2.13 Mutual Information ± (X1, X2) (3 point) I(X1) = H(X1) + H(X2) - H(X1) X2) where His entropy of 9 Hence as per given values for entropies in book = 1 log [211 e62] + 1 log [211 e62] -1 log [(21) e) (64-64 p2)] = log\_[21Te62] - 1 log[(2Te]2 64(1-p2)] power and = log 217e62 (+p2)1/2 using log & = loga = 10g (1-p2)1/2 If P= +1 or-1(x, x2 highely coone lated) then I (x, x2)= 00 justifies this i.e XIX2 are statisfically not correlated at out then I(x, x2) = log 1=0 justifies this.

MLE For the poisson distribution 3.6 Poisson Pmfi Poi (XIA) -  $e^{i}$   $\lambda^{x}$  [Note the support in 0,1,2. in all natural number]

Hence Let  $D = \{(x_i)\}_{i=1}^{N}$  be our  $\Lambda$  observations from this ( Points 4) distribution log liklihood of Dis = log P(D) = log II. Poi (xil) = > log Poi (xil) = E by e xi = \frac{N}{2} (-1) + \frac{N}{2} \times \log \lambda \cdot \frac{N}{2} \log \log \left( \cdot \c Taking derivative with respect to 1 and equaling to zero -N + \( \frac{1}{2} \times \) P(XID) & P(DIA) P(X) d (it Poi(x1/1)) Gra(1/4/b) (using Griven conjugate
prior Gra(1/4/b) for 1 (2 points 2 (1 E 1 (1 E 16) each  $\frac{x_{i}}{x_{i}} = \frac{x_{i}}{e}$ (a,b/--) = Ga (1 | a + Exi, b+N)  $E[\lambda ID] = \underbrace{af \sum_{i=1}^{\infty} x_i}_{L \subseteq IV}$ it tends to MLE estimate in on 1

3.11 confg For ENCE 4630)

3.11 confg For 109 likelihood proceed as in previous problem © it should be L(0) = NWO - 0 \( \infty \) \( \int \) \( \int \) For MLE estimete of 0, take derivative and equate to 3000  $\frac{\partial L(0)}{\partial \theta} = \frac{V}{\theta} - \frac{2}{5}xi \Rightarrow \hat{\theta} = \frac{2}{5}xi$  $\hat{G}_{MLE}(D) = \hat{\Theta}_{MLE}(\{x_1 = 5, x_2 = 6, x_3 = 4\})$  (:  $D = \{5, 6, 4\}$ )  $=\frac{3}{5+6+4}=\frac{3}{15}=\frac{1}{5}$  $|E(0)| = \sqrt{1 - \frac{1}{3}} \Rightarrow \hat{\lambda} = 3 \quad (|P(0)| = \frac{1}{3} = \frac{1}{3} = \frac{1}{3} \Rightarrow \hat{\lambda} = 3 \quad (|P(0)| = \frac{1}{3} = \frac{1}{3} = \frac{1}{3} \Rightarrow \hat{\lambda} = \frac{1}{3} = \frac{1}{3} \Rightarrow \hat{\lambda} = \frac{1}{3} \Rightarrow \hat{$ (d) Posterier P(OID, 21 & P(D10) P(OIS) is a special case of summa d 0 € 0 € 0 € 3 € 203-180 2 9-1-180 20-1-180 20-1-180 (-67/0/9,6) 20 EB (e) yes, exponential is a special case (f) posterier P(010,1) is Gra(014,18)

Hence mean = 4/18

(3) Posterior mean (4/8) is a probabilishe adjustement
between poier mean (3, expert choice) and deta
doven mean (MLE=1/5). In small smaple size we should
take expert advice "Hence posterior"

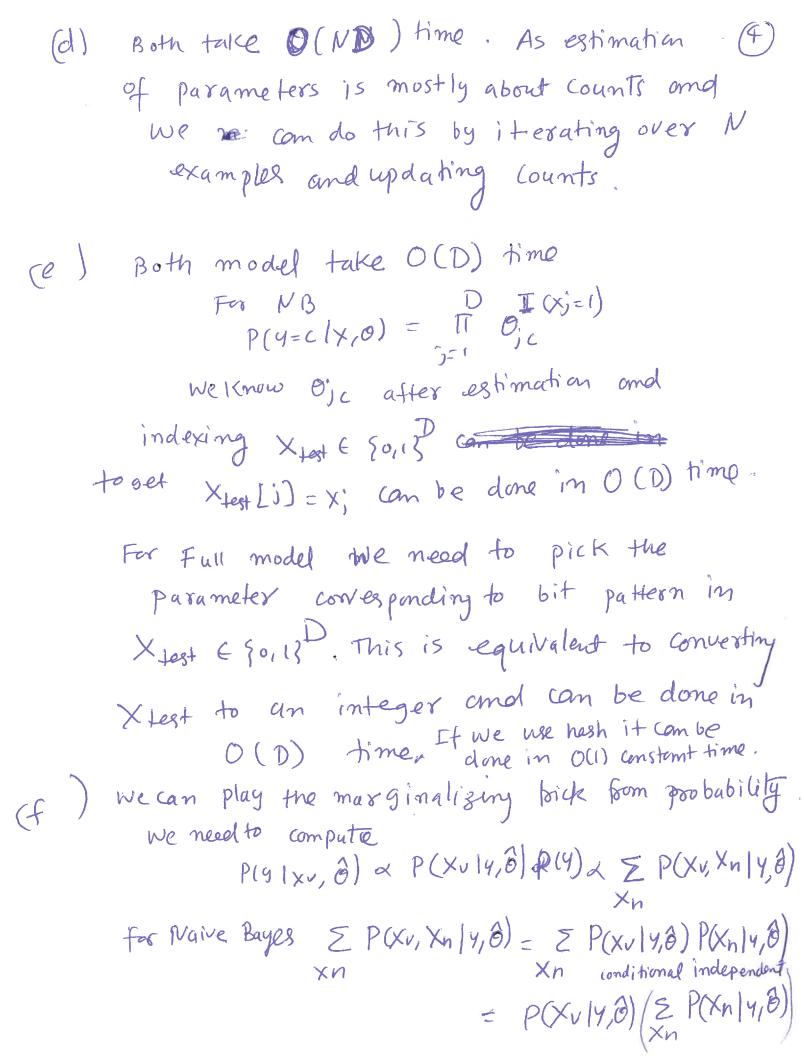
3.20 (point each)

(4) since feature are not conditionally indepent we need to specify probability for each configuration of bit in XE {011} Hence we need 2P-1 parameters | class or c (2P-1) parameter for classes

we would need a different probability distribution P'(X|C) or Histogram. [One ctroip can be

Lino mial (K; D, 0)? [ Liprobability of K success in D toial of coin with parameter 0] Note: We cannot use multivariate Granssian as data is bimary vector.

- (b) Maive Bages based model will work better as it has less number of parameters. With less sample size it will not overfit and parameters estimation will be more reliable.
- as it is more accurate and there is smough data to reliably restimate parameters.



Hence it takes  $O(D2^h)$  model we need O(x) time

For Full model we need to enquerate over

all  $2^h$  values of  $x_h \in x_0$ ,  $x_h$ Hence it takes  $O(D2^h)$  m  $O(x_h)$ computational time