

B. The Super-Heterodyne Receiver

The "super-het" is by far the most popular receiver architecture in use today.

HO: The Super-Heterodyne Receiver

Q: So how do we tune a super-het? To what frequency should we set the local oscillator?

A: HO: Super-Heterodyne Tuning

Another vital element of a super-het receiver is the preselector filter.

HO: The Preselector Filter

Q: So what should this preselector filter be? How should we determine the required order of this filter?

A: HO: The Image and Third-Order Signal Rejection

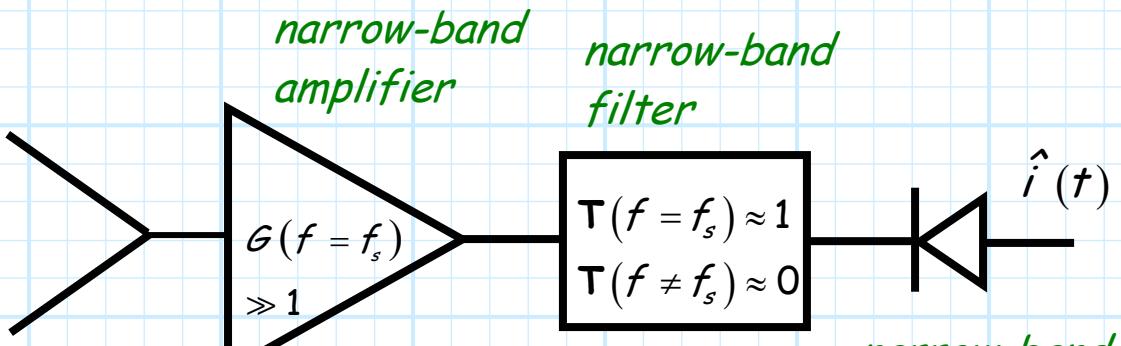
Q: I have heard of some receivers being described as up-conversion receivers, what exactly are they?

A: HO: Up-Conversion

There are many variants of the basic super-het receiver that can improve receiver performance. HO: Advanced Receiver Designs

The Super-Heterodyne Receiver

Note that the homodyne receiver would be an excellent design if we **always** wanted to receive a signal at **one** particular signal frequency (f_s , say):



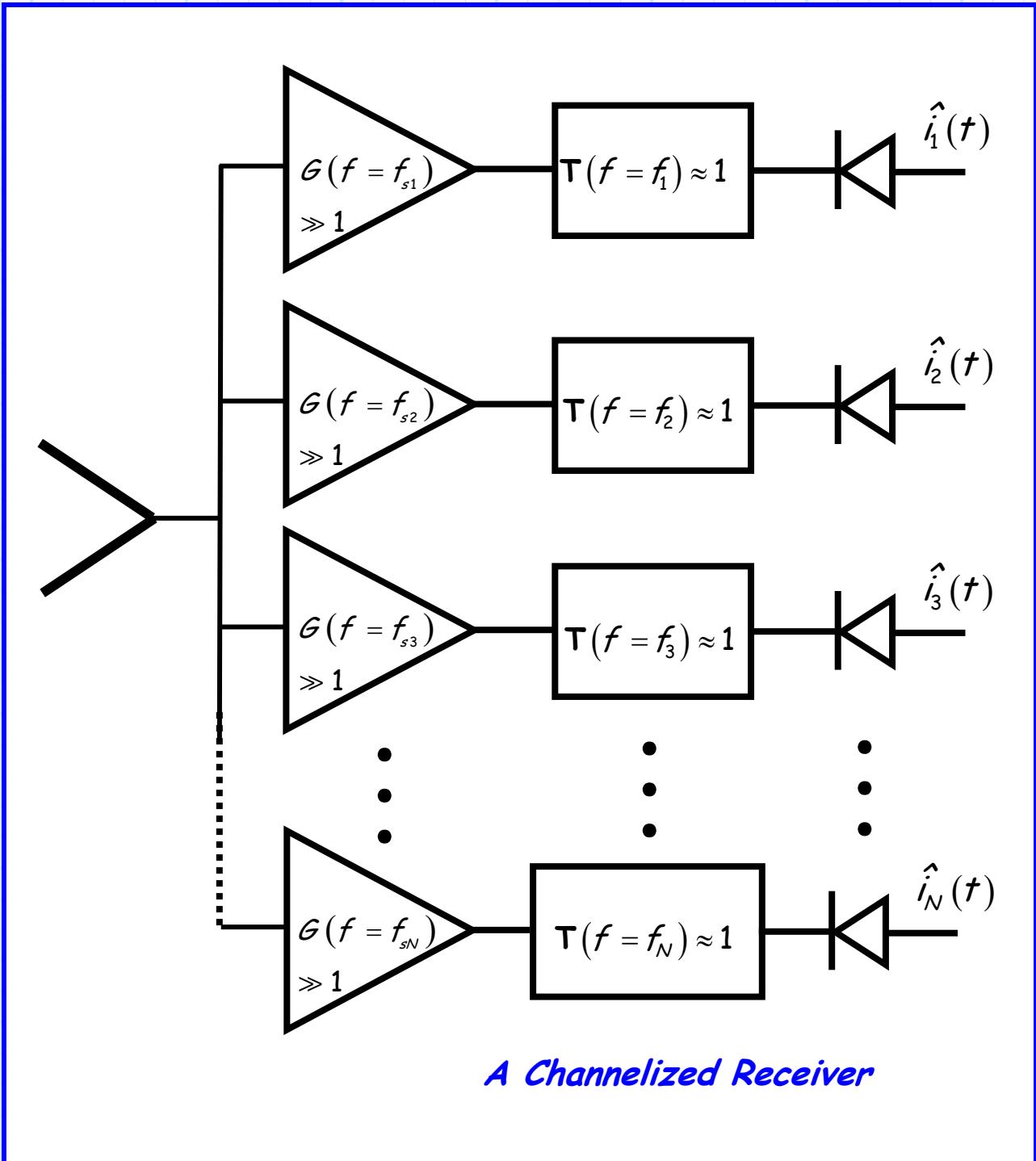
A Fixed-Frequency
Homodyne Receiver

No tuning is required!

Moreover, we can **optimize** the amplifier, filter, and detector performance for **one**—and **only one**—signal frequency (i.e., f_s).

Q: Couldn't we just build one of these fixed-frequency homodyne receivers for **each** and **every** signal frequency of interest?

A: Absolutely! And we sometimes (but not often) do. We call these receivers **channelized receivers**.



But, there are several important **problems** involving channelized receivers.

- They're big, power hungry, and **expensive!**

For **example**, consider a design for a channelized FM radio. The FM band has a **bandwidth** of $108-88 = 20$ MHz, and a **channel spacing** of 200 kHz. Thus we find that the **number** of FM channels (i.e., the number of possible FM radio stations) is:

$$\frac{20 \text{ MHz}}{200 \text{ kHz}} = 100 \text{ channels !!!}$$

Thus, a channelized FM radio would require **100 homodyne receivers!**

Q: Yikes! Aren't there **any good receiver designs!?**

A: Yes, there is a good receiver solution, one developed more than 80 years ago by—**Edwin Howard Armstrong!** In fact, it was such a good solution that it is **still the predominant receiver architecture used today.**

Armstrong's approach was both **simple** and **brilliant**:

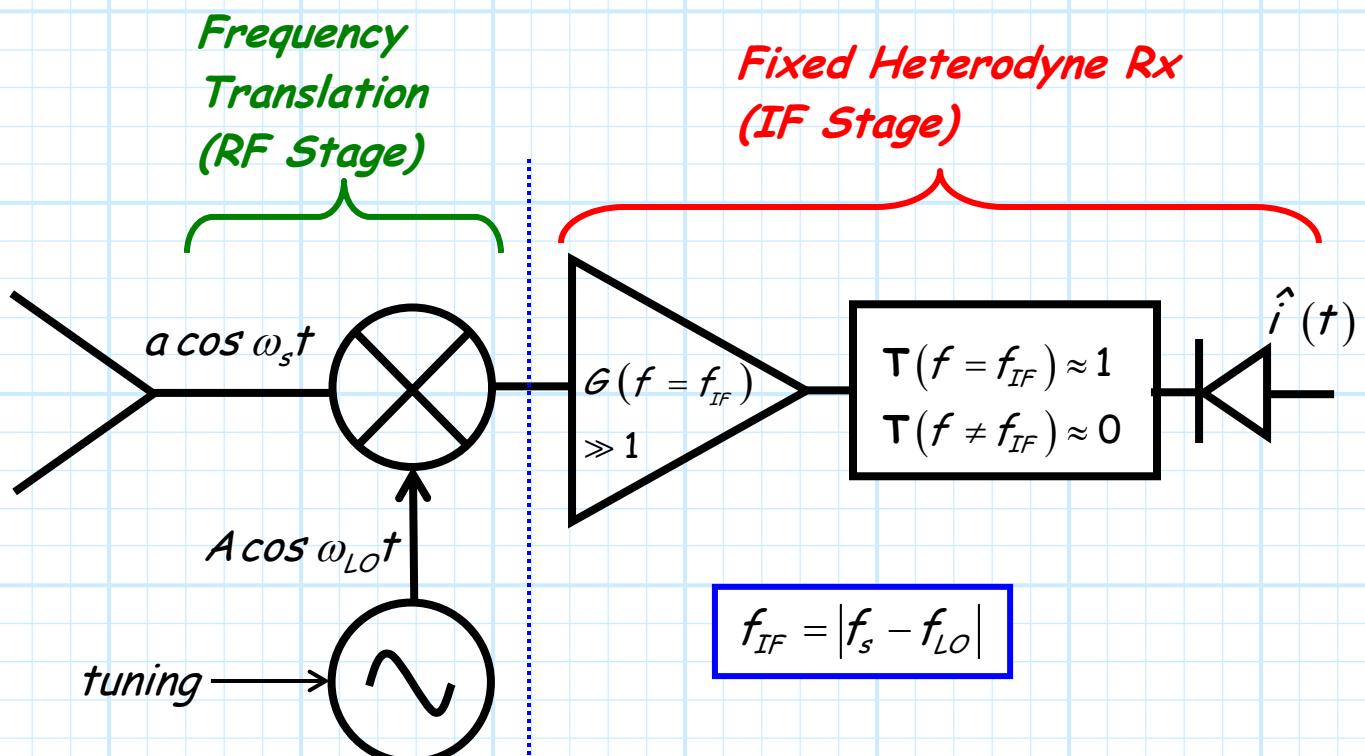
Instead of changing (tuning) the receiver hardware to match the desired signal frequency, we should change the **signal frequency to match the receiver hardware!**

Q: Change the signal frequency? How can we possibly do that?

A: We know how to do this! We mix the signal with a Local Oscillator!

We call this design the **Super-Heterodyne Receiver**!

A super-heterodyne receiver can be viewed as simply as a **fixed frequency homodyne receiver**, proceeded by a **frequency translation** (i.e., down-conversion) stage.



A Simple Super-Het Receiver Design

The **fixed** homodyne receiver (the one that we match the signal frequency to), is known as the **IF stage**. The fixed-frequency f_{IF} that this homodyne receiver is designed (and optimized!) for is called the **Intermediate Frequency (IF)**.

Q: *So what is the value of this Intermediate Frequency f_{IF} ? How does a receiver design engineer choose this value?*

A: Selecting the "IF frequency" value is perhaps the most important choice that a "super-het" receiver designer will make. It has many important ramifications, both in terms of performance and cost.

* We will discuss most of these ramifications later, but right now let's simply point out that the IF should be selected such that the cost and performance of the (IF) amplifier, (IF) filter, and detector/demodulator is good.

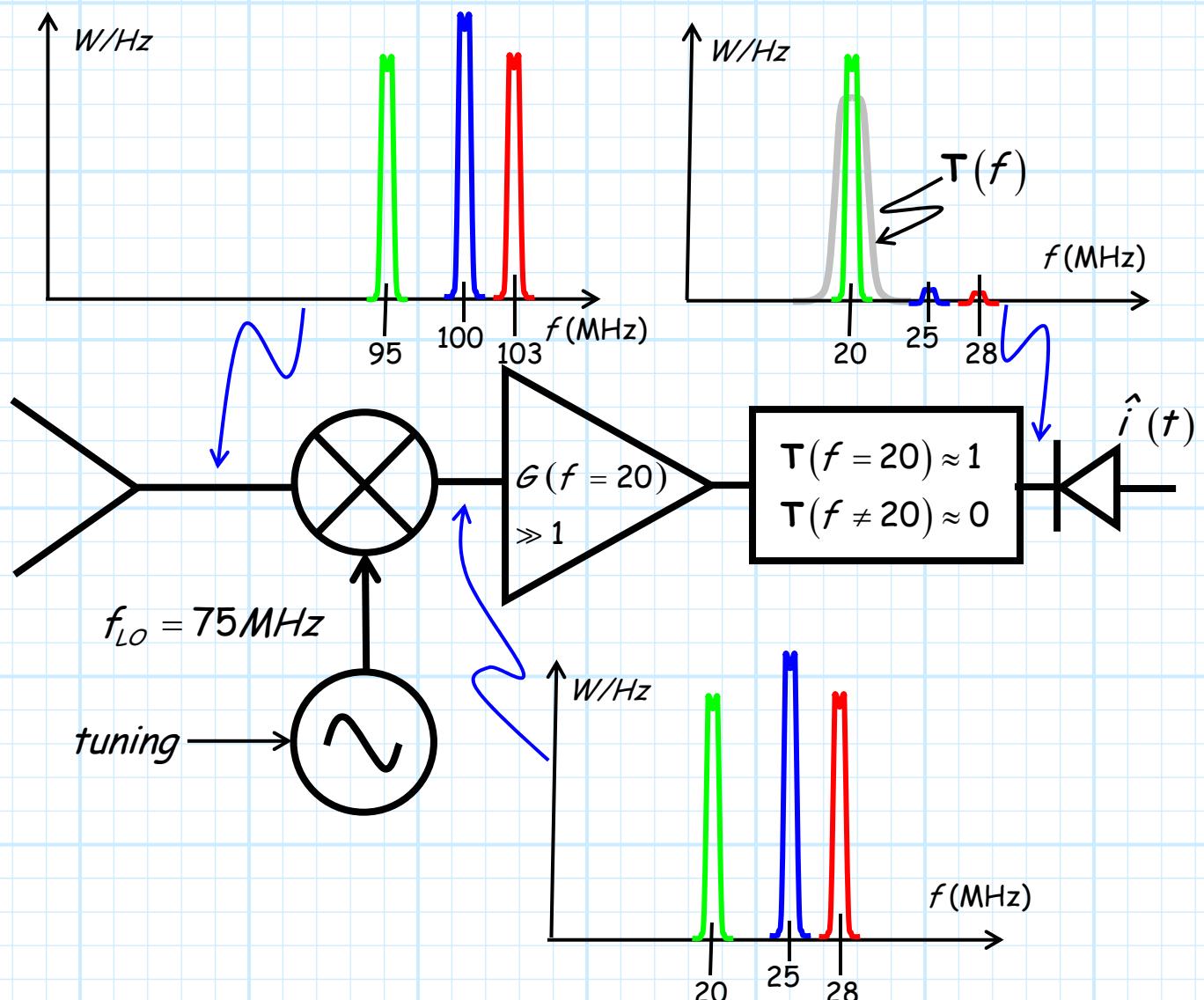
* Generally speaking, as we go **lower** in frequency, the cost of components go **down**, and their performance **increases** (these are both good things!). As a result, the IF frequency is **typically** (but **not always!**) selected such that it is much **less** (e.g., an order of magnitude or more) than the RF signal frequencies we are attempting to demodulate.

* Therefore, we typically use the mixer/LO to **down-convert** the signal frequency from its relatively **high RF frequency** to a relatively **low IF frequency**.

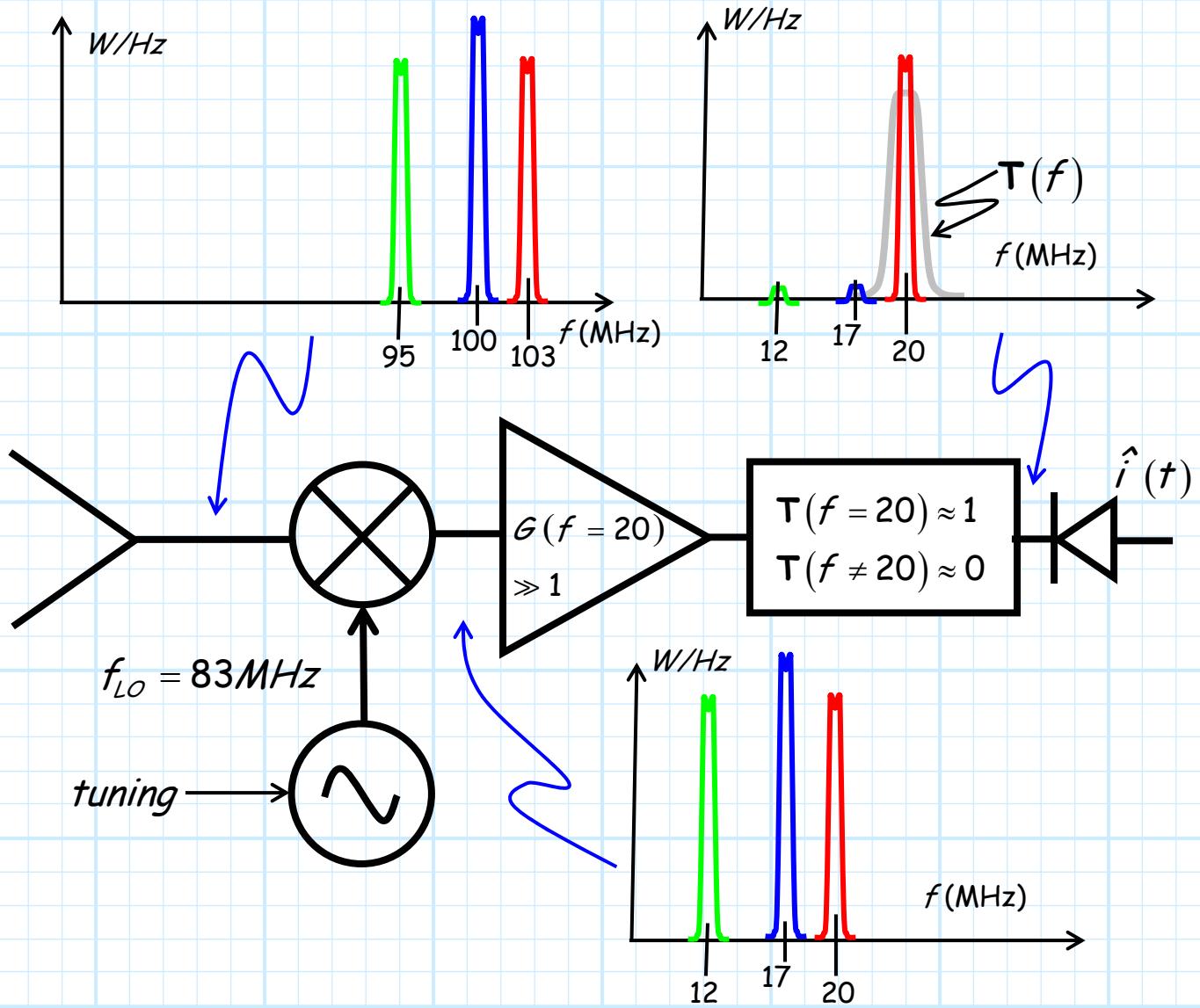
→ We are thus generally interested in the **second-order** mixer term $|f_{RF} - f_{LO}|$.

As a result, we must **tune** the LO so that $|f_s - f_{LO}| = f_{IF}$ —that is, if we wish to demodulated the RF signal at frequency f_s !

For **example**, say there exists radio signals (i.e., radio stations) at 95 MHz, 100 MHz, and 103 MHz. Likewise, say that the IF frequency selected by the receiver design engineer is $f_{IF} = 20 \text{ MHz}$. We can tune to the station at **95 MHz** by setting the Local Oscillator to $95 - 20 = 75 \text{ MHz}$:



Or, we could tune to the station at 103 MHz by tuning the Local Oscillator to $103 - 20 = 83$ MHz:



Q: Wait a second! You mean we need to **tune** an oscillator. How is that any **better** than having to **tune** an amplifier and/or filter?

A: Tuning the LO is **much** easier than tuning a band-pass filter. For an oscillator, we just need to change a **single** value—its **carrier frequency**! This can typically be done by changing a **single** component value (e.g., a **varactor diode**).

Contrast that to a **filter**. We must somehow change its center frequency, without altering its bandwidth, roll-off, or phase delay. Typically, this requires that **every** reactive element in the filter be altered or changed as we modify the center frequency (remember all those **control knobs!**!).

Q: *What about the IF filter? I understand that its **center frequency** is equal to the receiver Intermediate Frequency (f_{IF}), but what should its **bandwidth** Δf_{IF} be?*

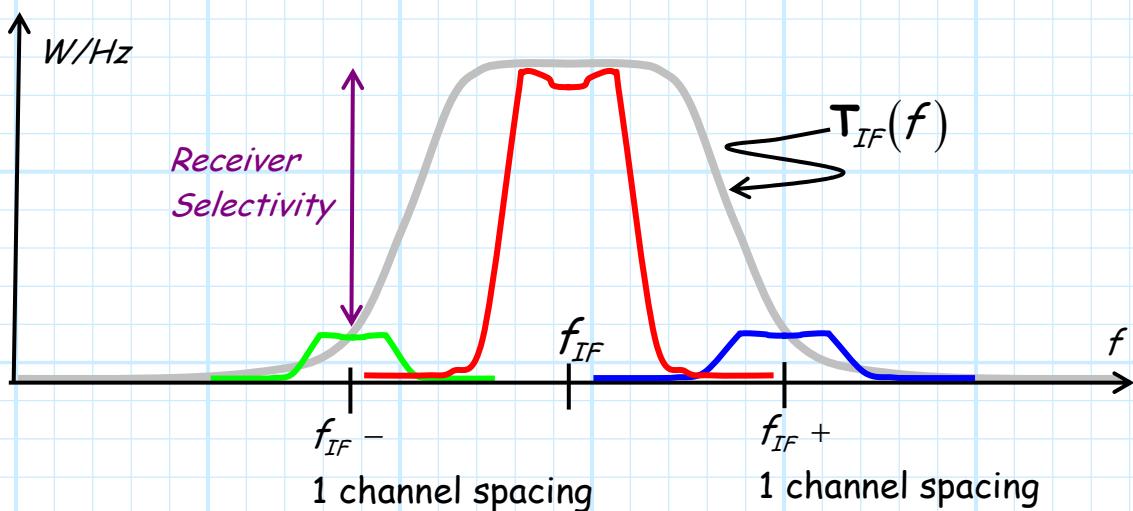
A: Remember, we want only **one** signal (the desired signal we tuned to) to appear at the demodulator, so the IF filter bandwidth should be **just** wide enough to allow for the desired signal bandwidth Δf_s . I.E.,:

$$\Delta f_{IF} = \Delta f_s$$

Q: *What about the filter "roll-off"? How much stop-band attenuation is required by the IF filter?*

A: The **most problematic** signals for the IF filter are the RF signals (e.g., radio stations) on either side of the desired RF signal frequency f_s .

These signals in **adjacent channels** are by definition very close in frequency to f_s , and thus are the most difficult to attenuate.



The attenuation of adjacent channels by the IF filter (in dB) defines **selectivity** of the receiver. Typically this value is between 30 dB and 60 dB.

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Super-Het Tuning

Say we wish to **recover** the information encoded on a radio signal operating at a RF frequency that we shall call f_s .

Recall that (typically) we must **down-convert** this signal to a lower IF frequency f_{IF} (i.e., $f_{IF} < f_s$), by tuning the LO frequency f_{LO} to a frequency such that this second-order equation:

$$|f_s - f_{LO}| = f_{IF}$$

is satisfied.

Note for a **given** f_s and f_{IF} , there are **two possible solutions** for the value of LO frequency f_{LO} :

$$\begin{aligned} f_s - f_{LO} &= \pm f_{IF} \\ -f_{LO} &= -f_s \pm f_{IF} \\ f_{LO} &= f_0 \mp f_{IF} \end{aligned}$$

Therefore, the two **down-conversion** solutions are:

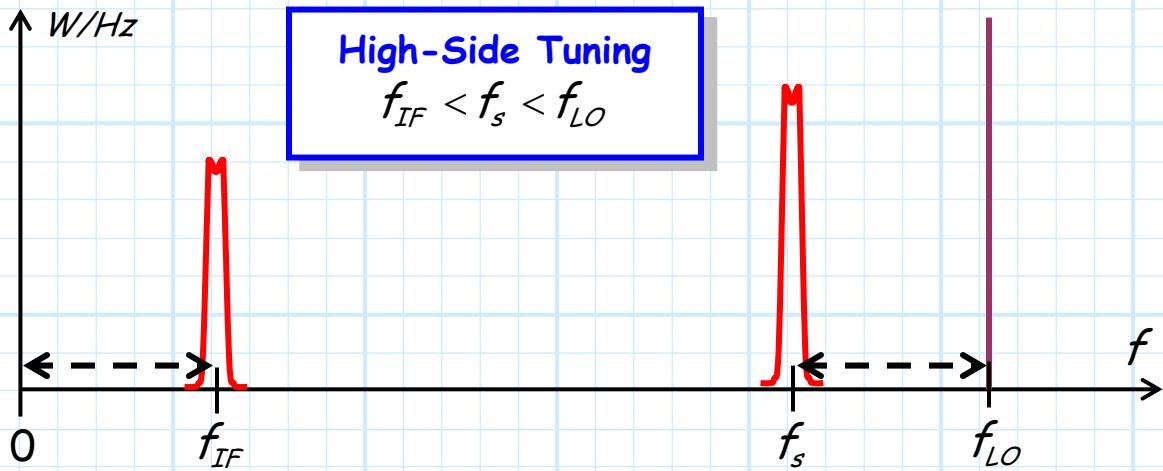
$$f_{LO} = f_s + f_{IF} \quad \text{OR} \quad f_{LO} = f_s - f_{IF}$$

In other words, the LO frequency f_{LO} should be set such that it is:

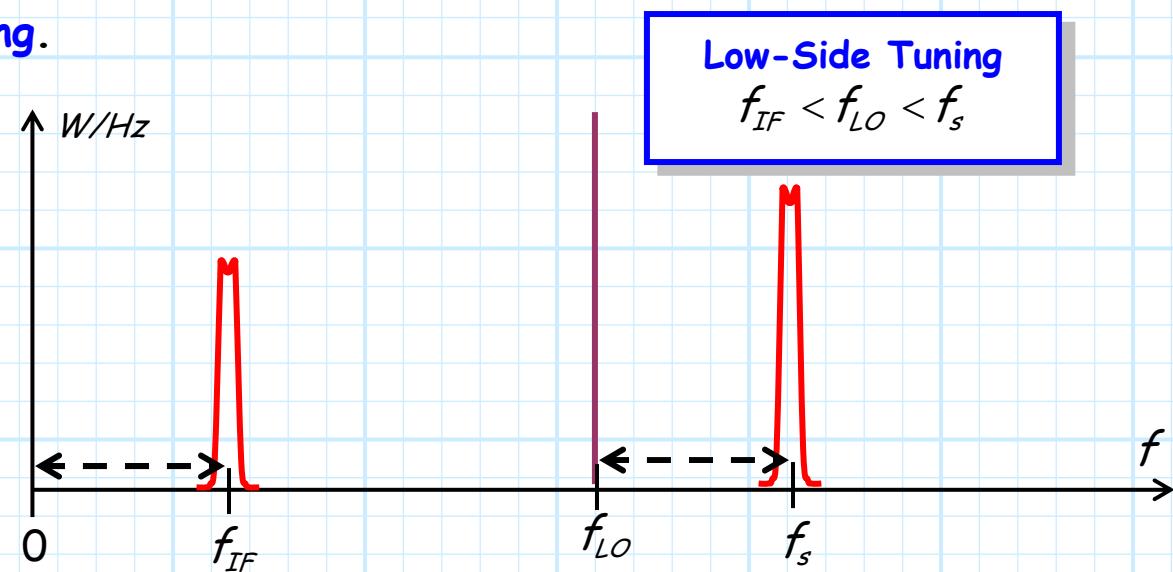
1) a value f_{IF} higher than the desired signal frequency
(i.e., $f_{LO} = f_s + f_{IF}$).

2) or, a value f_{IF} lower than the desired signal frequency
(i.e., $f_{LO} = f_s - f_{IF}$).

Note in the first case, the LO frequency will be **higher** than the signal frequency ($f_{LO} > f_s$). We call this solution **high-side tuning**.



For second case, the LO frequency will be **lower** than the signal frequency ($f_{LO} < f_s$). We call this solution **low-side tuning**.



For **example**, consider again the FM band. Say a radio engineer is designing an **FM radio**, and has selected an **IF** frequency of **30 MHz**. Since the FM band extends from **88 MHz** to **108 MHz** (i.e., $88 \text{ MHz} \leq f_s \leq 108 \text{ MHz}$), the radio engineer has two choices for LO bandwidth.

If she chooses **high-side tuning**, the LO bandwidth must be $f_{IF} = 30 \text{ MHz}$ **higher** than the RF bandwidth, i.e.:

$$\begin{aligned} 88 \text{ MHz} + f_{IF} &< f_{LO} < 108 \text{ MHz} + f_{IF} \\ 118 \text{ MHz} &< f_{LO} < 138 \text{ MHz} \end{aligned}$$

Alternatively, she can choose **low-side tuning**, with an LO bandwidth of:

$$\begin{aligned} 88 \text{ MHz} - f_{IF} &< f_{LO} < 108 \text{ MHz} - f_{IF} \\ 58 \text{ MHz} &< f_{LO} < 78 \text{ MHz} \end{aligned}$$

Q: Which of these two solutions should she choose?

A: It depends! Sometimes high-side tuning is better, other times low-side is the best choice. We shall see later that this choice affects spurious signal suppression. In addition, this choice affects the performance of our Local Oscillator (LO).

Let's look at the last consideration now. We'll be positive and look at the **advantages** of each solution:

Advantages of low-side tuning:

For low-side tuning, the LO will operate at **lower frequencies**, which generally results in:

1. Lower cost.
2. Slightly greater output power.
3. Lower phase-noise
4. Most importantly, lower frequency generally means better frequency accuracy.

Advantages of high-side tuning:

For high-side tuning, the LO will require a smaller **percentage bandwidth**, which generally results in:

1. Lower cost.
2. Lower phase-noise

Q: Percentage bandwidth? Just what does *that* mean?

A: Percentage bandwidth is simply the LO bandwidth Δf_{LO} , normalized to its center (i.e., average) frequency:

$$\% bw \doteq \frac{\Delta f_{LO}}{f_{LO} \text{ center frequency}}$$

For our example, **each** local oscillator solution (low-side and high-side) has a bandwidth of $\Delta f_{LO} = 20 \text{ MHz}$ (the same width as the FM band!).

However, the **center** (average) frequency of each solution is of course very different.

For **low-side** tuning:

$$\frac{58 + 78}{2} = 68 \text{ MHz}$$

And thus the **percentage bandwidth** is:

$$\% \text{ bandwidth} = \frac{20}{68} = 0.294 = 29.4\%$$

For **high-side** tuning:

$$\frac{118 + 138}{2} = 128 \text{ MHz}$$

And thus the **percentage bandwidth** is a far **smaller** value of:

$$\% \text{ bandwidth} = \frac{20}{128} = 0.156 = 15.6\%$$

A **really** wide LO bandwidth is generally **not** specified in terms of its % bandwidth, but instead in terms of the ratio of its highest and lowest frequency. For our examples, either:

$$\frac{78}{58} = 1.34$$

or

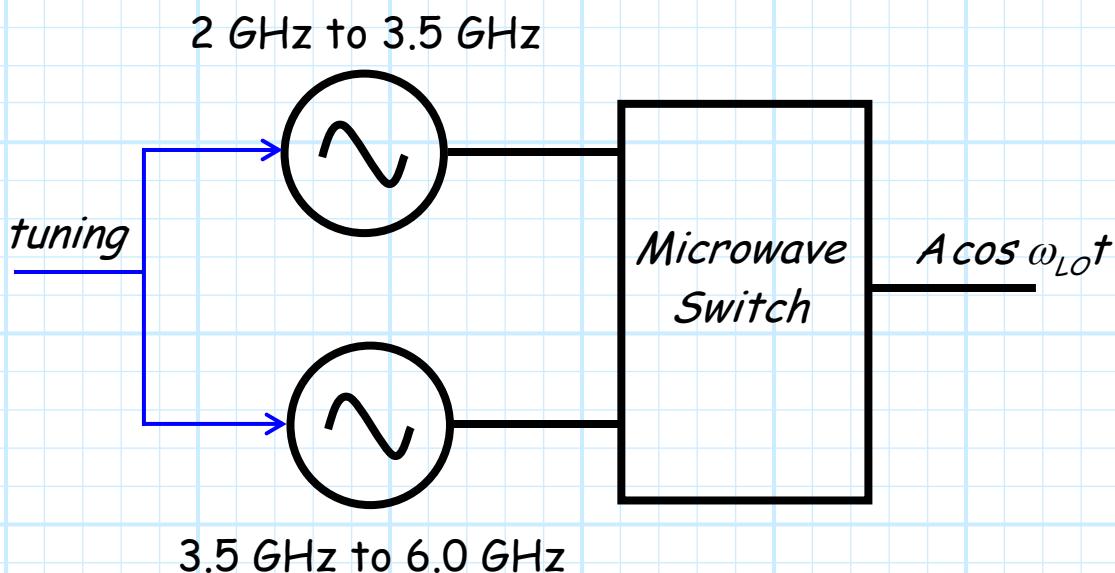
$$\frac{138}{118} = 1.17$$

Again, a **smaller** value is generally **better**.

If the LO bandwidth is **exceptionally** wide, this ratio can approach or exceed the value of 2.0. If the ratio is equal to 2.0, we say that the LO has an **octave** bandwidth (\rightarrow do you see why?).

Generally speaking, it is **difficult** to build a **single** oscillator with a octave or greater bandwidth. If our receiver design requires an octave or greater LO bandwidth, then the LO typically must be implemented using **multiple oscillators**, along with a microwave switch.

For example, an LO oscillator with a bandwidth from 2 to 6 GHz might be implemented as:



Q: You said that a lower frequency LO would provide **better accuracy**. Why is that? I thought that long-term stability (in ppm) would be relatively **constant** with respect to LO frequency.

A: Expressed in parts-per-million (ppm), it is!

But recall that ppm is essentially a **percentage** (i.e., geometric) error, whereas the importance value for receiver design is the **absolute** (ie., arithmetic) error in Hz!

Again consider the example. Say each LO solution (high-side and low-side) has a stability of ± 1.0 ppm (i.e., $1 \text{ Hz}/\text{MHz}$).

For the **low-side** solution, this means an **absolute error** ε_{LO} of:

$$\varepsilon_{LO} = 68 \text{ MHz} \left(\frac{\pm 1 \text{ Hz}}{\text{MHz}} \right) = \pm 68 \text{ Hz}$$

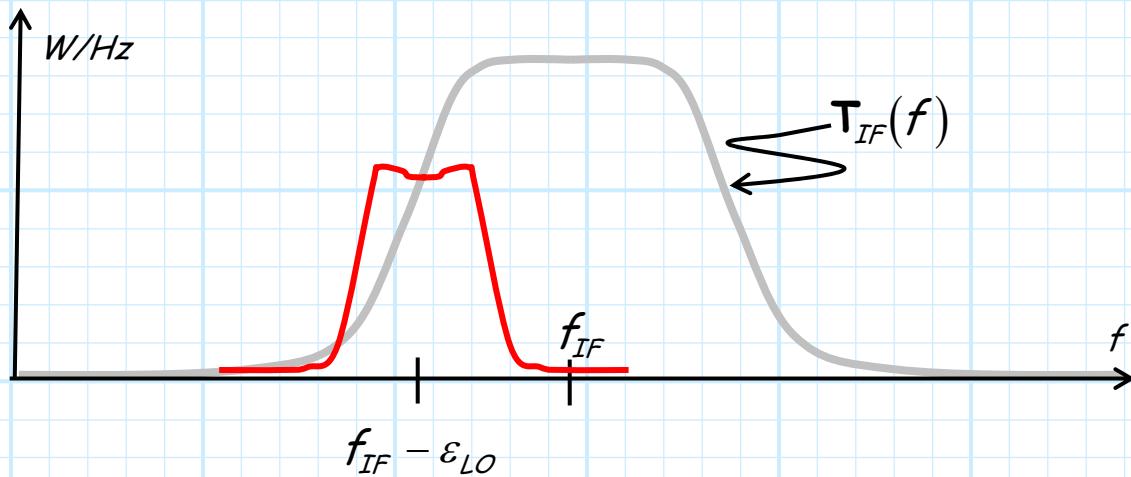
Whereas for **high-side**, the error is:

$$\varepsilon_{LO} = 128 \text{ MHz} \left(\frac{\pm 1 \text{ Hz}}{\text{MHz}} \right) = \pm 128 \text{ Hz}$$

The high-side solution has nearly **twice** as much error!

Q: How much LO accuracy do we **need**?

A: Remember, the LO must convert the desired RF signal to precisely the receiver IF frequency. If we are "off a little" then all or part of the desired signal might miss some of the narrowband IF filter!



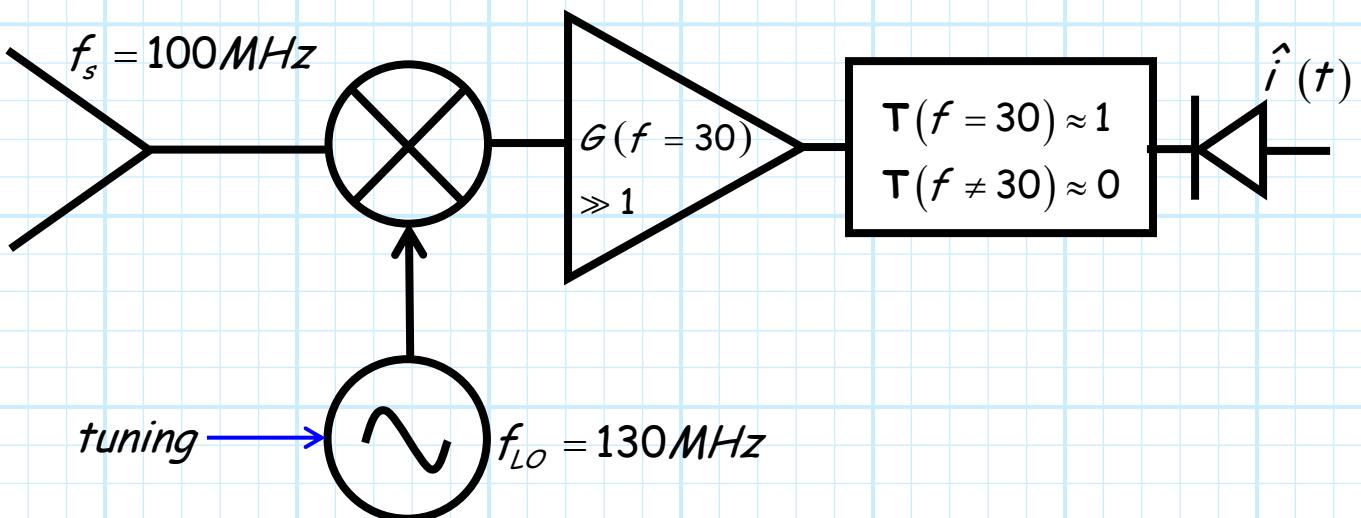
A designer "rule of thumb" is that the absolute LO **error** must be **less** than 10% of the IF filter **bandwidth**:

$$\epsilon_{LO} < 0.1 \Delta f_{IF}$$

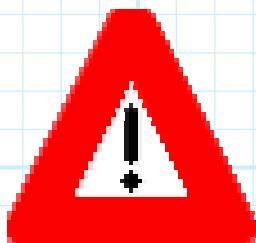
The Preselector Filter

Say we wish to **tune** a super-het receiver to receive a **radio station** broadcasting at 100 MHz .

If the receiver uses an **IF** frequency of $f_{IF} = 30 \text{ MHz}$, and uses **high-side tuning**, we must adjust the **local oscillator** to a frequency of $f_{LO} = 130 \text{ MHz}$.



Thus, the **desired RF signal will be down-converted to the IF frequency of 30 MHz .**



But **beware**, the desired radio station is **not** the only signal that will appear at the output of the mixer **at 30 MHz !**

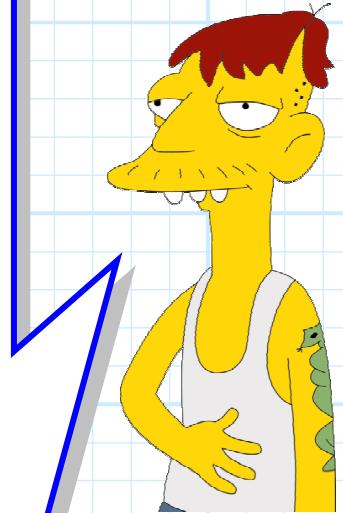
Q: Oh yes, we remember. The mixer will create all sorts of nasty, non-ideal **spurious signals at the mixer IF port**. Among these are signals at frequencies:

1st order: $f_{RF} = 100\text{MHz}$, $f_{LO} = 130\text{MHz}$

2nd order: $2f_{RF} = 200\text{MHz}$, $2f_{LO} = 260\text{MHz}$,
 $f_{RF} + f_{LO} = 230\text{MHz}$

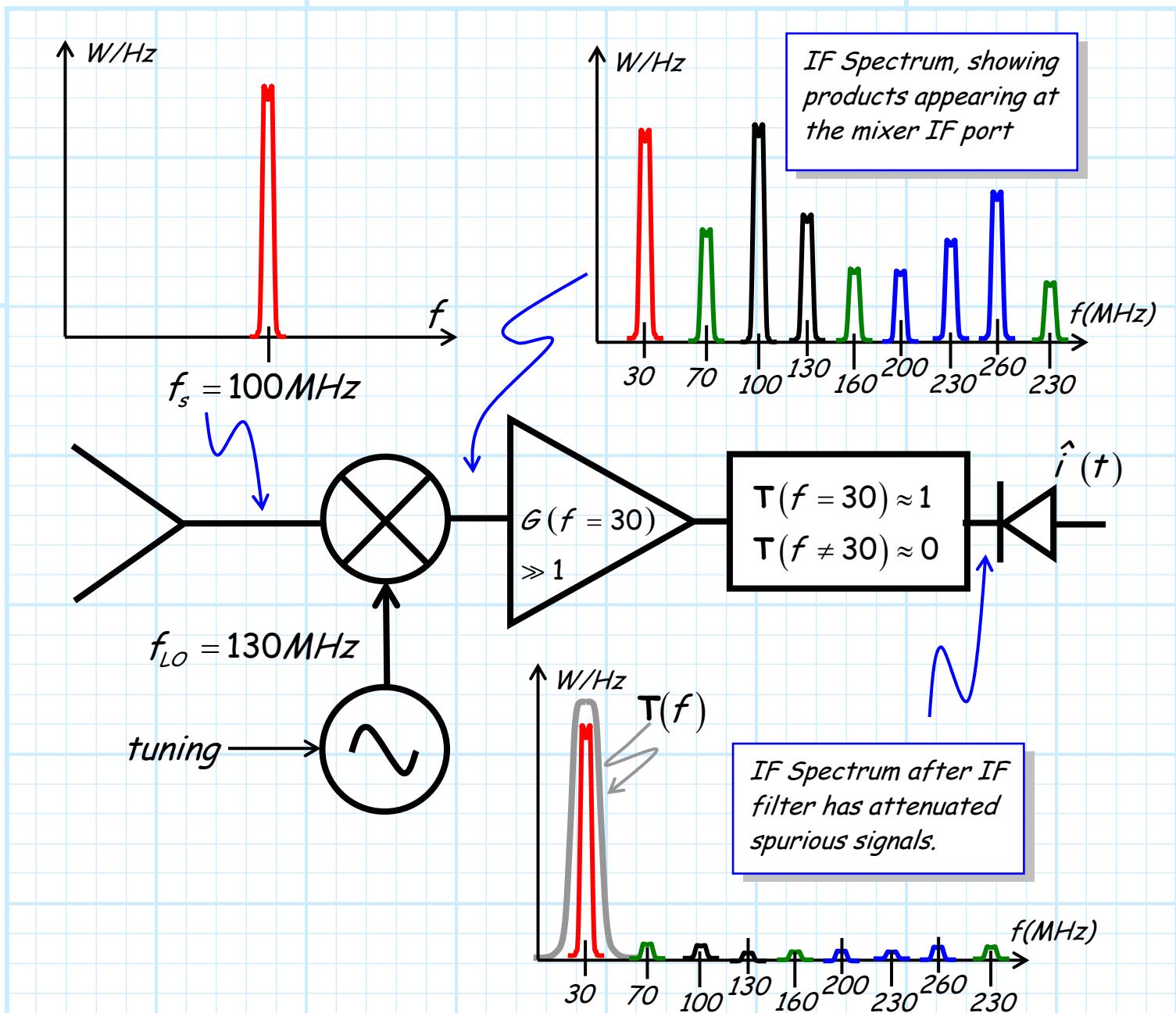
3rd order: $|2f_{RF} - f_{LO}| = 70\text{MHz}$,
 $|2f_{LO} - f_{RF}| = 160\text{MHz}$,
 $3f_{RF} = 300\text{MHz}$, $3f_{LO} = 390\text{MHz}$,
 $2f_{RF} + f_{LO} = 330\text{MHz}$,
 $f_{RF} + 2f_{LO} = 360\text{MHz}$

Right?



A: Not exactly. Although it is true that all of these products will exist at the **IF mixer port**—they will not pose any particular problem to us as radio engineers. The reason for this is that there is a narrow-band **IF filter** between the mixer IF port and the demodulator!

Look at the frequencies of the spurious signals created. They are all quite a bit larger than the filter center frequency of **30MHz**. All of the spurious signals are thus **rejected** by the filter—none (effectively) reach the detector/demodulator!



Now, look again at the statement I just made:

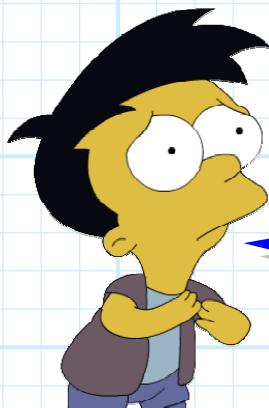


"But **beware** the desired radio station is **not** the only signal that will appear at the output of the mixer
AT 30 MHz!"

In other words, there can be **spurious signals** that appear **precisely at our IF frequency of 30 MHz**.

The IF filter will **not** of course filter **these** out (after all—they're at 30 MHz!), but instead let them pass through **unimpeded** to the demodulator.

The result → demodulated signal $\hat{i}(t)$ is an inaccurate, distorted mess!



Q: I'm just **totally baffled!**
Where do these unfilterable signals come from? How are they produced?

A: The answer is a **profound** one—an **incredibly important** fact that every radio engineer worth his or her salt must keep in mind at **all** times:



*The electromagnetic spectrum is full of radio signals. We **must** assume that the antenna delivers signals operating at **any** and **all** RF frequencies!*

In other words, we are only **interested** in a RF signal at 100 MHz; but that does **not** mean that other signals don't exist. **You** must always consider this fact!

Q: But I'm still confused. How do all these RF signals cause multiple signals precisely at our IF frequency?



A: Remember, each of the RF signals will mix with the LO drive signal, and thus each RF signal will produce its very own set of mixer products (1st order, 2nd order, 3rd order, etc.)

Here's the problem → some of these mixer products might lie at our IF frequency of 30 MHz!

To see which RF input signal frequencies will cause this problem, we must reverse the process of determining our mixer output products.

- * Recall earlier we started with known values of desired signal frequency (e.g., $f_s = 100$ MHz) and LO tuning frequency (e.g., $f_{LO} = 130$ MHz), and then determined all of the spurious signal frequencies created at the mixer IF port.
- * But now, we start with a known LO tuning frequency (e.g., $f_{LO} = 130$ MHz), and a known value of the receiver IF (e.g., $f_{IF} = 30$ MHz), and then we try to determine the frequency of the RF signal that would produce a spurious signal at precisely our receiver IF.

For **example**, let's start with the 3rd order product $|2f_{RF} - f_{LO}|$. In order for this product to be equal to the **receiver IF** frequency of 30 MHz, we find that:

$$|2f_{RF} - 130| = 30$$

$$2f_{RF} - 130 = \pm 30$$

$$2f_{RF} = 130 \pm 30$$

$$f_{RF} = \frac{130 \pm 30}{2}$$

$$f_{RF} = 50, 80$$

Thus, when attempting to "listen to" a radio station at $f_s=100$ MHz—by tuning the LO to $f_{LO}=130$ MHz—we find that radio stations at both **50 MHz** and **80 MHz** could **create** a 3rd order product at **30 MHz**—precisely at our **IF** filter center frequency!

But the **bad news** continues—there are **many** other mixer products to consider:

$$\underline{|2f_{LO} - f_{RF}|}$$

$$|2(130) - f_{RF}| = 30$$

$$260 - f_{RF} = \pm 30$$

$$\begin{aligned} f_{RF} &= 260 \mp 30 \\ &= 290, 230 \end{aligned}$$

$$\underline{2f_{LO} + f_{RF}}$$

$$2(130) + f_{RF} = 30$$

$$260 + f_{RF} = 30$$

$$\begin{aligned} f_{RF} &= 30 - 260 \\ &= -230 \end{aligned}$$

Q: What?! A radio station operating at a **negative** frequency of -230 MHz? Does this have any meaning?



A: Not in any **physical** sense! We ignore any **negative** frequency solutions—they are **not** a concern to us.

$$\underline{2f_{RF} + f_{LO}}$$

$$2f_{RF} + f_{LO} = 30$$

$$2f_{RF} + 130 = 30$$

$$f_{RF} = \frac{30 - 130}{2}$$

$$f_{RF} = -50$$

Again, a **negative** solution that we can ignore.

$$\underline{3f_{RF}}$$

$$3f_{RF} = 30$$

$$f_{RF} = \frac{30}{3}$$

$$f_{RF} = 10$$

OK, that's all the 3rd order products, now let's consider the second-order terms:

$$\underline{|f_{LO} - f_{RF}|}$$

$$|130 - f_{RF}| = 30$$

$$130 - f_{RF} = \pm 30$$

$$\begin{aligned} f_{RF} &= 130 \mp 30 \\ &= 100, 160 \end{aligned}$$

- * Note that this term is the term created by an **ideal** mixer. As a result, we find that **one** of the RF signals that will create a mixer product at 30 MHz is $f_{RF} = 100 \text{ MHz}$ - the frequency of the **desired** radio station !

- * However, we find that even this **ideal** mixer term causes **problems**, as there is a **second** solution. An RF signal at **160 MHz** would likewise result in a mixer product at 30 MHz— even in an **ideal** mixer!



We will find this **second** solution to this **ideal** mixer (i.e., down-conversion) term can be particularly **problematic** in receiver design. As such, this solution is given a specific name—the **image frequency**.

For this example, 160 MHz is the **image frequency** when we tune to a station at 100 MHz.

$$\underline{f_{LO} + f_{RF}}$$

$$130 + f_{RF} = 30$$

$$130f_{RF} = 30 - 130 \quad \text{No problem here!}$$

$$f_{RF} = -100$$

$$\underline{2f_{RF}}$$

$$2f_{RF} = 30$$

$$f_{RF} = \frac{30}{2}$$

$$f_{RF} = 15$$

Finally, we must consider one 1st order term:

$$\underline{f_{RF}}$$

$$f_{RF} = 30$$

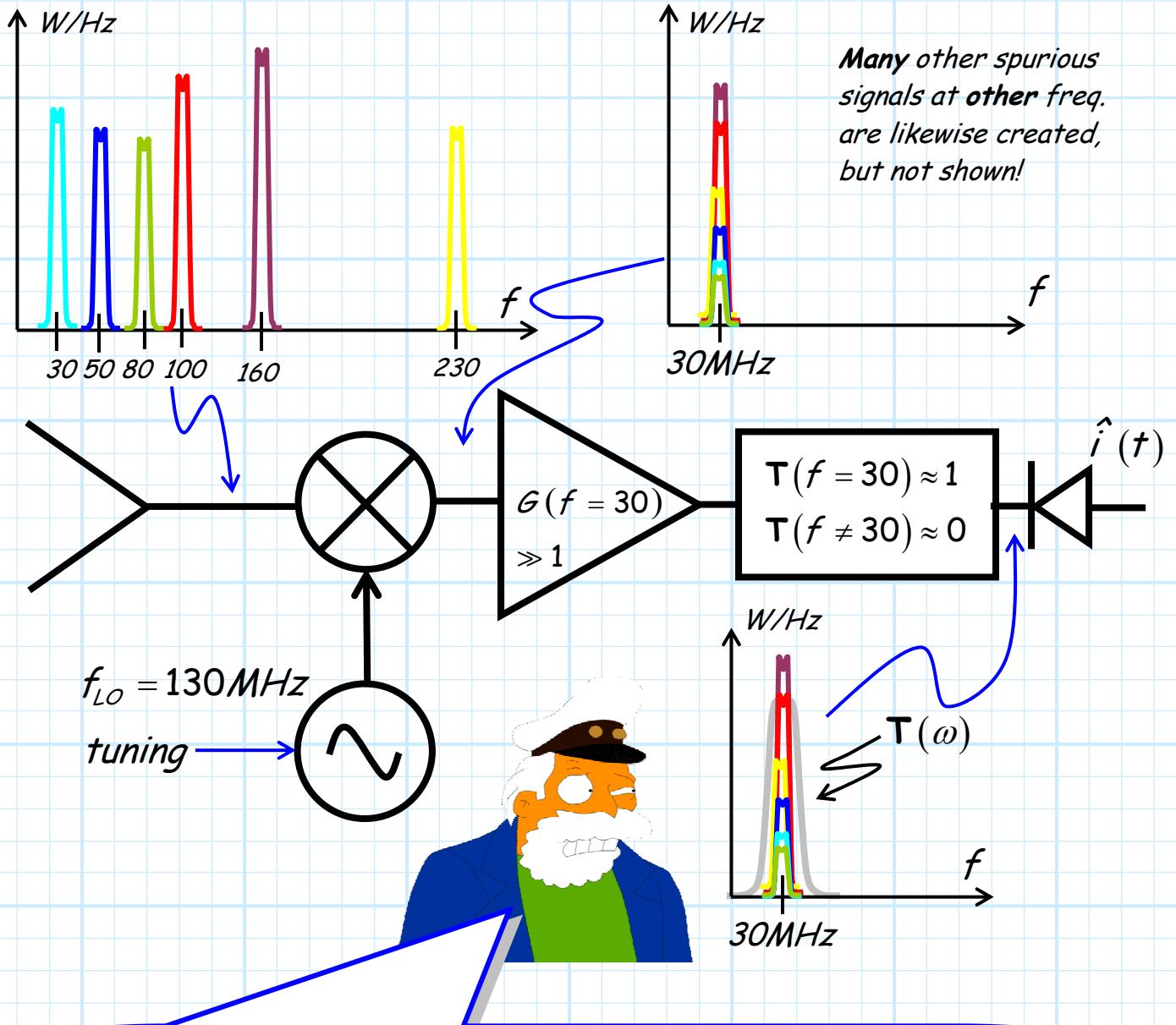
In other words, an RF signal at 30 MHz can "leak" through the mixer (recall mixer **RF isolation**) and appear at the IF port—after that there's no stopping it until it reaches the demodulator!

In summary, we have found that that:

- 1.** An RF signal (e.g., radio station) at **30 MHz** can cause a **1st-order** product at our IF filter frequency of 30 MHz.

- 2.** RF signals (e.g., radio stations) at either **15 MHz** or **160 MHz** can cause a **2nd -order** product at our IF filter frequency of 30 MHz.

3. RF signals (e.g., radio stations) at 10 MHz, 50MHz, 80 MHz, 230 MHz, or 290 MHz can cause a 3rd -order product at our IF filter frequency of 30 MHz.



Q: Arrrg! I now see the problem! There is no way to separate the spurious signals at the IF frequency of 30 MHz from the desired station at 30 MHz. Clearly, your hero E.H. Armstrong was wrong about this Super-Heterodyne receiver design!



There is an **additional element** of Armstrong's super-het design that we have **not** yet discussed.

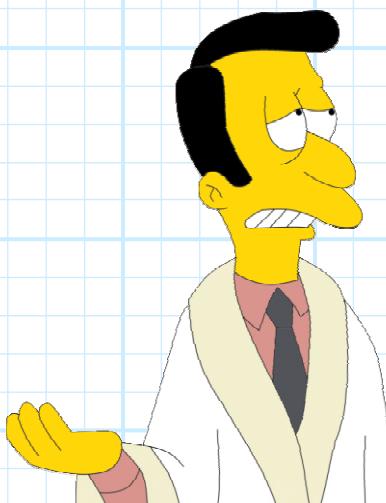
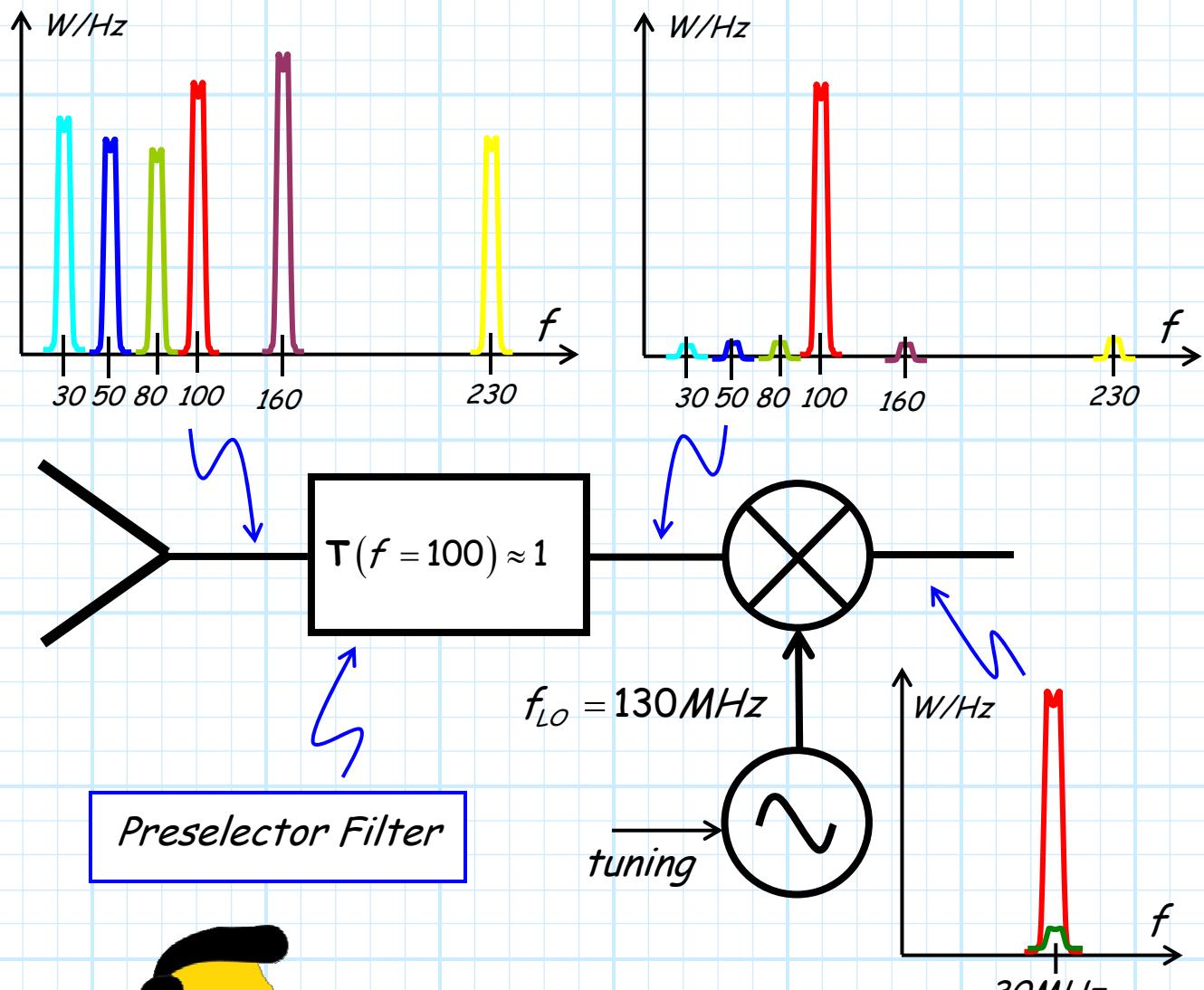
→ The preselector filter.

The **ONLY** way to keep the mixer from **creating** spurious signals at the receiver IF is to **keep** the signals that produce them from the mixer RF port!

Of course, we must **simultaneously** let the desired station reach the mixer.



A: That's correct! By inserting a **preselector filter** between the antenna and the mixer, we can **reject** the signals that create spurious signals at our IF center frequency, while **allowing** the desired station to pass through to the mixer unimpeded.



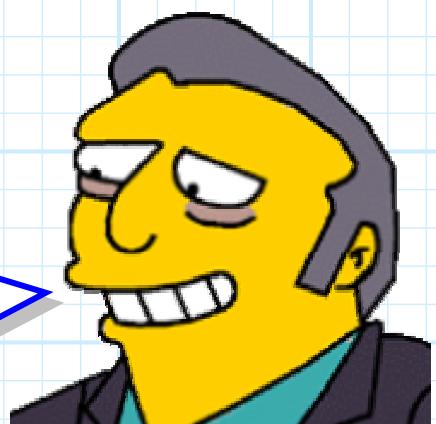
Q: So how *wide* should we make the *pass-band* of the preselector filter?

A: The pass-band of the preselector filter must be just wide enough to allow any and all potential **desired** signals to pass through.

- * Consider our **example** of $f_s = 100$ MHz. This signal is **smack-dab** in the middle of the **FM radio band**, and so let's assume it is an **FM radio station** (if it were, it would actually be at frequency 100.1 or 99.9 MHz).
- * If we are interested in tuning to **one** FM station, we might be interested in tuning into **any** of the others, and thus the preselector filter pass-band **must** extend from 88 MHz to 108 MHz (i.e., the FM band).
- * Note we would **not** want to extend the pass-band of the preselector filter any wider than the FM band, as we are (presumably) **not** interested in signals outside of this band, and those signals could **potentially** create spurious signals at our IF center frequency!

As a result, we find that the **preselector filter** effectively defines the **RF bandwidth** of a super-heterodyne receiver.

Q: OK, **one** last question. When calculating the products that could create a spurious signal **at the IF center frequency**, you **neglected** the terms f_{LO} , $2f_{LO}$ and $3f_{LO}$. Are these terms **not** important?



A: They are actually **very important!** However, the value of f_{LO} is **not** an unknown to be solved for, but in fact was (for our example) a **fixed** value of $f_{LO} = 130\text{MHz}$.

Thus, $2f_{LO} = 260\text{MHz}$, and $3f_{LO} = 390\text{MHz}$ —none of these are anywhere near the **IF** center frequency of 30 MHz, and so these products are easily **rejected** by the **IF filter**. However, this need not **always** be true!

- * Consider, for example, the case where we again have designed a receiver with an IF center frequency of 30 MHz. This time, however, we desire to tune to radio signal operating at 60 MHz.
- * Say we use **low-side** tuning in our design. In that case, the LO signal frequency must be $f_{LO} = 60 - 30 = 30\text{MHz}$.
- * Yikes! You **must** see the problem! The Local Oscillator frequency is **equal** to our IF center frequency ($f_{LO} = f_{IF}$). The LO signal will “leak” through mixer (recall mixer LO isolation) and into the IF, where it will pass **unimpeded** by the IF filter to the demodulator (this is a **very bad thing**).

Thus, when designing a receiver, it is **unfathomably important** that the LO frequency, along with **any** of its harmonics, lie **nowhere** near the **IF** center frequency!

Image and Third-Order Signal Rejection

Recall in a previous handout the **example** where a receiver had an IF frequency of $f_{IF} = 30 \text{ MHz}$. We desired to demodulate a radio station operating at $f_s = 100 \text{ MHz}$, so we set the LO to a frequency of $f_{LO} = 130 \text{ MHz}$ (i.e., high-side tuning).

We discovered that RF signals at many **other** frequencies would likewise produce signals at **precisely** the receiver IF frequency of 30 MHz—a **very** serious problem that can only be solved by the addition of a **preselector filter**.

Recall that this preselector filter **must** allow the **desired** signal (or band of signals) to pass through **unattenuated**, but likewise must sufficiently **reject** (i.e., attenuate) all the RF signals that could create **spurious** signals at the IF frequency.

We found for this **example** that these **annoying** RF signals reside at frequencies:

10 MHz, 15 MHz, 30 MHz, 80 MHz,
160 MHz, 230 MHz, and 290 MHz

Note that the most **problematic** of these RF signals are the two at **80 MHz** and **160 MHz**.

Q: Why do these two signals pose the greatest problems?

A: Because the frequencies 80 MHz and 160 MHz are the closest to the desired signal frequency of 100 MHz. Thus, they must be the closest to the pass-band of the preselector filter, and so will be attenuated the least of all the RF signals in the list above.

As a result, the 30 MHz mixer products produced by the RF signals at 80 MHz and 160 MHz will be likely be larger than those produced by the other problem frequencies—they are the ones most need to worry about!

Let's look closer at each of these two signals.

Image Frequency Rejection

We determined in an earlier handout that the radio frequency signal at 160 MHz was the RF image frequency for this particular example.

Recall the RF image frequency is the other f_{RF} solution to the (ideal) second-order mixer term $|f_{RF} - f_{LO}| = f_{IF}$! I.E.:

$$\begin{aligned}|f_{RF} - f_{LO}| &= f_{IF} \\ f_{RF} - f_{LO} &= \pm f_{IF} \\ f_{RF} &= f_{LO} \pm f_{IF}\end{aligned}$$

For low-side tuning, the desired RF signal is (by definition) the solution that is greater than f_{LO} :

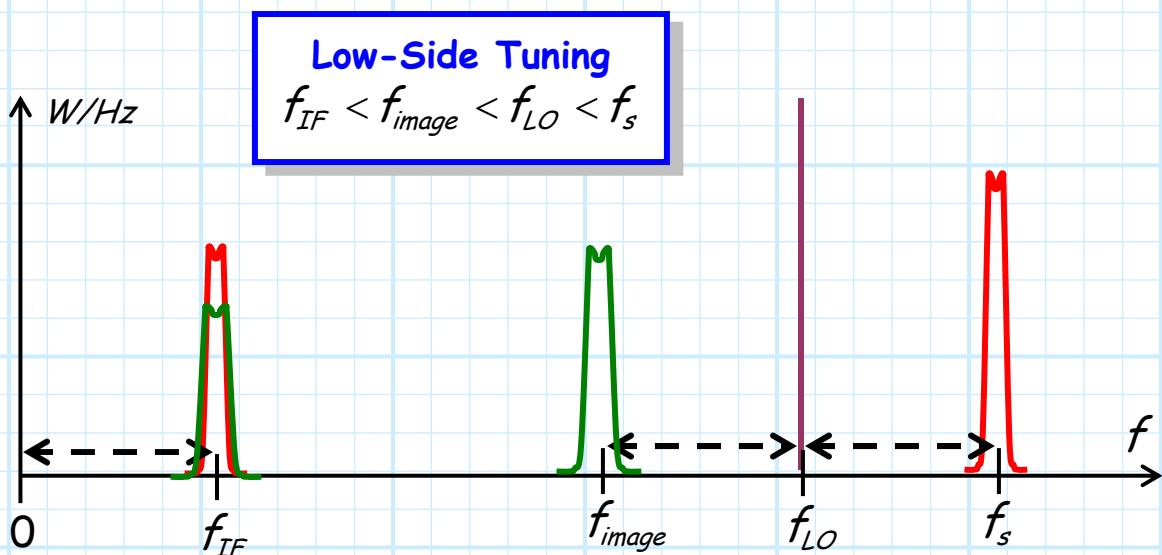
$$f_{LO} = f_s - f_{IF} \Rightarrow f_s = f_{LO} + f_{IF} \quad (\text{low-side tuning})$$

And thus—for low-side tuning—the RF **image** signal is the solution that is less than f_{LO} :

$$f_{\text{image}} = f_{LO} - f_{IF}$$

Using the fact that for low-side tuning $f_{LO} = f_s - f_{IF}$, we can likewise express the RF **image** frequency as:

$$\begin{aligned} f_{\text{image}} &= f_{LO} - f_{IF} \\ &= (f_s - f_{IF}) - f_{IF} \\ &= f_s - 2f_{IF} \end{aligned}$$



And thus in summary:

$$\begin{aligned} f_{\text{image}} &= f_{\text{LO}} - f_{\text{IF}} \\ &= f_s - 2f_{\text{IF}} \end{aligned} \quad (\text{low-side tuning})$$

Similarly, for **high-side tuning**, the **desired RF signal** is (by definition) the solution that is **less** than f_{LO} :

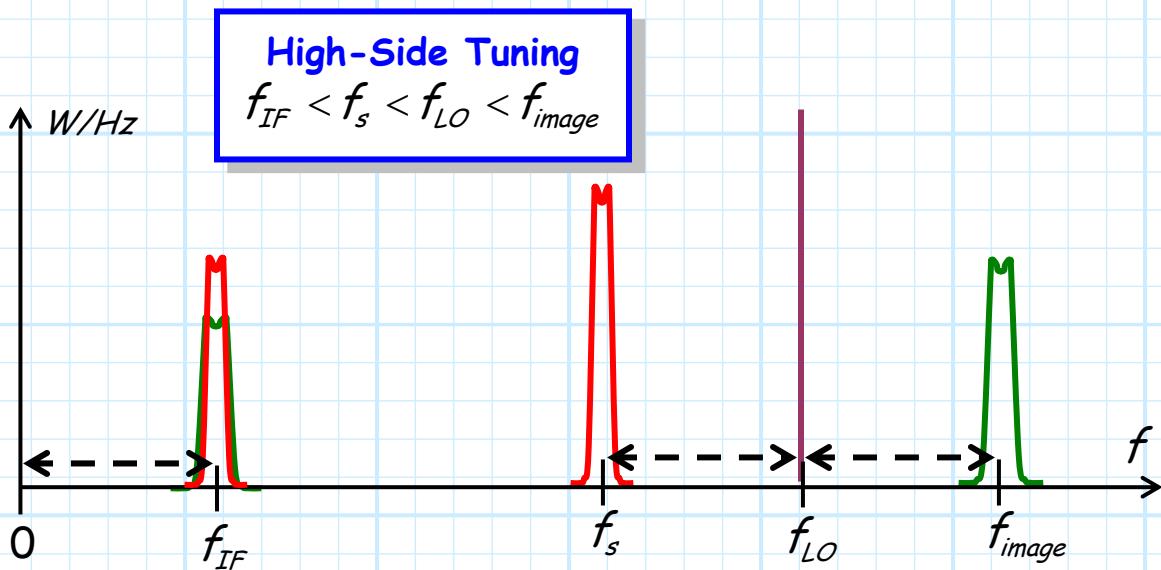
$$f_{\text{LO}} = f_s + f_{\text{IF}} \Rightarrow f_s = f_{\text{LO}} - f_{\text{IF}} \quad (\text{high-side tuning})$$

And thus—for high-side tuning—the **RF image** signal is the solution that is **greater** than f_{LO} :

$$f_{\text{image}} = f_{\text{LO}} + f_{\text{IF}}$$

Using the fact that for high-side tuning $f_{\text{LO}} = f_s + f_{\text{IF}}$, we can likewise express the **RF image** frequency as:

$$\begin{aligned} f_{\text{image}} &= f_{\text{LO}} + f_{\text{IF}} \\ &= (f_s + f_{\text{IF}}) + f_{\text{IF}} \\ &= f_s + 2f_{\text{IF}} \end{aligned}$$



And thus in summary:

$$\begin{aligned}
 f_{image} &= f_{LO} + f_{IF} \\
 &= f_s + 2f_{IF}
 \end{aligned}
 \quad (\text{high-side tuning})$$

Note for both high-side and low-side tuning, the difference between the desired RF signal and its RF image frequency is $2f_{IF}$:

$$|f_{RF} - f_{image}| = 2f_{IF}$$

This is a **very important result**, as it says that we can **increase** the "distance" between a desired RF signal and its image frequency by simply **increasing** the IF frequency of our receiver design!

For **example**, again consider the FM band (88 MHz to 108 MHz). Say we decide to design an FM radio with an IF of 20 MHz, using **high-side tuning**.

Thus, the **LO bandwidth** must extend from:

$$\begin{aligned}88 + f_{IF} &< f_{LO} < 108 + f_{IF} \\88 + 20 &< f_{LO} < 108 + 20 \\108 &< f_{LO} < 128\end{aligned}$$

The **RF image bandwidth** is therefore:

$$\begin{aligned}108 + f_{IF} &< f_{image} < 128 + f_{IF} \\108 + 20 &< f_{image} < 128 + 20 \\128 &< f_{image} < 148\end{aligned}$$

Thus, the **preselector filter** for this FM radio must have pass-band that extends from 88 to 108 MHz, but must also sufficiently **attenuate** the image signal band extending from 128 to 148 MHz.

Note that 128 MHz is **very close** to 108 MHz, so that attenuating the signal may be **very difficult**.

Q: *By how much do we need to attenuate these image signals?*

A: A very good question; one that leads to a very important point. Since the image frequency creates the same second-order product as the desired signal, the conversion loss associated with each signal is precisely the same (e.g. 6 dB)!

As a result, the IF signal created by image signals will typically be just as large as those created by the desired FM station.

This means that we must greatly attenuate the image band, typically by 40 dB or more!

Q: Yikes! It sounds like we might require a filter of very high order!?

A: That's certainly a possibility. However, we can always reduce this required preselector filter order if we simply increase our IF design frequency!

To see how this works, consider what happens if we increase the receiver IF frequency to $f_{IF} = 40\text{MHz}$. For this new IF, the LO bandwidth must increase to:

$$\begin{aligned} 88 + f_{IF} &< f_{LO} < 108 + f_{IF} \\ 88 + 40 &< f_{LO} < 108 + 40 \\ 128 &< f_{LO} < 148 \end{aligned}$$

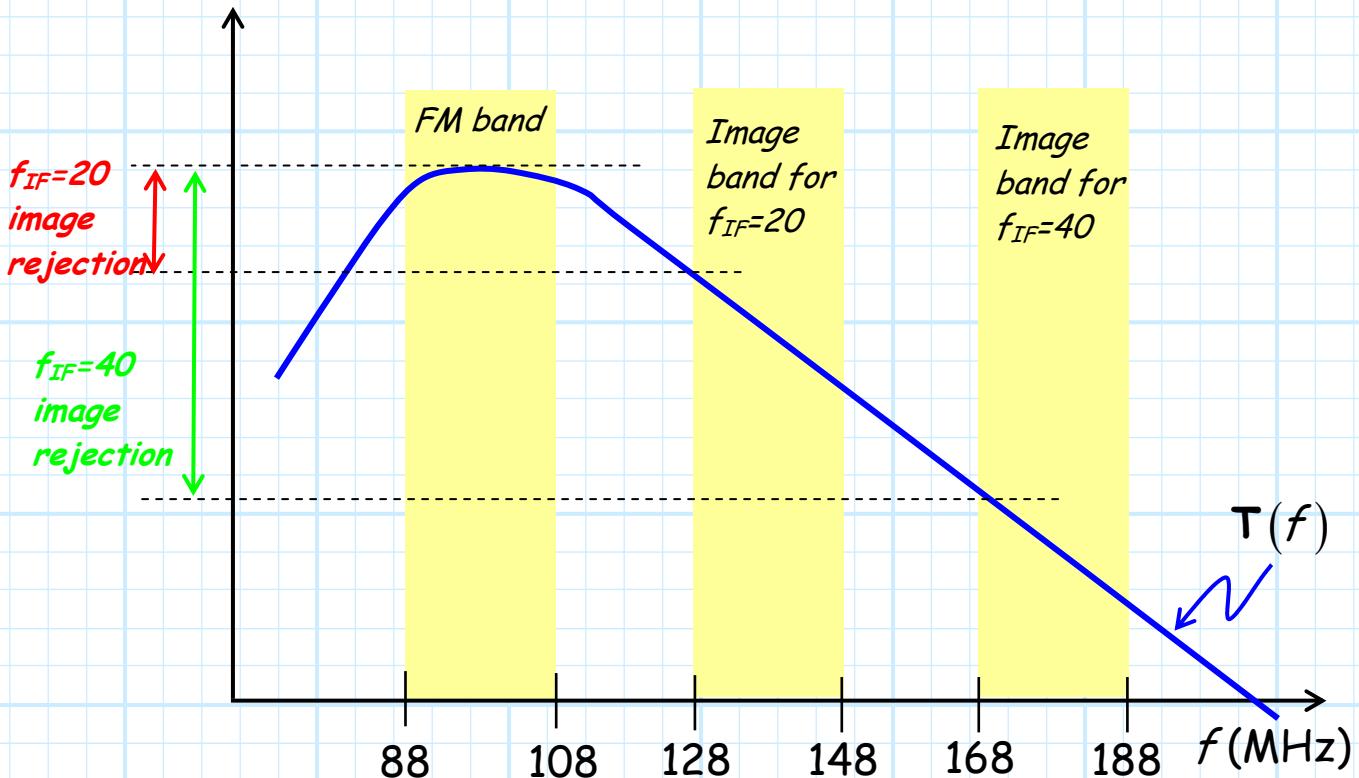
The new RF image bandwidth has therefore increased to:

$$108 + f_{IF} < f_{image} < 128 + f_{IF}$$

$$128 + 40 < f_{image} < 148 + 40$$

$$168 < f_{image} < 188$$

Note this image band is now much higher in frequency than the FM band—and thus much more **easily filtered!**



The amount by which the preselector attenuates the image signals is known as the **image rejection** of the receiver.

For **example**, if the preselector filter attenuates the image band by at least 50 dB, we say that the receiver has 50 dB of **image rejection**.

So by increasing the receiver IF frequency, we can either get greater image rejection from the same preselector filter order, or we can reduce the preselector filter order while maintaining sufficient image rejection.

But be careful! Increasing the IF frequency will also tend to increase cost and reduce detector performance.

3rd-Order Signal Rejection

In addition to the image frequency (the other solution to the second order term $|f_{RF} - f_{LO}| = f_{IF}$), the other radio signals that are particularly difficult to reject are the f_{RF} solutions to the 3rd-order product terms $|2f_{RF} - f_{LO}| = f_{IF}$ and $|2f_{LO} - f_{RF}| = f_{IF}$.

There are four possible RF solutions (two for each term):

$$f_1 = \frac{f_{LO} + f_{IF}}{2} \quad f_3 = 2f_{LO} + f_{IF}$$

$$f_2 = \frac{f_{LO} - f_{IF}}{2} \quad f_4 = 2f_{LO} - f_{IF}$$

Each of these four solutions represents the frequency of a radio signal that will create a 3rd-order product precisely at the receiver IF frequency, and thus all four must be adequately rejected by the preselector filter!

However, solutions f_1 and f_4 will **typically*** be the most problematic (i.e., closest to the desired RF frequency band). For instance, in our original **example**, the "problem" signal at 80 MHz is the term f_1 (i.e., $f_1 = 80 \text{ MHz}$).

For **low-side tuning**, where $f_{LO} = f_s - f_{IF}$, these 3rd-order RF solutions can likewise be expressed as:

$$\mathbf{f}_1 = \frac{f_s}{2} \quad f_3 = 2f_s - f_{IF}$$

(low-side tuning)

$$f_2 = \frac{f_s - 2f_{IF}}{2} \quad \mathbf{f}_4 = 2f_s - 3f_{IF}$$

And for **high-side tuning**, where $f_{LO} = f_s + f_{IF}$, these 3rd-order RF solutions can likewise be expressed as:

$$\mathbf{f}_1 = \frac{f_s + 2f_{IF}}{2} \quad f_3 = 2f_s + 3f_{IF}$$

(high-side tuning)

$$f_2 = \frac{f_s}{2} \quad \mathbf{f}_4 = 2f_s + f_{IF}$$

* Note that "typically" does **not** mean "always".

Of course, in a **good** receiver design the **preselector filter** will attenuate these problematic RF signals before they reach the mixer RF port.

The amount by which the preselector attenuates these 3rd-order solutions is known as the **3rd-order signal rejection** of the receiver.

Q: *By how much do we need to attenuate these signals?*

A: Since these signals produce 3rd-order mixer products, the IF signal power produced is generally much **less** than that of the (2nd order) image signal product. As a result, we can at times get by with as little as 20 dB of 3rd-order signal rejection—but this **depends** on the mixer used.

Q: *Just 20 dB of rejection? It sounds like achieving this will be a "piece of cake"—at least compared with satisfying the image rejection requirement!*

A: Not so fast! Often we will find that these 3rd-order signals will be **very close** to the **desired RF band**. In fact (if we're not careful when designing the receiver) these 3rd-order signals can lie **inside** the desired RF band—then they **cannot** be attenuated at all!

Thus, rejecting these 3rd order radio signals can be as difficult (or even **more** difficult) than rejecting the image signal.

Q: We found earlier that by *increasing the IF frequency*, we could make the *image rejection* problem much easier. Is there a *similar solution* to improving 3rd order signal rejection?

A: Yes there is—but you won't like this answer!

Look at **these** RF solutions for the 3rd-order mixer terms:

$$f_4 = 2f_s - 3f_{IF} \quad (\text{low-side tuning})$$

and:

$$f_1 = \frac{f_s + 2f_{IF}}{2} \quad (\text{high-side tuning})$$

From these solutions, it is evident that some 3rd-order RF solutions can be moved **away** from the desired RF band (thus making them **easier** to filter) by **decreasing** the IF frequency.

This solution of course is exactly **opposite** of the method used to improve image rejection. Thus, there is a **conflict** between the two design goals. It is **your** job as a receiver designer to arrive at the best possible **design compromise**, providing both sufficient image **and** 3rd-order signal rejection.

→ Radio Engineering is **not easy**! ←

Up-Conversion

Typically, we **down-convert** a desired RF signal at frequency f_s to a **lower** Intermediate Frequency (IF), such that:

$$f_{IF} < f_s$$

This down-conversion is a result of the ideal **2nd-order** mixer term:

$$|f_s - f_{LO}| = f_{IF} \quad \therefore f_{IF} < f_s$$

Recall, however, that there is a **second** ideal **2nd-order** mixer term:

$$f_s + f_{LO} = f_{IF} \quad \therefore f_{IF} > f_s$$

Note that the resulting frequency f_{IF} is **greater** than the original RF signal frequency f_s . This term produces an **up-conversion** f_s to a **higher** frequency f_{IF} .

The **tuning solution** for this up-conversion term is (**given** f_s and f_{IF}):

$$f_{LO} = f_{IF} - f_s \quad \therefore f_{IF} > f_{LO}$$

Note that unlike its down-conversion counterpart, the up-conversion term only has **one solution**!

Q: So, there is no such thing as **high-side tuning** or **low-side tuning** for up-conversion?

A: Yes and no. There is only **one** tuning solution, so we **do not choose** whether to implement a **high-side** solution ($f_{LO} > f_s$) or a **low-side** solution ($f_{LO} < f_s$).

Instead, the single solution $f_{LO} = f_{IF} - f_s$ will "choose" for us!

This solution for f_{LO} will either be greater than f_s (i.e., high-side), or less than f_s (i.e., low-side). Hopefully is apparent to you that a low-side solution will result if $f_{IF}/2 < f_s < f_{IF}$, whereas a high-side solution must occur if $0 < f_s < f_{IF}/2$.

Occasionally receivers **are** designed that indeed use up-conversion instead of down conversion!

Q: But wouldn't the IF frequency for these receivers be very high??

A: That's correct! The IF of an up-conversion receiver might be in the range of 1-6 GHz—or even higher!

Q: But that would seemingly **increase cost** and **reduce performance**. Why would a receiver designer do that?

A: Let's examine the frequencies (f_{RF}) of any **RF** signals that would create spurious responses **precisely** at an up-conversion

receiver IF, given this receiver IF (f_{IF}), and given that the LO is tuned to frequency f_{LO} .

They are:

1st -order

$$f_{RF} = f_{IF}$$

2nd-order

$$f_{RF} = f_{LO} \pm f_{IF} \quad f_{RF} = \frac{f_{IF}}{2}$$

3rd-order

$$f_{RF} = \frac{f_{IF}}{3} \quad f_{RF} = \frac{f_{IF} - f_{LO}}{2} \quad f_{RF} = f_{IF} - 2f_{LO}$$

$$f_{RF} = \frac{f_{LO} + f_{IF}}{2} \quad f_{RF} = 2f_{LO} + f_{IF}$$

$$f_{RF} = \frac{f_{LO} - f_{IF}}{2} \quad f_{RF} = 2f_{LO} - f_{IF}$$

Since we know that $f_{IF} > f_s$ and $f_{IF} > f_{LO}$ we can conclude that the terms above which are **most problematic** (i.e., they might be **close** to desired signal frequency f_s !) are:

$$f_{RF} = \frac{f_{IF}}{3}$$

$$f_{RF} = \frac{f_{IF} - f_{LO}}{2}$$

$$f_{RF} = f_{IF} - 2f_{LO}$$

$$f_{RF} = \frac{f_{IF}}{2}$$

$$f_{RF} = 2f_{LO} - f_{IF}$$

$$f_{RF} = \frac{f_{LO} + f_{IF}}{2}$$

Inserting the up-conversion tuning solution ($f_{LO} = f_{IF} - f_s$) into these results, we can determine the problematic RF frequencies in terms of IF frequency f_{IF} and desired RF signal frequency f_s :

$$f_{RF} = \frac{f_{IF}}{3}$$

$$f_{RF} = \frac{2f_{IF} + f_s}{2}$$

$$f_{RF} = 2f_s - f_{IF}$$

$$f_{RF} = \frac{f_{IF}}{2}$$

$$f_{RF} = f_{IF} - 2f_s$$

$$f_{RF} = \frac{2f_{IF} - f_s}{2}$$

There are some **important** things to note about these frequencies:

- 1)** The only 2nd-order term is $f_{RF} = f_{IF}/2$. In other words, there is **no image frequency!** This of course is a result of the fact that the up-conversion term $f_s + f_{LO} = f_{IF}$ has only **one** solution.
- 2)** These terms are **much different** than those deemed important for the **down-conversion receiver**.

3) As the value of the receiver IF frequency f_{IF} becomes **large** (i.e., $f_{IF} > 2f_s$) we find that the frequency of **all** these problematic RF signals likewise become **large** ($2f_s - f_{IF}$ becomes negative).

As a result, these spurious-signal causing RF signals can be (if they exist) at **much higher frequencies** than the desired signal f_s —they can be **easily filtered out** by a **preselector filter**, and thus the spurious signal (i.e., image and 3rd-order) **suppression can be very good** for up-conversion receivers.

For **example**, consider a **desired RF signal bandwidth** of:

$$0.5 \text{ GHz} \leq f_s \leq 0.6 \text{ GHz}$$

Say we design an **up-conversion receiver** with an IF of 3.0 GHz. The **problematic RF signals** are thus:

$$\frac{f_{IF}}{3} \Rightarrow f_{RF} = 1 \text{ GHz} \quad \frac{f_{IF}}{2} \Rightarrow f_{RF} = 1.5 \text{ GHz}$$

$$\frac{2f_{IF} + f_s}{2} \Rightarrow 3.25 \text{ GHz} \leq f_{RF} \leq 3.3 \text{ GHz}$$

$$f_{IF} - 2f_s \Rightarrow 1.8 \text{ GHz} \leq f_{RF} \leq 2.0 \text{ GHz}$$

$$\frac{2f_{IF} - f_s}{2} \Rightarrow 2.7 \text{ GHz} \leq f_{RF} \leq 2.75 \text{ GHz}$$

Note that the frequencies of all these potentially spur-creating RF signals are a significant "distance" from the desired RF signal band of $0.5 \text{ GHz} \leq f_s \leq 0.6 \text{ GHz}$.

Thus, a receiver designer can easily attenuate these problematic signals with a **preselector filter** whose passband extends from 0.5 GHz to 0.6 GHz.

Q: Wow! Why don't we just design receivers with very high IF frequencies?

A: Remember, increasing the receiver IF will in general increase cost and reduce performance (this is bad!).

In addition, note that increasing the center frequency of the IF filter (f_{IF})—while the IF bandwidth Δf_{IF} remains constant—decreases the percentage bandwidth of this IF filter. Recall there is a practical lower limit on the percentage bandwidth of a bandpass filter, thus there is a practical upper limit on receiver IF frequency, given an IF bandwidth Δf_{IF} !

For example, consider a desired signal with a bandwidth Δf_s of:

$$\Delta f_s = 10 \text{ MHz}$$

The receiver **IF filter**, therefore would likewise require a bandwidth of $\Delta f_{IF} = 10 \text{ MHz}$. If it is impractical for the IF

bandpass filter to have a **percentage** bandwidth **less** than 0.2%, then:

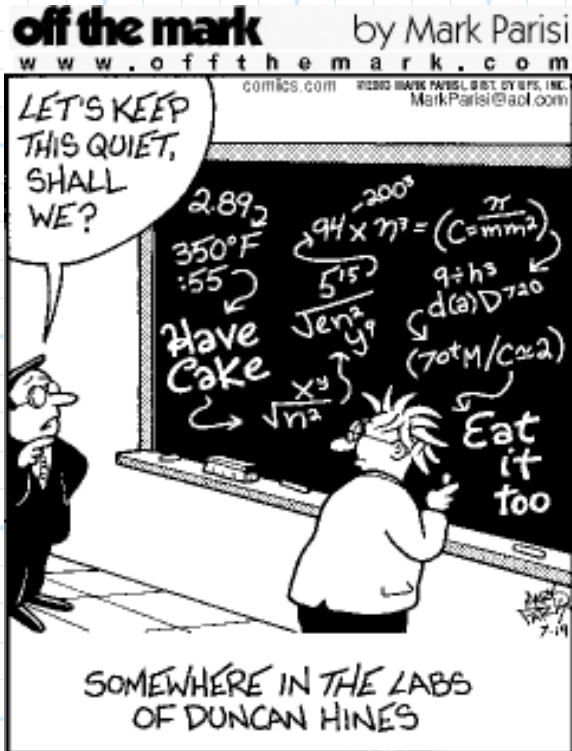
$$0.002 > \frac{\Delta f_{IF}}{f_{IF}}$$

And so:

$$f_{IF} > \frac{\Delta f_{IF}}{0.002} = \frac{10 \text{ MHz}}{0.002} = 5.0 \text{ GHz}$$

In other words, for this example, the receiver IF must be **less** than 5.0 GHz in order for the IF filter to be **practical**.

Advanced Receiver Designs



So, we know that as our IF frequency **increases**, the rejection of image and (some) other spurious signals will **improve**.

But, as our IF frequency **decreases**, the cost and performance of our receiver and demodulator will **improve**.

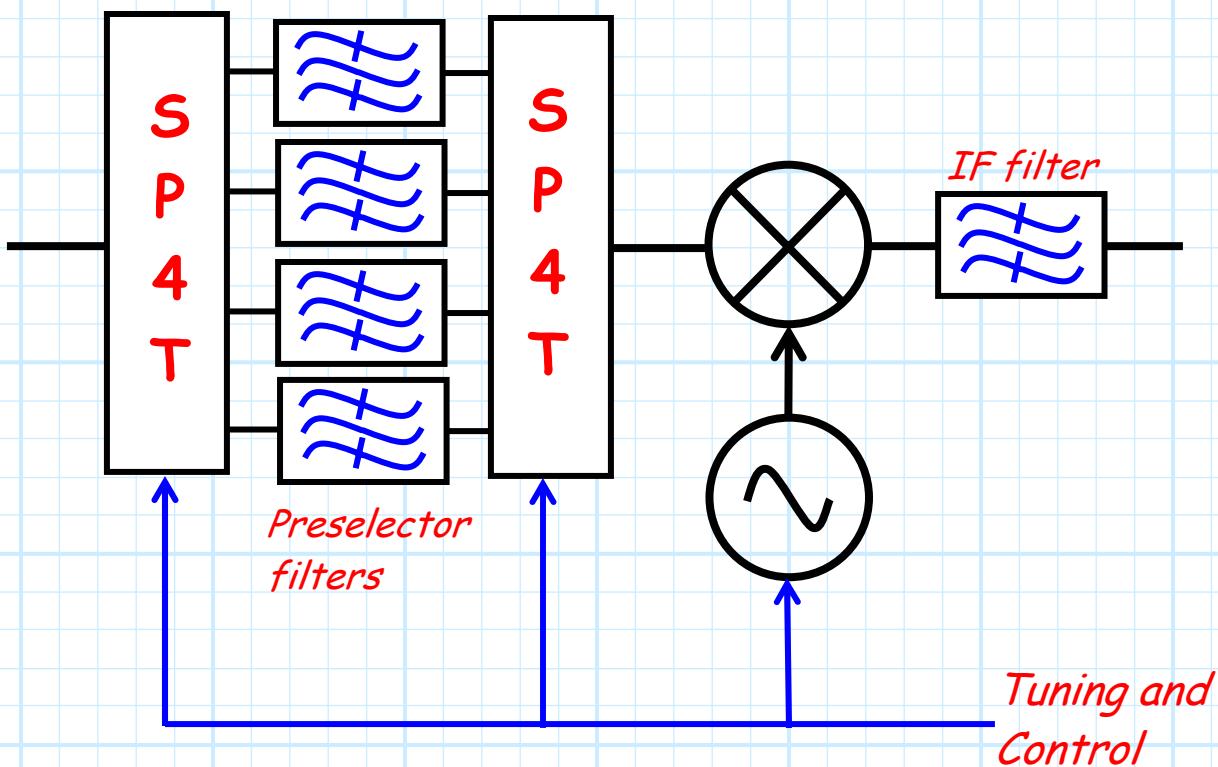
Q: Isn't there some way to have it **both ways**? Can't we have our cake and eat it **too**?

A: Yes, there is (sort of)!

To achieve **exceptional** image and 3rd-order product rejection, and enjoy the cost and performance benefits of a **low** IF frequency, receiver designers often employ these **two** advanced receiver architectures.

1. Selectable Preselection

Instead of implementing a single preselector filter, we can use a bank of **selectable** preselector filters:



In other words, we use multiple preselector filters to **span** the desired receiver RF bandwidth. This is particularly useful for **wideband** receiver design.

Q: Why? How is this useful? What good is this design?

A: Consider an **example**. Say we have been tasked to design a receiver with an RF bandwidth extending from 8 GHz to 12 GHz. A **standard** receiver design might implement a **single** preselector filter, extending from 8 GHz to 12 GHz.

Instead, we could implement a bank of preselector filters that span the RF bandwidth. We could implement 2, 3, 4, or even more filters to accomplish this.

Let's say we use four filters, each covering the bandwidths shown in the table below:

	Bandwidth
Filter #1	8 - 9 GHz
Filter #2	9 - 10 GHz
Filter #3	10 - 11 GHz
Filter #4	11 - 12 GHz

Say we wish to receive a signal at 10.3 GHz; we would tune the local oscillator to the proper frequency, **AND** we must select **filter #3** in our filter bank.

Thus, **all** signals from 10-11 GHz would pass through to the RF port of the mixer—a band that includes our **desired** signal at 10.3 GHz.

However, signals from 8-10 GHz and 11-12 GHz will be **attenuated by filter #3**—ideally, little signal energy from these bands would reach the RF port of the mixer. If we wish

to receive a signal in these bands, we must select a **different** filter (as well as **retune** the LO frequency).

→ As a result, signals over "just" **1GHz** of bandwidth reach the RF port of the mixer, as opposed to the single filter design wherein a signal spectrum **4GHz** wide reaches the mixer RF port!

Q: Again I ask the question: How is this helpful?

A: Let's say this receiver design likewise implements **low-side** tuning. If we wish to tune to a RF signal at **12 GHz** (i.e., $f_s = 12 \text{ GHz}$), we find that the **image** frequency lies at:

$$f_{\text{image}} = 12 \text{ GHz} - 2f_{\text{IF}}$$

Of course, we need the preselector filter to reject this image frequency. If we receiver design used just one preselector filter (from 8 to 12 GHz), then the image signal frequency f_{image} must be **much less** than 8 GHz (i.e., well outside the filter passband). As a result, the receiver IF frequency must be:

$$\begin{aligned} 8 \text{ GHz} &\gg 12 \text{ GHz} - 2f_{\text{IF}} \\ 8 \text{ GHz} + 2f_{\text{IF}} &\gg 12 \text{ GHz} \\ 2f_{\text{IF}} &\gg 4 \text{ GHz} \\ f_{\text{IF}} &\gg 2 \text{ GHz} \end{aligned}$$

In other words, the **4.0 GHz RF bandwidth** results in a requirement that the receiver Intermediate Frequency (**IF**) be much **greater than 2.0 GHz**.

→ This is a pretty darn high IF!

Instead, if we implement the bank of preselector filters, we would select **filter #4**, with a passband that extends from 12 GHz down to 11 GHz.

As a result, image rejection occurs if:

$$11\text{GHz} \gg 12\text{GHz} - 2f_{IF}$$

$$11\text{GHz} + 2f_{IF} \gg 12\text{GHz}$$

$$2f_{IF} \gg 1\text{GHz}$$

$$f_{IF} \gg 0.5\text{GHz}$$

In other words, **since** the preselector filter has a much **narrower** (i.e., 1GHz) bandwidth than before (i.e., 4GHz), we can get adequate image rejection with a **much lower IF frequency** (this is a good thing)!

Moreover, this improvement in spurious signal rejection likewise applies to other order terms, including that **annoying 3rd-order term!**

Thus, implementing a bank of preselector filters allows us to either:

1. Provide **better** image and spurious signal **rejection** at a given IF frequency.
2. Lower the **IF** frequency necessary to provide a **given** level of image and spurious signal rejection.

As we increase the **number** of preselector filters, the image and spurious signal rejection will increase **and/or** the required IF frequency will decrease.



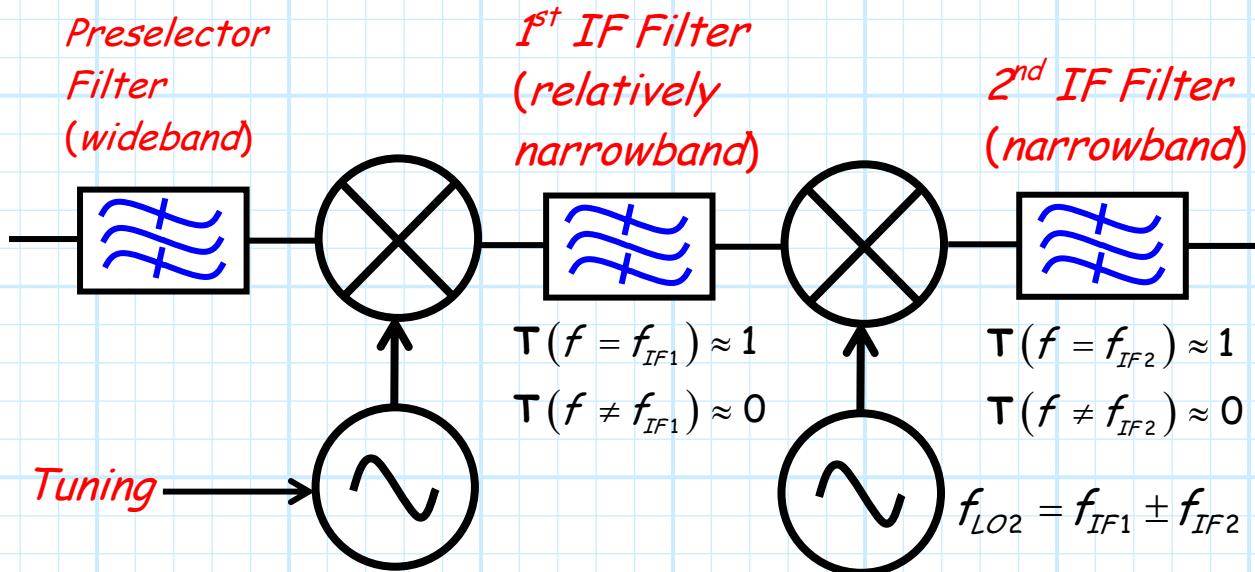
But beware! Adding filters will **increase** the cost and size of your receiver!

2. Dual Conversion Receivers

A **dual conversion** receiver is another great way of achieving exceptional image and spurious rejection, while maintaining the benefits of a low IF frequency.

In this architecture, instead of employing multiple preselector filters, we employ multiple (i.e. two) **IF filters**!

As the name implies, a **dual** conversion receiver converts the signal frequency—**twice**. As a result, this receiver architecture implements **two** Local Oscillators and **two** mixers.



Q: Two frequency conversions! Why would we want to do that?

A: The first mixer/local oscillator converts the RF signal to the first IF frequency f_{IF1} . The value of this first IF frequency is selected to optimize the **suppression** of the image frequency and all other RF signals that would produce spurious signals (e.g., 3rd order products) at the first IF.

Optimizing spurious signal suppression generally results in an IF frequency f_{IF1} that is **very high**—much higher than a typical IF frequency.

Q: But won't a high IF frequency result in **reduced IF component and demodulator performance**, as well as **higher cost**?

A: That's why we employ a **second conversion!**

The **second** mixer/local oscillator simply down converts the signal to a **lower** IF (f_{IF2})—a frequency where both component performance and cost is **good**.

Q: *What about spurious signals produced by this second conversion; don't we need to worry about them?*

A: Nope! The **first** conversion (if designed properly) has adequately suppressed them. The first IF filter (like all IF filters) is relatively **narrow band**, thus allowing **only** the desired signal to reach the RF port of the **second** mixer. We then simply need to down-convert this **one** signal to a lower, more **practical** IF frequency!

Now, some **very important** points about the dual-conversion receiver.

Point 1

The **first** LO must be **tunable**—just like a “normal” super-het local oscillator. However, the **second** LO has a **fixed** frequency—there is **no need** for it to be tunable!

Q: *Why is that?*

A: Think about it.

The signal at the RF port of the second mixer **must** be precisely at frequency f_{IF1} (it wouldn't have made it through the first IF filter otherwise!). We need to down-convert this

signal to a second IF frequency of f_{IF1} , thus the second LO frequency must be:

$$f_{LO2} = f_{IF1} + f_{IF2} \quad (\text{high-side tuning})$$

or:

$$f_{LO2} = f_{IF1} - f_{IF2} \quad (\text{low-side tuning})$$

Either way, no tuning is required for the second LO!

This of course means that we can use, for example, a **crystal or dielectric resonator oscillator** for this second LO.

Point 2

Recall the criteria for selecting the first IF is **solely** image and spurious signal suppression. Since the second conversion reduces the frequency to a lower (i.e., lower cost and higher performance) value, the first IF frequency f_{IF1} can be as **high as practical**.

In fact, the first IF frequency can actually be **higher than the RF signal**!

→ In other words, the first conversion can be an **up-conversion**.

For example, say our receiver has an **RF bandwidth** that extends from 900 MHz to 1300 MHz. We might choose a first

IF at $f_{IF1}=2500$ MHz, such that the first mixer/LO must perform an **up-conversion** of as much as 1600 MHz.

Q: Say again; why would this be a good idea?

A: Remember, we found that an **extremely high** first IF will make the preselector's job relatively easy—all RF signals that would produce spurious signals at the first IF are **well outside** the preselector bandwidth, and thus are **easily** and/or **greatly** suppressed.



But be **careful!** Remember, the RF signals that cause spurious signals when **up-converting** are not the “**usual suspects**” we found when **down-converting**.

You must carefully determine **all** offending RF signals produced from **all** mixer terms (1st, 2nd, and 3rd order)!



Point 3

The bandwidth of the first IF filter (Δf_{IF1}) should be narrow, but not as narrow as the bandwidth of the second IF filter (Δf_{IF2}):

$$\Delta f_{IF1} > \Delta f_{IF2}$$

Remember, the second IF filter will have a much lower center frequency, and so it will generally have a much larger percentage bandwidth, and typically better performance (e.g.,

insertion loss) than the higher frequency bandpass filter required for the first IF.

Thus, designers generally rely on the **second IF** to provide the requisite selectivity.

In fact, cascading two filters with the same 3dB bandwidth is a bad idea, as the 3dB bandwidth effectively becomes a $3+3=6\text{db}$ bandwidth!

A designer "rule-of-thumb" is to make the first IF filter bandwidth about **10 times** that of the second:

$$\Delta f_{IF1} \approx 10 \Delta f_{IF2}$$

*One last point. The **astute** receiver designer will often find that a **combination** of these two architectures (multiple preselection and dual conversion) will provide an elegant, effective, and cost efficient solution!*

