

1.a - conditional independence given class

1.b - discriminative

1.c - 25%

1.d -

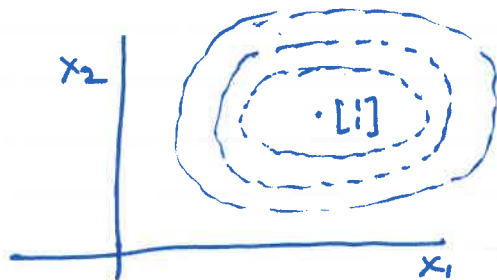
$$P(A|B) = \frac{P(A,B)}{\sum_{a \in A} P(A,B)} \quad \begin{array}{l} 1e - 1 \\ 1f - True \end{array}$$

$$1.g \quad P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

$$= \frac{0.07 \times 0.10}{0.05} = 0.07 \times 2 = 0.14$$

2.a  $\mu_{dx1}, \Sigma_{dxd}$

2.b



ellipses  
aligned along  
 $x_1$  (major axis)  
and  $x_2$  (minor axis)

2.c (COMP 3432)

$$\sum_{i=1}^D \frac{(x_i - \mu_i)^2}{\sigma_i^2}$$

2.c (COMP 4432)

2.B Gaussian density is

$$\frac{1}{(2\pi)^{1/2} |\Sigma_c|^{1/2}} \exp\left(-\frac{1}{2} \begin{bmatrix} x_1 - \mu_1 \\ x_2 - \mu_2 \end{bmatrix}^T \begin{bmatrix} \sigma_1^2 & 0 \\ 0 & \sigma_2^2 \end{bmatrix}^{-1} \begin{bmatrix} x_1 - \mu_1 \\ x_2 - \mu_2 \end{bmatrix}\right)$$

$$= \frac{1}{(2\pi)} (\sigma_1^2 \sigma_2^2)^{1/2} \exp\left[-\frac{1}{2} \left(\frac{(x_1 - \mu_1)^2}{\sigma_1^2} + \frac{(x_2 - \mu_2)^2}{\sigma_2^2}\right)\right]$$

$$= \frac{1}{(2\pi)^{1/2} \sigma_1} \exp\left(-\frac{1}{2} \frac{(x_1 - \mu_1)^2}{\sigma_1^2}\right) \frac{1}{(2\pi)^{1/2} \sigma_2} \exp\left(-\frac{1}{2} \frac{(x_2 - \mu_2)^2}{\sigma_2^2}\right)$$

$$= N(x_1; \mu_1, \sigma_1^2) N(x_2; \mu_2, \sigma_2^2)$$

(3) log likelihood, Find  $b$  s.t  $P(D)$  is maximum  
 or  $\log P(D) = \sum_{i=1}^N \log \frac{1}{2b} \exp\left(-\frac{|x_i|}{b}\right)$

$$= \sum_{i=1}^N \log \frac{1}{2b} - \sum_{i=1}^N \frac{|x_i|}{b}$$

$\uparrow$   
 $(F: i: d)$   
 condition

$$= - \sum_{i=1}^N \log 2b - \sum_{i=1}^N \frac{|x_i|}{b}$$

or minimize

$$F(b) = \sum_{i=1}^N \log 2b + \sum_{i=1}^N \frac{|x_i|}{b}$$

$$\frac{\partial F(b)}{\partial b} = \sum_{i=1}^N \frac{1}{b} - \sum_{i=1}^N \frac{|x_i|}{b^2}$$

$$\frac{1}{b} \left[ N - \sum_{i=1}^N \frac{|x_i|}{b} \right] = 0$$

$$b = \frac{\sum_{i=1}^N |x_i|}{N}$$

(4) -  $L_1$  - regularization

- $L_1$  solution is sparse (most of the coefficient are zero)
- bigger  $\lambda$  - more and more coefficient will become zero

. This will allow us to do feature selection when we have lots of features

(5) As per given Hint  
Decision boundary is all the  $x$   
s.t

$$P(y=1|x) = P(y=0|x)$$

$$\Leftrightarrow \sigma(w^T x) = 1 - \sigma(w^T x)$$

$$\Leftrightarrow \frac{1}{1 + e^{-w^T x}} = \frac{e^{-w^T x}}{1 + e^{-w^T x}}$$

$$\Leftrightarrow 1 = e^{-w^T x}$$

$$\Leftrightarrow \log 1 = \log e^{-w^T x} \quad (\because \text{taking log on both side})$$

$$\Leftrightarrow 0 = -w^T x$$

$\Leftrightarrow w^T x = 0$  which is a  
equation of line in  $D$

dimension passing through origin