# Cooperative Mobile Manipulation without Explicit Communication [Wang, 2016]

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## Outline

#### Motivation

Rigid Body Dynamics Translational Dynamics Rotational Dynamics

Constant Boost Force CB-ANTS CB-ANTS Global CB-ANTS Local

Proportional Force P-ANTS P-ANTS Global P-ANTS Local

Simulations

Conclusions

References

## Motivation

#### Communication networks of robots confronts various problems

- 1. Very noisy
- 2. Demands high computational power
- 3. Deals with uncertainty
- 4. Might get vanished

#### Instead, we employ affordable sensing information

- Motion planning imposed by the leader
- Utilize force feedback
- Information attained locally

## **Applications**

Both large and small number of robots can be used depending on the object's size

- Automated construction site
- Manufacturing facilities
- Structured environment

## Translational Object Dynamics

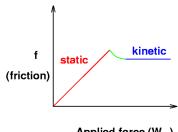
Translational motion subject to Newton's second law

$$M\dot{v} = \sum_{i=1}^{N} F_i - \mu_k Mg \frac{v}{||v||} - \mu_v v$$
 (1)

- $\blacktriangleright \mu_k$  coefficient of kinetic friction
- $\blacktriangleright \mu_{v}$  coefficient of rolling friction
- $ightharpoonup \frac{v}{||v||}$  unity tangent vector

### **Friction**

- Friction of rigid bodies discriminates in 2 regions
- Static proportional to force
- Kinetic friction assumed constant
- Spinning wheels can replace kinetic w/ viscous friction velocity related



Applied force (W<sub>x</sub>)

Source: http://deutsch.physics.ucsc.edu/ 6A/book/forces/node21.html

## Translational Dynamics Cases

1. For lightweight objects after Euler's discretization

$$M\frac{v_{t+1} - v_t}{\Delta t} = \sum_{i=1}^{N} F_i(t) - \mu_k Mg \frac{v_t}{||v_t||}$$
 (2)

2. For heavyweight objects

$$M\dot{\mathbf{v}} = \sum_{i=1}^{N} F_i - \mu_{\mathbf{v}} \mathbf{v} \tag{3}$$

**Assumption 1:** M,  $\mu_k$ ,  $\mu_v$ , g, N given

## Object's Rotational Dynamics

$$J\dot{\omega} = T_1 + \sum_{i=2}^{N} r_i \times F_i - T_f = T_1 + \sum_{i=2}^{N} r_i \times F_i - \frac{\mu_{\nu}}{M} J\omega$$
 (4)

- lacksquare  $T_f$ , static friction related torque, obect's motion  $Q \in \mathbb{R}^2$
- $ightharpoonup \sum_{i=2}^{N} r_i \times F_i$ , follower robots torque
- r<sub>i</sub>, vector from object's CoM to the contact point
- ► T<sub>I</sub>, leader's applied torque

**Assumption 2:** Leader know object's  $\omega$  and applies  $T_1$ 

#### **CB-ANTS** Case

Constant Boost force (CB-ANTS) case deals with dragging the object

- Lightweight objects
- Dominant friction is kinetic
- Both global and local information studies

## **CB-ANTS** Follower's Controller

Follower's force feedback controller

$$F_i^c = \frac{\mu_k Mg}{N} \frac{v^c}{||v^c||}, \quad i = \{2, 3, \dots, N\}$$
 (5)

- ▶ v<sup>c</sup>, object's velocity at CoM
- Includes information for the leader's motion intention
- Restricts the follower's forces so the leader's force dominates

#### CB-ANTS Leader's Controller

Leader's force feedback controller

$$F_{l}^{I} = f_{d} \frac{v_{d}^{I}}{||v_{d}^{I}||} = K_{p} \max\{||v_{d}^{I}|| - ||v^{I}||, 0\} \frac{v_{d}^{I}}{||v_{d}^{I}||}$$
(6)

- $\triangleright$   $v_d^l$ ,  $v^l$ , desired and current velocity of the leader
- $\triangleright$   $K_p$ , proportional gain
- Utilized max function to track the leader's velocity

**Overall goal:** Steer the object through a specific trajectory to the goal position

### **CB-ANTS** Consensus

**Theorem 1:** In CB-ANTS case by employing equations 2, 5, 6 all follower robots align to the leader's direction and converge at

$$\phi = (N-1)\frac{\mu_k Mg}{N} \tag{7}$$

- ▶ Time step needs to be bounded  $0 < \Delta t < N \frac{||v_t||}{\mu_k g}$
- Object's velocity converge to leader's velocity

**Theorem 2:** Follower forces converge to the leader's force exponential fast

## Object's Dynamics

Object's discrete dynamics

$$v_{t+1} = \left(1 - \frac{\mu_k g \Delta t}{N||v_t||}\right) v_t + \frac{\Delta t K_p \max\{||v_d'|| - ||v'||, 0\}}{M||v_d||} v_d \quad (8)$$

- Leader robot has to have specific force abilities to steer the object
- ▶ Leader's force needs to be at least above  $\mu_k Mg/N$ .

#### CB-ANTS Local Follower's Controller

Follower's force feedback controller using local measurements

$$F_{i} = \frac{\mu_{k} Mg}{N} \frac{v_{t} + \omega_{t} \times r_{i}}{||v_{t} + \omega_{t} \times r_{i}||}$$
(9)

- v<sub>t</sub>, object's velocity at CoM
- $\triangleright \omega_t \times r_i$ , angular velocity at contact point
- ▶ Includes information for the leader's motion intention
- Restricts the follower's forces so the leader's force dominates

Leader's force feedback remains the same as in equation 6

## Local Object's Dynamics

Object's discrete dynamics using local measurements

$$v_{t+1} = \frac{\Delta t}{M} f_d \frac{v_d}{||v_d||} + \sum_{i=2}^{N} \left( \frac{\mu_k g \Delta t}{N||v_t + \omega_t \times r_i||} \right) \omega_t \times r_i +$$

$$+ \left( 1 + \sum_{i=2}^{N} \frac{\mu_k g \Delta t}{N||v_t + \omega_t \times r_i||} - \frac{\mu_k g \Delta t}{||v_t||} \right) v_t$$

$$(10)$$

- ▶  $1^{st}$  term: Control input of the leader  $v_d$
- ▶ 2<sup>nd</sup> term: Disturbing term, we want to eliminate
- ▶  $3^{rd}$  term: Internal dynamics of the studied object, |a| < 1

## Angular velocity boundary

**Theorem 3:** Sufficient condition to maintain theorem 1 is to bound  $\omega$ 

$$||\omega_t|| < \frac{||v_t||}{N||r_m||} \tag{11}$$

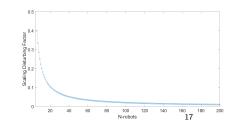
- m maximum radius value of CoM to contact point
- $m = \max_{i} ||r_i||, i = \{2, ..., N\}$

## Elimination of Disturbing Factor

**Theorem 4:** Under centrosymmetric contact points assumption, follow theorem 3, and utilize N-robots N > 3, then we can restrict the disturbing factor

$$\left| \left| \sum_{i=2}^{N} \left( \frac{\mu_k g \Delta t}{n ||v_t + \omega_t \times r_i||} \right) \omega_t \times r_i \right| \right| < \frac{\mu_k g \Delta t}{N} \left( \frac{2N - 1}{N^2 - N} \right) \quad (12)$$

- ▶ Inequality is direct related to a scaling factor  $(2N-1)/(N^2-N)$
- Disturbing term scales down exponentially



## P-ANTS Case

Proportional force (P-ANTS) case deals with lifting and pulling the object on rolling devices

- Heavyweight objects
- ▶ Dominant friction is the rolling friction of the wheel
- ▶ Both global and local information studies

## P-ANTS Follower's Controller

The consensus protocol commonly used for flocking

$$\dot{F}_i = \sum_{j \in N_i} (F_j - F_i) = \sum_{j \in N_i} F_j - NF_i$$
 (13)

N-complete graph

Employing equation 3

$$\dot{F}_i = M\dot{v} + \mu_{\nu}v - NF_i \tag{14}$$

▶ Reach consensus while the leader does not change its force

 $\dot{v}$ ,  $\dot{v}$ , v object's velocity and acceleration at the CoM

## P-ANTS State Equations

The state equations of P-ANTS

$$\dot{\eta} = -\eta + F_I \tag{15}$$

$$F_s = (N-1)\eta + F_I \tag{16}$$

- ▶ F<sub>I</sub>, leader's force and the input
- $\eta = (\sum_{i=2}^{N} F_i)/(N-1)$ , avg force of the followers and state
- $F_s = \sum_{i=1}^N F_i$ , total force and the output of our system

#### P-ANTS Local Follower's Controller

Follower's force feedback controller using local measurements

$$\dot{F}_i = (\sum_{j \in N} F_j - NF_i) - \frac{M}{J} r_i \times (\sum_{j \in N} r_j \times F_j)$$
 (17)

- ▶ 1<sup>st</sup> term: Similar to equation 13
- ▶ 2<sup>nd</sup> term: Disturbing term, we want to eliminate
- ▶ Leader's torque assumed to be negligible for many robots
- ▶ Under assumption 3 the centrifugal terms eliminated

## P-ANTS Local Follower's Controller Matrix Form

The matrix form of follower's force feedback controller using local measurements

$$\dot{F} = \left(-L_a - \frac{M}{J}R_a(t)\right)F = -LF \tag{18}$$

- $ightharpoonup F \in \mathbb{R}^{2N}$ , vector of followers and leader forces
- $ightharpoonup R_a(t) \in \mathbb{R}^{2N \times 2N}$ , product of skew matrices
- ► The matrix form only focus on 2D-space

## P-ANTS Local Follower's Controller Boundary Condition

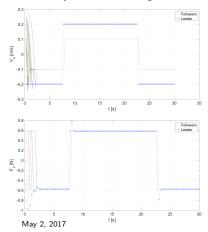
Eigenvalues o Laplacian matrix are less or equal to zero only if

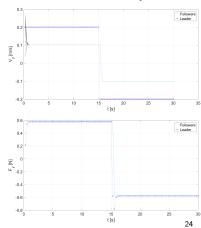
$$\frac{M}{J} \sum_{i=1}^{N} ||r_i||^2 < N \tag{19}$$

- Restricts the number of robots
  - 1. Object's mass M
  - 2. Inertia matrix J
  - 3. Radius from contact point to CoM of object  $r_i$

## **CB-ANTS Global**

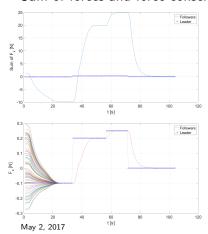
#### Velocity direction alignment and force consensus in x and y axes

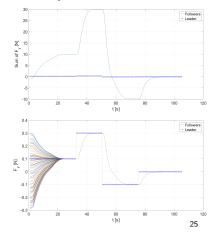




## P-ANTS Global

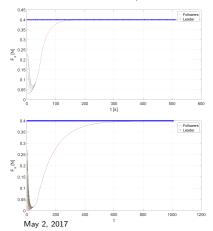
#### Sum of forces and force consensus in x and y axes

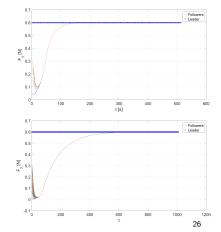




## P-ANTS Local

### Force consensus w/ 10 and 100 robots in x and y axes





## Conclusions

- Cooperative manipulation framework w/o explicit communication presented
- Force feedback information utilized
- ▶ Leader robot impose its force intention to the followers
- Two different cases studied depending on the object weight
  - ► CB-ANTS for lightweight objects by dragging
  - P-ANTS for heavyweight objects by lifting and pulling on rolling devices
- Two solutions presented for each case
  - Using global measurements
  - Using local measurements

## Random Thoughts

- Discretization of object's dynamics
- ► Assumption 1, 2, 3 make the methodology compatible only in structured environments
- Assumption 3 for CB-ANTS and small number of robots is not feasible
- ► State equations for P-ANTS should not be used, because they are based on *N*-Complete graph
- ► P-ANTS w/ local measurements should extend in 3*D*-space, because the inertia matrix is affected

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## Thank You!