

```

J0 = {{-sigma, sigma, 0}, {r - z, -1, -x}, {y, x, -b}};
{{-sigma, sigma, 0}, {r - z, -1, -x}, {y, x, -b}};
J = J0 /. {sigma -> 10, b -> 8/3, r -> 28};
eigens = Eigenvalues[J];

eigens1 = eigens /. {x -> 0, y -> 0, z -> 0};
AnyTrue[{Re[Evaluate[eigens1[[1]]]],
  Re[Evaluate[eigens1[[2]]]], Re[Evaluate[eigens1[[3]]]]}, LessThan[0]]

eigens2 = eigens /. {x -> -sqrt(6)/2, y -> -sqrt(6)/2, z -> 27};
AnyTrue[{Re[Evaluate[eigens1[[1]]]],
  Re[Evaluate[eigens1[[2]]]], Re[Evaluate[eigens1[[3]]]]}, LessThan[0]]

eigens2 = eigens /. {x -> sqrt(6)/2, y -> sqrt(6)/2, z -> 27};
AnyTrue[{Re[Evaluate[eigens1[[1]]]],
  Re[Evaluate[eigens1[[2]]]], Re[Evaluate[eigens1[[3]]]]}, LessThan[0]]

```

```
Tr[J0]
```

Out[]= True

Out[]= True

Out[]= True

Out[]= -1 - b - sigma

```

In[638]:= ClearAll["Global`*"]
sigma0 = 10;
b0 = 8/3;
r0 = 28;
tMax = 4;

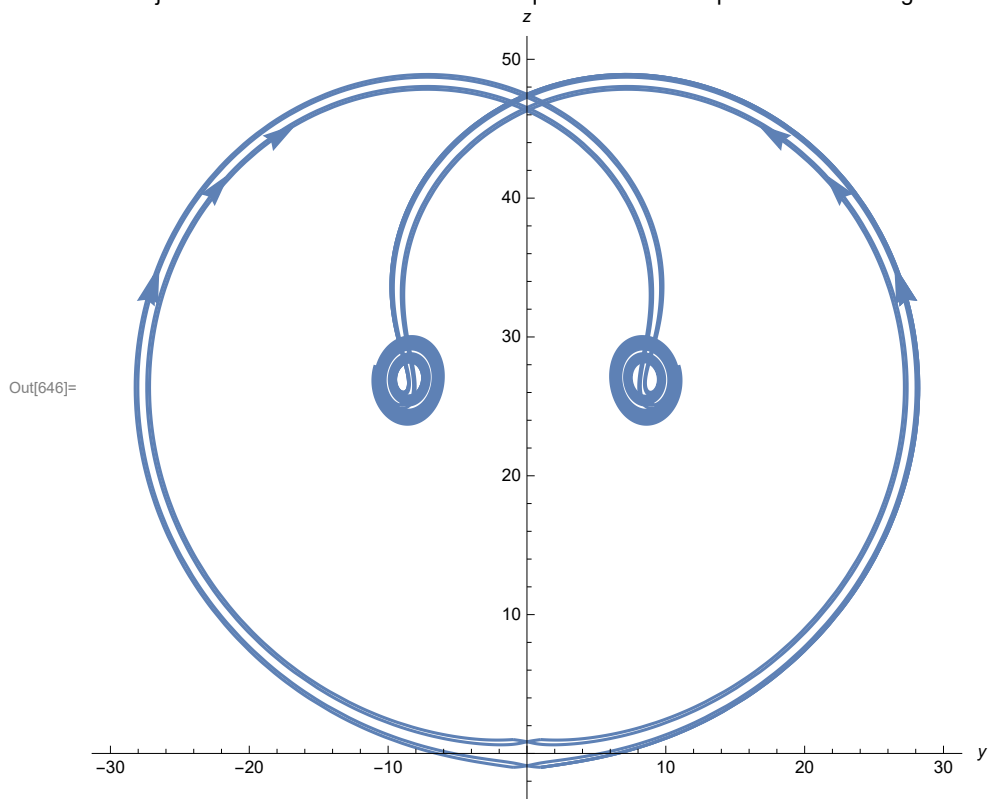
sol[u_, v_, w_] := NDSolve[{x'[t] == sigma0 * (y[t] - x[t]),
  y'[t] == r0 * x[t] - y[t] - x[t] * z[t],
  z'[t] == x[t] * y[t] - b0 * z[t],
  x[0] == u,
  y[0] == v,
  z[0] == w},
  {x, y, z},
  {t, 0, tMax}];

TableFinal = {{-1, -1, -1}, {-1, -1, 1}, {-1, 1, 1}, {-1, 1, -1},
  {1, 1, -1}, {1, -1, -1}, {1, -1, 1}, {1, 1, 1}, {1, 1, -1}, {1, 1, -1}};

title = "Trajectories of solutions of
  the Lorenz equations with start points near the origin";
Show[Table[ParametricPlot[Evaluate[{y[t], z[t]} /.
  sol[TableFinal[[i, 1]], TableFinal[[i, 2]], TableFinal[[i, 3]]], {t, 0, tMax},
  PlotRange -> All, AxesLabel -> {y, z}, PlotLabel -> Style[title, FontSize -> 12]] /.
  Line[x_] -> {Arrowheads[{0, 0.03, 0, 0}], Arrow[x]}, {i, Length[TableFinal]}]]

```

Trajectories of solutions of the Lorenz equations with start points near the origin



In[420]:= **TableFinal**

Out[420]= $\{ \{-1, -1.\}, \{-1, -0.9\}, \{-1, -0.8\}, \{-1, -0.7\}, \{-1, -0.6\}, \{-1, -0.5\},$
 $\{-1, -0.4\}, \{-1, -0.3\}, \{-1, -0.2\}, \{-1, -0.1\}, \{-1, 0.\}, \{-1, 0.1\}, \{-1, 0.2\},$
 $\{-1, 0.3\}, \{-1, 0.4\}, \{-1, 0.5\}, \{-1, 0.6\}, \{-1, 0.7\}, \{-1, 0.8\}, \{-1, 0.9\},$
 $\{-1, 1.\}, \{-1., 1\}, \{-0.9, 1\}, \{-0.8, 1\}, \{-0.7, 1\}, \{-0.6, 1\}, \{-0.5, 1\},$
 $\{-0.4, 1\}, \{-0.3, 1\}, \{-0.2, 1\}, \{-0.1, 1\}, \{0., 1\}, \{0.1, 1\}, \{0.2, 1\},$
 $\{0.3, 1\}, \{0.4, 1\}, \{0.5, 1\}, \{0.6, 1\}, \{0.7, 1\}, \{0.8, 1\}, \{0.9, 1\}, \{1., 1\},$
 $\{1, -1.\}, \{1, -0.9\}, \{1, -0.8\}, \{1, -0.7\}, \{1, -0.6\}, \{1, -0.5\}, \{1, -0.4\},$
 $\{1, -0.3\}, \{1, -0.2\}, \{1, -0.1\}, \{1, 0.\}, \{1, 0.1\}, \{1, 0.2\}, \{1, 0.3\},$
 $\{1, 0.4\}, \{1, 0.5\}, \{1, 0.6\}, \{1, 0.7\}, \{1, 0.8\}, \{1, 0.9\}, \{1, 1.\}, \{-1., -1\},$
 $\{-0.9, -1\}, \{-0.8, -1\}, \{-0.7, -1\}, \{-0.6, -1\}, \{-0.5, -1\}, \{-0.4, -1\},$
 $\{-0.3, -1\}, \{-0.2, -1\}, \{-0.1, -1\}, \{0., -1\}, \{0.1, -1\}, \{0.2, -1\}, \{0.3, -1\},$
 $\{0.4, -1\}, \{0.5, -1\}, \{0.6, -1\}, \{0.7, -1\}, \{0.8, -1\}, \{0.9, -1\}, \{1., -1\} \}$