#### emcee: An Affine-Invariant Sampler

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Symmetries Graduate School 2023-01-30

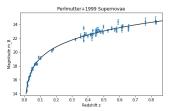
Borrowing heavily from Dan Foreman-Mackey's slides https://speakerdeck.com/dfm/data-analysis-with-mcmc1 These slides are available at

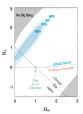
https://github.com/dstndstn/MCMC-talk/emcee-slides

### Recap from last week's lecture (1)

- Markov Chain Monte Carlo (MCMC) draws samples from a probability distribution when you can numerically evaluate the probability function (up to a constant)
- Used extensively in data analysis: inferring parameters of models, given observed data
- Usually in a Bayesian context; the probability function we run MCMC on is the *posterior* probability: posterior(params|data)  $\propto$

 $prior(params) \times likelihood(data|params)$ 



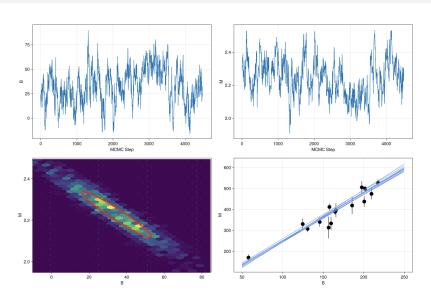


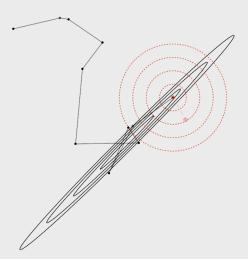
### Recap from last week's lecture (2)

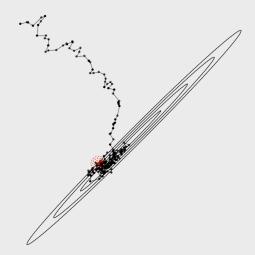
- ► The "classic" Markov Chain Monte Carlo algorithm is Metropolis—Hastings, which moves a walker or particle around the state space (model parameter space)
- A randomly-drawn proposed jump gets evaluated (by calling the probability function), and then accepted, or not
- ➤ A big difficulty is to customize the proposal distribution to get the algorithm to work efficiently

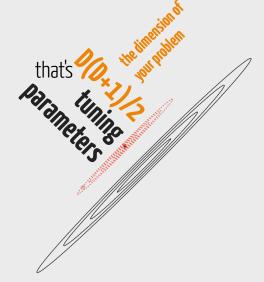


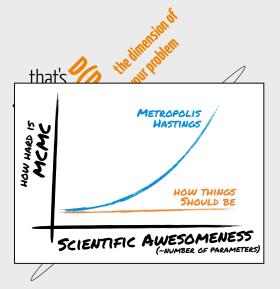
### MCMC for model parameter inference











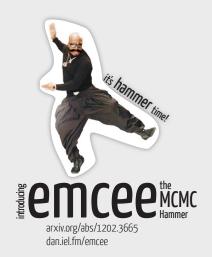




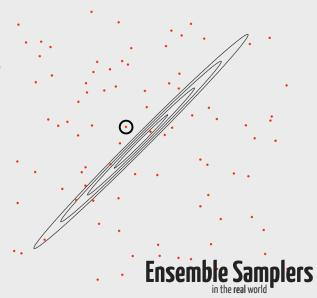


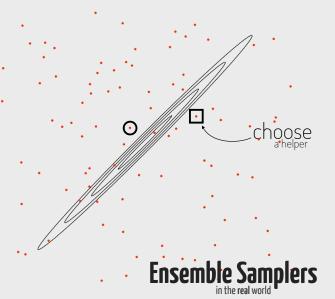
Jonathan Weare

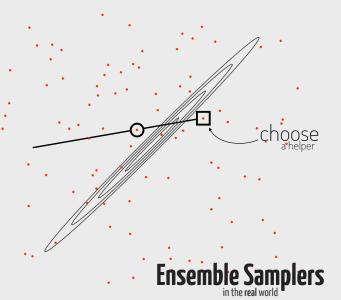
### "Ensemble samplers with affine invariance" (dfm.io/mcmc-gw10)



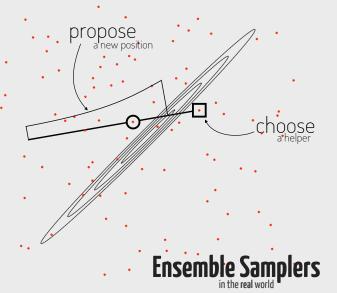




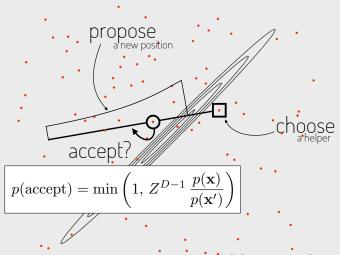




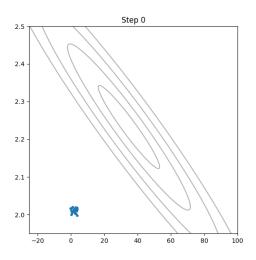
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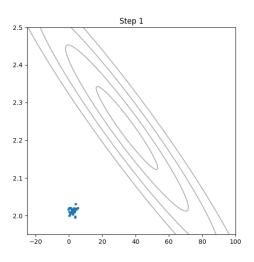


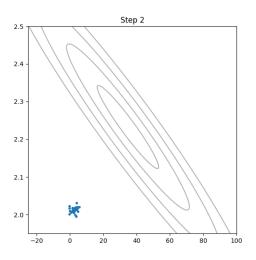
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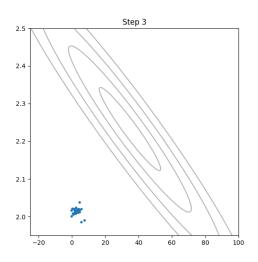


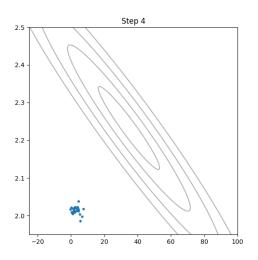
# Ensemble Samplers in the real world

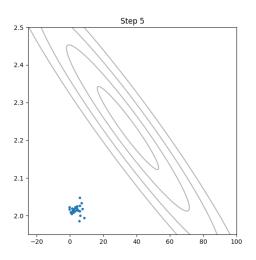


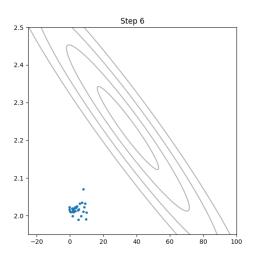


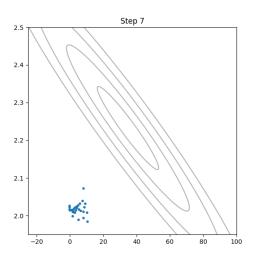


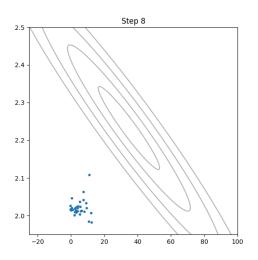


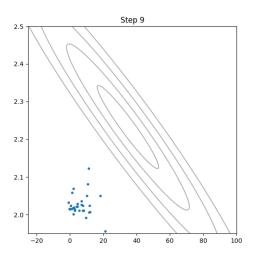


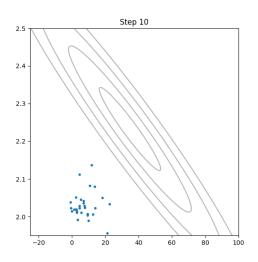


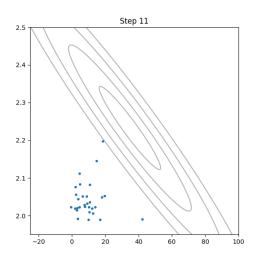


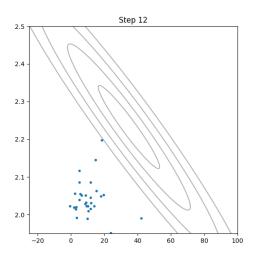


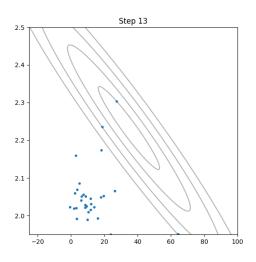


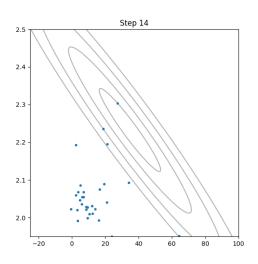


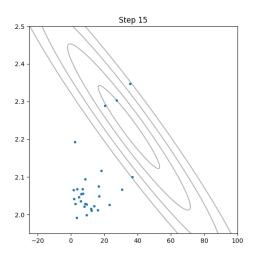


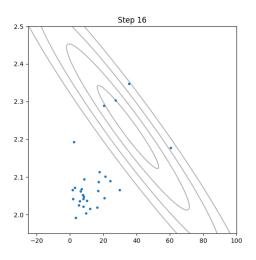


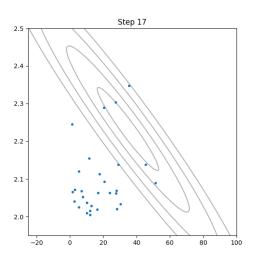


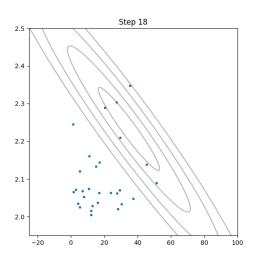


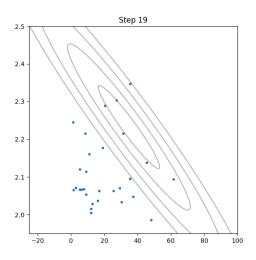


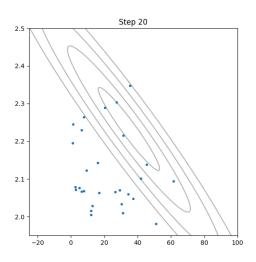


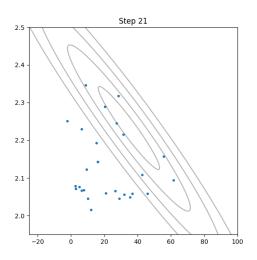


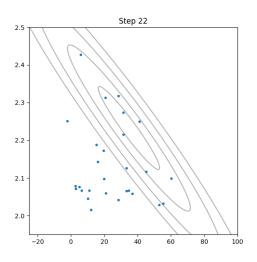


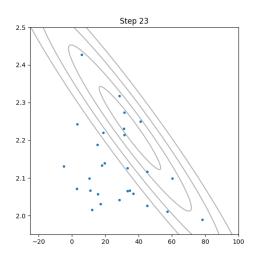


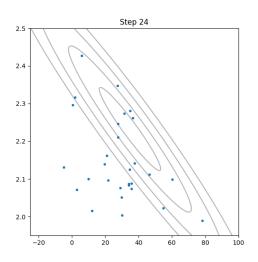


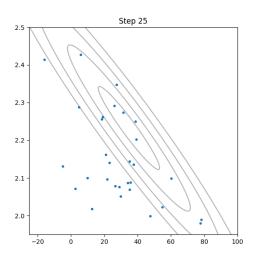


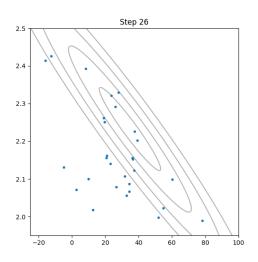


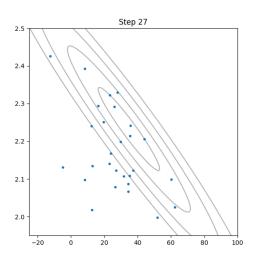


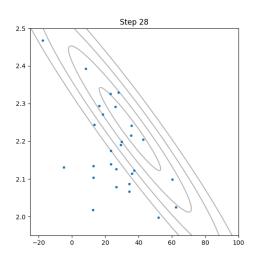


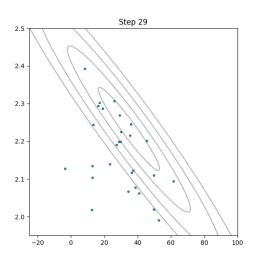


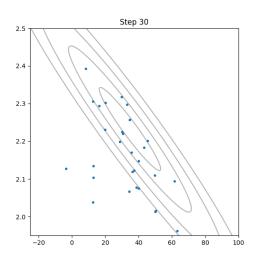


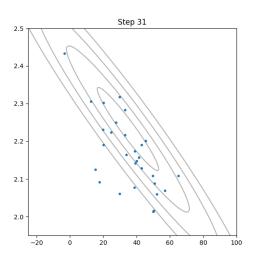


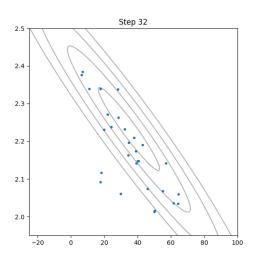


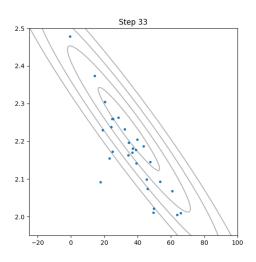


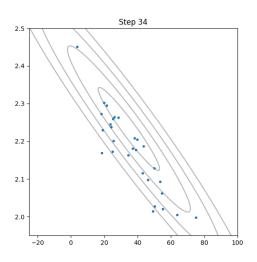


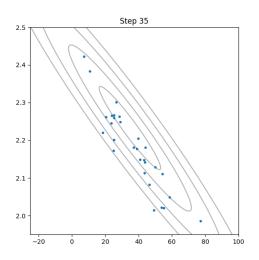


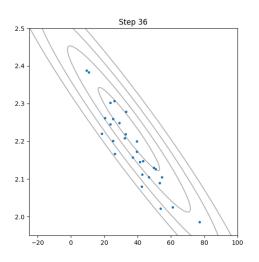


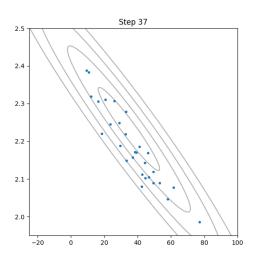


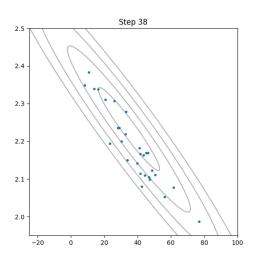


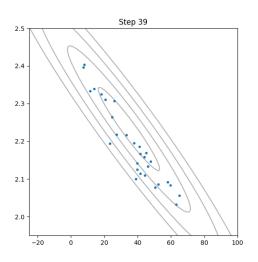


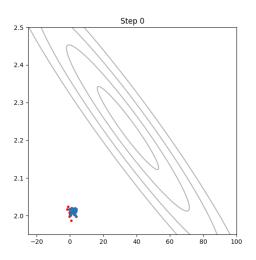


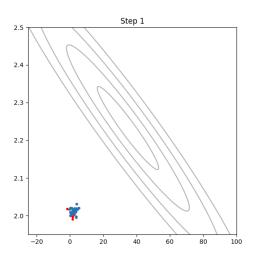


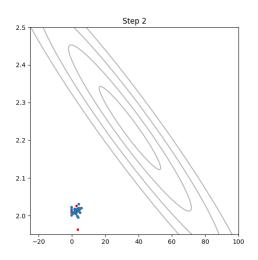


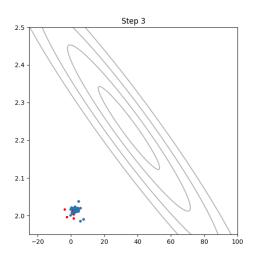


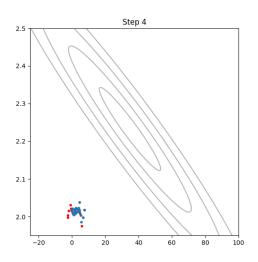


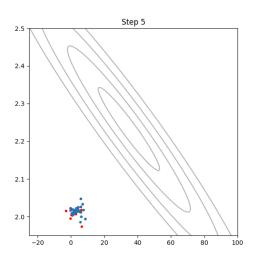


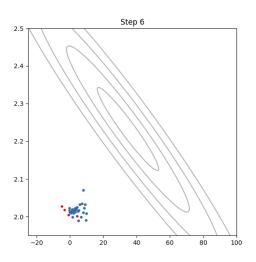


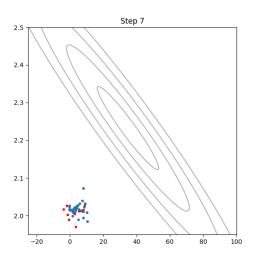


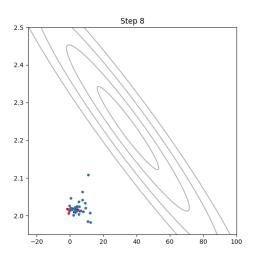


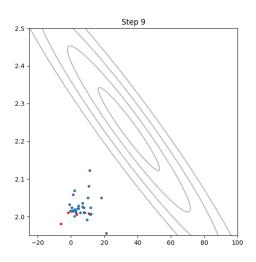


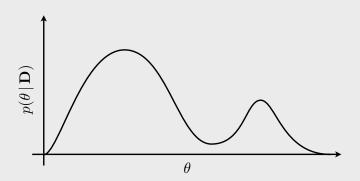


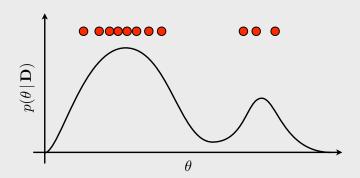


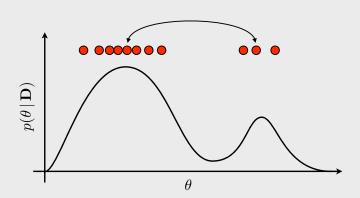






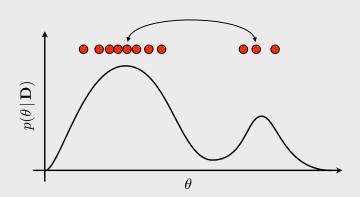






#### Differential Evolution move

- emcee allows us to use different move types (different proposal functions)
- ► The Differential Evolution (DE) move can improve the sampling for multi-modal distributions
- DE move: randomly select two "helpers"
- Propose moving by their vector difference
- (If they are from different modes, this proposes jumping between modes)
- Mixing in a fraction of DE moves with the regular "Stretch" move works well!



### Summary

- Traditional Metropolis—Hastings MCMC suffers from a lack of affine invariance – requires tuning parameters that change for each specific probability function
- Ensemble samplers like emcee use the distribution of the walkers to achieve affine invariance
- ➤ much easier to use, and faster sampling
- (Huge side effect: parallelizable!)
- Multi-modal distributions still hard, but DE Move can help
- MCMC isn't scary!