

An Embedded Scalable Linear Model Predictive Hardware-based Controller using ADMM

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Overview

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 - Model Predictive Optimal Control
 - Splitting Method
- 3 ADMM Hardware Architecture
 - Architecture Overview
 - Trajectory Setting During Runtime
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Quadratic Programming (QP) solutions

MPC can be posed as a Quadratic Programming problem.

QP problems can be solved reliably via various iterative methods.

- Interior-Point Method (IPM)
- Active Set Method (ASM)
- Splitting Method

FPGA-based QP solutions

Compare IPM and ASM in FPGA

- ASM gives lower computing complexity and converges faster when the number of decision variables and constraints are small.
- IPM is a better choice when considering scalability.

State Space Model

A discrete state-space model defines what state a system will be in one-time step into the future:

$$x_{k+1} = Ax_k + Bu_k \quad (1)$$

$$y_k = Cx_k + Du_k \quad (2)$$

- x_k represents the state of the system at time k
- u_k represents the input acting on the system at time k
- y_k represents outputs of the system at time k
- A is a matrix that defines the internal dynamics of the system
- B is a matrix that defines how the input acting upon the system impact its state
- C is a matrix that transforms states of the system into outputs (y_k)

Augmented Vector

$$U_k = \begin{bmatrix} u_k \\ u_{k+1} \\ \vdots \\ u_{k+H_u} \end{bmatrix}, \quad \Delta U_k = \begin{bmatrix} \Delta u_k \\ \Delta u_{k+1} \\ \vdots \\ \Delta u_{k+H_u-1} \end{bmatrix}, \quad X_k = \begin{bmatrix} x_k \\ x_{k+1} \\ \vdots \\ x_{k+H_p} \end{bmatrix} \quad (3)$$

Where:

- H_u : changeable future input horizon. We assume input u_k will be constant after H_u time steps.
- H_p : prediction horizon. Normally, $H_p \geq H_u$.
- $U_k \in \mathbb{R}^{M(H_u+1)}$, $\Delta U_k \in \mathbb{R}^{MH_u}$, $X_k \in \mathbb{R}^{N(H_p+1)}$.

Cost Function

$$\mathbb{C}(k) = \frac{1}{2} \left(\sum_{i=k}^{k+H_p} (x_i^T q_i x_i - 2r_i^T q_i x_i) + \sum_{i=k}^{k+H_u} u_i^T p_i u_i + \sum_{i=k}^{k+H_u-1} \Delta u_i^T s_i \Delta u_i \right) + Const \quad (4)$$

$$\mathbb{C}(k) = \frac{1}{2} \begin{bmatrix} X_k \\ U_k \\ \Delta U_k \end{bmatrix}^T \begin{bmatrix} Q & & \\ & P & \\ & & S \end{bmatrix} \begin{bmatrix} X_k \\ U_k \\ \Delta U_k \end{bmatrix} - R_k^T Q X_k \quad (5)$$

Paragraphs of Text

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Bullet Points

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Multiple Columns

Heading

- 1 Statement
- 2 Explanation
- 3 Example

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Table

Treatments	Response 1	Response 2
Treatment 1	0.0003262	0.562
Treatment 2	0.0015681	0.910
Treatment 3	0.0009271	0.296

Table: Table caption

Theorem

Theorem (Mass–energy equivalence)

$$E = mc^2$$

Verbatim

Example (Theorem Slide Code)

```
\begin{frame}  
\frametitle{Theorem}  
\begin{theorem}[Mass--energy equivalence]  
$E = mc^2$  
\end{theorem}  
\end{frame}
```

Figure

Uncomment the code on this slide to include your own image from the same directory as the template .TeX file.

Citation

An example of the `\cite` command to cite within the presentation:

This statement requires citation [Smith, 2012].

References



John Smith (2012)

Title of the publication

Journal Name 12(3), 45 – 678.

The End