

## Quiz 1

MACHINE LEARNING, SUMMER 2018

Name:

UID:

1. (2 point) If  $X$  and  $Y$  are conditionally independent given  $Z$ , then  $P(X, Y|Z) =$ .

$$P(X, Y|Z) = P(X|Z) P(Y|Z)$$

2 (point 2 = 1+1) What is the support of Beta distribution. What is the support of Dirichlet distribution in dimension  $D$ .

Support of Beta  $[0, 1]$   
Support of Dirichlet  $[0, 1]^D$

3 (2 point = 1+1) What is the difference between supervised and unsupervised machine learning.

— In supervised learning we have label  $y_i$  in training data  $D = \{(x_i, y_i)\}_{i=1}^N$ . This label is used in training phase to train algorithm.  
— In unsupervised we don't have  $y_i$  and need to find interesting pattern in data  $D = \{x_i\}$

4a. (3 points = 1+1+1) What is the difference between MLE and MAP estimate of parameters of a distribution. If you don't have many sample from distribution which estimate you will use.

— In MLE we find the parameters of the distribution in such a way that likelihood of event happened is maximum.  
— In MAP estimate we choose the mode from posterior distribution of the parameters.  
— choose MAP, following expert advice for prior.

4b. (points 3 = 1+1+1) Given  $\mathcal{D}$  data we observed and  $\theta$  is distribution of parameters. Draw arrow to show prior, likelihood and posterior terms in the following expression.

$$P(\theta|\mathcal{D}) = \frac{P(\mathcal{D}|\theta)P(\theta)}{P(\mathcal{D})}$$

likelihood  $\uparrow$  prior  $\rightarrow$   
posterior  $\rightarrow$