Value

If the vertex argument is not given, ie. the first form is used then a named list is returned with the following slots:

membership Integer vector giving the communities found. The communities have ids starting

from zero and for each graph vertex ids community id is given in this vector.

The sizes of the communities in the order of their ids.

modularity The (generalized) modularity score of the result, as defined in the Reichardt-

Bornholdt paper, see references. If gamma is one, then it simplifies to the

Newman-Girvan modularity score.

temperature The temperature of the system when the algorithm terminated.

If the vertex argument is present, ie. the second form is used then a named list is returned with the following components:

community Numeric vector giving the ids of the vertices in the same community as vertex.

cohesion The cohesion score of the result, see references.

adhesion The adhesion score of the result, see references.

inner.links The number of edges within the community of vertex.

outer.links The number of edges between the community of vertex and the rest of the

graph.

Author(s)

Jorg Reichardt <lastname@physik.uni-wuerzburg.de> for the original code and Gabor Csardi <csardi@rmki.kfki.hu> for the igraph glue code

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References

J. Reichardt and S. Bornholdt: Statistical Mechanics of Community Detection, *Phys. Rev. E*, 74, 016110 (2006), http://arxiv.org/abs/cond-mat/0603718

M. E. J. Newman and M. Girvan: Finding and evaluating community structure in networks, *Phys. Rev. E* 69, 026113 (2004)

See Also

clusters

Examples

```
g <- erdos.renyi.game(10, 5/10) %du% erdos.renyi.game(9, 5/9)
g <- add.edges(g, c(0, 11))
g <- subgraph(g, subcomponent(g, 0))
spinglass.community(g, spins=2)
spinglass.community(g, vertex=0)</pre>
```

structure.info

Gaining information about graph structure

Description

Functions for exploring the basic structure of a network: number of vertices and edges, the neighbors of a node, test whether two vertices are connected by an edge.

Usage

```
vcount(graph)
ecount(graph)
neighbors(graph, v, mode = 1)
is.directed(graph)
are.connected(graph, v1, v2)
get.edge(graph, id)
get.edges(graph, es)
```

Arguments

graph	The graph.
V	The vertex of which the neighbors are queried.
mode	Character string, specifying the type of neighboring vertices to list in a directed graph. If "out" the vertices <i>to</i> which an edge exist are listed, if "in" the vertices <i>from</i> which an edge is directed are listed, "all" lists all the vertices. This argument is ignored for undirected graphs.
v1	The id of the first vertex. For directed graphs only edges pointing from v1 to v2

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v2	The id of the second vertex. For directed graphs only edges pointing from v1 to v2 are searched.
id	A numeric edge id.
es	An edge sequence.

Details

These functions provide the basic structural information of a graph.

vocunt gives the number of vertices in the graph.

ecount gives the number of edges in the graph.

neighbors gives the neighbors of a vertex. The vertices connected by multiple edges are listed as many times as the number of connecting edges.

is directed gives whether the graph is directed or not. It just gives its directed attribute.

are. connected decides whether there is an edge from v1 to v2.

get. edge returns the end points of the edge with the supplied edge id. For directed graph the source vertex comes first, for undirected graphs, the order is arbitrary.

get.edges returns a matrix with the endpoints of the edges in the edge sequence argument.

Value

vcount and ecount return integer constants. neighbors returns an integer vector. is.directed and are.connected return boolean constants. get.edge returns a numeric vector of length two. get.edges returns a two-column matrix.

Author(s)

Gabor Csardi < csardi @rmki.kfki.hu>

See Also

graph

Examples

```
g <- graph.ring(10)
vcount(g)
ecount(g)
neighbors(g, 5)
are.connected(g, 1, 2)
are.connected(g, 2, 4)
get.edges(g, 0:5)</pre>
```

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subgraph

Subgraph of a graph

Description

subgraph creates a subgraph of a graph, containing only the specified vertices and all the edges among them.

Usage

```
subgraph(graph, v)
```

Arguments

graph

The original graph.

٧

Numeric vector, the vertices of the original graph which will form the subgraph.

Details

The ids of the vertices will change in the subgraph of course since these are always consecutive.

Value

A new graph object.

Author(s)

```
Gabor Csardi <csardi@rmki.kfki.hu>
```

Examples

```
g <- graph.ring(10)
g2 <- subgraph(g, 1:7)</pre>
```

tkigraph

Experimental basic igraph GUI

Description

This functions starts an experimental GUI to some igraph functions. The GUI was written in Tcl/Tk, so it is cross platform.

Usage

```
tkigraph()
```

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Details

tkigraph has its own online help system, please see that for the details about how to use it.

Value

```
Returns NULL, invisibly.
```

Author(s)

```
Gabor Csardi <Gabor. Csardi@unil.ch>
```

See Also

tkplot for interactive plotting of graphs.

tkplot

Interactive plotting of graphs

Description

tkplot and its companion functions serve as an interactive graph drawing facility. Not all parameters of the plot can be changed interactively right now though, eg. the colors of vertices, edges, and also others have to be pre-defined.

Usage

```
tkplot(graph, canvas.width=450, canvas.height=450, ...)
tkplot.close(tkp.id, window.close = TRUE)
tkplot.off()
tkplot.fit.to.screen(tkp.id, width = NULL, height = NULL)
tkplot.reshape(tkp.id, newlayout, ...)
tkplot.export.postscript(tkp.id)
tkplot.getcoords(tkp.id, norm = FALSE)
tkplot.center(tkp.id)
tkplot.rotate(tkp.id, degree = NULL, rad = NULL)
```

Arguments

graph The graph to plot. canvas.width,canvas.height

The size of the tkplot drawing area.

tkp.id The id of the tkplot window to close/reshape/etc.

window.close Leave this on the default value.

width The width of the rectangle for generating new coordinates.

height The height of the rectangle for generating new coordinates.

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newlayout The new layout, see the layout parameter of tkplot.

norm Logical, should we norm the coordinates.

degree The degree to rotate the plot.

rad The degree to rotate the plot, in radian.

... Not used right now.

Details

tkplot is an interactive graph drawing facility. It is not very well developed at this stage, but it should be still useful.

It's handling should be quite straightforward most of the time, here are some remarks and hints.

There are different popup menus, activated by the right mouse button, for vertices and edges. Both operate on the current selection if the vertex/edge under the cursor is part of the selection and operate on the vertex/edge under the cursor if it is not.

One selection can be active at a time, either a vertex or an edge selection. A vertex/edge can be added to a selection by holding the control key while clicking on it with the left mouse button. Doing this again deselect the vertex/edge.

Selections can be made also from the Select menu. The 'Select some vertices' dialog allows to give an expression for the vertices to be selected: this can be a list of numeric R expessions separated by commas, like '1,2:10,12,14,15' for example. Similarly in the 'Select some edges' dialog two such lists can be given and all edges connecting a vertex in the first list to one in the second list will be selected.

In the color dialog a color name like 'orange' or RGB notation can also be used.

The tkplot command creates a new Tk window with the graphical representation of graph. The command returns an integer number, the tkplot id. The other commands utilize this id to be able to query or manipulate the plot.

tkplot.close closes the Tk plot with id tkp.id.

tkplot.off closes all Tk plots.

tkplot.fit.to.screen fits the plot to the given rectange (width and height), if some of these are NULL the actual phisical width od height of the plot window is used.

tkplot.reshape applies a new layout to the plot, its optional parameters will be collected to a list analogous to layout.par.

tkplot.export.postscript creates a dialog window for saving the plot in postscript format.

tkplot.getcoords returns the coordinates of the vertices in a matrix. Each row corresponds to one vertex.

tkplot.center shifts the figure to the center of its plot window.

tkplot.rotate rotates the figure, its parameter can be given either in degrees or in radians.

Value

tkplot returns an integer, the id of the plot, this can be used to manipulate it from the command line.

tkplot.getcoords returns a matrix with the coordinates.

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tkplot.close, tkplot.off, tkplot.fit.to.screen, tkplot.reshape, tkplot.export.postscript, tkplot.center and tkplot.rotate return NULL invisibly.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

```
plot.igraph, layout
```

Examples

```
g <- graph.ring(10)
## Not run: tkplot(g)</pre>
```

topological.sort

Topological sorting of vertices in a graph

Description

A topological sorting of a directed acyclic graph is a linear ordering of its nodes where each node comes before all nodes to which it has edges.

Usage

```
topological.sort(graph, mode=c("out", "all", "in"))
```

Arguments

graph The input graph, should be directed

mode Specifies how to use the direction of the edges. For "out", the sorting order

ensures that each node comes before all nodes to which it has edges, so nodes with no incoming edges go first. For "in", it is quite the opposite: each node comes before all nodes from which it receives edges. Nodes with no outgoing

edges go first.

Details

Every DAG has at least one topological sort, and may have many. This function returns a possible topological sort among them. If the graph is not acyclic (it has at least one cycle), a partial topological sort is returned and a warning is issued.

Value

A numeric vector containing vertex ids in topologically sorted order.

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Author(s)

Tamas Nepusz <ntamas@rmki.kfki.hu> and Gabor Csardi <csardi@rmki.kfki.hu> for the R interface

Examples

```
g <- barabasi.game(100)
topological.sort(g)</pre>
```

traits

Graph generation based on different vertex types

Description

These functions implement evolving network models based on different vertex types.

Usage

Arguments

nodes The number of vertices in the graph.

types The number of different vertex types.

edge.per.step The number of edges to add to the graph per time step.

type.dist The distribution of the vertex types. This is assumed to be stationary in time.

pref.matrix A matrix giving the preferences of the given vertex types. These should be

probabilities, ie. numbers between zero and one.

directed Logical constant, whether to generate directed graphs.

k The number of trials per time step, see details below.

Details

For callaway.traits.game the simulation goes like this: in each discrete time step a new vertex is added to the graph. The type of this vertex is generated based on type.dist. Then two vertices are selected uniformly randomly from the graph. The probability that they will be connected depends on the types of these vertices and is taken from pref.matrix. Then another two vertices are selected and this is repeated edges.per.step times in each time step.

For establishment.game the simulation goes like this: a single vertex is added at each time step. This new vertex tries to connect to k vertices in the graph. The probability that such a connection is realized depends on the types of the vertices involved and is taken from pref.matrix.

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Value

A new graph object.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

Examples

```
# two types of vertices, they like only themselves
g1 <- callaway.traits.game(1000, 2, pref.matrix=matrix( c(1,0,0,1), nc=2))
g2 <- establishment.game(1000, 2, k=2, pref.matrix=matrix( c(1,0,0,1), nc=2))</pre>
```

transitivity

Transitivity of a graph

Description

Transitivity measures the probability that the adjacent vertices of a vertex are connected. This is sometimes also called the clustering coefficient.

Usage

Arguments

graph

The graph to analyze.

type

The type of the transitivity to calculate. Possible values:

- globalThe global transitivity of an undirected graph (directed graphs are considered as undirected ones as well). This is simply the ratio of the triangles and the connected triples in the graph. For directed graph the direction of the edges is ignored.
- localThe local transitivity of an undirected graph, this is calculated for each vertex given in the vids argument. The local transitivity of a vertex is the ratio of the triangles connected to the vertex and the triples centered on the vertex. For directed graph the direction of the edges is ignored.
- undirectedThis is the same as global.
- globalundirectedThis is the same as global.
- localundirectedThis is the same as local.

vids

The vertex ids for the local transitivity will be calculated. This will be ignored for global transitivity types. The default value is NULL, in this case all vertices are considered. It is slightly faster to supply NULL here than V(graph).

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Value

For 'global' a single number, or NaN if there are no connected triples in the graph.

For 'local' a vector of transitivity scores, one for each vertex in 'vids'.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

Wasserman, S., and Faust, K. (1994). *Social Network Analysis: Methods and Applications*. Cambridge: Cambridge University Press.

Examples

```
g <- graph.ring(10)
transitivity(g)
g2 <- erdos.renyi.game(1000, 10/1000)
transitivity(g2) # this is about 10/1000</pre>
```

triad.census

Triad census, subgraphs with three vertices

Description

This function counts the different subgraphs of three vertices in a graph.

Usage

```
triad.census(graph)
```

Arguments

graph

The input graph, it should be directed. An undirected graph results a warning, and undefined results.

Details

Triad census was defined by David and Leinhardt (see References below). Every triple of vertices (A, B, C) are classified into the 16 possible states:

- 003A,B,C, the empty graph.
- 012A->B, C, the graph with a single directed edge.
- 102A<->B, C, the graph with a mutual connection between two vertices.
- 021DA<-B->C, the out-star.
- 021UA->B<-C, the in-star.

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- 021CA->B->C, directed line.
- 111DA<->B<-C.
- 111UA<->B->C.
- 030TA->B<-C, A->C.
- 030CA<-B<-C, A->C.
- 201A<->B<->C.
- 120DA<-B->C, A<->C.
- 120UA->B<-C, A<->C.
- 120CA->B->C, A<->C.
- 210A->B<->C, A<->C.
- 300A<->B<->C, A<->C, the complete graph.

This functions uses the RANDESU motif finder algorithm to find and count the subgraphs, see graph.motifs.

Value

A numeric vector, the subgraph counts, in the order given in the above description.

Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

References

See also Davis, J.A. and Leinhardt, S. (1972). The Structure of Positive Interpersonal Relations in Small Groups. In J. Berger (Ed.), Sociological Theories in Progress, Volume 2, 218-251. Boston: Houghton Mifflin.

See Also

dyad.census for classifying binary relationships, graph.motifs for the underlying implementa-

Examples

```
g <- erdos.renyi.game(15, 45, type="gnm", dir=TRUE)
triad.census(g)</pre>
```

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Convert a general graph into a forest

Description

Perform a breadth-first search on a graph and convert it into a tree or forest by replicating vertices that were found more than once.

Usage

```
unfold.tree(graph, mode = c("all", "out", "in", "total"), roots)
```

Arguments

graph The input graph, it can be either directed or undirected.

mode Character string, defined the types of the paths used for the breadth-first search.

"out" follows the outgoing, "in" the incoming edges, "all" and "total" both of

them. This argument is ignored for undirected graphs.

roots A vector giving the vertices from which the breadth-first search is performed.

Typically it contains one vertex per component.

Details

A forest is a graph, whose components are trees.

The roots vector can be calculated by simply doing a topological sort in all components of the graph, see the examples below.

Value

A list with two components:

tree The result, an igraph object, a tree or a forest.

vertex_index A numeric vector, it gives a mapping from the vertices of the new graph to the

vertices of the old graph.

Author(s)

```
Gabor Csardi <csardi.gabor@gmail.com>
```

Examples

Vertex shapes 171

Vertex shapes

Various vertex shapes when plotting igraph graphs

Description

Starting from version 0.5.1 igraph supports different vertex shapes when plotting graphs.

Details

Note that the current vertex shape implementation is experimental and it might change in the future. Currently vertex shapes are implemented only for plot.igraph.

In igraph a vertex shape is defined by a function that 1) provides information about the size of the shape for clipping the edges and 2) plots the shape if requested. These functions are called "shape functions" in the rest of this manual page.

Shape functions have a 'mode' argument that decides in which mode they should operate. 'clip' selects clipping mode and 'plot' selects plotting mode.

In clipping mode a shape function has the following arguments:

- coordsA matrix with four columns, it contains the coordinates of the vertices for the edge list supplied in the el argument.
- elA matrix with two columns, the edges of which some end points will be clipped. It should have the same number of rows as coords.
- mode"clip" for choosing clipping mode.
- paramsThis is a function object that can be called to query vertex/edge/plot graphical parameters. The first argument of the function is "vertex", "edge" or "plot" to decide the type of the parameter, the second is a character string giving the name of the parameter. E.g.

```
params("vertex", "size")
```

• endCharacter string, it gives which end points will be used. Possible values are "both", "from" and "to". If "from" the function is expected to clip the first column in the el edge list, "to" selects the second column, "both" selects both.

In 'clipping' mode, a shape function should return a matrix with the same number of rows as the el arguments. If end is both then the matrix must have four columns, otherwise two. The matrix contains the modified coordinates, with the clipping applied.

In plotting mode the following arguments are supplied to the shape function:

- coordsThe coordinates of the vertices, a matrix with two columns.
- vThe ids of the vertices to plot. It should match the number of rows in the coords argument.
- mode"plot" for choosing plotting mode.
- paramsThe same as in clipping mode, see above.

In 'plotting' mode the return value of the shape function is not used.

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Author(s)

Gabor Csardi <csardi@rmki.kfki.hu>

See Also

```
igraph.plotting, plot.igraph
```

Examples

```
## Not run:
g <- graph.ring(10, dir=TRUE, mut=TRUE)
plot(g, vertex.shape="rectangle", layout=layout.circle)
## End(Not run)</pre>
```

vertex.connectivity

Vertex connectivity.

Description

The vertex connectivity of a graph or two vertices, this is recently also called group cohesion.

Usage

```
vertex.connectivity(graph, source=NULL, target=NULL, checks=TRUE)
vertex.disjoint.paths(graph, source, target)
graph.cohesion(graph, checks=TRUE)
```

Arguments

graph	The input graph.
source	The id of the source vertex, for vertex.connectivity it can be NULL, see details below.
target	The id of the target vertex, for vertex.connectivity it can be NULL, see details below.
checks	Logical constant. Whether to check that the graph is connected and also the degree of the vertices. If the graph is not (strongly) connected then the connectivity is obviously zero. Otherwise if the minimum degree is one then the vertex connectivity is also one. It is a good idea to perform these checks, as they can be done quickly compared to the connectivity calculation itself. They were suggested by Peter McMahan, thanks Peter.

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Details

The vertex connectivity of two vertices (source and target) in a directed graph is the minimum number of vertices needed to remove from the graph to eliminate all (directed) paths from source to target. vertex.connectivity calculates this quantity if both the source and target arguments are given and they're not NULL.

The vertex connectivity of a graph is the minimum vertex connectivity of all (ordered) pairs of vertices in the graph. In other words this is the minimum number of vertices needed to remove to make the graph not strongly connected. (If the graph is not strongly connected then this is zero.) vertex.connectivity calculates this quantity if neither the source nor target arguments are given. (Ie. they are both NULL.)

A set of vertex disjoint directed paths from source to vertex is a set of directed paths between them whose vertices do not contain common vertices (apart from source and target). The maximum number of vertex disjoint paths between two vertices is the same as their vertex connectivity.

The cohesion of a graph (as defined by White and Harary, see references), is the vertex connectivity of the graph. This is calculated by graph.cohesion.

These three functions essentially calculate the same measure(s), more precisely vertex.connectivity is the most general, the other two are included only for the ease of using more descriptive function names.

Value

A scalar real value.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

References

Douglas R. White and Frank Harary: The cohesiveness of blocks in social networks: node connectivity and conditional density, TODO: citation

See Also

graph.maxflow, edge.connectivity, edge.disjoint.paths, graph.adhesion

Examples

```
g <- barabasi.game(100, m=1)
g <- delete.edges(g, E(g)[ 99 %--% 0 ])
g2 <- barabasi.game(100, m=5)
g2 <- delete.edges(g2, E(g2)[ 99 %--% 0])
vertex.connectivity(g, 99, 0)
vertex.connectivity(g2, 99, 0)
vertex.disjoint.paths(g2, 99, 0)
g <- erdos.renyi.game(50, 5/50)
g <- as.directed(g)
g <- subgraph(g, subcomponent(g, 1))</pre>
```

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graph.cohesion(g)

walktrap.community

Community strucure via short random walks

Description

This function tries to find densely connected subgraphs, also called communities in a graph via random walks. The idea is that short random walks tend to stay in the same community.

Usage

Arguments

graph The input graph, edge directions are ignored in directed graphs.

weights The edge weights.

steps The length of the random walks to perform.

merges Logical scalar, whether to include the merge matrix in the result.

modularity Logical scalar, whether to include the vector of the modularity scores in the

result. If the membership argument is true, then it will be always calculated.

labels Logical scalar, if TRUE and the graph has a vertex attribute called name then it

will be included in the result, in the list member called labels.

membership Logical scalar, whether to calculate the membership vector for the split corre-

sponding to the highest modularity value.

Details

This function is the implementation of the Walktrap community finding algorithm, see Pascal Pons, Matthieu Latapy: Computing communities in large networks using random walks, http://arxiv.org/abs/physics/0512106

Value

A named list with three members:

merges

The merges performed by the algorithm will be stored here. Each merge is a row in a two-column matrix and contains the ids of the merged communities. Communities are numbered from zero and cluster number smaller than the number of nodes in the network belong to the individual vertices as singleton communities. In each step a new community is created from two other communities and its id will be one larger than the largest community id so far. This means that before the first merge we have n communities (the number of vertices in the graph) numbered from zero to n-1. The first merge created community n, the second community n+1, etc.

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modularity Numeric vector, the modularity score of the current community structure after

each merge operation.

labels The labels of the vertices in the graph. The name vertex attribute will be copied

here, if exists.

membership If requested, then the membership vector that belongs to the best split, in terms

of highest modularity score.

Author(s)

Pascal Pons <google@for.it> and Gabor Csardi <csardi@rmki.kfki.hu> for the R and igraph interface

References

Pascal Pons, Matthieu Latapy: Computing communities in large networks using random walks, http://arxiv.org/abs/physics/0512106

See Also

modularity and fastgreedy.community, spinglass.community, leading.eigenvector.community, edge.betweenness.community for other community detection methods.

Examples

```
g <- graph.full(5) %du% graph.full(5) %du% graph.full(5) g <- add.edges(g, c(0,5, 0,10, 5, 10)) walktrap.community(g)
```

watts.strogatz.game

The Watts-Strogatz small-world model

Description

Generate a graph according to the Watts-Strogatz network model.

Usage

```
watts.strogatz.game(dim, size, nei, p)
```

Arguments

dim	Integer constant, the dimension of the starting lattice.
size	Integer constant, the size of the lattice along each dimension.
nei	Integer constant, the neighborhood within which the vertices of the lattice will be connected.
р	Real constant between zero and one, the rewiring probability.

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Details

First a lattice is created with the given dim, size and nei arguments. Then the edges of the lattice are rewired uniformly randomly with probability p.

Note that this function might create graphs with loops and/or multiple edges. You can use simplify to get rid of these.

Value

A graph object.

Author(s)

Gabor Csardi < csardi@rmki.kfki.hu>

References

Duncan J Watts and Steven H Strogatz: Collective dynamics of 'small world' networks, Nature 393, 440-442, 1998.

See Also

```
graph.lattice, rewire.edges
```

Examples

```
g <- watts.strogatz.game(1, 100, 5, 0.05)
average.path.length(g)
transitivity(g, type="average")</pre>
```

write.graph

Writing the graph to a file in some format

Description

write.graph is a general function for exporting graphs to foreign file formats, however not many formats are implemented right now.

Usage

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Arguments

graph The graph to export.

file A connection or a string giving the file name to write the graph to.

format Character string giving the file format. Right now pajek, graphml, dot, gml,

edgelist, lgl, ncol and dimacs are implemented. As of igraph 0.4 this argu-

ment is case insensitive.

... Other, format specific arguments, see below.

Details

The edgelist format is a simple text file, with one edge in a line, the two vertex ids separated by a space character. The file is sorted by the first and the second column. This format has no additional arguments.

The Pajek format is a text file, see read.graph for details. Appropriate vertex and edge attributes are also written to the file. This format has no additional arguments.

The GraphML format is a flexible XML based format. See read.graph for GraphML details. Vertex and edge attributes are also written to the file. This format has no additional arguments.

The dot format is used by the popular GraphViz program. Vertex and edge attributes are written to the file. There are no additional arguments for this format.

The 1g1 format is also a simple text file, this is the format expected by the 'Large Graph Layout' layout generator software. See read.graph for details. Additional arguments:

- namesIf you want to write symbolic vertex names instead of vertex ids, supply the name of the
 vertex attribute containing the symbolic names here. By default the 'name' attribute is used
 if there is one. Supply NULL if you want to use numeric vertex ids even if there is a 'name'
 vertex attribute.
- weightsIf you want to write edge weights to the file, supply the name of the edge attribute here. By defaults the vertex attribute 'weights' are used if they are installed. Supply NULL here if you want to omit the weights.
- isolatesLogical, if TRUE the isolate vertices are also written to the file, they are omitted by default.

The ncol format is also used by LGL, it is a text file, see read.graph for details. Additional arguments:

- namesIf you want to write symbolic vertex names instead of vertex ids, supply the name of the vertex attribute containing the symbolic names here. By default the 'name' attribute is used if there is one. Supply NULL if you want to use numeric vertex ids even if there is a 'name' vertex attribute.
- weightsIf you want to write edge weights to the file, supply the name of the edge attribute here. By defaults the vertex attribute 'weights' are used if they are installed. Supply NULL here if you want to omit the weights.

The dimacs file format, more specifically the version for network flow problems, see the files at ftp://dimacs.rutgers.edu/pub/netflow/general-info/

This is a line-oriented text file (ASCII) format. The first character of each line defines the type of the line. If the first character is c the line is a comment line and it is ignored. There is one problem

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line (p in the file, it must appear before any node and arc descriptor lines. The problem line has three fields separated by spaces: the problem type (min, max or asn), the number of vertices and number of edges in the graph. Exactly two node identification lines are expected (n), one for the source, one for the target vertex. These have two fields: the id of the vertex and the type of the vertex, either s (=source) or t (=target). Arc lines start with a and have three fields: the source vertex, the target vertex and the edge capacity.

Vertex ids are numbered from 1.

Additional arguments:

- sourceThe id of the source vertex, if NULL (the default) then it is taken from the source graph attribute.
- targetThe id of the target vertex, if NULL (the default) then it is taken from the target graph attribute.
- capacityA numeric vector giving the edge capacities. If NULL (the default) then it is taken from the capacity edge attribute.

GML is a quite general textual format, see http://www.infosun.fim.uni-passau.de/Graphlet/GML/ for details.

The graph, vertex and edges attributes are written to the file as well, if they are numeric of string.

As igraph is more forgiving about attribute names, it might be neccessary to simplify the them before writing to the GML file. This way we'll have a syntactically correct GML file. The following simple procedure is performed on each attribute name: first the alphanumeric characters are extracted, the others are ignored. Then if the first character is not a letter then the attribute name is prefixed with <quote>igraph</quote>. Note that this might result identical names for two attributes, igraph does not check this.

The "id" vertex attribute is treated specially. If the id argument is not NULL then it should be a numeric vector with the vertex ids and the "id" vertex attribute is ignored (if there is one). If id is 0 and there is a numeric id vertex attribute that is used instead. If ids are not specified in either way then the regular igraph vertex ids are used.

Note that whichever way vertex ids are specified, their uniqueness is not checked.

If the graph has edge attributes named "source" or "target" they're silently ignored. GML uses these attributes to specify the edges, so we cannot write them to the file. Rename them before calling this function if you want to preserve them.

Additional arguments:

- idNULL or a numeric vector giving the vertex ids. See details above.
- creatorA character scalar to be added to the "Creator" line in the GML file. If this is NULL (the default) then the current date and time is added.

Value

A NULL, invisibly.

Author(s)

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References

Adai AT, Date SV, Wieland S, Marcotte EM. LGL: creating a map of protein function with an algorithm for visualizing very large biological networks. *J Mol Biol.* 2004 Jun 25;340(1):179-90.

See Also

```
read.graph
```

Examples

```
g <- graph.ring(10)
## Not run: write.graph(g, "/tmp/g.txt", "edgelist")</pre>
```

write.pajek.bgraph

Write graphs and their cohesive block hierarchy as Pajek files

Description

Creates a series of Pajek-compatible files from a bgraph object as output by cohesive.blocks.

Usage

```
write.pajek.bgraph(graph, filename, hierarchy = FALSE)
```

Arguments

graph A bgraph object as output by cohesive.blocks.

filename *without file extension* to use.

hierarchy Logical. Should a separate .clu file be created for each block in the graph? (see

details)

Details

This function writes at least two files to disk. First, the file filename.net contains the basic graph structure—vertices and edges. The second is the file filename.clu, which clusters the vertices according to vertex connectivity of their maxmally cohesive subgraph. This uses the same logic as the default vertex coloring in plot.bgraph.

If hierarchy is TRUE, more detailed and complete information is written to a further series of files. For each block a seperate .clu file is written, each named like "filename_block2(1).clu", where the first number refers to the block number and the number in parenthesis refers to that block's cohesion. Finally, if hierarchy is TRUE, a tree representing the block hierarchy is written to filename_blocktree.net, allowing the subset-structure of the individual block structures to be determined.

Note

This function has not been thoroughly tested, and may contain bugs

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References

Pajek website: http://vlado.fmf.uni-lj.si/pub/networks/pajek/

See Also

cohesive.blocks, plot.bgraph, write.graph

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