

CSE 1325: Object-Oriented Programming

Lecture 21 / Chapters 20-21

Standard Template Library (STL)

Containers and Iterators

Mr. George F. Rice

george.rice@uta.edu

Based on material by Bjarne Stroustrup

www.stroustrup.com/Programming

ERB 402

Office Hours:

Tuesday Thursday 11 - 12

Or by appointment

Overview: Containers and Iterators

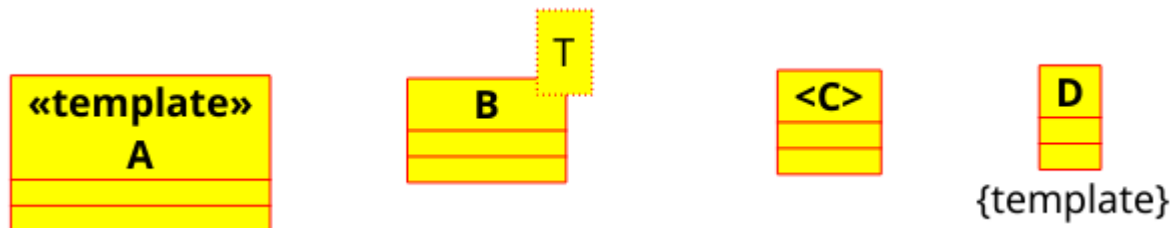
- Containers
 - Sequence Containers
 - Container Adapters
 - Associative Containers
 - Unordered Associative Containers
- Iterators



Lecture 20

Quick Review

- Writing algorithms in terms of types that are specified as parameters during instantiation or invocation is called **Generic Programming**.
- A **template** is a C++ construct representing a function or class in terms of generic types.
- **True** or False: Both the declaration AND definition of a template class must be placed in the header file.
- The **Standard Template Library** provides a good variety of well-implemented, mostly non-numerical algorithms focused on organizing code and data as C++ templates.
- A template is represented in the UML as **B**.





Review

Template Summary

- **Template** – A C++ construct representing a function or class in terms of generic types
 - This enables the algorithm to be written independent of the types of data to which it applies
 - A type must be specified when the template class is instantiated or the template function is called
 - Templates rely on “Duck Typing”: The type must supply whatever methods are access by the template
- Potentially reusable algorithms that are suitable should generally be defined as templates

Review

Vector v0.4 – Now a Template

UML Template Class indicator

T

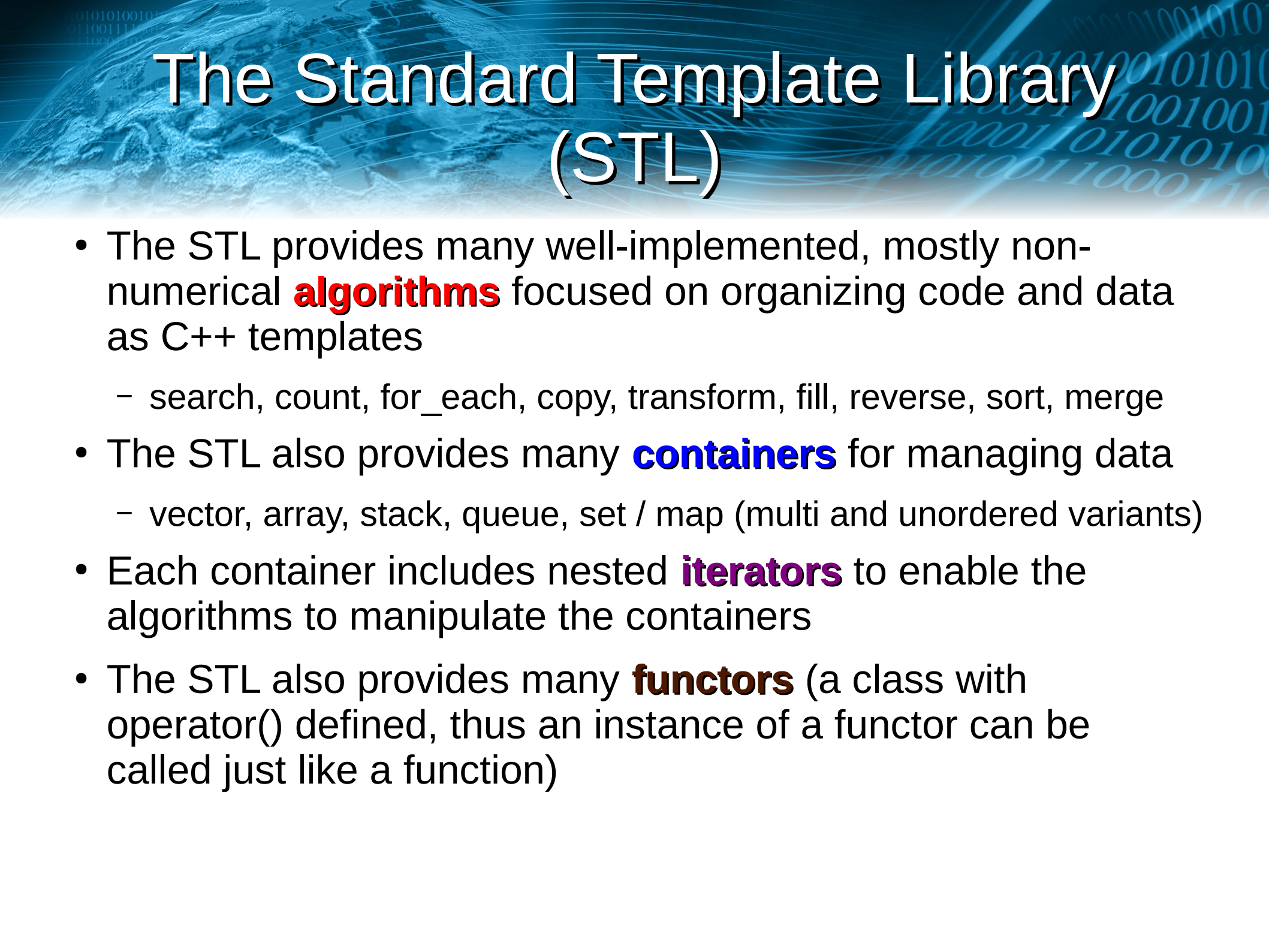
```
template <class T>
class vector {
    int sz;          // the size
    T* elem;         // a pointer to the elements
public:
    vector(int s) : sz(s), elem{new T[s]} { }
    ~vector() {delete[ ] elem; }
    T get(int n) const { return elem[n]; } // access: read
    void set(int n, T v) { elem[n]=v; }    // access: write
};
```

vector

- sz : int
- elem : T*
- + vector(s : int)
- + ~vector()
- + get(n : int) : T
- + set(n : int, v : T)

- To convert a class to a template:
 - Add template specifier before the class declaration
 - Replace the type with T

```
ricegfp@pluto:~/dev/cpp/201801/21$ make vector
g++ -std=c++14 vector.cpp -o vector
ricegfp@pluto:~/dev/cpp/201801/21$ ./vector
ricegfp@pluto:~/dev/cpp/201801/21$
```



The Standard Template Library (STL)

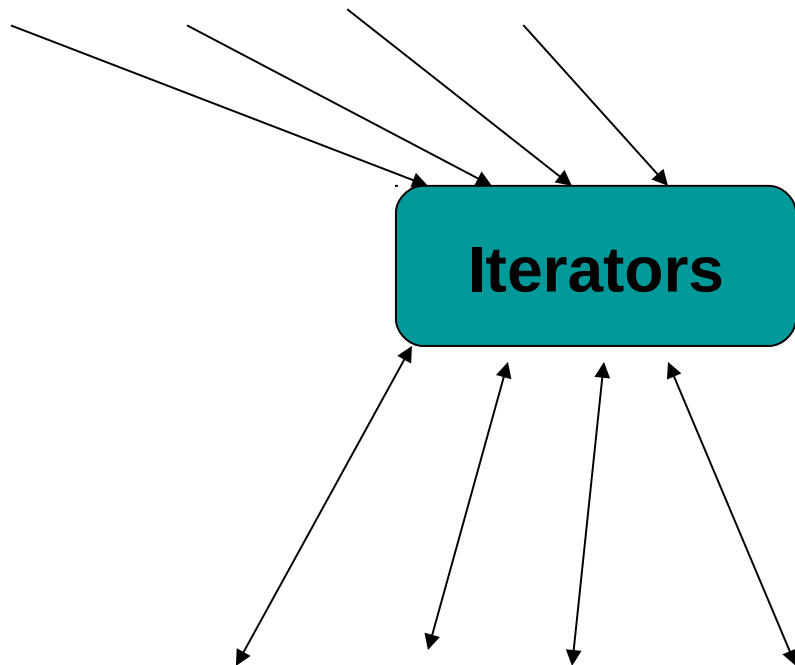
- The STL provides many well-implemented, mostly non-numerical **algorithms** focused on organizing code and data as C++ templates
 - search, count, for_each, copy, transform, fill, reverse, sort, merge
- The STL also provides many **containers** for managing data
 - vector, array, stack, queue, set / map (multi and unordered variants)
- Each container includes nested **iterators** to enable the algorithms to manipulate the containers
- The STL also provides many **functors** (a class with operator() defined, thus an instance of a functor can be called just like a function)

Review

Basic STL Model

Algorithms

Sort, find, search, copy, ...



vector, list, map, unordered_map, ...

Containers

- Separation of concerns
 - Algorithms manipulate data, but don't know about containers
 - Containers store data, but don't know about algorithms
 - Algorithms and containers interact through iterators
 - Each container has its own iterator types

The STL also defines some **Functors**, but we'll ignore those...



STL Container Overview

- The STL contains the following containers of interest
 - **Sequence Containers** store data linearly
 - vector, array, list, forward_list, and deque (string is a non-STL sequence container)
 - **Container Adapters** are façades to Sequence Containers
 - stack, queue, and priority_queue
 - **(Ordered) Associative Containers** provide fast lookup via keys by maintaining the data in sort order
 - set, map, multiset, and multimap
 - **Unordered Associative Containers** are unsorted, and thus provide somewhat faster insertion but slower lookups via a hash
 - unordered_set, unordered_map, unordered_multiset, unordered_multimap
- Let's take a brief look at each



Sequence Containers

vector and **array**

- **Vector** provides a resizable, flexible version of the C / C++ standard array
 - Very fast lookup (e.g., `foo[42]`)
 - Relatively slow insert / delete except at end
- We already know vector fairly well
- **Array** is basically a fixed-size vector
 - All memory is allocated when instanced
 - While vector has 24 additional bytes of overhead beyond the data buffer, array has none
 - Array is very useful for memory-constrained systems and for embedded programming

<http://www.cplusplus.com/reference/vector/vector/>

<http://www.cplusplus.com/reference/array/array>

Sequence Containers

deque (**d**ouble-**e**nded **q**ueue)

- **Deque** provides a version of vector that supports fast additions at *both ends* of the underlying array
 - Very fast lookup (e.g., `foo[42]`)
 - Relatively slow insert / delete except at the beginning or end
- Deques can `push_back` and `pop_back` like a vector, but also `push_front` and `pop_front`
- Supports operator[] just like vector (indexes always start at 0)



Sequence Containers

list and **forward_list**

- Linked lists provide chains of data objects connected via one or more pointers
 - Relatively slow lookup (requires iterators, q.v.)
 - Very fast insert / delete anywhere
- Two types of lists are supported
 - **List** provides a double-linked list that can be navigated forward (++) or backward (–)
 - **Forward_list** provides a single-linked list that can be navigated forward (++) only, using slightly less memory with faster insertion / deletion compared to list
- Lists do NOT support operator[]

<http://www.cplusplus.com/reference/list/list>

http://www.cplusplus.com/reference/forward_list/forward_list/



Sequence Containers

string

- OK, this is NOT a “real” STL container, but it works very much like a vector of char
 - Relatively fast lookup (e.g., `foo[42]`)
 - Very slow insert / delete
- Actually, `string` is just a typedef for `basic_string<char>`
 - Other string types are not uncommon, e.g., `basic_string<wchar>`
 - More on this next week



Sequence Adapters

stack and queue

- **Stack** provides a Last-In, First-Out (LIFO) stack
 - Very fast single-ended push and pop only
 - By default, stack is a façade for a **deque**
 - Can be specified to wrap a **vector** or **list** instead, e.g., `stack<int, std::vector<int>> lifo_of_ints;`
- **Queue** provides a First-In, First-Out (FIFO) stack
 - Very fast opposite-ended push and pop only
 - By default, queue is a façade for a **deque**
 - Can be specified to wrap a **list** instead, e.g., `stack<int, std::list<int>> fifo_of_ints;`



Sequence Adapters `priority_queue`

- **Priority_queue** provides a stack for which the *highest priority* item is always popped next
 - Fast push and constant time lookup for pop
 - By default, `priority_queue` is a façade for a **vector**
 - Can be specified to wrap a **deque** instead, e.g.,
`stack<int, std::list<int>> fifo_of_ints;`
- As with `sort`, you may need to provide a comparator method for `priority_queue` to use



Associative Containers **set** and **map**

- **set** is a collection of keys, sorted by keys
 - Essentially a vector of objects with duplicates automatically removed, and always sorted
- **map** is a collection of key-value pairs sorted by keys
 - Essentially a vector of objects with (almost) any type as the key, and always sorted
 - Elements are accessed like a vector, e.g., `foo["bar"]`
- As with `sort` and `priority_queue`, you may need to provide a comparator method for ordered containers
 - Associative Containers also allow non-default allocators, which we won't cover in this class



Associative Containers

multiset and **multimap**

- **multiset** and **multimap** are similar to set and map, but permit duplicate keys
 - For example, a multiset of chars would allow you to store every character in a document separately, then use the count method to determine how many
 - Access is a bit trickier – foo[“bar”] is ambiguous – so iterators are needed (coming shortly)
- As with set and map, you may need to provide a comparator method for ordered containers
 - You may again provide a non-default allocator

<http://www.cplusplus.com/reference/set/multiset/>

<http://www.cplusplus.com/reference/map/multimap/>



Unordered Associative Containers

Unordered_*

- **Unordered_set, unordered_map, unordered_multiset, unordered_multimap**, similar to the ordered versions
 - Because they are not sorted, insertions are slightly faster but lookups are slightly slower
 - I've never actually needed one of these
- As with set and map, you may need to provide a comparator method for ordered containers
 - Unordered Associative Containers also allow non-default allocators and hashes, which we won't cover in this class

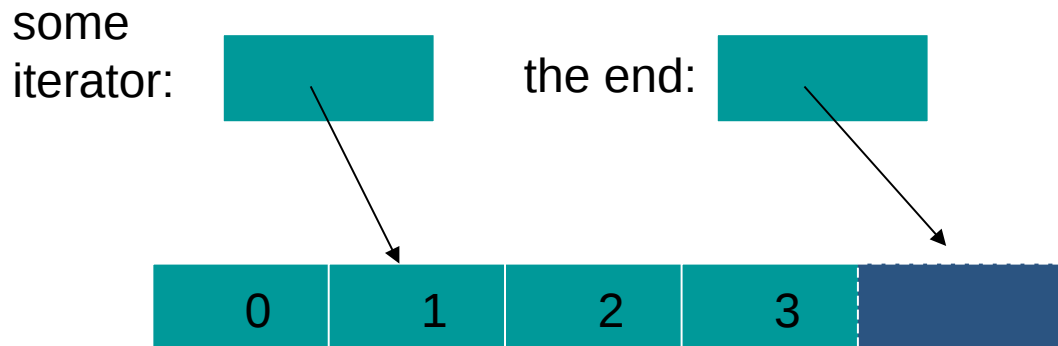


Iterators

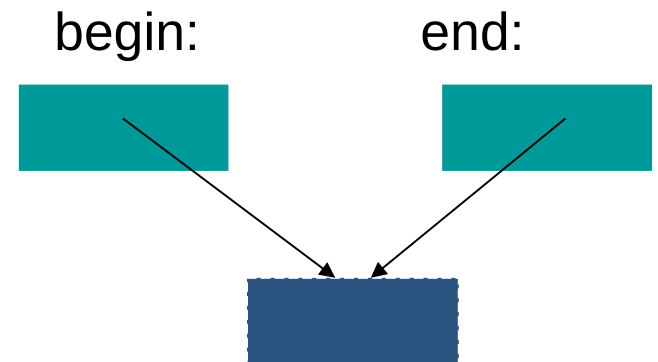
- **Iterator**: A pointer-like instance of a nested class used to access items managed by the outer class instance
 - An iterator can always be incremented via ++, dereferenced with *, and compared to other iterators
 - The outer class provides pre-instanced iterators using methods such as begin() and end()
- Two complementary nested iterator classes are typically provided by a container
 - Iterator allows the dereferenced item to be modified
 - const_iterator prevents modification to the dereferenced item

Algorithms and Iterators

- An iterator object points to (refers to, denotes) an element of a container, e.g., a sequence
- The end of the sequence is “one past the last element”
 - Not “the last element”
 - That’s necessary to elegantly represent an empty sequence
 - One-past-the-last-element isn’t an element
 - You can compare an iterator pointing to it
 - You can’t dereference it (read its value)
- Returning the end of the sequence is the standard idiom for “not found” or “unsuccessful”



An empty sequence:



Iterating Through a Vector

With and Without Iterators

```
#include <vector>
#include <iostream>
using namespace std;
```

```
int main() {
    vector<int> v = {1, 2, 3, 4, 5};
```

```
    // Old school - 3-term counted loop
    for(int i=0; i<v.size(); ++i) cout << v[i] << " ";
```

```
    // Verbose school (but more technically accurate) - 3-term counted loop
    for(vector<int>::size_type i=0; i<v.size(); ++i) cout << v[i] << " ";
```

```
    // Verbose school - 1-term for-each loop
    for(vector<int>::value_type i : v) cout << i << " ";
```

```
    // Classic school - 1-term for-each loop with known type
    for(int& i: v) cout << i << " ";
```

```
    // Auto school - 1-term for-each loop where the compiler figures out the type
    for(auto& i : v) cout << i << " ";
```

```
    // Explicit school - iterator is a nested class inside vector that returns
    // a pointer to a vector item (or the address past the last item v.end())
    for(vector<int>::iterator p = v.begin(); p!=v.end(); ++p) cout << *p << " ";
}
```

```
ricegfp@pluto:~/dev/cpp/201801/21$ make iteration
g++ -std=c++14 iteration.cpp -o iteration
ricegfp@pluto:~/dev/cpp/201801/21$ ./iteration
1 2 3 4 5
1 2 3 4 5
1 2 3 4 5
1 2 3 4 5
1 2 3 4 5
1 2 3 4 5
1 2 3 4 5
ricegfp@pluto:~/dev/cpp/201801/21$
```

The 1-term for-each loops
depend on iterators

Common Iterator Methods

- All iterators must provide:
 - copy constructor and destructor
 - operator=, operator++ and operator*
- Input iterators add:
 - operator== and operator!=
- Output iterators add:
 - Dereferencing as an lvalue (e.g., *x = t)
- Forward iterators add:
 - Default constructor
- Bidirectional iterators add:
 - operator--
- Random access iterators add:
 - operator+, operator-, operator< et al, operator+= and operator-=, operator[]

Containers that support iterators usually provide (x is item, p is iterator):

- begin() - returns p pointing to first item
- end() - returns p pointing one past last item
- front(), back() - first / last item
- size() - number of elements
- empty() - true if no elements
- push_back(x) / push_front(x) – insert at end / begin
- insert(p, x) – insert x immediately before p
- pop_back() / pop_front() – delete at end / begin
- erase(p) – remove item at p

These are conventions – the compiler doesn't care



Writing Iterators for Custom Classes

- Writing an iterator from scratch is fairly complex
 - But we usually don't need to write from scratch
- Four common scenarios
 - **Pointers** – A pointer is by definition a (non-class) iterator, so if one accesses your data, just return the pointer
 - **Nested container** (e.g., vector inside a wrapper class) – Just delegate to the nested container's iterator
 - **Iterator++** (e.g., a range-checked array accessor) – This also relies on delegation to the extended iterator, but can be tricky to implement given compiler limitations
 - **Written from scratch** – Hard, but rarely necessary

A Nested Container Example

- Let's produce an "order book" that lists orders for a sales associate in a store
 - The book will identify the sales associate's name, and also include a vector of orders
 - Iterating through the book should return the orders

```
#include <iostream>
#include <vector>
using namespace std;
```

```
class Order {
public:
    Order(string customer, string model) : _customer{customer}, _model{model} { }
    string customer() {return _customer;}
    string model() {return _model;}
private:
    string _customer;
    string _model;
};
```

An Order simply associates
a customer with a model number

Defining an Order Book: A Nested Container Example

- In addition to the usual structure, we delegate 4 members to vector

```
class Order_book {  
    private:  
        string _sa;                // Sales Associate who owns this book  
        typedef vector<Order> Orders;  
        Orders orders;             // This SA's list of orders  
    public:  
        Order_book(string sales_associate) : _sa{sales_associate} { }  
        string sales_associate() {return _sa;}  
        void add_order(Order order) {orders.push_back(order); }  
        typedef Orders::iterator iterator;  
        typedef Orders::const_iterator const_iterator;  
        iterator begin() {return orders.begin();}  
        iterator end() {return orders.end();}  
};
```

- That's all there is to it!

A Nested Container Example

- Our order book is now an enhanced vector (adding info on the sales associate) that still iterates
 - This is sometimes called “composite inheritance”

```
int main() {  
    Order_book book{"Prof Rice"};  
    book.add_order(Order{"Larry", "Crazy Cukes"});  
    book.add_order(Order{"Curly", "Zany Zeros"});  
    book.add_order(Order{"Moe", "Quick Quirks"});  
  
    cout << "ORDER BOOK: " << book.sales_associate() << endl;  
    for(Order o: book) {  
        cout << o.customer() << " ordered " << o.model() << endl;  
    }  
}
```

```
ricegf@pluto:~/dev/cpp/201801/21$ make order_book  
g++ -std=c++14 order_book.cpp -o order_book  
ricegf@pluto:~/dev/cpp/201801/21$ ./order_book  
ORDER BOOK: Prof Rice  
Larry ordered Crazy Cukes  
Curly ordered Zany Zeros  
Moe ordered Quick Quirks  
ricegf@pluto:~/dev/cpp/201801/21$
```



Inheritance vs Composites

- Extending a class via composition often yields the same or similar benefits as inheritance
 - This has led to some debate: “Composition over Inheritance” vs “True Inheritance”
 - We can leave that to the theoreticians (until you become one) – use what works best per application
- With STL classes, you have no choice
 - **Never inherit from an STL class** – use composition
 - You can violate this rule after years of experience – but by then you probably won’t want to...



Class Constructors and Destructors

- C++ classes require (up to) 4 essential operations
 - Default and Non-default constructors (defaults to: nothing)
 - No default if any non-default constructors are declared
 - Copy constructor (defaults to: copy the member)
 - Needed if the class includes pointers or dynamic memory allocation
 - Copy assignment (defaults to: copy the members)
 - Used when an instance is to the left of the “=” operator
 - Destructor (defaults to: nothing)
 - Used to “clean up” e.g., dynamically allocated memory when an object is deleted (destroyed)

Constructors and destructors are described in detail in chapters 17-19

Review

Default Constructor Only

```
#include <iostream>
using namespace std;

// previous slide's code goes here

class Date {
public:
    void set_date(int y, Month m, int d) {year=y; month=m; day=d;}
    void print_date() {cout << month_to_string(month) << " " <<
                        day << ", " << year << endl;}

private:
    int year;
    Month month;
    int day;
};

int main() {
    Date my_birthday;
    my_birthday.print_date(); // Oops - we haven't provided any data yet!
    my_birthday.set_date(1950, Month::dec, 30); // OK
    my_birthday.print_date(); // Better
}
```

```
ricegf@pluto:~/dev/cpp/201701/16$ c++ -std=c++11 enum_class_io_no_constructor.cpp
ricegf@pluto:~/dev/cpp/201701/16$ ./a.out
Unknown 0, -1162798832
December 30, 1950
ricegf@pluto:~/dev/cpp/201701/16$
```


Review

Non-Default Constructors

```
#include <iostream>
using namespace std;
```

```
// previous slide's code goes here
```

```
class Date {
public:
```

```
    Date(int y, Month m, int d) : year{y}, month{m}, day{d} { }
```

```
    Date() : Date(1970, Month::jan, 1) { }
```

```
    void set_date(int y, Month m, int d) {year=y; month=m; day=d;}
```

```
    void print_date() {cout << month_to_string(month) << " " <<
                        day << ", " << year << endl;}
```

```
private:
```

```
    int year;
```

```
    Month month;
```

```
    int day;
```

```
};
```

```
int main() {
```

```
    Date unix_epoch; // or unix_epoch{} - Default constructor
```

```
    unix_epoch.print_date();
```

```
    Date my_birthday{1950, Month::dec, 30}; // Non-default constructor
```

```
    my_birthday.print_date();
```

```
}
```

Multiple constructors (with or without a default)
is fine and quite common

```
ricegf@pluto:~/dev/cpp/201801/21$ make date
g++ -std=c++14 date.cpp -o date
ricegf@pluto:~/dev/cpp/201801/21$ ./date
January 1, 1970
December 30, 1950
ricegf@pluto:~/dev/cpp/201801/21$
```

Initialization vs Assignment

This is important for understanding
copy constructors vs copy assignment

- Initialization causes *a new object* to have the same value as an existing object
 - `Robot r1 = r2; // initialization`
 - `Robot r1{r2}; // initialization - exactly the same`
- Assignment causes *an existing object* to have the same value as an existing object
 - `Robot r1;`
 - `r1 = r2; // assignment`
- These are two distinct operations in C++

Default Copy Constructors and Copy Assignment

```
#include <iostream>
using namespace std;
```

```
class Foo {
    int _val;
public:
    Foo(int val) : _val{val} {} // Non-default constructor
    Foo() : Foo(0) {}           // Default constructor
    int val() {return _val;}
};
```

```
int main() {
    Foo bar0;                // Default constructor
    cout << "bar0 = " << bar0.val() << endl;
    Foo bar1{1};             // Non-default constructor
    cout << "bar1 = " << bar1.val() << endl;
    Foo bar2{bar1};          // Default copy constructor for initialization
    // Foo bar2 = bar1; // Exactly the same thing: bar2 has same values as bar1
    cout << "bar2 = " << bar2.val() << endl;
    bar0 = bar1;             // Default copy assignment for assignment
    cout << "bar0 now = " << bar0.val() << endl;
}
```

```
ricegfp@pluto:~/dev/cpp/201801/21$ make cc_and_cao2
g++ -std=c++14 cc_and_cao2.cpp -o cc_and_cao2
ricegfp@pluto:~/dev/cpp/201801/21$ ./cc_and_cao2
bar0 = 0
bar1 = 1
bar2 = 1
bar0 now = 1
ricegfp@pluto:~/dev/cpp/201801/21$
```



Copy Constructor

- For initialization, C++ actually invokes a special constructor – the copy constructor
 - If you have not specified one, you'll get the default – all of your variables will be copied directly across
- The copy constructor is thus invoked when:
 - You initialize a new object to an existing object
 - `Foo bar2 = bar1; // Identical to Foo bar2{bar1};`
 - You pass an object as a non-reference parameter
 - `analyze(bar1); // A copy of bar1 is created for analyze`
 - You return an object from a function
 - `return bar1; // A copy of bar1 is created and returned`

Declaring a Copy Constructor

- A copy constructor is just a constructor that accepts a const reference to the object to be copied
 - I *know* this isn't useful here – we'll come back to when writing a copy constructor is useful shortly

```
#include <iostream>
using namespace std;

class Foo {
    int _val;
public:
    Foo(int val) : _val{val} {}           // Non-default constructor
    Foo() : Foo(0) {}                     // Default constructor
    Foo(const Foo &rhs) : _val{rhs.val()} {} // Copy constructor
    int val() {return _val;}
};
```



Copy Assignment

- For assignment, C++ invokes the assignment operator to overwrite the left-hand object's values
 - If you have not specified one, you'll get the default – all of your variables will be copied directly across
- The copy assignment is thus invoked when:
 - You assign to an existing object the value of another (*or the same*) existing object
 - `bar2 = bar1; // bar2 was existing, so we overwrite it`

Declaring a Copy Assignment

- A copy assignment is a definition of the = operator to handle copying members as needed
 - Not useful here, either – almost there!

```
class Foo {  
    int _val;  
public:  
    Foo(int val) : _val{val} {}           // Non-default constructor  
    Foo() : Foo(0) {}                     // Default constructor  
    Foo(const Foo &rhs) : _val{rhs.val()} {} // Copy constructor  
    Foo& operator=(const Foo &rhs) {      // Copy assignment  
        if (this != &rhs) _val = rhs.val();  
        return *this;  
    }  
    int val() const {return _val;}  
};
```

Destructors

- The destructor is invoked when the object itself is being deleted
 - *Really* useless here! Next slide, promise!

```
class Foo {  
    int _val;  
public:  
    Foo(int val) : _val{val} {}           // Non-default constructor  
    Foo() : Foo(0) {}                     // Default constructor  
    Foo(const Foo &rhs) : _val{rhs.val()} {} // Copy constructor  
    Foo& operator=(const Foo &rhs) {       // Copy assignment  
        if (this != &rhs) _val = rhs.val();  
        return *this;  
    }  
    ~Foo() {}                             // Destructor  
    int val() const {return _val;}  
};
```


Practical Use and the Rule of Three

- So when would copy constructors, copy assignment, and destructors actually be *useful*?
 - Typically, when your class allocates memory from the heap, keeping a pointer to its address
 - To copy the object, you also need to “deep copy” the allocated heap memory to another heap memory area
 - To assign the object, you need to deallocate the existing heap memory before doing the “deep copy” to allocate the new heap memory
 - To delete the object, you also need to delete the heap memory

Rule of Three: If you define one of the above, you probably need to define all three of the above!

For more detail, I recommend the following paper. This isn't required for the exam.

http://www.keithschwarz.com/cs106l/winter20072008/handouts/170_Copy_Constructor_Assignment_Operator.pdf

Rule of 3 Implementation of Foo

- Allocating and deallocating private variables
- Copy and assignment allocate new heap
 - Rather than pointing to the *same* heap!

```
class Foo {  
    int* _val;  
public:  
    Foo(int* val) : _val{val} {} // Non-default constructor  
    Foo() : Foo(new int{0}) {} // Default constructor  
    Foo(const Foo &rhs) : _val{new int{*rhs.get()}} {} // Copy constructor  
    Foo& operator=(const Foo &rhs) { // Copy assignment  
        if (this != &rhs) _val = new int{*rhs.get()};  
        return *this;  
    }  
    ~Foo() {delete _val;} // Destructor  
    int* get() const {return _val;} // Getter  
    void set(int* v) {_val = *v;} // Setter  
};
```


Testing the Rule of 3

- Unfortunately, the C++ standard provides no way to determine if a pointer has been deleted, so...

```
int main() {
    Foo foo1{new int{42}};                // Non-default constructor
    // Test non-default constructor
    if (*foo1.get() != 42) std::cerr << "foo1 set to 42 but is now "
        << *foo1.get() << std::endl;

    Foo foo2{foo1};                       // Copy constructor
    Foo foo3;                             // Default constructor
    // Test default constructor
    if (*foo3.get() != 0) std::cerr << "foo3 default constructor set value to "
        << *foo3.get() << std::endl;

    foo3 = foo1;                          // Copy assignment operator

    // This should NOT modify foo2 or foo3!
    int i = 17;
    foo1.set(&i);

    // Test copy constructor
    if (*foo2.get() != 42) std::cerr << "foo2 changed from 42 to "
        << *foo2.get() << std::endl;

    // Test copy assignment operator
    if (*foo3.get() != 42) std::cerr << "foo3 changed from 42 to "
        << *foo3.get() << std::endl;
}
```

```
ricegfp@pluto:~/dev/cpp/201801/21$ make cc_and_caol
g++ -std=c++14 cc_and_caol.cpp -o cc_and_caol
ricegfp@pluto:~/dev/cpp/201801/21$ ./cc_and_caol
ricegfp@pluto:~/dev/cpp/201801/21$
```



Quick Review

- The four basic types of STL containers in C++ are
(a) Memory Managed Containers (b) Unmanaged Containers
(c) Sequence Containers (d) Sequence Adapters
(e) Associative Containers (f) Associative Adapters
(g) Unordered Associative Containers
- _____ are a façade for _____,
- A(n) _____ is a pointer-like instance of a nested class used to access items managed by the outer class instance/
- True or False: With iterators, the end of the sequence is “one past the last element”, not “the last element”
- Two types of iterators are typically provided, _____ and _____.
- Name some common iterator and container methods in the STL.
- True or False: It is a good practice to derive your classes from STL classes.
- What is a copy constructor? Copy assignment operator?
- Define the Rule of 3.



For Next Class

- (Optional) Read Chapters 20-21 in Stroustrup
 - Do the Drills!
- Skim Chapters 23-24 for next class
 - We'll discuss text manipulation (including regular expressions in more detail) and numerics
- **Sprint #2 now in progress: Our first GUI!**