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#!/usr/bin/env python
# coding: utf-8
# Import Numpy & PyTorch
import torch
import numpy as np
import matplotlib.pyplot as plt
import logging, sys, os
import torch.nn as nn
from torch.utils.data import TensorDataset, DataLoader
# Import nn.functional
import torch.nn.functional as F
# class LogFile(object):
      """File-like object to log text using the `logging` module."""
      def __init__(self, name=None):
          self.logger = logging.getLogger(name)
      def write(self, msg, level=logging.INFO):
#
          self.logger.log(level, msg)
      def flush(self):
#
#
          for handler in self.logger.handlers:
              handler.flush()
# logging.basicConfig(filename = "Linear Regression Exercise.log")
# # Redirect stdout and stderr
# sys.stdout = LogFile('stdout')
# sys.stderr = LogFile('stderr')
logging.basicConfig(filename='Linear Regression.log', encoding='utf-8', level=logging.DEBUG)
# Define the data
T = np.array([1,1])
T = T.reshape(2,1)
n = 100
# Create empty file
logfile = os.path.realpath(__file__)[0:-2] + "log"
with open(logfile, "w") as f: pass
def xprint(msg):
    print(msg)
    f = open(logfile, "a")
    f.write(msg + "\n")
    f.close()
def reg_compare(T,n):
    # Define loss function
    def mse(t1, t2):
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diff = t1 - t2
    return torch.sum(diff * diff) / diff.numel()
# Define model 1 (manual)
def model(x):
    return x@w.t()
# Define a utility function to train the model
def fit(num_epochs, model, loss_fn, opt, inputs):
    for epoch in range(num epochs):
        for xb,yb in train_dl:
            # Generate predictions
            pred = model(xb)
            loss = loss_fn(pred, yb)
            # Perform gradient descent
            loss.backward()
            opt.step()
            opt.zero grad()
    return model(inputs)
class SimpleNet(nn.Module):
    # Initialize the layers
    def __init__(self):
        super(). init ()
        self.linear1 = nn.Linear(2, 2)
        self.act1 = nn.ReLU() # Activation function
        self.linear2 = nn.Linear(2, 1)
    # Perform the computation
    def forward(self, x):
        x = self.linear1(x)
        x = self.act1(x)
        x = self.linear2(x)
        return x
# Define model 2 (PyTorch)
model2 = nn.Linear(2, 1)
opt_2 = torch.optim.SGD(model2.parameters(), lr=.001)
loss_fn = F.mse_loss
#loss = loss fn(model2(inputs), targets)
# Define model 3 (Neural Network)
model3 = SimpleNet()
opt_n = torch.optim.SGD(model3.parameters(), .003)
loss_fn = F.mse_loss
# Define Data
X = 10 * np.random.rand(n,1)
b = np.ones_like(X)
X1 = np.hstack((b,X))
X1_d = X1.astype(np.float32)
F1 = np.dot(X1, T)
eps = np.random.randn(n,1)
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Y1 = F1 + eps
Y1_d = Y1.astype(np.float32)
# Define PyTorch tensors
\#X_{tens} = torch.tensor(X)
#X1 tens = torch.tensor(X1)
#X1 tens = x
X1_d_tens = torch.from_numpy(X1_d)
#F1_tens = torch.from_numpy(F1)
Y1 tens = torch.from numpy(Y1)
Y2_d_tens = torch.from_numpy(Y1_d)
#Y1 tens = y
# Define model inputs and targets and initalize weights and bias
#inputs d = X1 d tens
inputs = X1 d tens
#inputs2 = X1_tens
targets = Y1_tens
targets2 = Y2_d_tens
w = torch.randn(1,2, requires_grad=True)
train_ds = TensorDataset(inputs, targets2)
# Define data Loader
batch_size = 5
train_dl = DataLoader(train_ds, batch_size, shuffle=True)
# Closed form
h = X1.transpose() @ X1
h_inv = np.linalg.inv(h)
p = np.dot(X1.transpose(), Y1)
theta_closed = h_inv @ p
y1_closed = np.dot(X1, theta_closed)
e_closed_sum = np.sqrt(1/n*np.dot((F1-y1_closed).transpose(),(F1-y1_closed)))
#Train model for 100 epochs
# Iterate and modify via gradient decent
for i in range(500):
    preds = model(inputs)
    loss = mse(preds, targets)
    loss.backward()
    with torch.no_grad():
        w -= w.grad * .01
        w.grad.zero_()
y1_grad = preds
e_1grad_sum = np.sqrt(1/n*np.dot((F1-y1_grad.detach().numpy()).transpose(),(F1-y1_grad.detach()
# Train the model 2 for 100 epochs
y2_grad = fit(100, model2, loss_fn, opt_2, inputs)
e_2grad_sum = np.sqrt(1/n*np.dot((F1-y2_grad.detach().numpy()).transpose(),(F1-y2_grad.detach()
# Train model 3 for 100 epochs
y3_network = fit(500, model3, loss_fn, opt_n, inputs)
e_network_sum = np.sqrt(1/n*np.dot((F1-y3_network.detach().numpy()).transpose(),(F1-y3_network.
data_return = [X, Y1, y1_closed, y1_grad, y2_grad, y3_network, F1]
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return e closed sum, e 1grad sum, e 2grad sum, e network sum, data return
error_closed_sum = 0
error_1grad_sum = 0
error 2grad sum = 0
error_network_sum = 0
# Set number of iterations
N = 100
for j in range(N):
    e_closed_sum, e_1grad_sum, e_2grad_sum, e_network_sum, data_return = reg_compare(T,n)
    error_closed_sum += e_closed_sum
    error 1grad sum += e 1grad sum
    error_2grad_sum += e_2grad_sum
    error_network_sum += e_network_sum
    if j < N-1:
        del data return
# Calculate average error
error_closed = error_closed_sum / N
error_1grad = error_1grad_sum / N
error_2grad = error_2grad_sum / N
error network = error network sum / N
xprint('Average Matrix inverion solution error = '+ str(error closed))
xprint('Average Manual model solution error = '+ str(error_1grad))
xprint('Average Pytorch model solution error = '+ str(error 2grad))
xprint('Average Single layer neural network solution error = '+ str(error network))
# Plot data points
fig, bx = plt.subplots()
bx.scatter(data_return[0],data_return[1])
bx.plot(data return[0],data return[2], color='k')
bx.plot(data return[0], data_return[3].detach().numpy(), color='g')
bx.plot(data_return[0],data_return[4].detach().numpy(), color='c')
bx.plot(data_return[0],data_return[5].detach().numpy(), color='m')
bx.plot(data return[0], data return[6], color='r')
plt.xlabel("X")
plt.ylabel("Y")
plt.title("Linear Regression")
bx.legend(['Matrix Inversion', 'Manual Model', 'PyTorch Model', 'Single Layer Neural Net', 'True','
plt.savefig('Comparison plot.pdf')
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