

$$\begin{aligned} & t_{init} \\ & t_{final} \\ & \mathcal{R} \\ & B \\ & \dot{q}(t) = f(q(t), u(t)) \end{aligned}$$

$$\begin{aligned} & q \in \\ & R^n \\ & u \in \\ & R^p \\ & R_b, R_b \in \\ & \mathcal{R}, b \in \\ & \{0, \dots, B-1\} \\ & \rho_b \\ & (x_b, y_b) \\ & t_{b,init} \\ & t_{b,final} \leq \\ & t_{final} \\ & q_{init}, q_{goal} \\ & q_{init}, q_{goal} \end{aligned}$$

$$\begin{aligned} & \mathcal{O} \\ & M \\ & O_m, O_m \in \mathcal{O}, \\ & m \in \{0, \dots, M-1\} \\ & r_{O_m} \\ & (x_{O_m}, y_{O_m}) \\ & t \in \\ & [t_{init}, t_{final}] \end{aligned}$$

$$\begin{aligned} & O_m \\ & R_b \\ & d_{b,sen} \\ & R_b \\ & \mathcal{O}_b \\ & \mathcal{O}_b \subset \\ & \mathcal{O} \\ & R_b \\ & R_b \\ & |u_{b,i}(t)| \leq \\ & u_{b,i,max}, \forall i \in \\ & [1, p], \forall t \in \\ & [t_{init}, t_{final}] \\ & (q^*(t), u^*(t)) \\ & (q_b^*(t), u_b^*(t)) \\ & ? \\ & (q^*(t), u^*(t)) \\ & (q^*(t), u^*(t)) \\ & R_b \\ & (q_b^*(t), u_b^*(t)) \\ & \dot{q}_b^*(t) = f(q_b^*(t), u_b^*(t)), \forall t \in [t_{init}, t_{final}], \forall b \in \{0, \dots, B-1\}. \end{aligned}$$

$$(1) \begin{aligned} & R_b \\ & R_b \\ & {}^*(t_{init}) = \\ & q_{b,init}, \\ & u_b^*(t_{init}) = \\ & u_{b,init}, \forall b \in \\ & \{0, \dots, B-1\}. \\ & R_b \\ & R_b \\ & {}^*(t_{final}) = \\ & q_{b,goal}, \\ & u_b^*(t_{final}) = \\ & u_{b,goal}, \forall b \in \\ & \{0, \dots, B-1\}. \\ & \forall t \in \\ & [t_{init}, t_{final}] \\ & \forall i \in \\ & [1, 2, \dots, p] \\ & \forall b \in \\ & \{0, \dots, B-1\} \end{aligned}$$

$$(2) \quad |u_{b,i}^*(t)| \leq u_{b,i,max}.$$

$$(3) \quad L(q(t), u(t)) = \sum_{b=0}^{B-1} L_b(q_b(t), u_b(t), q_{b,goal}, u_{b,goal})$$

$$\begin{aligned} & L_b(q_b(t), u_b(t), q_{b,goal}, u_{b,goal}) \\ & R_b \\ & ? \end{aligned}$$