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In[956]:= ClearAll["Global`"]
 $\mu = 1/10;$ 
 $\omega = 1;$ 
 $\nu = 1;$ 
 $r0 = \text{Sqrt}[\mu];$ 
 $T = 2 * \text{Pi} / (\mu * \nu + \omega);$ 
 $r\text{Dot}[r\_] = \mu * r - r^3;$ 
 $\theta\text{Dot}[r\_] = \omega + \nu * r^2;$ 

JacobianPolar[r_, theta_] =
  {{D[rDot[r], r], D[rDot[r], theta]}, {D[thetaDot[r], r], D[thetaDot[r], theta]}};

JacobianLimitCycle = JacobianPolar[r0, theta];
M[t] = {{M11[t], M12[t]}, {M21[t], M22[t]}};

eqs = {D[M[t], t] == JacobianLimitCycle.M[t],
  (M[t] /. t -> 0) == IdentityMatrix[2]};

sol = FullSimplify[DSolve[eqs, {M11[t], M12[t], M21[t], M22[t]}, t]];
MPolar = M[t] /. sol[[1]] /. t -> T;

r[x_, y_] = Sqrt[x^2 + y^2];
theta[x_, y_] = ArcTan[y / x];
JacobianTransformation =
  {{D[r[x, y], x], D[r[x, y], y]}, {D[theta[x, y], x], D[theta[x, y], y]}};
MCartesian = Inverse[JacobianTransformation].MPolar.JacobianTransformation;
MCartesianLimitCycle = MCartesian /. {x -> r0, y -> 0}

eigenval = Eigenvalues[MCartesianLimitCycle];
sigma1 = 1/T * Log[eigenval[[1]]];
sigma2 = 1/T * Log[eigenval[[2]]];
{sigma2, sigma1}

Out[974]= {{e-4  $\pi$ /11, 0}, {1 - e-4  $\pi$ /11, 1}}

Out[978]= {- $\frac{1}{5}$ , 0}

Out[346]= {{e-t/5, 0}, { $\sqrt{10}$  (1 - e-t/5), 1}}

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