

Master Thesis

Morphology Optimization of a Tilt-Rotor MAV

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Declaration of Originality

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Morphology Optimization of a Tilt-Rotor MAV

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Abstract

Hier kommt der Abstact hin ...

Symbols

Symbols

ϕ, θ, ψ	roll, pitch and yaw angle
\mathcal{F}_W	inertial world frame
\mathcal{F}_B	inertial body frame
\mathcal{F}_{P_i}	i-th propeller frame
p	position of the MAV in \mathcal{F}_W
ω_B	angular velocity of the MAV in \mathcal{F}_B
${}^W R_B$	rotation matrix from \mathcal{F}_B to \mathcal{F}_W
${}^B R_{P_i}$	rotation matrix from \mathcal{F}_{P_i} to \mathcal{F}_B
$R_X(\gamma)$	canonical rotation matrix about the X axis of angle γ
$R_Y(\gamma)$	canonical rotation matrix about the Y axis of angle γ
$R_Z(\gamma)$	canonical rotation matrix about the Z axis of angle γ
α_i	i-th propeller tilt angle
w_i	i-th propeller rotation speed
τ_{ext_i}	i-th propeller counter rotation torque
T_i	i-th thrust
m	total mass of the MAV
I_B	body inertia of the MAV
n	MAV's number of propellers
L	MAV's arms length
κ_f	propeller thrust coefficient
κ_m	propeller drag coefficient
g	gravity constant

Acronyms and Abbreviations

ETH	Eidgenössische Technische Hochschule
MAV	Micro Aerial Vehicle
ROS	Robotic Operating System
UAV	Unmanned Aerial Vehicle
cw	clockwise
ccw	counterclockwise

Chapter 1

Introduction

Rotary wing micro aerial vehicles (MAVs) have been well studied in academia and found a lot of applications in the world such as search operations [1], photography [2] or even toys [3]. They encountered such a broad success because of their agility and mechanical simplicity. Nevertheless, traditional multi-rotor vehicles are under-actuated, which means that they cannot control their torque and force independently [4]. They are thus unable to change their position without changing their orientation.

Recently the focus has been on designing MAVs able to perform more complex tasks such as camera motion for the film industry [5] or bridge inspection where huge resources (i.e. cranes and large man-power) are needed. The ultimate goal would be for a drone to be able to interact with its surrounding and apply forces to it, in order to perform maintenance where human can not access, or to do construction work in harsh environments.

To perform these tasks, an MAV has to be able to hover in any orientation, and for a proper disturbance rejection while manipulating, the drone must have the potential to accelerate instantaneously in any direction. Hence, the MAV has to be able to decouple its orientation and position control. A drone that has a decoupled force and torque control is referred to as an omni-directional MAV.

The problem of overcoming the under-actuation and achieving omni-directionality is not straightforward. To address this problem, several MAV's designs have been presented over the past years. For instance, in [5], Voliro (name of the vehicle) is based on a traditional hexa-copter (see Figure 1.1). The omni-directionality issue is addressed by adding motors to rotate the thrusters around their arm axis, thus allowing a control not only of the thrust produced by each propeller, but also on the orientation of this thrust. This tilting rotor system allows for decoupling the control of position and orientation. By using a control scheme based on an allocation technique, the system provides very good maneuverability.



Figure 1.1: Voliro [5].

In [4], the Omnicopter (name of the vehicle) is described. It is a drone with eight fixed rotors and the drone shape is the result of a mathematical optimization (see Figure 1.2) which maximizes the vehicle's agility with the constraint that its dynamical properties would be as independent as possible on the vehicle orientation.

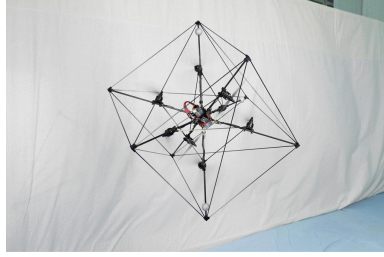


Figure 1.2: Omnicopter [4].

In [6], the MAV is a fixed propeller multi-rotor. The design is also the result of an optimization, which tends to minimize the body volume, maximize the controllability of the system, avoid eventual aerodynamic interactions and maximizes the efficiency in performing manipulation tasks.

The idea presented in [7] is a mix between Voliro and the Omnicopter because the design is a modified hexarotor (see Figure 1.3), which achieves full control over the vehicle's position and orientation using manually tiltable propellers. The paper also provides a methodology to optimize the fixed tilting angles depending on the desired trajectory.



Figure 1.3: Hexacopter with manually tiltable rotors [7].

Yet, nothing in the literature is found about the morphology optimization of MAVs with tilting rotors. Hence the need for the present research project. The aim of this thesis is thus to design a morphology optimization problem for a tilt rotor MAV that accounts for the different factors that influence the morphology such as:

- Omni-directionality
- Flight efficiency
- Controllability

To reach this goal the chosen approach is to build an optimization engine that solves the optimization problem and returns different MAV designs. The most interesting designs are then tested in simulation.

In this report the methods used to build the optimization engine and to simulate the results are discussed. Afterwards, the results returned by the engine are shown and compared based on different criteria. Finally, the results gathered during the simulation phase are also discussed.

Chapter 2

Method

As explained in Chapter 1 the aim of this work is to find a drone design that is the result of an optimization problem, which tends to maximize the MAV's omnidirectionality, flight efficiency and controllability. To do so it is important to first state what are the parameters that define the design of an MAV. These parameters are defined as:

- β (angles formed by the arms with the horizontal plane see Figure 2.1)
- θ (angles formed by the arms in the horizontal plane see Figure 2.1)
- L (arm length)
- n (number of propeller)

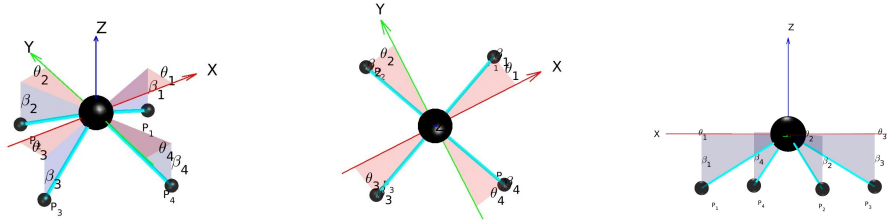


Figure 2.1: Quadcopter to illustrate the parameters that define the morphology of an MAV ($n = 4$, $\beta = [30, 30, 30, 30][^\circ]$, $\theta = [22, 22, 22, 22][^\circ]$, and $L = 0.4[m]$).

To solve the problem an optimization engine is developed with Matlab[®]. This tool returns the aforementioned parameters along with other information on the corresponding MAV design. The interesting drone designs outputted by the tool are then simulated on Gazebo¹ and the control of the different models is achieved using a Robotic Operating System² (ROS) node.

This chapter first covers the theory needed to obtain a generalize mathematical model for a n -rotor MAV with an arbitrary morphology. Then, the optimization problem is defined. Afterwards, the optimization tool is described. In the end, the theoretical background needed to perform the simulations is covered.

¹An open source robot simulator [8].

²An open source collection of software that help developers to create robot applications [9].

2.1 Modelisation of MAVs

In the following part, a dynamical model for a general design of MAV is presented. This model is inspired from the models presented in [5] and [10].

Initial Definitions

In order to understand correctly the dynamical model, a few definitions are much needed. First, let us define $\mathcal{F}_W : \{O_W; X_W, Y_W, Z_W\}$ as the world fixed inertial frame and $\mathcal{F}_B : \{O_B, X_B, Y_B, Z_B\}$ as a moving frame attached to the MAV. Also, $\mathcal{F}_{P_i} : \{O_{P_i}; X_{P_i}, Y_{P_i}, Z_{P_i}\}, i = 1 \dots n$ is the frame of the i -th propeller. The propeller rotate around the axis Z_{P_i} , and thus the thrust T_i is produced along this axis. The tilt movement of the rotors is a simple rotation around X_{P_i} . Now let ${}^W R_B$ be the orientation of the body frame with respect to the world frame and ${}^B R_{P_i}$ be the orientation of the i -th propeller with respect to the body frame. From there, it straightforward with the help of Figure 2.2 that

$${}^B R_{P_i} = R_Z\left((i-1)\frac{2\pi}{n}\right)R_Z(\theta_i)R_Y(\beta_i)R_X(\alpha_i), \quad i = 1 \dots n. \quad (2.1)$$

Equivalently, let

$${}^B O_{P_i} = R_Z\left((i-1)\frac{2\pi}{n}\right)R_Z(\theta_i)R_Y(\beta_i) \begin{bmatrix} L \\ 0 \\ 0 \end{bmatrix}, \quad i = 1 \dots n \quad (2.2)$$

be the origin of the i -th propeller frame \mathcal{F}_{P_i} . In Equation (2.1) and (2.2), $(i-1)\frac{2\pi}{n}$ is the angle that the i -th arm would form with axis X_B if the arms of the drone are evenly distributed in the horizontal plane, θ_i is the angle that i -th arm forms in the horizontal plane with respect to its evenly distributed position (see Figure 2.1), β_i is the angle that the i -th arm forms with the horizontal plane (see Figure 2.1), α_i is the tilting angles of the i -th propeller about the X_{P_i} axis, L is the arm length and n is the number of propellers.

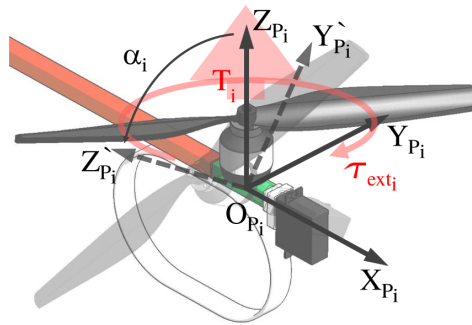


Figure 2.2: Representation of the i -th tilting arm [10].

Assumptions

In this model the first assumption is that the MAV is composed of $n+1$ rigid bodies: one for each propeller P_i and one for the body B . Then, it is considered that the motors that actuate the propellers can only rotate in one direction. Finally, the airflow interactions between the different rotors are neglected.

Equations of motion

Using Newton-Euler formalism, it follows that

$$\begin{cases} \dot{\omega}_B = I_B^{-1} \sum_{n=1}^n ({}^B O_{P_i} \tau_{ext,i} + \tau_{Bi}) , \\ \ddot{p} = \begin{bmatrix} 0 \\ 0 \\ g \end{bmatrix} {}^W R_B \sum_{n=1}^n T_i . \end{cases} \quad (2.3)$$

Where

$$\tau_{Bi} = {}^B O_{P_i} \times {}^B R_{P_i} T_{P,i} \quad (2.4)$$

$$\tau_{ext,i} = \begin{bmatrix} 0 & 0 & -c_i \kappa_m w_i^2 \end{bmatrix}^T \begin{cases} c_i = 1, & \text{if } i \text{ is odd (} cw \text{ rotation)} \\ c_i = -1 & \text{if } i \text{ is even (} ccw \text{ rotation)} \end{cases} \quad (2.5)$$

and

$$T_i = {}^B R_{P_i} T_{P,i}, \quad T_{P,i} = \begin{bmatrix} 0 & 0 & \kappa_f w_i^2 \end{bmatrix}^T, \quad (2.6)$$

2.2 Optimization problem

Define morphology optimization problem

2.3 Optimization tool

Show resulting optimization tool.

2.4 Simulation Approach

Chapter 3

Optimization Results

Show results produced by the engine.

3.1 Even Designs

3.1.1 Platonic Solids

3.1.2 Quad-copter

3.1.3 Hexa-copter

3.1.4 Octa-copter

3.2 Odd Designs

3.2.1 Tri-copter

Show tricopter.

3.2.2 Penta-copter

3.2.3 Hepta-copter

3.3 Comparison of Different Designs

$$\cos(\beta) = \sqrt{\left(\frac{2}{3}\right)} \Rightarrow \beta = 35.26^\circ$$

$$F_{min} = 34.74, F_{max} = 42.55, M_{min} = 17.42, M_{max} = 21.34, H_{eff,min} = 81.65\%, H_{eff,max} = 100\%$$

$$F_{min} = 26.6, F_{max} = 52.11, M_{min} = 15.1, M_{max} = 26.13, H_{eff,min} = 75\%, H_{eff,max} = 100\%$$

$$\text{Design 1: } F_{min} = 23.18, F_{max} = 28.56, M_{min} = 11.61, M_{max} = 14.3, H_{eff,min} = 81.11\%, H_{eff,max} = 95.2\%$$

$$\text{Design 2: } F_{min} = 23.22, F_{max} = 28.37, M_{min} = 11.65, M_{max} = 14.23, H_{eff,min} = 81.65\%, H_{eff,max} = 94.73\%$$

$$F_{min} = 44.7, F_{max} = 58.8, M_{min} = 22.4, M_{max} = 29.5, H_{eff,min} = 81.78\%, H_{eff,max} = 96.65\%$$

$$F_{min} = 46.46, F_{max} = 56.73, M_{min} = 23.3, M_{max} = 28.45, H_{eff,min} = 81.64\%, H_{eff,max} = 94.77\%$$

Table 3.1: Comparison between the different number of propellers.

MAV Design	$F_{min}[N]$	$F_{max}[N]$	$F_{mean}[N]$	$M_{min}[Nm]$	$M_{max}[Nm]$	$M_{mean}[Nm]$	$H_{eff,mean}[\%]$
Tri-copter	17.17	21.21	17.95	8.61	10.64	9	85.46
Quad-copter	23.22	28.37	26.87	11.65	14.23	13.47	87.1
Penta-copter	28.95	35.46	29.4	14.52	17.78	14.74	85.35
Hexa-copter	34.74	42.55	39.52	17.42	21.34	19.82	88.9
Hepta-copter	39.96	49.44	47.2	20.04	24.8	23.66	91.1
Octa-copter	44.7	58.8	53.95	22.4	29.48	27.06	91.42

Chapter 4

Simulation Results

Evaluate results in simulation.

4.1 Hexa-copter

4.2 Hepta-copter

4.3 Octa-copter

Chapter 5

Conclusion

5.1 Summary/Achieved

5.2 Improvements

5.3 Further Developement

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Appendix A

UML: Activity Diagram

