# Dynamic Validation of Multi-robot Motion Planning Using a Distributed Receding Horizon Approach

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Abstract—This paper analyzes the real-time implementation of an algorithm for collision-free motion planning of a team of wheeled mobile robots in the presence of obstacles in a realistic environment. Planning and navigation are simulated with three robots. Deviations from the planned motion caused by the system dynamics can be overcome by doing few changes in the optimization problem uderlying the planning algorithm and using a feedback controller.

#### I. Introduction

The capability of defining a collistion-free motion plan for passing from one configuration to another is a crutial aspect of robotics that can be specially hard to solve for mobile multi-robot systems. A trending application that require this capability is the use of robotic systems in industrial supply chains for processing orders and optimizing the storage and distribution of products. For example, Amazon employs the Kiva mobile-robot system, and IDEA Groupe employs the Scallog system for autonomously processing client orders [?], [?]. Such logistics tasks became increasingly complex as sources of uncertainty, such as human presence, are admitted in the work environment.

For efficiently solving the motion planning problem, different constraints must be taken into account, in particular, geometric, kinematic and dynamic constraints. The first constraints result from the need of preventing the robot to assume specific configurations in order to avoid collisions, communication loss, etc. Kinematic constraints derive directly from the mobile robot architecture implying, in particular, in nonholonomic constraints. Dynamics constraints come mainly from inertial effects and interaction between different bodies in contact.

In [1], a Distributed Receding Horizon Motion Planning is presented. It is intended for planning the motion of a team of nonholonomic mobile robots, in a partially known environment occupied by static obstacles, being efficient with respect to the travel time (amount of time to go from initial to goal configuration). However, only kinematic validation of that approach was done and its applicability in a more realistic scenario remained to be tested.

This work builds directly on that approach and aims to analyze that motion planning method in a realistic scenario. By means of a physics engine that can simulate rigid body dynamics (including collision detection), the aproach is tested, evaluated and improved. The improvements are meant to overcome possible deviations between the executed and planned motion.

Related work (...)

This paper outline is as follows. The second section gives an overview of the Distributed Receding Horizon Motion Planning. It shows how this approach manages to find motion plans that respect geometric and kinematics cosntraints while minimizing the travel time of each robot in the team. The third section proposes a simple change on the optimization problem uderlying the motion planning for providing better plans with respect to the system dynamics. It also proposes a predictive feedback control that asymptotically stabilizes the tracking error. The forth section is dedicated to the dynamic simulation aspects and the results of using the proposed motion planning in that realistic scenario. Finally, in last section we present our conclusions and perspectives.

## II. DISTRIBUTED RECEDING HORIZON MOTION PLANNING

As a team of robots evolves in their work environment they progressively perceive new obstacles in their way to their goal configuration. Thus, try to plan for the whole motion from initial to goal configurations is not a satisfying approach. Planning locally and replanning is more suitable for taking new information into account as it comes.

In the Distributed Reciding Horizon approach for motion planning, each robot in the team computes its own local plan. Two fundamental concepts of this approach are the planning horizon  $T_p$  and update/computation horizon  $T_c$ .  $T_p$  is the timespan for which a solution will be computed and  $T_c$  is the time horizon during which a plan is executed while the next plan, valid for the next timespan  $T_p$ , is being computed. The problem of producing a motion plan for a  $T_p$  horizon during the  $T_c$  time interval is called here a receding horizon planning problem.

For each receding horizon planning problem, the following steps are performed:

Step 1: Each robot in the team computes it own intended solution trajectory (denoted  $(\hat{q}_b(t), \hat{u}_b(t))$  with  $q_b$  the configuration vector a robot b and  $u_b$  its input vector) by solving a constrained optimization problem that takes geometric and kinematic constraints into account. Coupling constraints, that is, constraints that involve solving a conflict between two robots such as collision or loss of communication, are ignored at this step.

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Step 2: Robots involved in a potential conflict (risk of collision, lost of communication) update their trajectories computed during Step 1 by solving a second constrained optimization problem that additionally takes into account geometric constraints for avoiding the conflict. This is done by using the intended trajectories of other robots computed in the previous step as an estimate of those robots' final trajectories. If a robot is not involved in any conflict, Step 2 is not executed and its final solution trajectory is identical to the one estimated in Step 1.

Robots may not use the same  $T_p$  and  $T_c$  but in these cases a way of considering other robots intended trajectories even though they are not valid for the same time-horizon has to be provided.

For each of these steps and for each robot in the team, one constrained optimization problem is resolved. The cost function to be minimized in those optimization problems is the geodesic distance of a robot's current position to its goal position. This assures that the robots are driven towards their goal.

However, when a robot arrives closer to its goal the receding horizon planning scheme does not produce the desired effect. For instance, near the goal, a plan for reaching it can possibly take less time than the  $T_p$  planning horizon.

In [1] a termination procedure for reaching the goal is proposed. It takes the goal configuration as a hard constraint in the optimization problem and uses the time for reaching the goal as the cost function to be minimized.

Figure 1 illustrates how plans would be generated through time by the receding horizon scheme with termination plan.

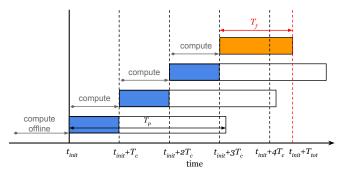


Fig. 1: Receding horizon scheme with termination plan. The timespan  $T_f$  represents the duration of the plan for reaching the goal configuration.

The plans generated with this approach are feasable regarding kinematics but not necessarely regarding the dynamics of the robots.

For that including constraints related to acceleration in the optimization problems and a predictive control are proposed in the next section.

#### III. DYNAMICS

A. Adding acceleration constraints

B. Predictive Control

1) Extended Unicycle Model:

To find a predictive control law an extended model of the mobile robot which integrates its dynamics is needed. We can derive from [2] the following dynamic model:

$$\begin{bmatrix}
\dot{x} \\
\dot{y} \\
\dot{v} \\
\dot{v} \\
\dot{\omega}
\end{bmatrix} = \begin{bmatrix}
v\cos\psi \\
v\sin\psi \\
\omega \\
\frac{\theta_3}{\theta_1}\omega^2 - \frac{\theta_4}{\theta_1}v \\
-\frac{\theta_5}{\theta_2}v\omega - \frac{\theta_6}{\theta_2}\omega
\end{bmatrix} + \begin{bmatrix}
0 & 0 \\
0 & 0 \\
0 & 0 \\
\frac{1}{\theta_1} & 0 \\
0 & \frac{1}{\theta_2}
\end{bmatrix} \underbrace{\begin{bmatrix}
u_1 \\
u_2
\end{bmatrix}}_{u} (1)$$

where  $q \in Q \subset \mathbb{R}^n$  is the state vector and  $u \in U \subset \mathbb{R}^p$  the input. The parameters vector  $\theta \in \mathbb{R}^6$  characterizing the dynamics of the robot can be determined by system identification or based on properties of the unicycle such as mass, moment of inertia, impedance of motors using the equations provided in [2]. For our particular, simulated case an identification algorithm was used based on the minimization of error in velocities followed by minimization of error in position.

The above equations represent a non-linear control-affine system respecting the following form:

$$\dot{q} = f(q, u)$$

$$= f_a(q) + \sum_{j=1}^p f_{b,j} u_j \tag{2}$$

For these kind of systems an asymptotically stabilizing, static, stationary and continue state feedback can be found whenever a Lyapunov function strictly assignable to the system and continue at the origin exists.

#### 2) Optimal predictive control:

The objective is to synthesize a control law that minimizes the quadratic error in position and orientation (i.e. pose) over a time horizon ahead of the current instant t.

Since only error in pose is to be minimized, the system output can be written as follows:

$$y(t) = h(q(t)) = \begin{bmatrix} x \\ y \\ \psi \end{bmatrix}$$

with  $y \in Y \subset \mathbb{R}^m$ . And the error as:

$$e(t) = y(t) - y_{\text{ref}}(t)$$

where  $y_{ref}(t)$  is derived from the planner's output.

The criterion to be minimized represented by J can be written as:

$$J = \sum_{i=1}^{m} J_i$$

with

$$J_i = \frac{1}{2} \int_0^{T_i} (e_i(t+\tau))^2 d\tau$$

where  $T_i$  is the prediction horizon and  $e_i(t+\tau)$  represents the prediction error at  $t + \tau$  with  $0 < \tau \le T_i$ . In this particular case, to find the control law that minimizes J is to find u satisfying the equation:

$$\frac{\partial J}{\partial u} = 0_{p \times 1}$$

For solving the above equation an expression for the prediction error must be defined and the criterion rewritten in a matrix form.

### 3) Predictive error definition:

Similarly to what is done in [3] the ith element of  $y(t+\tau)$ can be written as bellow using Taylor series:

$$y_i(t+\tau) = \sum_{k=0}^{\rho_i} y_i^{(k)}(t) \frac{\tau^k}{k!} + \epsilon(\tau^{\rho_i})$$

As explained in [3] the vector  $\rho = [\rho_1 \ldots \rho_m]$  is the relative degrees of a non-linear MIMO system (Multiple Input Multiple Output). It is a vector compose by possibly different values of relative degrees  $\rho_i$  for each output  $y_i$ .  $\rho_i$ is the least number of derivatives required to make explicit in the expression of  $y_i$  at least one component of the input

Furthermore, a non-linear control-affine MIMO system (equation 2) has a relative degree vector  $\rho = [\rho_1 \dots \rho_m]$ 

- 1)  $L_{f_{b,j}}^{(k)}L_{f_a}^{(k)}y_i=0$  for all  $1\leq j\leq p$ , for all  $k<\rho_i-1$ , for all  $1\leq i\leq m$  and for all q in the neighborhood
- 2) the product  $D^tD$  is non-singular, D being the decoupling matrix of dimension  $m \times p$ , given by:

$$D = \begin{bmatrix} L_{f_{b,1}} L_{f_a}^{(\rho_1 - 1)} y_1 & \dots & L_{f_{b,p}} L_{f_a}^{(\rho_1 - 1)} y_1 \\ \vdots & \ddots & \vdots \\ L_{f_{b,1}} L_{f_a}^{(\rho_m - 1)} y_m & \dots & L_{f_{b,p}} L_{f_a}^{(\rho_m - 1)} y_m \end{bmatrix}$$
a valid reference trajectory is a valid reference trajectory in the control of the property of the control of

Here we use the standard geometric notiation for Lie derivaties sumurized bellow:

$$\begin{cases} L_f^{(0)} y_i &= y_i \\ L_f^{(k)} y_i &= L_f L_f^{(k-1)} y_i = \frac{\partial L_f^{(k-1)} y_i}{\partial q} f = y_i^{(k)} \end{cases}$$

Rewriting the expression for  $y_i(t + \tau)$  in a matrix form and excluding the remainder term we obtain the following approximation:

$$y_{i}(t+\tau) \simeq \underbrace{\left[\begin{array}{cccc} 1 & \tau & \frac{\tau^{2}}{2} & \dots & \frac{\tau^{\rho_{i}}}{\rho_{i}!} \end{array}\right]}_{\Lambda_{i}} \begin{bmatrix} y_{i}(t) \\ \dot{y}_{i}(t) \\ \ddot{y}_{i}(t) \\ \vdots \\ y_{i}^{(\rho_{i})}(t) \end{bmatrix}$$
(4)

Replacing the first matrix by the more compact notation  $\Lambda_i$  and using Lie derivatives the previous can be written as:

$$y_i(t+\tau) \simeq \Lambda_i L_{y_i} \tag{5}$$

where

$$\begin{split} L_{y_i} &= \begin{bmatrix} L_f^{(0)} y_i(t) \\ L_f^{(1)} y_i(t) \\ \vdots \\ L_f^{(\rho_i-1)} y_i(t) \\ L_f^{(\rho_i)} y_i(t) \end{bmatrix} \\ &\text{Assuming 1:} \\ &= \begin{bmatrix} L_{f_a}^{(0)} y_i(t) \\ L_{f_a}^{(1)} y_i(t) \\ \vdots \\ L_{f_a}^{(\rho_i-1)} y_i(t) \\ L_{f_a}^{(\rho_i-1)} y_i(t) \\ L_{f_a}^{(\rho_i-1)} y_i(t) + L_{f_b}(L_{f_a}^{(\rho_i-1)} y_i(t)) u(t) \end{bmatrix} \end{split}$$

The second term in the prediction error expression,  $y_{\rm ref}(t+\tau)$ , can be given by the planner for any  $\tau \mid 0 < \tau \leq T_i$  as long as  $T_i \leq T_p - T_c$ . This is because  $y_{\rm ref}(t+T_p-T_c)$  is the further in time the planner can output a valid reference trajectory for any given t.

After some algebraic manipulation we can show that:

$$\begin{split} J_{i} &= \frac{1}{2} \int_{0}^{T_{i}} (y_{i} - y_{i,\text{ref}})^{2} d\tau \\ &= \frac{1}{2} \int_{0}^{T_{i}} y_{i}^{2} d\tau - \int_{0}^{T_{i}} y_{i} y_{i,\text{ref}} d\tau + \frac{1}{2} \int_{0}^{T_{i}} y_{i,\text{ref}}^{2} d\tau \\ &= \frac{1}{2} \int_{0}^{T_{i}} L_{y_{i}}^{t} \Lambda_{i}^{t} \Lambda_{i} L_{y_{i}} d\tau - \int_{0}^{T_{i}} y_{i,\text{ref}} \Lambda_{i} L_{y_{i}} d\tau \\ &+ \underbrace{\frac{1}{2} \int_{0}^{T_{i}} y_{i,\text{ref}}^{2} d\tau}_{C_{i}} \\ &= \underbrace{\frac{1}{2} L_{y_{i}}^{t} \int_{0}^{T_{i}} \Lambda_{i}^{t} \Lambda_{i} d\tau}_{K_{i}} L_{y_{i}} - \underbrace{\int_{0}^{T_{i}} y_{i,\text{ref}} \Lambda_{i} d\tau}_{R_{i}} L_{y_{i}} + C_{i} \end{split}$$

$$\begin{array}{lll} \frac{\partial J}{\partial u} & = & \displaystyle\sum_{i=1}^{m} \left(\frac{1}{2} \frac{\partial L_{y_i}^t K_i L_{y_i}}{\partial u} - \frac{\partial R_i L_{y_i}}{\partial u} + \frac{\partial \mathcal{Q}_i^t}{\partial u}\right) \\ & = & \displaystyle\sum_{i=1}^{m} \left(\begin{bmatrix} L_{f_{b,1}} L_{f_a}^{(\rho-1)} y_i \\ \vdots \\ L_{f_{b,p}} L_{f_a}^{(\rho-1)} y_i \end{bmatrix} (K_i^s L_{y_i} - R_i^s) \right) \\ & = & \displaystyle\begin{bmatrix} L_{f_{b,1}} L_{f_a}^{(\rho-1)} y_1 & \dots & L_{f_{b,1}} L_{f_a}^{(\rho-1)} y_m \\ \vdots \\ L_{f_{b,p}} L_{f_a}^{(\rho-1)} y_1 & \dots & L_{f_{b,p}} L_{f_a}^{(\rho-1)} y_m \end{bmatrix} \\ & = & \displaystyle\begin{bmatrix} K_1^s L_{y_1} \\ \vdots \\ K_m^s L_{y_m} \end{bmatrix} - \begin{bmatrix} R_1^s \\ \vdots \\ R_m^s \end{bmatrix} \right) \\ & = & D \left(\begin{bmatrix} K_1^s L_{y_1} \\ \vdots \\ K_m^s L_{y_m} \end{bmatrix} - \begin{bmatrix} R_1^s \\ \vdots \\ R_m^s \end{bmatrix} \right) \\ & = & D \left(\begin{bmatrix} K_1^s L_{y_1} \\ \vdots \\ K_m^s L_{y_m} \end{bmatrix} - R^s = 0_{m \times 1} \right) \\ & = & K^{ss} D \left(\begin{bmatrix} u_1 \\ \vdots \\ u_p \end{bmatrix} + K^s \left(\begin{bmatrix} y_1 \\ \vdots \\ y_m \\ \vdots \\ L_{f_a}^{(\rho_n)} y_m \end{bmatrix} - R^s \right) \\ & = & K^{ss} Du + K^s L_y - R^s = 0 \Rightarrow \\ \Rightarrow & u = -(D^t D)^{-1} D^t (K^{ss})^{-1} (K^s L_y - R^s) \end{array}$$

with D the decoupling matrix,  $K^{ss}$  and  $K^{s}$  matrices derived from the gain matrices,  $K_1, \ldots, K_m, L_y$  the prediction output matrix and  $R^{s}$  the future output of reference matrix:

$$D = \begin{bmatrix} L_{f_{b,1}} L_{f_a}^{\rho_1 - 1} y_1 & \dots & L_{f_{b,p}} L_{f_a}^{\rho_1 - 1} y_1 \\ \vdots & \ddots & \vdots \\ L_{f_{b,1}} L_{f_a}^{\rho_m - 1} y_m & \dots & L_{f_{b,p}} L_{f_a}^{\rho_m - 1} y_m \end{bmatrix}$$
(6)

$$K^{s} = \begin{bmatrix} K_1^{s} & 0 \\ & \ddots & \\ 0 & K_m^{s} \end{bmatrix} \tag{7}$$

$$K^{ss} = \begin{bmatrix} K_1^{ss} & 0 \\ & \ddots \\ 0 & K_m^{ss} \end{bmatrix}$$
 (8)

with  $K_i^s$  the last line of the matrix  $K_i$  and  $K_i^{ss}$  the last element of the vector  $K_i^s$ .

 $K_i$  being defined as:

$$K_i = \int_0^{T_i} \Lambda_i^t \Lambda_i d\tau$$

which gives the following expression for each element of  $K_i$ :

$$K_{i,(a,b)} = \frac{T_i^{(a+b)+1}}{((a+b)+1)a!b!}$$

with  $a, b \in [0, \rho_i] \subset \mathbb{Z}$  the row and column indexes.

$$L_{y} = \begin{bmatrix} y_{1} \\ \vdots \\ L_{f_{a}}^{(\rho_{1})} y_{1} \\ \vdots \\ y_{m} \\ \vdots \\ L_{f_{-}}^{(\rho_{m})} y_{m} \end{bmatrix}$$

$$(9)$$

$$R^{s} = \begin{bmatrix} R_{1}^{s} \\ \vdots \\ R_{m}^{s} \end{bmatrix}$$
 (10)

 $R_i^s$  being the last element of the row vector  $R_i$ , where

$$R_i = \int_0^{T_i} y_{i,\text{ref}} \Lambda_i d\tau \tag{11}$$

#### 5) Finding u for the unicycle case:

A way of trying to find a vector  $\rho$  for our particular system is by computing  $L_{f_{b,j}}L_{f_a}^{(k)}y_i$  for k beginning at 0 and incrementing it until the conditions above are satisfied.

For  $\rho=[1\ 1\ 1]$ ,  $L_{f_{b,j}}L_{f_a}^{(0)}y_i=L_{f_{b,j}}y_i=0$  for all  $1\leq j\leq p$ , for all  $1\leq i\leq m$  which does not satisfy the second condition.

For computing  $L_{f_{b,j}}L_{f_a}^{(k)}y_i$  with  $\rho=[2\ 2\ 2]$  we need first  $L_fy_i$ :

(6) 
$$\begin{cases} L_f y_1 &= [1\ 0\ 0\ 0\ 0] f(q) = v \cos \psi \\ L_f y_2 &= [0\ 1\ 0\ 0\ 0] f(q) = v \sin \psi \\ L_f y_3 &= [0\ 0\ 1\ 0\ 0] f(q) = \omega \end{cases}$$

Computing now  $L_{f_{b,i}}L_fy_i$  we obtain:

#### REFERENCES

$$\begin{cases} L_{f_{b,1}} L_f y_1 &= [0 \ 0 \ -v \sin \psi \ \cos \psi \ 0 \ 0] g_1(q) = \cos \psi / \theta_1^{[1]} \\ L_{f_{b,1}} L_f y_2 &= [0 \ 0 \ v \cos \psi \ \sin \psi \ 0 \ 0] g_1(q) = \sin \psi / \theta_1 \\ L_{f_{b,1}} L_f y_3 &= [0 \ 0 \ 0 \ 0 \ 0 \ 1] g_1(q) = 0 \end{cases}$$

$$\begin{cases} L_{g_2}L_fy_1 &= [0\ 0\ -v\sin\psi\ \cos\psi\ 0\ 0]g_2(q) = 0\\ L_{g_2}L_fy_2 &= [0\ 0\ v\cos\psi\ \sin\psi\ 0\ 0]g_2(q) = 0\\ L_{g_2}L_fy_3 &= [0\ 0\ 0\ 0\ 1]g_2(q) = 1/\theta_2 \end{cases} \tag{14}$$

which gives the following decoupling matrix:

$$D = \begin{bmatrix} \frac{\cos \psi}{\theta_1} & 0\\ \frac{\sin \psi}{\theta_1} & 0\\ 0 & \frac{1}{\theta_2} \end{bmatrix}$$
 (15)

and consequently:

$$D^t D = \begin{bmatrix} \frac{1}{\theta_1^2} & 0\\ 0 & \frac{1}{\theta_2^2} \end{bmatrix} \tag{16}$$

which is non-singular for all  $\theta_1, \theta_2 \neq 0$ . Besides, the first condition is also met:  $L_{f_{b,j}}L_f^{(k_i)}y_i=0 \ \forall \ k_i<\rho_i-1$  . Using  $\rho=[2\ 2\ 2]$ , matrices  $K^s$ ,  $K^{ss}$  and  $L_y$  can be

written as bellow:

$$K^{s} = \begin{bmatrix} \frac{T_{1}^{3}}{6} & \frac{T_{1}^{4}}{8} & \frac{T_{1}^{5}}{20} & 0 & 0 & 0 & 0 & 0\\ 0 & 0 & 0 & \frac{T_{2}^{3}}{6} & \frac{T_{2}^{4}}{8} & \frac{T_{2}^{5}}{20} & 0 & 0 & 0\\ 0 & 0 & 0 & 0 & 0 & 0 & \frac{T_{3}^{3}}{6} & \frac{T_{3}^{4}}{8} & \frac{T_{3}^{5}}{20} \end{bmatrix}$$
(17)

$$K^{ss} = \begin{bmatrix} \frac{T_1^5}{20} & 0 & 0\\ 0 & \frac{T_2^5}{20} & 0\\ 0 & 0 & \frac{T_3^5}{20} \end{bmatrix}$$
 (18)

$$L_{y} = \begin{bmatrix} x \\ v \cos \psi \\ \left(\frac{\theta_{3}}{\theta_{1}}\omega^{2} - \frac{\theta_{4}}{\theta_{1}}v\right)\cos\psi - v\omega\sin\psi \\ y \\ v \sin\psi \\ \left(\frac{\theta_{3}}{\theta_{1}}\omega^{2} - \frac{\theta_{4}}{\theta_{1}}v\right)\sin\psi + v\omega\cos\psi \\ \psi \\ \omega \\ -\frac{\theta_{5}}{\theta_{2}}v\omega - \frac{\theta_{6}}{\theta_{2}}\omega \end{bmatrix}$$
(19)

 $R^s$  can be found (numerically or analytically) from the planner's output according with the folling expression:

$$R^{s} = \frac{1}{2} \begin{bmatrix} \int_{0}^{T_{1}} x_{\text{ref}}(t+\tau)\tau^{2}d\tau \\ \int_{0}^{T_{2}} y_{\text{ref}}(t+\tau)\tau^{2}d\tau \\ \int_{0}^{T_{3}} \psi_{\text{ref}}(t+\tau)\tau^{2}d\tau \end{bmatrix}$$
 (20)

 $\left\{ \begin{array}{ll} L_{fb,1}L_fy_1 &=& [0\ 0\ -v\sin\psi\ \cos\psi\ 0\ 0]g_1(q) = \cos\psi/\theta_1^{[1]} \ \text{J. M. Mendes Filho and E. Lucet, "Multi-robot motion planning:} \\ L_{fb,1}L_fy_2 &=& [0\ 0\ v\cos\psi\ \sin\psi\ 0\ 0]g_1(q) = \sin\psi/\theta_1 \\ L_{fb,1}L_fy_3 &=& [0\ 0\ 0\ 0\ 1]g_1(q) = 0 \end{array} \right. \right.$ cvut.cz/demur15/wp-content/uploads/2015/09/demur15-filho.pdf

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