

In[1723]:=

```
minxplot = -1;
maxxplot = 1;
minyplot = -1;
maxyplot = 1;

tMax = 50;
 $\mu$  = 0.066;
title = StringForm[" $\mu =$ `1`.",  $\mu$ ];

sol[u_, v_] :=
  NDSolve[{x'[t] ==  $\mu$ *x[t] + y[t] - x[t]^2, y'[t] == -x[t] +  $\mu$ *y[t] + 2*x[t]^2,
    x[0] == u, y[0] == v}, {x, y}, {t, tMax}, Method -> "StiffnessSwitching"]

p1 = ParametricPlot[Evaluate[{x[t], y[t]} /. sol[0.05, 0.05]],
  {t, 0, tMax}, PlotRange -> {{minxplot, maxxplot}, {minyplot, maxyplot}},
  PlotLabel -> Style[title, FontSize -> 15]] /.
  Line[x_] -> {Arrowheads[{0.02, 0.}], Arrow[x]};

p2 = ParametricPlot[Evaluate[{x[t], y[t]} /. sol[0.1, 0]],
  {t, 0, tMax}, PlotRange -> {{minxplot, maxxplot}, {minyplot, maxyplot}},
  PlotLabel -> Style[title, FontSize -> 15]] /.
  Line[x_] -> {Arrowheads[{0.02, 0.}], Arrow[x]};

p3 = ParametricPlot[Evaluate[{x[t], y[t]} /. sol[0.01, 0.01]],
  {t, 0, tMax}, PlotRange -> {{minxplot, maxxplot}, {minyplot, maxyplot}},
  PlotLabel -> Style[title, FontSize -> 15]] /.
  Line[x_] -> {Arrowheads[{0.02, 0.}], Arrow[x]};

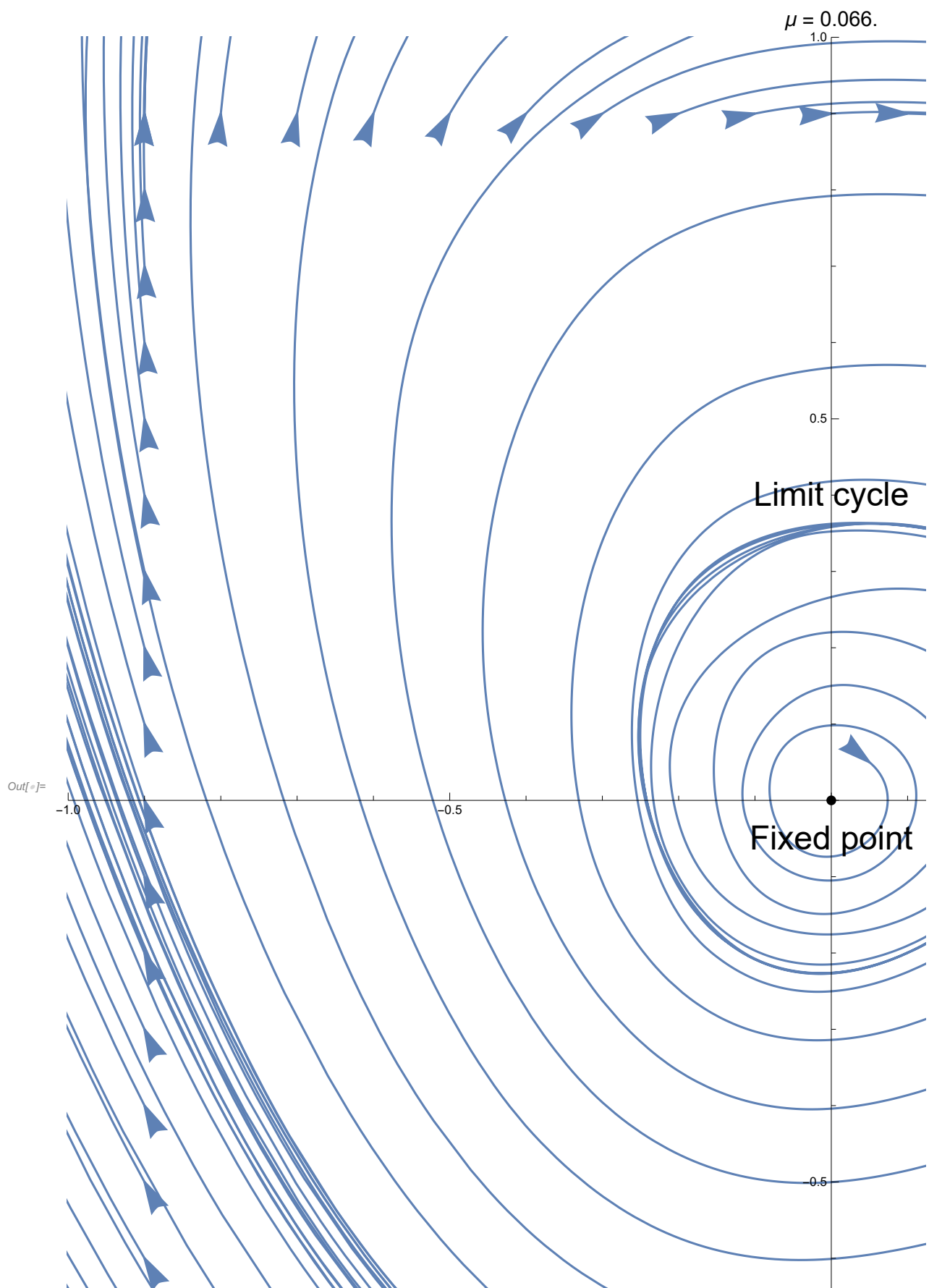
miny = -0.9;
maxy = 0.9;
minx = -0.9;
maxx = 0.9;
step = 0.1;

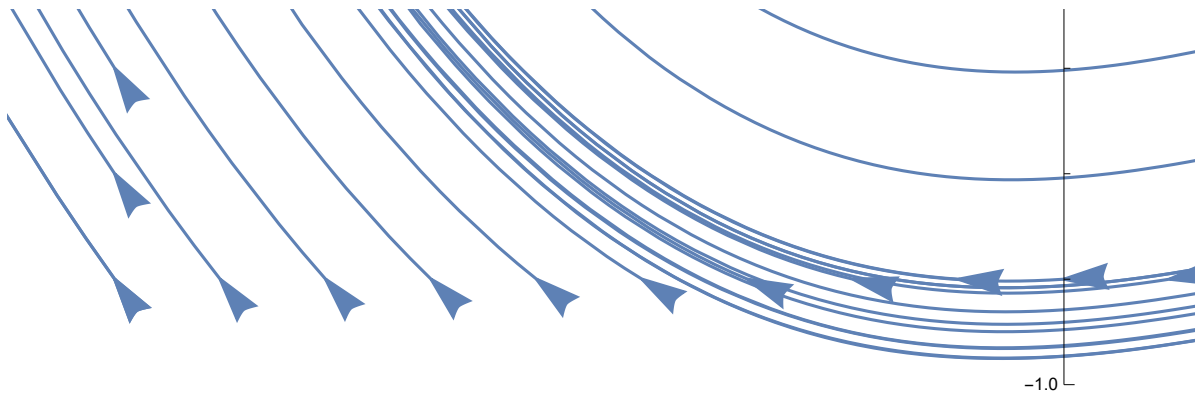
Table11 = Table[{minx, y}, {y, miny, maxy, step}];
Table12 = Table[{x, maxy}, {x, minx, maxx, step}];
Table13 = Table[{maxx, y}, {y, miny, maxy, step}];
Table14 = Table[{x, miny}, {x, minx, maxx, step}];

TableFinal = Join[Table11, Table12, Table13, Table14];
xStar = ( $\mu^2 + 1$ ) / ( $\mu + 2$ );
yStar = xStar^2 -  $\mu$ *xStar;

Show[p1,
  Table[ParametricPlot[
    Evaluate[{x[t], y[t]} /. sol[TableFinal[[i, 1]], TableFinal[[i, 2]]]],
    {t, 0, tMax}, PlotRange -> {{minxplot, maxxplot}, {minyplot, maxyplot}},
    PlotLabel -> Style[title, FontSize -> 15]] /.
    Line[x_] -> {Arrowheads[{0.02, 0.}], Arrow[x]}, {i, Length[TableFinal]}],
  Graphics[{PointSize[Large], Point[{0, 0}]}],
  Graphics[Text[Style["Fixed point", Large], {0, -0.05}]],
  Graphics[{PointSize[Large], Point[{xStar, yStar}]}],
  Graphics[Text[Style["Fixed point", Large], {xStar, yStar - 0.05}]],
  Graphics[Text[Style["Limit cycle", Large], {0, 0.4}]]]
```

]





```
In[ ]:= xStar = (μ^2 + 1) / (μ + 2)
      yStar = xStar^2 - μ * xStar
```

```
Out[ ]:= 1/2
```

```
In[ ]:= yStar
```

```
Out[ ]:= 6
```