

Maxwell equations

$$\oint_S \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

$$\oint_S \mathbf{B} \cdot d\mathbf{A} = 0$$

$$\oint_C \mathbf{B} \cdot d\mathbf{l} = \mu_0 \int_S \left(\mathbf{j} + \epsilon_0 \frac{\partial \mathbf{E}}{\partial t} \right) \cdot d\mathbf{A}$$

$$\oint_C \mathbf{E} \cdot d\mathbf{l} = -\frac{d}{dt} \int_S \mathbf{B} \cdot d\mathbf{A}$$

Other Electricity and Magnetism key equations

$$\mathbf{F} = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} \hat{\mathbf{r}}$$

Coulomb's Law

$$\mathbf{F} = q\mathbf{E}$$

Force in E-field

$$\oint_S \mathbf{E} \cdot d\mathbf{A} = \frac{Q}{\epsilon_0}$$

Gauss' Law for electric field

$$\mathbf{E} = \frac{q}{4\pi\epsilon_0 r^2} \hat{\mathbf{r}}$$

E-field for a point charge

$$\mathbf{E} = \frac{\lambda}{2\pi r \epsilon_0} \hat{\mathbf{r}}$$

E-field for a line charge

$$\mathbf{E} = \frac{\sigma}{2\epsilon_0} \hat{\mathbf{z}}$$

E-field for a plane of charge

$$\oint_C \mathbf{E} \cdot d\mathbf{l} = 0$$

Electrostatic circulation of E-field

$$\phi(r) = -\int_{\infty}^r \mathbf{E} \cdot d\mathbf{l}$$

Scalar electric potential

$$\mathbf{E} = -\nabla\phi$$

Electric field from potential

$$\Delta\phi = IR$$

Ohm's law

$$I = \int_S \mathbf{j} \cdot d\mathbf{A}$$

Current and current density

$$u_E = \frac{\epsilon_0 E^2}{2}$$

E-field energy density

$$\mathbf{p} = q\mathbf{d}$$

Electric dipole

$$\phi(\theta) = \frac{Qd \cos \theta}{4\pi\epsilon_0 r^2}$$

Electric dipole potential

$$\mathbf{E} = \frac{Qd}{4\pi\epsilon_0 r^3} (2 \cos \theta \hat{\mathbf{r}} + \sin \theta \hat{\boldsymbol{\theta}})$$

Electric dipole field

$$\boldsymbol{\tau} = \mathbf{p} \times \mathbf{E}$$

Torque on electric dipole

$$U = -\mathbf{p} \cdot \mathbf{E}$$

Electric dipole energy

$$\mathbf{F} = q(\mathbf{v} \times \mathbf{B})$$

Magnetic force

$$\mathbf{F} = q(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

Lorentz force

$$\oint_S \mathbf{B} \cdot d\mathbf{A} = 0$$

Gauss' Law for magnetic field

$$\oint_C \mathbf{B} \cdot d\mathbf{l} = \mu_0 I_{enc}$$

Ampère's Law (magnetostatics)

$$\mathbf{F}_{wire} = l(\mathbf{I} \times \mathbf{B})$$

Force on a wire

$$\mathbf{I} = nAq\mathbf{v}$$

Electric current

$$d\mathbf{B} = \frac{\mu_0 I}{4\pi r^2} d\mathbf{l} \times \hat{\mathbf{r}}$$

Biot-Savart Law

$$\mathbf{B}(z=0) = \frac{\mu_0 I}{2a} \hat{\mathbf{z}}$$

Field from loop of current

$$\mathbf{B}(s) = \frac{\mu_0 I}{2\pi s} \hat{\boldsymbol{\theta}}$$

Field from infinite wire

$$\frac{F}{l} = \frac{\mu_0 I_1 I_2}{2\pi s}$$

Force on parallel currents

$$\Phi_m = \int_S \mathbf{B} \cdot d\mathbf{A}$$

Magnetic flux

$$\mathcal{E} = -\oint_C \mathbf{E} \cdot d\mathbf{l}$$

Motional EMF in B-field

$$\mathcal{E} = -\frac{d\Phi_m}{dt}$$

Faraday's Law

$$B_{in} = \mu_0 n I$$

Field in a solenoid

$$\boldsymbol{\mu} = I\mathbf{A}$$

Magnetic moment

$$\boldsymbol{\tau} = \boldsymbol{\mu} \times \mathbf{B}$$

Torque on magnetic dipole

$$U = -\boldsymbol{\mu} \cdot \mathbf{B}$$

Magnetic dipole energy

$$\oint_C \mathbf{B} \cdot d\mathbf{l} = \mu_0 \left(I_{enc} + \epsilon_0 A \frac{\partial E}{\partial t} \right)$$

Ampère-Maxwell Law

$$\Phi_{21} = M_{21} I_1$$

Mutual induction

$$M = \frac{\mu_0 N_1 N_2 A}{l}$$

Mutual inductance

$$\mathcal{E}_1 = \frac{N_1}{N_2} \mathcal{E}_2$$

Transformer EMF

$$\mathcal{E}_1 I_1 = \mathcal{E}_2 I_2$$

Transformer power conservation

$$\mathcal{E} = -L \frac{dI}{dt}$$

Back EMF in a solenoid

$$\Phi = LI$$

Self inductance

$$L = \mu_0 n^2 l A$$

Self inductance of a solenoid

$$u_B = \frac{B^2}{2\mu_0}$$

B-field energy density