

# Interacting multiple model-based human motion prediction for motion planning of companion robots\*

Donghan Lee<sup>1</sup>, Chang Liu<sup>2</sup> and J. Karl Hedrick<sup>3</sup>

**Abstract**—Motion planning of human-companion robots is a challenging problem and its solution has numerous applications. This paper proposes a motion planning method for human-companion robots to accompany humans in a socially desirable manner, which takes into account the safety, comfortableness and naturalness requirements. A unified Interacting Multiple Model (IMM) framework is developed to estimate human motion states from noisy sensor data and predict human positions in a finite horizon. The robot motion planning is formulated as a model predictive control problem to generate socially desirable motion behavior based on the predicted human positions. The effectiveness of the proposed motion planning method in facilitating the socially desirable companion behavior is evaluated through simulations and the advantage of IMM framework for human motion estimation and prediction compared to traditional single-model approaches has been demonstrated.

[Note:] add more plots for explanation; add comparison of single-model, IMM and no-prediction (maybe) results

[Note:] dh: in above note, does no-prediction means reactive method?

## I. INTRODUCTION

The application of autonomous robots for search and rescue missions have received considerable attentions in last decades. One particular scenario that is interesting to us is allowing autonomous robots to accompany humans in the search and rescue process. Robots can follow and assist humans by carrying heavy apparatus, exploring dangerous areas and detecting signals of survivors. To enable socially desirable companion behavior, certain requirements needs to be satisfied, which includes safety, comfortableness and naturalness. Safety serves as the fundamental requirement for companion robots that collision with humans should be avoided. (TODO: use lit from the survey paper. explain many aspects of social navigation. However, in problem formulation, just list what is done in this paper: focus on comfortableness (distance using proxemics and velocity similarity)) Comfortableness and naturalness compose constraints on the social aspects of robots; the former requires robots to pose little annoyance and stress for the accompanied humans

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and the latter emphasizes the similarity between robots and humans in low-level behavior patterns [1].

There exist several works on human-companion robots. Cosgun et al. [8] develops a robot for telepresence usage, which uses the laser scanner to track human movement and predicts human path by extrapolating the estimated current human position and velocity. It applies the depth-limited breadth-first search to find the waypoints for the robot to move to so that the robot can always face the accompanied human.

[Note:] dh: do we need to explain more detail about the depth-limited breadth-first search?

Hoeller et al. [9] uses the laser range finder and data association filters for estimating human positions. Potential field method is utilized for predicting human motion and the expansive-spaces trees method is utilized for motion planning. In [6], Wu et al. specifically focuses on the human motion estimation and prediction for robot motion planning. It develops an effective (TODO: describe what the filter actually is) filter for human motion estimation that can deal with abrupt human direction change when he/she makes turns.

An effective motion planner that generates socially desirable motion behavior necessitates accurate human motion estimation and prediction, which is then utilized for robot motion planning. To be specific, a robot needs to estimate motion states of the accompanied human in real time based on measurements from equipments such as GPS or cameras and then predict human future trajectory.

[Note:] explain more on KF, EKF, UKF

There exist several estimation methods, such as the Kalman filter [2], which is applicable to linear dynamic systems with Gaussian noise,

[Note:] dh: I can explain KF like this; KF is a special case of the recursive Bayesian estimation algorithm with assumptions of linear dynamic model and Gaussian noise

and the Extended Kalman filter and Unscented Kalman filter [12], which are suitable for nonlinear systems.

[Note:] dh: EKF and UKF are extension of the KF for a nonlinear dynamics. EKF can be obtained by a series expansion of the nonlinear dynamics while UKF uses a deterministic sampling technique known to pick a minimal set of sample points around the mean

Based on the estimated states, extrapolation assuming known human motion models, such as the constant velocity model (TODO: lit review)

[Note:] dh: constant velocity and constant turn model

, can be applied for predicting human positions in a finite horizon.

[Note:] try to merge the following sentence with the previous one.

These methods usually utilize single motion model for estimation and prediction and have been widely applied in motion planning and localization in the field of robotics [3]. However, human motion usually involves different motion models, such as straight-line movement, making turns and change of speed, which makes it difficult for the methods that use single motion model to accurately estimate and predict human movements.

Time-efficient motion planning approaches that generate socially desirable trajectory is desirable. Various planning algorithms, such as the potential field method [7] (TODO: explain more details) and the graph-search-based techniques [8] (TODO: explain more details) have been developed and successfully applied. However they usually assume simple kinematic model of robots and cannot take into account complex constraints, which renders these methods less suitable for human-companion motion planning in a socially desirable manner.

In this work, a model predictive control (MPC)-based motion planner incorporating human motion estimation and prediction capabilities is developed for a companion robot to autonomously accompany a target person in a socially desirable manner, which takes into consideration the safety, comfortableness and naturalness requirements. To estimate and predict human motion states, the Interacting Multiple Model (IMM) framework is utilized, which can incorporate different dynamic models and computes mode probabilities of each model. To deal with the nonlinear dynamics of the human motion, Unscented Kalman filter (UKF) is applied to each model in the IMM framework, resulting in the so-called IMM-UKF approach. Such approach can achieve higher accuracy compared to traditional estimation and prediction methods that utilize a single motion model. By using the predicted human positions in the prediction horizon, the robot motion planning is formulated as an MPC problem that explicitly considers safety, comfortableness and naturalness requirements on the robot motion behavior.

The proposed motion planning method differs from those works in several aspects. First, different from the single-model based estimation and prediction approach used in [8], the IMM-UKF method incorporates different human movement models into account, which results in higher estimation and prediction accuracy, especially when humans motion involves complex patterns. (TODO: emphasize that this is a model-based approach without necessity of data training.) Second, such IMM-based prediction approach does not require large data training, which differs from the ANN method in [6]. (TODO: emphasize on the benefit of MPC) Additionally, MPC-based path planning enables the optimal path planning over finite horizon, considering the safety, comfortableness and naturalness requirements. This cannot

be easily achieved by methods in [9] as it needs careful design of potential functions to enforce all these requirements.

The remainder of this paper is organized as follows: first, the problem of motion planning of a human-companion robot is formulated; second, human estimation and prediction methods and robot motion planning approach are described; next, simulation setup and results on evaluating the proposed approach are presented and lastly, concluding remarks and ideas of future work are described.

## II. PROBLEM FORMULATION

Consider

[Note:] dh: Considering?

a scenario (??) in which a companion robot, denoted as the red dot, needs to accompany a human, represented by the green triangle, who will move sequentially to several destinations, shown as blue hollow stars, in the field. The robot has no knowledge about the positions of destinations. However, it can measure human positions in real-time from a GPS sensor via cellphone communication.

[Note:] dh: sensors like GPS or Camera

There exist several obstacles in the field, the positions of which are known and are shown as the blue circle and semicircles.

[Note:] dh: I guess we need to explain more detailed about obstacles in the scenario to show the effort that mimic the real environment. for example, we can say that there are two moving and six stationay obstacles in the scenario

To make socially desirable behavior, the robot should satisfy the aforementioned safety, comfortableness and naturalness requirements (TODO: add formal definitions for these concepts). In this scenario, the safety concern requires the robot to avoid colliding with either the human or any obstacles. Comfortableness requires that the robot maintain a proper distance from the human and naturalness necessitates that the robot keep the velocity similar to that of the human. (TODO: make it clear that how these requirements are instantiated in this paper.)

## III. METHODS

### A. Human Motion Estimation

The Interacting Multiple Model (IMM) approach are applied for estimating the human motion from the noisy sensor data. The IMM approach has been generally considered as the mainstream method for maneuvering target estimation. It utilizes a bank of  $r$  number of filters, each designed to model a different dynamics. In the IMM estimator, state estimate at time  $k$  is computed with mode probability and state estimates from each possible current model associated with one of the  $r$  filters, using the following formula:

$$\hat{x}(k|k) = \sum_{j=1}^r \mu_j(k) \hat{x}^j(k|k)$$

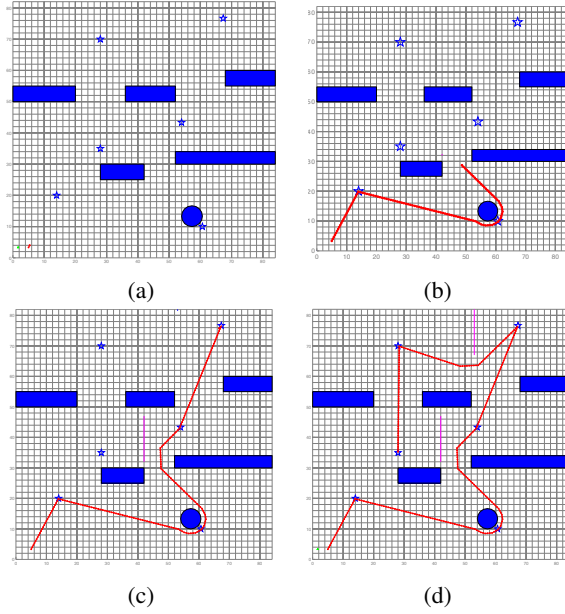


Fig. 1: (a) A scenario for the companion robot to accompany a human. The red circle and the green triangle represent the human and the robot, respectively. Stars denote human destinations and the blue circle and semicircles stand for obstacles. (b) An obstacle starts moving. (c) Another obstacle starts moving. (d) The full human trajectory.

**[Note:]** dh: we need to show more clear plots, especially lines for the moving obstacles. And I guess it had better to use '1st', '2nd' instead of 'an', 'another'

where  $r$  denotes the number of models;  $\hat{x}^j(k|k)$  represents the state estimate from the  $j^{\text{th}}$  filter;  $\mu_j(k)$  stands for the mode probability and is computed as follows:

$$\mu_j(k) = \frac{1}{c} \sum_{i=1}^r L_{ij}(k) p_{ij} \mu_j(k-1)$$

where  $c$  denotes the normalizing factor;  $L_{ij}(k)$  stands for the likelihood function and  $p_{ij}$  represents the mode transition probability from the  $i^{\text{th}}$  to the  $j^{\text{th}}$  model. Each filter uses the mixed initial state estimate and covariance from different combination of the previous model. Readers interested in the details of the IMM approach can refer to [10].

Two different dynamic models are used in the IMM framework. One is the coordinated turn motion model and the other is the uniform motion model. The equation of motion for the both the coordinated turn motion and uniform motion

model becomes the following

$$x^h(k+1) = f(x^h(k)) + Gw(k) \quad (1a)$$

$$f(x^h(k)) = \begin{bmatrix} p_1^h + \frac{\sin(\omega^h T)}{\omega^h} v_1^h - \frac{1 - \cos(\omega^h T)}{\omega^h} v_2^h \\ \cos(\omega^h T) v_1^h - \sin(\omega^h T) v_2^h \\ p_2^h + \frac{1 - \cos(\omega^h T)}{\omega^h} v_1^h + \frac{\sin(\omega^h T)}{\omega^h} v_2^h \\ \sin(\omega^h T) v_1^h + \cos(\omega^h T) v_2^h \\ \omega^h \end{bmatrix} \quad (1b)$$

$$G = \begin{bmatrix} \frac{T^2}{2} & 0 & 0 \\ \frac{T}{2} & 0 & 0 \\ 0 & \frac{T^2}{2} & 0 \\ 0 & T & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (1c)$$

$$w \sim \mathcal{N}(0, Q) \quad (1d)$$

where  $x^h(k)$  represents the human motion state including five elements:  $p_1^h, v_1^h, p_2^h, v_2^h, \omega^h$ , where  $p_1^h, p_2^h$  denote the longitudinal and lateral position of the human,  $v_1^h, v_2^h$  the corresponding velocity and  $\omega^h$  the turn rate of the human;  $w(k)$  represents process noise;  $T$  represents the sampling time;  $Q$  is the covariance matrix of the process noise.

The uniform motion model is nothing more than the limiting case of the coordinated turn motion model as turn rate,  $\omega$ , goes to zero while the coordinated turn motion model consider that turn rate is modeled as time-varying. If all motions are covered by a single model, the need for the IMM is eliminated. Although computations are reduced by using a single model, it happens to lose the ability to quickly detect the change of motions. This trade-off between computation and motion-change detection is main argument when choosing a single or a multiple model approach. The decision is a bit clearer in linear case since the turn rate is fixed in linear dynamic models. With a single nonlinear model, it is possible to provide accurate state estimates. However, it is common to include one uniform motion model and one coordinated turn motion model for quick motion-change detection. Since human motion usually involves different motions in the real world, the ability to quickly detect the change of the motion is one of the important properties for the estimation and prediction.

The equation of the uniform motion model is shown as follows:

$$\dot{x}^h(k+1) = Ax^h(k) + Bw(k) \quad (2a)$$

$$A = \begin{bmatrix} 1 & T & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & T & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \quad B = \begin{bmatrix} \frac{T^2}{2} & 0 & 0 \\ \frac{T}{2} & 0 & 0 \\ 0 & \frac{T^2}{2} & 0 \\ 0 & T & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad (2b)$$

The observation equation is represented as :

$$y^h(k) = Cx^h(k) + v(k) \quad (3a)$$

where  $y^h(k)$  denotes the human motion observation at the time step  $k$ ;  $v(k)$  stands for measurement noise

We assume that only the human position can be measured. Therefore, the parameters in observation model Eq. (3a) can be defined as:

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{bmatrix}, \quad (4a)$$

$$v \sim \mathcal{N}(0, V) \quad (4b)$$

where  $V$  is the covariance matrix of the measurement noise. The above two models are used for human motion state estimation using the Unscented Kalman Filter.

### B. Unscented Kalman Filter

The Unscented Kalman Filter (UKF) is an effective state estimation technique for nonlinear systems by implementing the Unscented Transformation (UT) to calculate the statistics of a random vector that undergoes a nonlinear transformation [12]. Given an  $L$ -dimensional Gaussian Random Vector (GRV)  $x$  with mean  $\hat{x}$  and covariance  $P_x$ , the statistics of  $z = f(x)$  are approximated by the selection of  $2L+1$  discrete sample points  $\{\chi^{(i)}\}_{i=0}^{2L} = \{\hat{x} \text{ and } \hat{x} \pm \sigma_j, j = 1, \dots, L\}$  where  $\sigma_i$  is the  $i^{th}$  column of the matrix  $\sqrt{(L+\lambda)P_x}$ .  $\lambda$  is a scaling parameter, defined below.

$$\lambda = \alpha^2(L + \kappa) - L \quad (5a)$$

$$W_0^{(m)} = \frac{\lambda}{L + \lambda} \quad (5b)$$

$$W_0^{(c)} = \frac{\lambda}{L + \lambda} + 1 - \alpha^2 + \beta \quad (5c)$$

$$W_i^{(m)} = W_i^{(c)} = \frac{1}{L + \lambda}, \quad i = 1, \dots, 2L \quad (5d)$$

where  $\alpha$  determines the spread of sigma points about the mean  $\hat{x}$ ;  $\kappa$  is a secondary scaling parameter;  $\beta$  is used to incorporate prior knowledge of the distribution. (our simulation uses  $L = 5, \alpha = 0.001, \kappa = 0, \beta = 2$ )

Once the discrete sample points  $\{\chi^{(i)}\}_{i=0}^{2L}$ , called *sigma points*, have been generated, each point is passed through the nonlinear function  $z = f(x)$ , i.e. each column of the sigma points is propagated through the non-linearity, as in  $\zeta = f(\chi), i = 0, \dots, 2L$ . The mean  $\hat{z}$  and the covariance  $P_z$  are approximated as  $\hat{z} \simeq \sum_{i=0}^{2L} W_i^{(m)} \zeta^{(i)}$  and  $P_z \simeq \sum_{i=0}^{2L} W_i^{(c)} (\zeta^{(i)} - \hat{z})(\zeta^{(i)} - \hat{z})^T$ , are calculated as given in above equations of the weights and parameters [13]. Readers can refer to [12] for more details of UKF algorithm.

### C. Human Motion Prediction

The estimated human motion states and the mode probabilities are utilized for predicting human future states. Let  $\hat{x}^{h,j}(k|k)$  and  $\hat{x}^{h,j}(k+i|k)$  represent the estimated and predicted human states associated with the  $j^{th}$  model at time  $k$  and  $k+i$  ( $i \geq 0$ ), respectively, based on the observation up to time  $k$ . Using the uniform motion model and the turn motion model, human positions for each model can be extrapolated and combined with the mode probabilities. To

be specific, the prediction procedure works as follows:

$$\hat{x}^h(k+l+1|k) = \sum_{j=1}^r \mu_j \hat{x}^{h,j}(k+l+1|k) \quad (6a)$$

$$l = 0, \dots, N-1 \quad (6b)$$

$$\hat{x}^{h,j}(k+l+1|k) = \hat{x}^{h,j}(k+l+1|k) \quad j = 1, \dots, r \quad (6c)$$

$$= \sum_{i=0}^{2L} W_i^{(m)} \chi_{k+l+1|k}^{(i)} \quad (6d)$$

$$\chi_{k+l+1|k}^{(i)} = f(\chi_{k+l|k}^{(i)}) \quad i = 0, \dots, 2L \quad (6e)$$

where  $N$  denotes the prediction horizon;  $r$  represents the number of models;  $L$  is the dimension of  $x^{h,j}$ . For the purpose of simplicity, we define  $p^h(k) = \begin{bmatrix} p_1^h(k) \\ p_2^h(k) \end{bmatrix}$  and

$v^h(k) = \left\| \begin{bmatrix} v_1^h(k) \\ v_2^h(k) \end{bmatrix} \right\|_2$  to represent the position vector and the speed of the human at time  $k$ , respectively. Notations for the estimated and predicted position vector and speed can be defined as  $\hat{p}^h(k|k), \hat{p}^h(k+i|k), \hat{v}^h(k|k), \hat{v}^h(k+i|k)$ , respectively.

### D. Robot Path Planning

The model predictive control (MPC) method provides an effective framework for incorporating the safety, comfortableness and naturalness requirements into the robot motion planning. MPC iteratively solves a finite time constrained optimal control problem. After obtaining the optimal series of control inputs at current state, it implements the first input and then computes for a new series of control inputs, starting from the new state. Use  $(p^r(k), v^r(k), \theta^r(k))$  to denote the robot state at time  $k$ , representing the position, speed and heading angle, respectively. The control input consists of the acceleration  $a^r(k)$  and the angular velocity  $\omega^r(k)$ . The robot motion planning problem is formulated as an MPC problem that incorporates the kinematics of the robot and

the aforementioned requirements:

$$\min_{\mathbf{A}_k, \mathbf{\Theta}_k} \sum_{i=1}^N q_1 \|\bar{p}^r(k+i|k) - \hat{p}^h(k+i|k)\|_2^2 +$$

$$q_2 \|\bar{v}^r(k+i|k) - \hat{v}^h(k+i|k)\|^2 \quad (7a)$$

$$\text{subject to } \bar{p}^r(k+i+1|k) = \bar{p}^r(k+i|k) + \bar{v}^r(k+i|k) \begin{bmatrix} \cos \bar{\theta}(k+i|k) \\ \sin \bar{\theta}(k+i|k) \end{bmatrix} T \quad (7b)$$

$$\bar{v}^r(k+i+1|k) = \bar{v}^r(k+i|k) + \bar{a}(k+i|k)T \quad (7c)$$

$$\bar{\theta}^r(k+i+1|k) = \bar{\theta}^r(k+i|k) + \bar{w}(k+i|k)T \quad (7d)$$

$$a_{lb} \leq \bar{a}^r(k+i|k) \leq a_{ub} \quad (7e)$$

$$w_{lb} \leq \bar{w}^r(k+i|k) \leq w_{ub} \quad (7f)$$

$$\|\bar{p}^r(k+i+1|k) - \hat{p}^h(k+i+1|k)\|_2 \geq d_s \quad (7g)$$

$$\|\bar{p}^r(k+i+1|k) - p_l^{obs}\|_2 \geq r_l^{obs} \quad (7h)$$

$$\|\lambda \bar{p}^r(k+i|k) + (1-\lambda) \bar{p}^r(k+i+1|k) - p_l^{obs}\|_2 \geq r_l^{obs}, \quad \forall l = 1, \dots, m, 0 \leq \lambda \leq 1 \quad (7i)$$

$$\bar{p}^r(k|k) = p^r(k) \quad (7j)$$

$$\bar{v}^r(k|k) = v^r(k) \quad (7k)$$

$$\bar{\theta}^r(k|k) = \theta^r(k) \quad (7l)$$

where  $\bar{p}^r(k+i|k)$ ,  $\bar{v}^r(k+i|k)$  and  $\bar{\theta}(k+i|k)$ ,  $0 \leq i \leq N$  represent the planned positions, velocities and heading angles of the robot at time  $k+i$ , respectively;  $m$  is the number of obstacles and  $p_l^{obs}$  and  $r_l^{obs}$  denote the position and the radius of the  $l^{\text{th}}$  obstacle;  $(\mathbf{A}_k, \mathbf{\Theta}_k)$  stand for the set of optimal acceleration and angular velocity in the prediction horizon  $[k, k+N-1]$ , obtained by solving the MPC problem at time  $k$ .

The objective function Eq. (7a) consists of two terms, standing for the square sum of position and velocity differences between planned robot states and predicted human states over the horizon  $N$ . This reflects the comfortableness and naturalness requirements that the robot stay close to the accompanied human and keep similar pace.  $q_1$  and  $q_2$  denote the weights for these two terms. Eqs. (7b) to (7f) represent the robot's discrete-time kinematic model with limited acceleration and angular velocity, with  $a_{lb}$ ,  $w_{lb}$  being the corresponding lower bounds and  $a_{ub}$ ,  $w_{ub}$  the upper bounds. Eq. (7g) imposes the safety constraints that the robot should maintain a minimum distance  $d_s$  from the human in order to avoid collision. Eqs. (7h) and (7i) enforces the requirements on collision avoidance with obstacles. In particular, Eq. (7h) demands that each way point of the robot be kept outside of obstacles and Eq. (7i) requires that the trajectory connecting the adjacent way points not intersect with obstacles. Eqs. (7j) to (7l) shows the constraints on robot's initial state at time  $k$ .

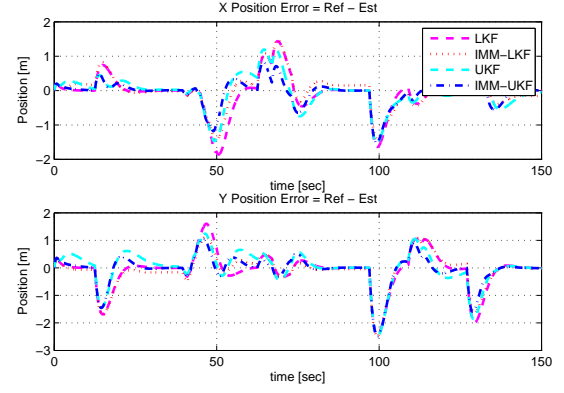


Fig. 2: Comparison of position estimation error with LKF, IMM-LKF, UKF and IMM-UKF

## IV. SIMULATION RESULTS & DISCUSSION

### A. Simulation setup

Simulations have been run to evaluate the proposed robot motion planning approach. There are one human and one robot with five targets and four obstacles in a  $84m \times 82m$  field. The human speed in the simulation is set to be constant at  $1.5m/s$ . The human will follow the trajectory shown in Fig. 1d. However, this trajectory is unrevealed to the robot. The safety distance  $d_s$  is chosen as  $2m$ . The sampling rate of GPS sensor is  $20Hz$  and the variance of sensor measurement noise is considered as  $2m$ . The robot's maximum acceleration and deceleration are set to be  $1m/s^2$  and  $-3m/s^2$  respectively and the angular velocity range is chosen to be  $[-30^\circ/s, 30^\circ/s]$ . In the IMM estimator, the process noise and the measurement noise are set to be  $1.5 \times 10^{-2}$  and  $1.5$ , respectively. The prediction horizon for the human motion is chosen as  $500ms$  and the robot recomputes the MPC problem every  $500ms$ .

### B. Simulation results

We evaluate the performance of human motion estimation and prediction and robot motion planning methods, respectively.

1) *Human motion estimation*: The error between the estimated and the actual human position and velocity at each time step are compared to evaluate the estimation accuracy. The position error vector can be formulated as:

$$\Delta_p^t(k) = p^h(k) - \hat{p}^h(k|k)$$

where  $p^h(k)$  denotes the actual human position at time  $k$ .

Fig. 2 shows the position estimation error on longitudinal and lateral directions using four different estimators: Linear Kalman Filter (LKF), IMM-LKF, UKF and IMM-UKF. In the simulation, the same turn motion model in IMM-UKF is adopted for the system dynamics in UKF and the uniform motion model in IMM-LKF is also applied to the dynamic model in LKF. There are two observations in this figure. First, the responses of the nonlinear estimators such as UKF and IMM-UKF are faster than the linear



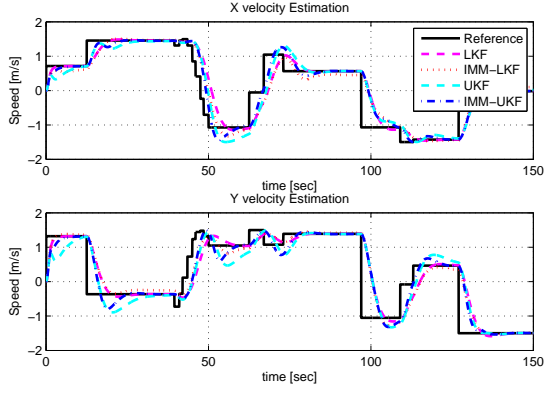


Fig. 3: Comparison of the estimated velocity using the IMM-based and the single-model approaches

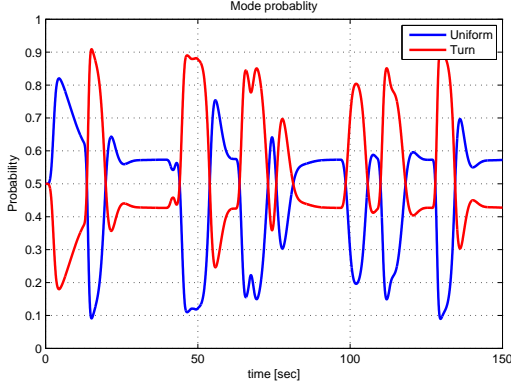


Fig. 4: Model probabilities of two models in the IMM-UKF estimator

estimators. Second, the IMM-based approaches show better performance in accuracy than the single-model approaches. Besides, IMM-UKF achieves the fastest response and best accuracy compared to other methods, especially when the human turns around the circular obstacle at time 50 and makes sharp turn after arriving at a destination at time 110. Fig. 3 compares the velocity estimation using four estimators. Overall, the nonlinear estimators (UKF and IMM-UKF) show faster response compared to the linear estimators (LKF and IMM-LKF), though they have overshoots due to the fast response. It is worth noting that the overshoots of IMM-UKF are smaller than UKF while keeping the fast response at time 53 and 118 when the velocity changes abruptly. This makes sense as the UKF-IMM estimator incorporates uniform motion model that can capture the sudden velocity changes. Fig. 4 shows the mode probabilities of the uniform motion model and turn motion model in IMM-UKF over time. When the human speed changes, the mode probability of the turn motion becomes higher than that of the uniform motion. These changes illustrates the reason that IMM-based estimators achieve more accurate and faster estimation than the single-model estimator at the sharp turn and circular

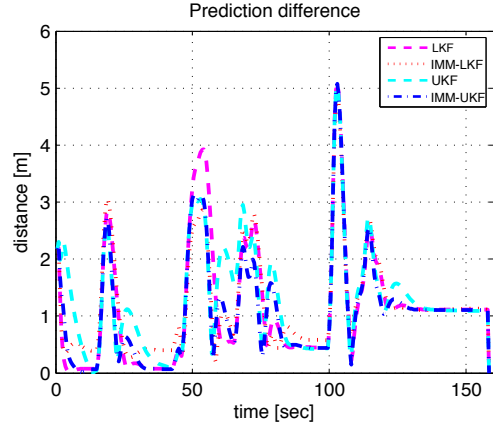


Fig. 5: Comparison of prediction error between the IMM-based and single-model approaches

turn, thus demonstrating the necessity of applying IMM-UKF estimator for human tracking.

2) *Human motion prediction*: To evaluate the IMM-based prediction approaches, the average prediction error over the prediction horizon is computed and compared with the single-model approaches. At time  $k$ , the prediction error is defined as:

$$\Delta_p(k) = \frac{1}{N} \sum_{i=1}^N \|\hat{p}^h(k+i|k) - p^h(k+i)\|_2 \quad (8)$$

Different from the IMM-based prediction approaches that extrapolate the human position by a weighted sum of the predicted positions from each model, the single-model methods only utilize the uniform motion model for prediction.

Fig. 5 shows the comparison of prediction error using two single-model approaches (LKF, UKF) and two IMM-based methods (IMM-LKF, IMM-UKF). It can be noticed that single-model approaches generate larger prediction error than IMM-based methods, especially when the human makes turns, such as at time 50. This makes sense as IMM-based method considers different dynamic models related to the human motion. Based on the simulation results, IMM-UKF outperforms the other three methods for prediction.

3) *Robot motion planning*: Fig. 6 shows a screenshot of the simulation that the robot accompanies the target person moving in the field. The performance of the robot motion planning is evaluated using the criterion of safety, comfortableness and naturalness. To be specific, we measure the distance and speed difference between the robot and the human at each time step. At time  $k$ , they can be defined as:

$$\Delta_d(k) = \|z^r(k) - z^h(k)\|_2 - d_s \quad (9a)$$

$$\Delta_v(k) = |v^r(k) - v^h(k)| \quad (9b)$$

To evaluate the accompanying performance using single-model predictor and multiple-model predictor, the UKF and IMM-UKF are used in conjunction with MPC to generate two sets of simulation, the results of which are compared.

Fig. 7 compares the distances between the human and the robot using these two predictors. Notice that the distances

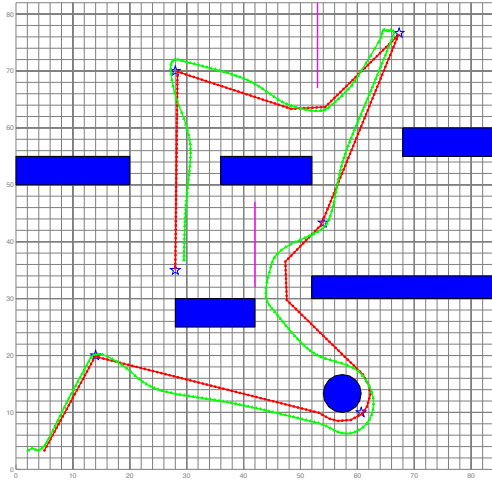


Fig. 6: A screenshot of the simulation. The red line represents the human trajectory and the green on shows the companion robot's trajectory. For most of the time, the robot follows the human from behind

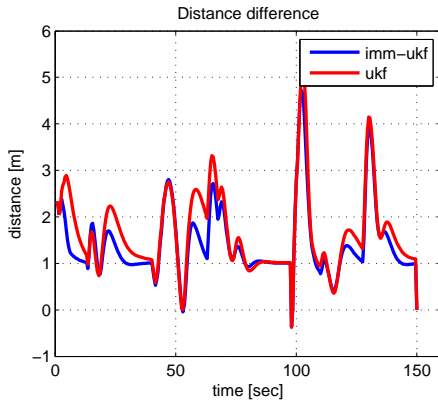


Fig. 7: Comparison of distance (subtracted by the safety distance) between the human and the robot using the MPC and the reactive methods

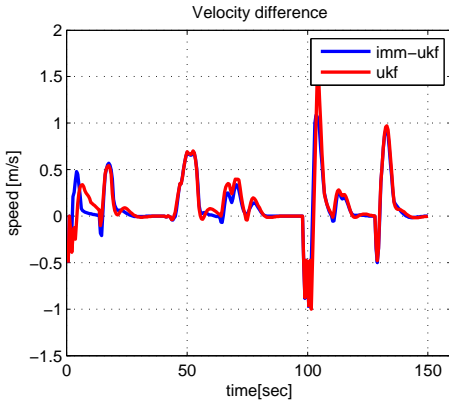


Fig. 8: Comparison of velocity difference between the human and the robot using the MPC and the reactive methods

in the plot has been subtracted by the safety distance  $d_s$ . Therefore, the ideal distance is zero at each time step. We can notice that the IMM-UKF predictor generates smaller distance difference than the UKF predictor. **Table xxx shows the statistics of the performance. The IMM-UKF method achieves xxx% improvement on average distance, xxx% on maximum distance and also minimum distance. In addition, the robot using IMM-UKF as the predictor can achieve less unsafe distance than the UKF method. Such improvement is desirable for an accompanying robot as it keeps proper distance from the human and only moves within the unsafe distance for xxx long. Such unsafety is caused when the human makes sharp turns, which has been discussed in Sections IV-B.1 and IV-B.2. The UKF and IMM-UKF predictor result in similar velocity behavior, as shown in Fig. 8. The statistics also shows smaller velocity difference using the IMM-UKF predictor.**

The simulation results shows the superiority of using the MPC approach for motion planning.

## V. CONCLUSION

We have developed a model predictive control (MPC)-based motion planning approach for human-companion robots to accompany a target person in a socially desirable manner, which considers the safety, comfortableness and naturalness. The IMM-UKF approach that incorporates the uniform motion model and the coordinated turn motion models is developed for human position estimation and prediction. Based on the predicted human positions, an MPC problem is formulated for robot motion planning. The estimation and prediction accuracy using IMM-UKF is compared with two single-model methods (LFK and UKF) and IMM-LKF. Comparison results show superior accuracy and response in estimation and prediction using IMM-UKF approach, especially when the human makes circular motion or sharp turns. The MPC motion planning approach is compared with a reactive method and shows that the MPC method achieves better performance in generating smaller human-robot distance while similar performance in the velocity difference.

In the future work, we plan to investigate other motion prediction methods, such as the autoregressivemoving-average method, to compare with IMM-UKF method. Besides, enabling the robot to learn human motion model in real time is an attractive topic and may provide more accurate human motion prediction and results in better human-companion behaviors.

## VI. APPENDIX

Similar to IMM-UKF, IMM-LKF works with two dynamic models: one is the uniform motion model; the other is the coordinated turn motion model. If the turn rate is a known constant in the coordinated turn motion model in ??, the human estimation procedure can be modeled with the

discrete time linear state space system as follows:

$$x^h(k+1) = Ax^h(k) + B_w w(k) \quad (10a)$$

$$y^h(k) = Cx^h(k) + v(k) \quad (10b)$$

where  $x^h(k)$  and  $y^h(k)$  represent the human motion state and the observation, respectively, at the time step  $k$ ;  $w(k)$  and  $v(k)$  represent process noise and measurement noise, respectively.  $x^h(k)$  consists of four elements:  $p_1^h, v_1^h, p_2^h, v_2^h$ , where  $p_1^h, p_2^h$  denote the longitudinal and lateral position of the human and  $v_1^h, v_2^h$  the corresponding velocity. We use two Linear Kalman Filters in the IMM for human tracking, each corresponding to a different dynamics model: the uniform motion model and the turn motion model. Two models differ in the  $A$  matrix and  $w$  in Eq. (10a) while sharing the same  $B_w$ . In particular, we define the matrices as follows:

$$A_U = \begin{bmatrix} 1 & T & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & T \\ 0 & 0 & 0 & 1 \end{bmatrix}, \quad (11a)$$

$$A_T = \begin{bmatrix} 1 & \frac{\sin(\omega T)}{\omega} & 0 & \frac{1-\cos(\omega T)}{\omega} \\ 0 & \cos(\omega T) & 0 & -\sin(\omega T) \\ 0 & \frac{1-\cos(\omega T)}{\omega} & 1 & \frac{\sin(\omega T)}{\omega} \\ 0 & \sin(\omega T) & 0 & \cos(\omega T) \end{bmatrix}, \quad (11b)$$

$$B_w = \begin{bmatrix} T & 1 & 0 & 0 \\ 0 & 0 & T & 1 \end{bmatrix}, \quad (11c)$$

$$w_U \sim \mathcal{N}(0, Q_U) \quad w_T \sim \mathcal{N}(0, Q_T) \quad (11d)$$

where  $A_U$  and  $A_T$  stand for the  $A$  matrices of the uniform motion model and turn motion model, respectively;  $w_U$  and  $w_T$  denote the process noise of the uniform motion model and turn motion model, respectively;  $T$  represents the sampling time;  $\omega$  represents the constant turn rate.

We assume that only the human position can be measured. Therefore, the parameters in observation model Eq. (10b) can be defined as:

$$C = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}, \quad (12a)$$

$$v \sim \mathcal{N}(0, V) \quad (12b)$$

Above linear state space models are used in LKF and IMM-LKF in this paper. Moreover, we set the turn rate  $\omega$  to be 0.1 rad/s as a known constant, in the turn motion model in IMM-LKF.

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