# Changing Times Call for Changing Stats

Danny Kaplan

USCOTS "Ignite" Session May 15, 2013

# A Physicist Lapsed into Statistics

Rutherford (1871-1937)



#### DTK

- I studied physics, philosophy, and political science in college.
- I never took a statistics course.

#### Lord Rutherford

"If your experiment needs statistics, you ought to have done a better experiment."

# Biomedical Engineering and Physiology

#### My Ph.D. work

Getting physiological information from signals

ECG, EEG, Respiration and heart rate variability



- Signal processing
- Classification and Bayes' Rule, not hypothesis testing
- Sensitivity and specificity, not Type I and Type II



#### But You Need a CI to Publish

#### Sources for scientists:

- Numerical Recipes
- Brad Efron's SIAM

SIAM REVIEW Vol. 21, No. 4, October 1979 © 1979 Society for Industrial and Applied Mathematics 0036-1445/79/2104-0002501.00/0

#### COMPUTERS AND THE THEORY OF STATISTICS: THINKING THE UNTHINKABLE\*

BRADLEY EFRONT

Abstract. This is a survey article concerning recent advances in certain areas of statistical theory, written for a mathematical audience with no background in statistics. The topics are chosen to illustrate a special point: how the advent of the high-speed computer has affected the development of statistical theory. The topics discussed include nonparametric methods, the jackknife, the bootstrap, cross-validation, error-rate estimation in discriminant analysis, robust estimation, the influence function, censored data, the EM algorithm, and Cox's likelihood function. The exposition is mainly by example, with only a little offered in the way of theoretical development.

1. Introduction. The editors have been kind enough to invite a survey article concerning what's new in the theory of statistics. Any answer to this question must be either incomplete or bewildering to the reader. Here I have tried to be incomplete, selecting my topics to illustrate a special point: how the advent of the high-speed computer has affected the theoretical structure of statistics.

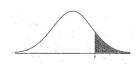


#### "Yes" is the Correct Answer



"Can you teach intro stats?"

Thank goodness I wasn't asked, "What's a t-test?"



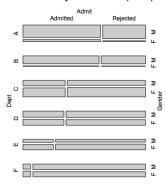
Tail probability p												
ďf	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0003
1	1.000	1,376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.3	318.3	636.6
2	.816	1.061	1.386	1.386	2.920	4.303	4,849	6.965	9.925	14.09	22.33	31.60
3	.765	.978	1.250	1.638	2.353	3,182	3,482	4.541	5.841	7,453	10.21	12.93
4	.741	.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610
5	.727	.920	1.156	1,476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6,869
6	.718	.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959
7	.711	.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5,408
8	.706	.889	1,108	1.397	1.860	2.306	2,449	2.896	3.355	3.833	4.501	5:041
9	.703	.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4,781
10	.700	.879	1.093	1.372	1.812	2,228	2.359	2.764	3.169	3.581	4.144	4.587
11	.697	.876	1.088	1.363	1.796	2,201	2.328	2.718	3.106	3,497	4,025	4.431
12	.695	.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	.694	.870	1.079	1.350	1.771	2.160	2.282	2.650	3.012	3.372	3.852	4,221
14	.692	.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	- 4.140
15	.691	.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.073
16	.690	.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252-	3.686	4.015
17	.689	.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	.688	.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	.688	.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	.687	.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3,552	3.850
21	.686	.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831.	3.135	3.527	3.819
22	.686	.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
23	.685	.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
24	685	.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745
25	.684	.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3,450	3.725
26	.684	.856	1.058	1.315	1.706	2.056	2.162	2,479	2.779	3.067	3.435	3.707
27	.684	.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
28	.683	.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674
29	.683	.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3,659
30	.683	.854	1.055	1.310	1.697	2.042	2.147	2:457	2.750	3.030	3.385	3.646
40	.681	.351	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551
50	.679	.849	1.047	1.299	1.676	2.009	2.109	2,403	2.678	2.937	3.261	3,496
60	.679	.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.460
80	.678	.346	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
100	.677	.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
000	.675	.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3,300
**	.674	.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%

### Resampling Seemed the Natural Way to Teach and Learn

I worked to make resampling easier and more accessible:

### Simpson's Paradox and Philosophy

#### UC Berkeley Admissions (1973)



More selective departments are female-heavy.

I thought students should know something about inductive reasoning and its traps.

Simpson's Paradox seemed a good angle to give students an appropriate level of skepticism about induction.

### The Wrong Lesson

#### What I was saying ...

Data don't speak, they inform our judgment.

Interpret data in the context of a whole system

#### What they were hearing ...

The data will say anything you want, depending on how you cut it.

### Avoiding the Abstinence-Based Curriculum

Causation is often the issue. But

- Confounding is common
- Adjustment provides insight if not proof
- It's very common in the literature

I don't want students to be powerless about covariation and causation.

But how to do this?



"Never, ever, think outside the box."

Never, ever, think outside the box.



### Statistics and Geometry

#### My epiphany

The links between modeling and geometry of subspaces.

#### Case Space versus Variable Space

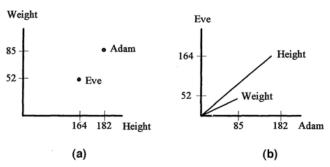
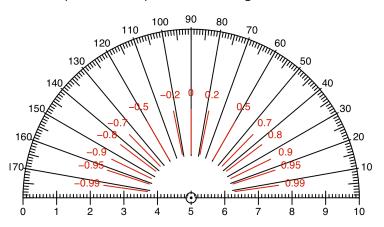


Figure 1. Two Geometrical Presentations of the Data in Table 1: (a) Variable-Axes and (b) Observation-Axes.



#### Correlation is an Angle

Statistics formulas (e.g. correlation) are based on linear algebra but fail to present the operations at a high level.



### When it's hard, We're doing the wrong thing

The purpose of expertise should be to find ways to make it obvious.

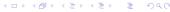
A difficult theoretical question ...

Where does the t-distribution come from?

The back of the book!



7-year old eyeballs the p-value



### Things Have Changed

In the 16 years since my job interview...

- Every student has access to a computer, in class and out.
- Software is free.
- Data is everywhere.
- People want to use data for decision-making, not just for publishing research.

### We Should Change, Too

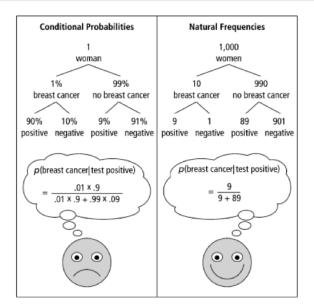
- Prepare students for technical computing.
- Mathematics should be about multiple variables.
- Make modeling central.

#### Statistics as the Science of Data

Insofar as we believe this, we should be helping students gain:

- The ability to access data.
- The ability to organize data.

## Basic Concepts for Decision Making



### Change at Macalester

- Redirecting Calculus to support statistics.
- Redirecting Statistics to support science.
- Redirecting Computation to support data.
- Teaching Quantitative Literacy in context: Epidemiology

## Collaborative and Community Change

- Colleagues at Macalester
- The R Project
- Randy Pruim & Nick Horton and Project MOSAIC
- JJ Allaire and RStudio







## The Golden Age of Statistics

**Now** is the golden age of statistics and scientific education.

- The demand is there.
- The technology is there.
- What's missing is the human capital.

We need a new organization of educational work

- More collaboration
- More ongoing training

#### Statistics with Confidence

Statistics is the quantitative/scientific/technical area that most strongly unites areas of research.

 This increases our responsibility to look after education generally.