# Control of a multi-robot cooperative team guided by a human operator

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#### Human-robot team interaction

Humans come with superior foresight and robustness to incidents. Cooperative robot teams allow for a variety of complex tasks.



Coordinated use of tools: Pipe cutting [MHI14]

Unstructured environments demand the human's direct involvement in the control loop.

Intuitive user interfaces enable robot operation by untrained personnel.

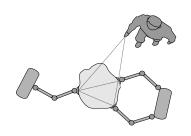
Is the human a fail-safe mechanism?



## **Problem setting**

A set of robots manipulating a common object A human guiding the formation by hand motion

- Multiple robots need to be controlled simultaneously
- The formation constraints have to be satisfied
- The input method is non-reactive any trajectory is possible



#### Goal

- Object-centred user interface
- Autonomous preservation of formation
- Stability and safety with arbitrary commands





#### **Related Work**

#### Low-level coordination

- (Inverse) grasp-matrix approaches [SC92,CCMV08]
- Virtual structures [Str01,SMH15]

#### Human in the loop

- Bilateral tele-manipulation [LS05]
- Human leader robotic followers [SMH15,SMP14]
- Gesture-based Control [GFS+14]

#### Safety by energy-regulation

- Adaptive impedance control of a single manipulator [TVS14]
- Energy observer in physical human-robot interaction [GSLP16]

#### Conclusion

- Stability with non-restrictive input interfaces is unexplored
- Passivity is commonly used to cope with unmodelled dynamics
- Energy-based safety metrics apply for impact limitation







### port-Hamiltonian systems

Visualize power flow, allow for model-based control design, facilitate stability proofs

**Hamiltonian**  $\mathcal{H}$ : total energy of the system

 $\textbf{Port} \colon \mathsf{power}\text{-}\mathsf{conjugated} \ \mathsf{dual} \ \mathsf{pair} \ (u,y) \ \mathsf{of} \ \mathit{flow} \ u \ \mathsf{and} \ \mathit{effort} \ y$ 

$$\dot{x} = [J(x) - R(x)] \frac{\partial \mathcal{H}}{\partial x}(x) + B(x)u$$
$$y = B^{T}(x) \frac{\partial \mathcal{H}}{\partial x}(x)$$

input-state-output form with structure- J(x), dissipation- R(x) and mapping matrix B(x)

**Energy balance:**  $\frac{d}{dt}\mathcal{H} = y^T u - \frac{\partial^T \mathcal{H}}{\partial x}R(x)\frac{\partial \mathcal{H}}{\partial x}$  ( $\rightarrow$  passive)





# Model-based control design

Plants and controllers are energy-transforming devices, which we interconnect to achieve the desired behaviour. [OSMMO1]

Modelling leads to a virtual structure



	Spring	Mass	Damper
Effort variable	Wrench $W$	Twist $T$	Wrench $W$
Flow variable	Twist $T$	Wrench $W$	Twist T
State variable	Config. $H$	Momentum $P$	-
Energy function	$V_{P}(H)$	$V_{K} = \frac{1}{2} P^T M^{-1} P$	$V_{D}^* = \frac{1}{2} T^T D T$

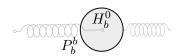
Model errors never influence passivity nor stability [Str01]



## **Example controller derivation (IPC)**

Starting from the virtual object...

$$\dot{P}_b^b = C_b \frac{\partial \mathcal{H}}{\partial P_b^b} + I_6 W_b^b$$
$$T_b^{b,0} = I_6 \frac{\partial \mathcal{H}}{\partial P_b^b}$$



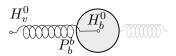
Momentum  $P_b^b$  (state), wrench  $W_b^b$  (flow), twist  $T_b^{b,0}$  (effort), centrifugal and Coriolis terms  $C_b$ Hamiltonian  $\mathcal{H} = \frac{1}{2} P_b^{bT} M_b^{-1} P_b^b$ 



## Example controller derivation (IPC)

... adding a coupling spring to the user...

$$\begin{pmatrix} \dot{H}^{v}_{b} \\ \dot{P}^{b}_{b} \end{pmatrix} = \begin{pmatrix} 0 & H^{v}_{b} \\ -H^{vT}_{b} & C_{b} \end{pmatrix} \begin{pmatrix} \frac{\partial \mathcal{H}}{\partial H^{v}_{b}} \\ \frac{\partial \mathcal{H}}{\partial P^{b}_{b}} \end{pmatrix} + \begin{pmatrix} -H^{v}_{b}Ad_{H^{b}_{0}} & 0 \\ 0 & I_{6} \end{pmatrix} \begin{pmatrix} T^{0}_{v} \\ W^{b}_{b} \end{pmatrix}$$
 
$$\begin{pmatrix} W^{0}_{v} \\ T^{b,0}_{b} \end{pmatrix} = \begin{pmatrix} -Ad^{T}_{H^{b}_{0}}H^{vT}_{b} & 0 \\ 0 & I_{6} \end{pmatrix} \begin{pmatrix} \frac{\partial \mathcal{H}}{\partial H^{v}_{b}} \\ \frac{\partial \mathcal{H}}{\partial P^{b}_{b}} \end{pmatrix}$$



relative configuration  $H^v_h$  (state), desired twist  $T^0_{s^*}$  (flow). wrench  $W_v^0$  (effort), adjoint mapping  $Ad_{H_o^b}$ 

Hamiltonian 
$$\mathcal{H} = \frac{1}{2} P_b^{bT} M_b^{-1} P_b^b + V_P(H_b^v)$$



## Example controller derivation (IPC)

... and another spring to the *i*-th manipulator.

$$\begin{pmatrix} \dot{H}_{b}^{v} \\ \dot{P}_{b}^{b} \\ \dot{H}_{b(i)}^{i} \end{pmatrix} = \begin{pmatrix} 0 & H_{b}^{v} & 0 \\ -H_{b}^{vT} & C_{b} & -Ad_{H_{b}^{b(i)}}^{T}H_{b(i)}^{i} & T \\ 0 & H_{b(i)}^{i}Ad_{H_{b}^{b(i)}} & 0 \end{pmatrix} \begin{pmatrix} \frac{\partial \mathcal{H}}{\partial H_{b}^{v}} \\ \frac{\partial \mathcal{H}}{\partial P^{b}} \\ \frac{\partial \mathcal{H}}{\partial P^{b}} \\ \frac{\partial \mathcal{H}}{\partial P^{b}} \end{pmatrix}$$

$$+ \begin{pmatrix} -H_{b}^{v}Ad_{H_{b}^{b}} & 0 \\ 0 & 0 \\ 0 & -H_{b(i)}^{i}Ad_{H_{0}^{b(i)}} \end{pmatrix} \begin{pmatrix} T_{v}^{0} \\ T_{i}^{0} \end{pmatrix}$$

$$\begin{pmatrix} W_{v}^{0} \\ W_{i}^{0} \end{pmatrix} = \begin{pmatrix} -Ad_{H_{b}^{b}}^{T}H_{b}^{vT} & 0 & 0 \\ 0 & 0 & -Ad_{H_{0}^{b(i)}}^{T}H_{b(i)}^{i} & T \end{pmatrix} \begin{pmatrix} \frac{\partial \mathcal{H}}{\partial H_{b}^{v}} \\ \frac{\partial \mathcal{H}}{\partial P^{b}} \\ \frac{\partial \mathcal{H}}{\partial H_{b(i)}^{b}} \end{pmatrix}$$

$$H_{v}^{0} \qquad H_{b(i)}^{0} \qquad H_{b}^{0}$$

**Hamiltonian** 
$$\mathcal{H} = \frac{1}{2} P_b^{bT} M_b^{-1} P_b^b + V_P(H_b^v) + V_P(H_{b(i)}^i)$$

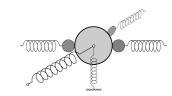


Results

## Modelling of constrained contact

Manipulator inertias, connected rigidly to the object, impose kinematic constraints.

$$\begin{split} \dot{x} &= \left[J(x) - R(x)\right] \frac{\partial \mathcal{H}}{\partial x}(x) + B(x)u + A(x)\lambda \\ 0 &= A^T(x) \frac{\partial \mathcal{H}}{\partial x} \ \to \text{DAE form} \end{split}$$



#### Solved input-state-output form

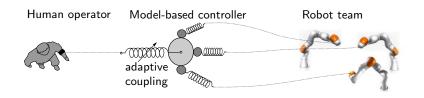
Solved input-state-output form 
$$\dot{x} = [J - R] \frac{\partial \mathcal{H}}{\partial x} + Bu + A(A^T M^{-1} A)^{-1} A^T M^{-1} (u + C \frac{\partial \mathcal{H}}{\partial x})$$
 
$$y = B^T \frac{\partial \mathcal{H}}{\partial x}$$

Constraint matrix A, Lagrange multipliers  $\lambda$ Rigid connections are power-conservative.





## Adaptive coupling of the operator



Human hand is stiff when moving slow, compliant when fast [Hog84] **Energy-adapted human coupling:** reduced stiffness  $\kappa$  and damping above a threshold energy level  $\mathcal{H}_{\text{th}}$ 

$$\kappa = \begin{cases} k_{vb} & \text{if } \mathcal{H}(x) < \mathcal{H}_{\mathsf{th}} \\ k_{vb} \frac{\mathcal{H}_{\mathsf{max}} - \mathcal{H}(x)}{\mathcal{H}_{\mathsf{max}} - \mathcal{H}_{\mathsf{th}}} & \text{if } \mathcal{H}(x) \geq \mathcal{H}_{\mathsf{th}} \end{cases}$$

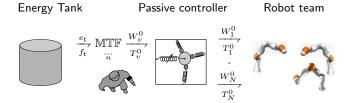
At a maximum energy level  $\mathcal{H}_{max}$  the operator is decoupled





## Passivation of the coupling

Varying the stiffness  $\kappa$  changes the energy  $V_{\rm P}$  of the spring Buffered with an **Energy Tank** by the power port  $(\dot{\kappa}, \frac{\partial V_{\rm P}}{\partial \kappa})$ 



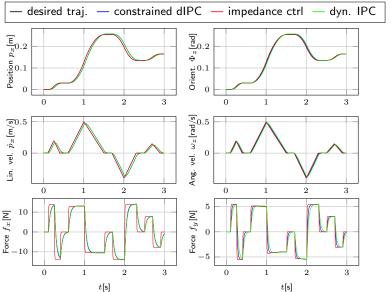
Human operator is energetically decoupled Modulated Transformer  $\mathbb{MTF}$  with ratio n

$$\begin{array}{ll} T_v^0 & = \boldsymbol{n} e_{\mathsf{t}} \\ f_{\mathsf{t}} & = -\boldsymbol{n}^T W_v^0 \ \Rightarrow \ \text{new input} \ \boldsymbol{n} = \frac{1}{e_{\mathsf{t}}} T_{v,h}^0 \end{array}$$

Tank effort  $e_{\rm t}$  and flow  $f_{\rm t}$ , human trajectory input  $T_{v,h}^0$ 

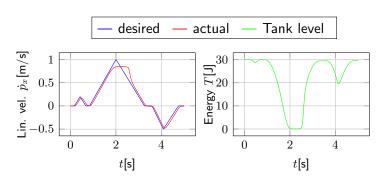


# **Trajectory tracking: Comparison**





# **Energy-bounded trajectory tracking**



- Controller is an energetic model of the real system
- Velocity and possible forces are limited by the energy budget
- No permanent deviations in position tracking
- Maximum energy defined by safety metrics: Safe human-robot co-working



#### Conclusion & future work

- Energy-consistent modelling and control of a cooperative set-up
- Intrinsically passive controller with energy-adapted coupling of the user
- Energy budget at the user's disposal to operate the system
- System behaves save and stable with arbitrary user commands

#### **Future work**

Introduction

- Experimental implementation
- Evaluation of safety metrics for violent pressure
- Leader-follower guidance in direct human-robot team interaction





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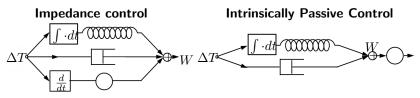




## **Backup Trajectory tracking: Comparison**

 constrained dIPC — impedance control — dynamic IPC  $\cdot 10^{-2}$  $\cdot 10^{-2}$ Position  $\Delta p_x[\mathbf{m}]$  0 -2 $\Delta\Phi_z$ [rad] Orient. 2 3 0 0  $\cdot 10^{-2}$  $\cdot 10^{-2}$ Lin. vel.  $\Delta \dot{p}_x$  [m/s]  $\stackrel{|}{c}_{r}$  0  $\stackrel{|}{c}_{r}$  $\Delta \omega_z [{\sf rad/s}]$ Ang. vel. 0 t[s]t[s]

## **Backup Trajectory tracking: Interpretation**



Different role of inertias in the controllers: force gradients cause performance gap

