Parallel Algorithms and Programming

Lab 5 report

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1 Fox Algorithm

We successfully implemented the Fox's algorithm with MPI.

Since we do not handle the data distribution in this exercises, all the processes are initialized with a value a and b as a block of matrix A and B. Also a variable c to store the result of computation of the final matrix in the same block.

Given the number or process available N, we always create a matrix of size $n \times n$ where $n = \sqrt{N}$ if $N \mod 2 = 0$ or $\sqrt{N-1}$ if $N \mod 2 \neq 0$

We create a grid process, and 2 sub-communicator are for row and column. The row communicator is used for broadcasting the value of matrix A as every stage, the whole row using the same value of a certain block in that row. The column matrix is used for shifting the value of matrix B.

N.B: The code provided has the matrix value initialized in each block corresponded to the same rank of the process holding it for the purpose of testing, the code for random value also provided

2 Cannon Algorithm

We successfully implemented the algorithm with MPI.

The same setup is used from the previous exercise: Matrix value initialization, Grid size, sub-communicator. The different comes from the algorithm itself, when we have to do a pre-skewing and post-skewing stage before and after the loop run.

There are optimization we did in this exercise, we created more local variables to store values of matrix A and B during the shifting. Because of that, we avoid modifying the original value of matrix A and B. Thanks to this, the post-skewing stage is unnecessary. This will save us some communication cost to restore the initial state of the matrix.

N.B: The optimization is done in file ex2-op.c

3 Data distribution

For this exercises, we tried to utilized the vector datatype of MPI by define a typeMatCol, and type MatRow. While doing the Scatterv function, we stuck dealing with distributing the MatB while MatA is run perfectly.

The only thing, we noticed is that the blocks of value that got problem are all supposed to have the same data. We have that problem and don't know how to fix it. We did try to used both dynamic allocation and static allocation.

4 Performance Evaluation

We did some performance test with Fox Algorithm, Cannon Algorithm, also with a sequential code (written by ourselves)

```
Performance counter stats for 'mpirun -n 64 ./ex1':
     52160.572306
                        task-clock (msec)
                                                        23.311 CPUs utilized
          239,729
                        context-switches
                                                         0.005 M/sec
                                                   #
           53,888
                        cpu-migrations
                                                         0.001 M/sec
                        page-faults
          263,539
                                                         0.005 M/sec
  144,663,274,711
                        cvcles
                                                         2.773 GHz
                                                                                          (50.95%)
   41,422,459,797
                        instructions
                                                         0.29
                                                               insn per cycle
                                                                                          (63.41%)
                                                       175.299 M/sec
    9,143,703,012
                        branches
                                                                                          (63.03%)
       85,878,529
                                                         0.94% of all branches
                        branch-misses
                                                                                          (62.67%)
     ,816,350,157
                        L1-dcache-loads
                                                       226.538 M/sec
                                                                                          (62.30%)
      251,219,612
                        L1-dcache-load-misses
                                                   #
                                                         2.13% of all L1-dcache hits
                                                                                          (62.32\%)
       31,174,136
                        LLC-loads
                                                         0.598 M/sec
                                                                                          (50.20%)
                                                        14.84% of all LL-cache hits
        4,625,911
                        LLC-load-misses
      2.237566214 seconds time elapsed
```

Figure 1: Fox algorithm with 8x8 matrix

```
Performance counter stats for 'mpirun -n 64 ./ex2':
     58236.937831
                                                       24.493 CPUs utilized
                        task-clock (msec)
                                                   #
          292,254
                        context-switches
                                                   #
                                                        0.005 M/sec
                        cpu-migrations
           54,002
                                                   #
                                                        0.927 K/sec
                                                   #
          263,832
                        page-faults
                                                        0.005 M/sec
  161,953,265,688
                        cycles
                                                        2.781 GHz
                                                   #
                                                                                         (50.62\%)
   46,264,153,570
                                                        0.29 insn per cycle
                        instructions
                                                                                         (63.13\%)
                                                   #
   10,329,897,081
                        branches
                                                   #
                                                      177.377 M/sec
                                                                                         (62.85\%)
                                                        0.88% of all branches
       90,991,829
                        branch-misses
                                                   #
                                                                                         (62.73\%)
   13,356,160,516
                        L1-dcache-loads
                                                      229.342 M/sec
                                                                                         (62.54\%)
                                                   #
      280,486,560
                        L1-dcache-load-misses
                                                   #
                                                       2.10% of all L1-dcache hits
                                                                                         (62.42\%)
       32,486,627
                        LLC-loads
                                                   #
                                                        0.558 M/sec
                                                                                         (50.18\%)
        5,067,407
                                                       15.60% of all LL-cache hits
                        LLC-load-misses
                                                   #
                                                                                         (50.46\%)
      2.377730854 seconds time elapsed
```

Figure 2: Cannon algorithm with 8x8 matrix

```
Performance counter stats for 'mpirun -n 64 ./ex2-op':
     56279.062778
                        task-clock (msec)
                                                         23.791 CPUs utilized
          318,358
                        context-switches
                                                     #
                                                          0.006 M/sec
           55,810
                        cpu-migrations
                                                     #
                                                          0.992 K/sec
                        page-faults
                                                          0.005 M/sec
          263,474
  156,844,996,423
                        cycles
                                                     #
                                                          2.787 GHz
                                                                                            (50.27%)
   42,703,411,774
9,430,690,073
                        instructions
                                                     #
                                                          0.27 insn per cycle
                                                                                            (62.96\%)
                                                        167.570 M/sec
                        branches
                                                     #
                                                                                            (62.93\%)
       92,212,928
                        branch-misses
                                                     #
                                                          0.98% of all branches
                                                                                            (62.90\%)
   12,310,408,203
304,046,317
                        L1-dcache-loads
                                                        218.739 M/sec
                                                                                            (62.80\%)
                        L1-dcache-load-misses
                                                          2.47% of all L1-dcache hits
                                                     #
                                                                                            (62.81\%)
       29,167,822
                        LLC-loads
                                                     #
                                                          0.518 M/sec
                                                                                            (49.96\%)
        4,780,283
                        LLC-load-misses
                                                     #
                                                         16.39% of all LL-cache hits
                                                                                            (50.28\%)
      2.365564677 seconds time elapsed
```

Figure 3: Cannon algorithm with 8x8 matrix (optimized version)

```
Performance counter stats for 'mpirun -n 64 ./seq':
       175.417895
                        task-clock (msec)
                                                         0.362 CPUs utilized
                        context-switches
              409
                                                    #
                                                         0.002 M/sec
                                                         0.764 K/sec
                                                    #
              134
                        cpu-migrations
           19,608
                        page-faults
                                                    #
                                                         0.112 M/sec
      533,461,438
                        cycles
                                                         3.041 GHz
                                                                                          (52.08\%)
                                                    #
      604,911,838
                                                    #
                        instructions
                                                         1.13 insn per cycle
                                                                                           (68.31\%)
      135,044,141
2,772,900
                        branches
                                                    #
                                                       769.842 M/sec
                                                                                           (69.04\%)
                                                        2.05% of all branches
                                                                                           (79.44\%)
                        branch-misses
                                                   #
      171,242,657
                        L1-dcache-loads
                                                    #
                                                      976.198 M/sec
                                                                                           (76.67\%)
       11,774,676
                        L1-dcache-load-misses
                                                        6.88% of all L1-dcache hits
                                                                                           (71.33\%)
        1,414,084
                        LLC-loads
                                                         8.061 M/sec
                                                                                           (54.93\%)
                                                    #
          238,117
                        LLC-load-misses
                                                    #
                                                        16.84% of all LL-cache hits
                                                                                           (48.05\%)
      0.484986967 seconds time elapsed
```

Figure 4: Sequential with 8x8 matrix

We realized that our implementation has a very simple local computation as 1 value is hold in one process. This make the sequential time so small as they don't have communication cost.

There is one remark is our Canon optimized version actually run faster than the normal implementation. But since the size of the matrix that we test is not very big, the amount is not much.