PageRank Project Report

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We implement node-by-node and blocked PageRank algorithm, as well as Jacobi version Blocked PageRank and Random partition Blocked Pagerank

Filter Parameter:

netid: zx78

rejectMin: 0.87 * 0.99 = 0.8613

rejectLimit: 0.87 * 0.99 + 0.01 = 0.8713 number of edges selected : 7524770

We preprocessed the data (DataProcessor.java) from edges.txt and create a new file that used as input for MapReduce. The format of each line of the new file is:

< NodeID + PageRank + Degree + NeighborNodes >

All input file, output files and .jar is stored in bucket: edu-cornell-cs-cs5300s14-zx78-project2

Simple PageRank

In simplePageRank package, there are four java classes:

- 1) SimplePageRank
- 2) SimplePageRankMapper
- 3) SimplePageRankReducer
- 4) Counter

SimplePageRank

This class contains the main method. MapReduce job is configured with certain input/output format and input/output path.

In our implementation, we stored intermediate results in HDFS to improve efficiency since it's faster than read from/write to AWS S3.

SimplePageRankMapper

Since we use the default *TextInputFormat*, the key of the InputSplit is the offset of line, value is the content of the line. In our new created input file, each line correspond to a node.

We pass two kinds of information to reducer:

1. <srcNode, "prevNodeInfo" + PageRank + srcDegree > if srcDegree = 0

<srcNode, "prevNodeInfo" + PageRank + srcDegree + dstNodes>, otherwise
this is for the purpose of reconstructing the node.

2. <dstNode, srcPageRank/srcDegree> this is to compute new pagerank value for "dstNode".

SimplePageRankReducer

In reducer, it simply reconstruct the node and using the second type of information passed from mapper to compute new PageRank value for this node.

Then it increments the RESIDUAL_COUNTER in Counter class. The output of reducer in current iteration is the input for mapper in next iteration.

Counter

Since we use counter, in each pass, only one MapReduce job is required. There is only one field in Counter: RESIDUAL_COUNTER.

Every reducer increments RESIDUAL_COUNTER after computing residual error. After all reducer finishes working, we output the average residual error according to the counter value.

Result of Simple PageRank

run 6 iterations:

```
Iteration 0 Avg. residual error: 2.3385827422062664
Iteration 1 Avg. residual error: 0.3229186718255184
Iteration 2 Avg. residual error: 0.19205372241145308
Iteration 3 Avg. residual error: 0.09416565085445763
Iteration 4 Avg. residual error: 0.06287620062460779
Iteration 5 Avg. residual error: 0.03389726990207667
```

Blocked PageRank

It takes 7 passes to converge globally

There are four classes in this package, code structure is similar to simple PageRank:

- 1) BlockedPageRank
- 2) BlockedPageRankMapper
- 3) BlockedPageRankReducer
- 4) BlockCounter

BlockedPageRank

The class contains main method. Block boundaries are hard-coded for convenience.

MapReduce passes are implemented until global average residual error is lower than desired lower bound: 0.001. In the end of each termination, we output the average iteration within blocks and the average redisual error. After termination, output pageranks of highest numbered nodes in every blocks.

BlockedPageRankMapper

In mapper, we implement the *blockIDofNode* method and runs in constant time. Three types of information were passed to reducer:

- If srcDegree = 0:
 <srcBlock, "prevNodeInfo" + srcNode + pageRank + srcDegree>
 otherwise:
 <srcBlock, "prevNodeInfo" + srcNode + PageRank + srcDegree + dstNodes>
- 2. for edges within block, $\{ \langle u, v \rangle \mid u \in B \land u \rightarrow v \}$ $\langle dstBlock, "BE" + srcNode(u) + dstNode(v) \rangle$
- 3. for edges entering{ $< u, v, R > | u \notin B \land v \in B \land u \rightarrow v \land R = PR(u)/deg(u) }$ < dstBlock, "BC" + dstNode(v) + srcPR(u)/deg(u) >

BlockedPageRankReducer

We use several HashMaps to store node information and edges information. In IteratorBlockOnce, we first backup current pageranks and then recompute pageranks according to edges related and then compute average residual errors within the block.

The termination condition in reducer is while the nodes within the block are converged.

After termination, increase counter REDUCER_COUNTER by 1, INNER_ITERATION_COUNTER by # of iterations of IteratorBlockOnce, RESIDUAL_COUNTER by the total residual errors in the block and corresponding PAGERANK[blockID] by the pagerank of the highest numbered nodes in block.

BlockCounter:

RESIDUAL_COUNTER: sum of residual errors
REDUCER_COUNTER: # of reducers
INNER_ITERATION_COUNTER: sum of iterations within blocks

Avg iterations = INNER_ITERATION_COUNTER / REDUCER_COUNTER

PAGERANKO – PAGERANK67: store pagerank of highest numbered nodes in the corresponding block

Result of Blocked PageRank:

Avg. residual error: 2.8157218713967214, Avg. iteration: 17.485294 [pass 0] Avg. residual error: 0.03790001912624106, Avg. iteration: 7.161765 [pass 1] [pass 2] Avg. residual error: 0.023992188521758957, Avg. iteration: 5.867647 [pass 3] Avg. residual error: 0.009920314455334589, Avg. iteration: 3.897059 Avg. residual error: 0.00395191477851447, Avg. iteration: 2.558824 [pass 4] [pass 5] Avg. residual error: 0.0010555445699314391, Avg. iteration: 1.426471 [pass 6] Avg. residual error: 6.622697747534988E-4, Avg. iteration: 1.176471

sample pageranks:

[block 0] Max node: 10327 PageRank: 1.87285E-6 [block 1] Max node: 20372 PageRank: 5.2155E-7 Max node: 30628 [block 2] PageRank: 3.0675E-7 Max node: 40644 PageRank: 2.8092E-7 [block 3] [block 4] Max node: 50461 PageRank: 3.0002E-7 [block 5] Max node: 60840 PageRank: 2.189E-7 [block 6] Max node: 70590 PageRank: 3.0011E-7 Max node: 80117 PageRank: 2.189E-7 [block 7] Max node: 90496 PageRank: 8.664012E-4 [block 8] [block 9] Max node: 100500 PageRank: 2.5982E-7 [block 10] Max node: 110566 PageRank: 2.02975E-6 Max node: 120944 PageRank: 4.8272E-7 [block 11] [block 12] Max node: 130998 PageRank: 2.3553E-7 Max node: 140573 [block 13] PageRank: 6.2776E-7 Max node: 150952 [block 14] PageRank: 2.189E-7 PageRank: 2.189E-7 [block 15] Max node: 161331 Max node: 171153 [block 16] PageRank: 5.6226E-7 [block 17] Max node: 181513 PageRank: 3.4393E-7 [block 18] Max node: 191624 PageRank: 5.27754E-6 Max node: 202003 [block 19] PageRank: 4.14836E-6 [block 20] Max node: 212382 PageRank: 2.6175E-7 [block 21] Max node: 222761 PageRank: 0.0012286764 [block 22] Max node: 232592 PageRank: 1.2014965E-4 [block 23] Max node: 242877 PageRank: 5.6451E-7 [block 24] Max node: 252937 PageRank: 2.189E-7 [block 25] Max node: 263148 PageRank: 2.9941E-7 [block 26] Max node: 273209 PageRank: 2.189E-7 [block 27] Max node: 283472 PageRank: 3.658E-7 [block 28] Max node: 293254 PageRank: 2.6175E-7 [block 29] Max node: 303042 PageRank: 4.94703E-6

```
Max node: 313369
[block 30]
                               PageRank: 8.7558E-7
[block 31]
           Max node: 323521
                               PageRank: 2.189E-7
[block 32]
           Max node: 333882
                               PageRank: 5.1807E-7
[block 33]
           Max node: 343662
                               PageRank: 2.5204E-7
                               PageRank: 4.3791E-7
[block 34]
           Max node: 353644
[block 35]
           Max node: 363928
                               PageRank: 3.5619E-7
[block 36]
           Max node: 374235
                               PageRank: 3.26453E-6
[block 37]
           Max node: 384553
                               PageRank: 4.272E-7
[block 38]
           Max node: 394928
                               PageRank: 6.6669E-7
[block 39]
           Max node: 404711
                               PageRank: 2.4565E-7
[block 40]
           Max node: 414616
                               PageRank: 3.1166E-7
[block 41]
           Max node: 424746
                               PageRank: 2.02404E-6
[block 42]
           Max node: 434706
                               PageRank: 2.81297E-6
[block 43]
           Max node: 444488
                               PageRank: 3.82919E-6
[block 44]
           Max node: 454284
                               PageRank: 4.9751E-7
[block 45]
           Max node: 464397
                               PageRank: 1.105941E-5
[block 46]
           Max node: 474195
                               PageRank: 9.6575E-7
[block 47]
           Max node: 484049
                               PageRank: 5.9304E-7
                               PageRank: 2.189E-7
[block 48]
           Max node: 493967
[block 49]
           Max node: 503751
                               PageRank: 6.68699E-6
[block 50]
           Max node: 514130
                               PageRank: 6.1659E-7
[block 51]
           Max node: 524509
                               PageRank: 9.8640168E-4
           Max node: 534708
                               PageRank: 2.300763E-5
[block 52]
[block 53]
           Max node: 545087
                               PageRank: 0.00257605008
[block 54]
           Max node: 555466
                               PageRank: 0.00120386992
[block 55]
           Max node: 565845
                               PageRank: 1.64321E-6
[block 56]
           Max node: 576224
                               PageRank: 1.10812E-6
           Max node: 586603
                               PageRank: 9.565E-7
[block 57]
[block 58]
           Max node: 596584
                               PageRank: 4.10833E-6
[block 59]
           Max node: 606366
                               PageRank: 4.2766E-7
[block 60]
                               PageRank: 6.2093E-7
           Max node: 616147
[block 61]
           Max node: 626447
                               PageRank: 1.565152E-5
[block 62]
           Max node: 636239
                               PageRank: 1.02763E-6
[block 63]
           Max node: 646021
                               PageRank: 3.1193E-7
[block 64]
           Max node: 655803
                               PageRank: 2.189E-7
[block 65]
           Max node: 665665
                               PageRank: 9.9855E-7
[block 66]
           Max node: 675447
                               PageRank: 1.0857E-6
[block 67]
           Max node: 685229
                               PageRank: 3.5609E-7
```

Randomed Block Partition

We define hash(nodeID) = nodeID so that blockIDofNode(nodeID) = nodeID % NUM_OF_BLOCKS

It takes 22 passes to converge globally, much slower than intelligently partitioned blocks since in bad partition, most edges are between blocks and few edges are within blocks. The performance of randome block partition is basically differs little from node-by-node implementation.

Result:

```
[pass 0] Avg. residual error: 2.3392050529342736, Avg. iteration: 3.000000
         Avg. residual error: 0.322338531099608, Avg. iteration: 2.720588
[pass 1]
[pass 2] Avg. residual error: 0.19120350060835012, Avg. iteration: 2.000000
         Avg. residual error: 0.09352085277190784, Avg. iteration: 2.000000
[pass 3]
[pass 4] Avg. residual error: 0.062049689719819, Avg. iteration: 2.000000
[pass 5]
         Avg. residual error: 0.03343268009401611,
                                                     Avg. iteration: 2.000000
[pass 6] Avg. residual error: 0.026737168901070005, Avg. iteration: 2.000000
[pass 7]
         Avg. residual error: 0.016329769738696306,
                                                      Avg. iteration: 2.000000
[pass 8] Avg. residual error: 0.014039672567498987, Avg. iteration: 2.000000
[pass 9] Avg. residual error: 0.009590845800121406, Avg. iteration: 2.000000
[pass 10] Avg. residual error: 0.008232902427247786, Avg. iteration: 2.000000
[pass 11] Avg. residual error: 0.005990730327351765,
                                                       Avg. iteration: 2.000000
[pass 12]
          Avg. residual error: 0.0052024045009531105,
                                                        Avg. iteration: 2.000000
          Avg. residual error: 0.003905294158274054,
                                                       Avg. iteration: 2.000000
[pass 13]
[pass 14]
          Avg. residual error: 0.003378213739316799,
                                                       Avg. iteration: 2.000000
[pass 15]
          Avg. residual error: 0.002622637238369467,
                                                       Avg. iteration: 2.000000
          Avg. residual error: 0.0022454500814906527,
                                                        Avg. iteration: 2.000000
[pass 16]
[pass 17]
          Avg. residual error: 0.0017787145639380354,
                                                        Avg. iteration: 2.000000
[pass 18]
          Avg. residual error: 0.0015187079725565138,
                                                        Avg. iteration: 2.000000
          Avg. residual error: 0.0012179097482476395,
                                                        Avg. iteration: 2.000000
[pass 19]
[pass 20]
          Avg. residual error: 0.001034286744685084, Avg. iteration: 1.779412
[pass 21] Avg. residual error: 8.398437107079812E-4, Avg. iteration: 1.000000
```

Sample pageranks:

```
[block 0]
         Max node: 685168
                            PageRank: 3.49887E-6
[block 1]
         Max node: 685169
                            PageRank: 7.26665E-6
[block 2]
         Max node: 685170
                            PageRank: 7.36389E-6
[block 3]
         Max node: 685171
                            PageRank: 7.84502E-6
[block 4]
         Max node: 685172
                            PageRank: 3.5926E-7
[block 5]
         Max node: 685173
                            PageRank: 4.2094E-7
```

```
[block 6]
          Max node: 685174
                             PageRank: 6.71932E-6
```

- PageRank: 8.16817E-6 [block 7] Max node: 685175
- Max node: 685176 PageRank: 2.8461E-7 [block 8]
- [block 9] Max node: 685177 PageRank: 6.71489E-6
- [block 10] Max node: 685178 PageRank: 6.68529E-6
- [block 11] Max node: 685179 PageRank: 6.71046E-6
- [block 12] Max node: 685180 PageRank: 5.9564E-7
- [block 13] Max node: 685181 PageRank: 3.5831E-7
- [block 14] Max node: 685182 PageRank: 5.3393E-7
- [block 15] Max node: 685183 PageRank: 4.7868E-7
- [block 16] Max node: 685184 PageRank: 4.8401E-7
- [block 17] Max node: 685185 PageRank: 3.5831E-7
- [block 18] Max node: 685186 PageRank: 6.8677E-7
- [block 19] Max node: 685187 PageRank: 3.7121E-7
- Max node: 685188
- [block 20] PageRank: 4.8401E-7
- [block 21] Max node: 685189 PageRank: 4.7868E-7
- [block 22] Max node: 685190 PageRank: 4.224E-7
- [block 23] Max node: 685191 PageRank: 7.815E-7
- [block 24] Max node: 685192 PageRank: 4.8401E-7
- [block 25] Max node: 685193 PageRank: 4.8401E-7
- [block 26] Max node: 685194 PageRank: 3.5831E-7
- Max node: 685195 [block 27] PageRank: 4.7868E-7
- [block 28] Max node: 685196 PageRank: 4.5694E-7
- [block 29] Max node: 685197 PageRank: 3.2065E-7
- [block 30] Max node: 685198 PageRank: 4.8401E-7
- [block 31] Max node: 685199 PageRank: 1.45206E-6
- [block 32] Max node: 685200 PageRank: 4.6583E-7
- [block 33] Max node: 685201 PageRank: 4.6583E-7
- [block 34] Max node: 685202 PageRank: 6.5998E-7
- [block 35] Max node: 685203 PageRank: 4.2232E-7
- [block 36] Max node: 685204 PageRank: 4.8401E-7
- [block 37] Max node: 685205 PageRank: 3.5831E-7
- [block 38] Max node: 685206 PageRank: 3.7121E-7
- [block 39] Max node: 685207 PageRank: 6.8677E-7
- [block 40] Max node: 685208 PageRank: 4.8401E-7
- [block 41] Max node: 685209 PageRank: 4.8401E-7
- [block 42] Max node: 685210 PageRank: 4.8401E-7
- [block 43] Max node: 685211 PageRank: 3.5831E-7
- [block 44] Max node: 685212 PageRank: 1.79671E-6
- [block 45] Max node: 685213 PageRank: 1.79671E-6
- [block 46] Max node: 685214 PageRank: 1.79671E-6

```
[block 47] Max node: 685215 PageRank: 1.79671E-6
[block 48] Max node: 685216 PageRank: 1.79671E-6
[block 49] Max node: 685217
                             PageRank: 1.79671E-6
[block 50] Max node: 685218
                             PageRank: 4.7868E-7
[block 51] Max node: 685219
                             PageRank: 2.189E-7
[block 52] Max node: 685220
                             PageRank: 8.1196E-7
                             PageRank: 6.5998E-7
[block 53] Max node: 685221
[block 54] Max node: 685222
                             PageRank: 7.8008E-7
                             PageRank: 3.5831E-7
[block 55] Max node: 685223
[block 56] Max node: 685224
                             PageRank: 3.7482E-7
[block 57] Max node: 685225
                             PageRank: 4.2232E-7
[block 58] Max node: 685226
                             PageRank: 4.2232E-7
[block 59] Max node: 685227
                             PageRank: 1.9606E-6
[block 60] Max node: 685228
                             PageRank: 1.88119E-6
[block 61] Max node: 685229
                             PageRank: 3.5831E-7
[block 62] Max node: 685162
                             PageRank: 2.72815E-6
[block 63] Max node: 685163 PageRank: 2.72815E-6
[block 64] Max node: 685164
                             PageRank: 2.72372E-6
[block 65] Max node: 685165 PageRank: 2.69502E-6
[block 66] Max node: 685166
                             PageRank: 2.71929E-6
[block 67] Max node: 685167
                             PageRank: 2.72815E-6
```

Gauss-Seidel

The implementation is silimar to that of Blocked PageRank, only with a little difference in the reducer.

The following equation defines the PageRank value using Gauss-Seidel method:

$$PR(i)^{(k+1)} = (1-\alpha)/NUM_OF_NODES + \alpha \left(\sum_{i < j} PR(j)^k/deg(j) + \sum_{i > j} PR(j)^{(k+1)}/deg(j)\right)$$
 < j , $i > \in \mathbf{E}$

The number of passes using Gauss-Seidel method is the same as Jacobi method, however, the average number of iterations in reducer is smaller than Jacobi.

Result:

```
[pass 0] Avg. residual error: 2.816151834165567, Avg. iteration: 10.088235 [pass 1] Avg. residual error: 0.038937140946554455, Avg. iteration: 5.102941 [pass 2] Avg. residual error: 0.02530163499966147, Avg. iteration: 4.367647
```

- [pass 3] Avg. residual error: 0.01116037507638657, Avg. iteration: 3.220588
- [pass 4] Avg. residual error: 0.005083253142829371, Avg. iteration: 2.367647
- $[pass \, 5] \quad \text{Avg. residual error: } 0.0019187138620793164, \quad \text{Avg. iteration: } 1.661765$
- [pass 6] Avg. residual error: 8.445789655928958E-4, Avg. iteration: 1.308824

Sample PageRanks:

- [block 0] Max node: 10327 PageRank: 1.87275E-6
- [block 1] Max node: 20372 PageRank: 5.2159E-7
- [block 2] Max node: 30628 PageRank: 3.062E-7
- [block 3] Max node: 40644 PageRank: 2.8092E-7
- [block 4] Max node: 50461 PageRank: 2.9947E-7
- [block 5] Max node: 60840 PageRank: 2.189E-7
- [block 6] Max node: 70590 PageRank: 3.0011E-7
- [block 7] Max node: 80117 PageRank: 2.189E-7
- [block 8] Max node: 90496 PageRank: 8.6470304E-4
- [block 9] Max node: 100500 PageRank: 2.5989E-7
- [block 10] Max node: 110566 PageRank: 2.03005E-6
- [block 11] Max node: 120944 PageRank: 4.7697E-7
- [block 12] Max node: 130998 PageRank: 2.3454E-7
- [block 13] Max node: 140573 PageRank: 6.3159E-7
- [block 14] Max node: 150952 PageRank: 2.189E-7
- [block 15] Max node: 161331 PageRank: 2.189E-7
- [block 16] Max node: 171153 PageRank: 5.6224E-7
- [block 17] Max node: 181513 PageRank: 3.4387E-7
- [block 18] Max node: 191624 PageRank: 5.27752E-6
- [block 19] Max node: 202003 PageRank: 4.14219E-6
- [block 20] Max node: 212382 PageRank: 2.6175E-7
- [block 21] Max node: 222761 PageRank: 0.00120921152
- [block 22] Max node: 232592 PageRank: 1.0427226E-4
- [block 23] Max node: 242877 PageRank: 5.6716E-7
- [block 24] Max node: 252937 PageRank: 2.189E-7
- [block 25] Max node: 263148 PageRank: 2.9941E-7
- [block 26] Max node: 273209 PageRank: 2.189E-7
- [block 27] Max node: 283472 PageRank: 3.657E-7
- [block 28] Max node: 293254 PageRank: 2.6175E-7
- [block 29] Max node: 303042 PageRank: 4.94705E-6
- [block 30] Max node: 313369 PageRank: 8.9347E-7
- [block 31] Max node: 323521 PageRank: 2.189E-7
- [block 32] Max node: 333882 PageRank: 5.1807E-7
- [block 33] Max node: 343662 PageRank: 2.5204E-7
- [block 34] Max node: 353644 PageRank: 4.5195E-7

- [block 35] Max node: 363928 PageRank: 3.564E-7
- [block 36] Max node: 374235 PageRank: 3.76355E-6
- [block 37] Max node: 384553 PageRank: 4.2771E-7
- [block 38] Max node: 394928 PageRank: 6.6675E-7
- [block 39] Max node: 404711 PageRank: 2.4567E-7
- [block 40] Max node: 414616 PageRank: 3.1167E-7
- [block 41] Max node: 424746 PageRank: 2.1234E-6
- [block 42] Max node: 434706 PageRank: 2.81472E-6
- [block 43] Max node: 444488 PageRank: 3.80724E-6
- [block 44] Max node: 454284 PageRank: 4.9751E-7
- [block 45] Max node: 464397 PageRank: 1.117764E-5
- [block 46] Max node: 474195 PageRank: 9.659E-7
- [block 47] Max node: 484049 PageRank: 5.9322E-7
- [block 48] Max node: 493967 PageRank: 2.189E-7
- [block 49] Max node: 503751 PageRank: 6.7826E-6
- [block 50] Max node: 514130 PageRank: 6.1659E-7
- [block 51] Max node: 524509 PageRank: 9.8739784E-4
- [block 52] Max node: 534708 PageRank: 2.281982E-5
- [block 53] Max node: 545087 PageRank: 0.00258417872
- [block 54] Max node: 555466 PageRank: 0.00120476768
- [block 55] Max node: 565845 PageRank: 1.64295E-6
- [block 56] Max node: 576224 PageRank: 1.10794E-6
- [block 57] Max node: 586603 PageRank: 9.5652E-7
- [block 58] Max node: 596584 PageRank: 4.07348E-6
- [block 59] Max node: 606366 PageRank: 4.2702E-7
- [block 60] Max node: 616147 PageRank: 6.2176E-7
- [block 61] Max node: 626447 PageRank: 1.716388E-5
- [block 62] Max node: 636239 PageRank: 1.02692E-6
- [block 63] Max node: 646021 PageRank: 3.1193E-7
- [block 64] Max node: 655803 PageRank: 2.189E-7
- [block 65] Max node: 665665 PageRank: 9.9978E-7
- [block 66] Max node: 675447 PageRank: 1.08566E-6
- [block 67] Max node: 685229 PageRank: 3.568E-7