

E. Rectangle Land

PROBLEM DESCRIPTION

Given a list of rectangles, calculate the total area covered by these rectangles.

SOLUTION TECHNIQUES

Sweeping Lines / Discrete Segment Tree

SOLUTION SKETCHES

This is a somewhat known application with Sweeping Lines algorithm.

The top-level idea is that we use the x axis as our time frame and use a data structure (Segment Tree in this case) on the y axis to maintain the area and number of layers covered.

Each rectangle is represented by 2 individual events.

Suppose the rectangle is denoted by $(x1, y1)$ and $(x2, y2)$,

1. Starting from $x1$, $[y1, y2]$ is covered with 1 additional layer.
2. Ending in $x2$, $[y1, y2]$ is covered with 1 less layer.

We increase x incrementally (ie. Sweep from left to right) and sum up the areas.

TIME COMPLEXITY

$O(N \log N)$

SOLUTION PROGRAM FOR REFERENCE

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1. #include <cstdio>
2. #include <cstring>
3. #include <algorithm>
4. #include <vector>
5. #include <map>
6. #include <queue>
7.
8. using namespace std;
9. typedef long long ll;
10.
11. const int N = 1e6 + 5;
12. const int X = 2e6 + 5;
13. const int S = 1e6;
14.
15. vector<int> x, y;
16. int lx[X], ly[X];
17.
18. struct node
19. {
20.     int mx, mxs, cov;
21. } s[N << 3];
22.
23. struct event
24. {
25.     int x;
26.     int y1, y2;
27.     int u; // 1 for add, 0 for subtract
28.     bool operator < (const event &rhs) const
29.     {
30.         if (x != rhs.x)
31.             return x < rhs.x;
32.         else
33.             return u > rhs.u;
34.     }
35. };
36. vector<event> a, m;
37.
38. void build(int i, int l, int r)
39. {
40.     s[i].mx = s[i].cov = 0;
41.     s[i].mxs = y[r] - y[l]; // change
42.     if (r - l == 1) return ;
43.     int m = (l + r) >> 1;
44.     build(i << 1, l, m);
45.     build(i << 1 | 1, m, r);
46. }
47.
48. int upd(int i, int l, int r, int ql, int qr, int u)
49. {
50.     if (qr <= l || ql >= r) return s[i].mx + s[i].cov;
51.     if (ql <= l && r <= qr)
52.     {
53.         s[i].cov += u;
54.         return s[i].mx + s[i].cov;
55.     }
56.     int m = (l + r) >> 1;
57.     s[i].mx = max(upd(i << 1, l, m, ql, qr, u), upd(i << 1 | 1, m, r, ql, qr, u));
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58.     s[i].mxs = s[i << 1].mx + s[i << 1].cov == s[i].mx ? s[i << 1].mxs : 0;
59.     s[i].mxs += s[i<<1|1].mx + s[i<<1|1].cov == s[i].mx ? s[i<<1|1].mxs : 0;
60.     return s[i].mx + s[i].cov;
61. }
62.
63. int main()
64. {
65.     int i, tt, n, x1, y1, x2, y2, c;
66.     int xx, ai, mi;
67.     ll ans, anss;
68.     scanf("%d", &tt);
69.     while (tt--)
70.     {
71.         scanf("%d", &n);
72.         x.clear(); x.reserve(n << 1);
73.         y.clear(); y.reserve(n << 1);
74.         a.clear(); a.reserve(n << 1);
75.         m.clear(); m.reserve(n << 1);
76.         ai = mi = 0;
77.         ans = 0;
78.         for (i = 0; i < n; i++)
79.         {
80.             scanf("%d%d%d%d", &x1, &y1, &x2, &y2, &c);
81.             x.push_back(x1); x.push_back(x2);
82.             y.push_back(y1); y.push_back(y2);
83.             if (x1 > x2) swap(x1, x2);
84.             if (y1 > y2) swap(y1, y2);
85.             a.push_back( (event){x1, y1, y2, c} );
86.             m.push_back( (event){x2, y1, y2, -c} );
87.         }
88.         sort(x.begin(), x.end());
89.         sort(y.begin(), y.end());
90.         unique(x.begin(), x.end());
91.         unique(y.begin(), y.end());
92.         for (i = 0; i < x.size(); i++)
93.             lx[x[i] + S] = i;
94.         for (i = 0; i < y.size(); i++)
95.             ly[y[i] + S] = i;
96.         sort(a.begin(), a.end());
97.         sort(m.begin(), m.end());
98.         build(1, 0, y.size() - 1);
99.         for (xx = 1; xx < x.size(); xx++)
100.        {
101.            while (ai < a.size() && lx[a[ai].x + S] < xx)
102.            {
103.                upd(1, 0, y.size() - 1, ly[a[ai].y1 + S], ly[a[ai].y2 + S], a[ai
104.                ].u);
105.                ai++;
106.            }
107.            while (mi < m.size() && lx[m[mi].x + S] < xx)
108.            {
109.                upd(1, 0, y.size() - 1, ly[m[mi].y1 + S], ly[m[mi].y2 + S], m[mi
110.                ].u);
111.                mi++;
112.            }
113.            if (s[1].mx + s[1].cov > ans)
114.            {
115.                ans = s[1].mx + s[1].cov;
116.                anss = (ll)s[1].mxs * (x[xx] - x[xx - 1]);
117.            }
118.            else if (s[1].mx + s[1].cov == ans)

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117.             anss += (ll)s[1].mxs * (x[xx] - x[xx - 1]);
118.         }
119.         printf("%lld %lld\n", ans, anss);
120.     }
121.     return 0;
122. }
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