

# Quiz: Heavy Hitters

Practice Quiz, 5 questions

**4/5 points (80.00%)**

## Congratulations! You passed!

[Next Item](#)1 / 1  
point

1.

What is the set of top 2 most frequent items in the following stream?

1 2 5 3 1 1 2 4 4 3 3 3



1 3

**Correct**

That's right!



1 2



4 5

1 / 1  
point

2.

Suppose that we would like to use Chebyshev's inequality to bound  $\text{Prob}[|X| \geq 3]$ , where  $X$  is a normally distributed random variable with unit variance. Chebyshev's inequality gives

Chebyshev's inequality does not apply to this setting

 $\text{Prob}[|X| \geq 3] \leq 1/9$ **Correct**

That's right!

 $\text{Prob}[|X| \geq 3] \leq 1/3$

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3.

Suppose that we would like to use Chebyshev's inequality to bound  $\text{Prob}[|X| \geq 3]$ , where  $X$  is a random variable with the Cauchy distribution, i.e. the p.d.f. of  $X$  is  $\frac{1}{\pi(1+x^2)}$ . Chebyshev's inequality gives

- ☐  $\text{Prob}[|X| \geq 3] \leq 1/9$
- ☒ Chebyshev's inequality does not apply to this setting

**Correct**

Exactly! Chebyshev's inequality does not apply to this setting, as  $X$  does not have a finite variance.

- ☐  $\text{Prob}[|X| \geq 3] \leq 1/3$

1 / 1  
point

4.

Suppose that the stream contains items 1 with frequency  $N^\alpha$  for a constant  $\alpha < 1/2$ , and all other elements appear in the stream exactly once. How much space suffices for CountSketch to find the most frequent element in this stream?

- ☐  $O(n^\alpha \log n)$
- ☒  $O(n^{1-2\alpha} \log n)$

**Correct**

That's right! This is because  $\sum_{i \in \text{TAIL}} f_i^2 \leq N$ , and  $f_1^2 = n^{2\alpha}$ . So  $b = O(n^{1-2\alpha})$  suffices.

- ☐  $O(n^{1-4\alpha^2} \log n)$

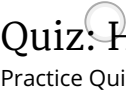
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point

5.

Suppose that we would like to use Markov's inequality to bound  $\text{Prob}[X \geq 3]$ , where  $X$  is a normally distributed random variable with unit variance. Markov's inequality gives

- ☐  $\text{Prob}[X \geq 3] \leq 1/9$
- ☒  $\text{Prob}[X \geq 3] \leq 1/3$

**This should not be selected**



Markov's inequality does not apply to this setting

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