

# Accelerating colour space conversion on reconfigurable hardware

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## Abstract

Colour space conversion is very important in many types of image processing applications including video compression. This operation consumes up to 40% of the entire processing power of a highly optimised decoder. Therefore, techniques which efficiently implement this conversion are desired. This paper presents two novel architectures for efficient implementation of a Colour Space Converter (CSC) suitable for Field Programmable Gate Array (FPGAs) and VLSI. The proposed architectures are based on Distributed Arithmetic (DA) ROM accumulator principles. The architectures have been implemented and verified using the Celoxica RC1000 FPGA development board. In addition, they are platform independent and have a low latency (eight cycles). The first architecture has a throughput of height, while the second one is fully pipelined and has a throughput of one and capable of sustained data rate of over 234 mega-conversions/s.

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## 1. Introduction

Colour is a visual sensation produced by the light in the visible region of the spectrum incident on the retina. Since the human visual system has three types of colour photoreceptor cone cells, three components are necessary and sufficient to describe a color [1].

Colour spaces (also called colour models or colour systems) is a method by which we can specify, create and visualize colour. There are many existing colour spaces and most of them represent each colour as a point in a three-dimensional coordinate system. Each colour space is optimised for a well-defined application area [3]. The three most popular colour models are RGB (used in colour printing). All of the colour spaces can be derived from the RGB information supplied by devices such as cameras and scanners.

Processing an image in the RGB colour space, with a set of RGB values for each pixel is not the most efficient method. To speed up some processing steps many broadcast, video and imaging standards use luminance and colour difference video signals, such as YCrCb, making a mechanism for converting between formats necessary. Several cores for RGB to YCrCb conversion can be found in the market, which have been designed for FPGA implementation, such as the cross proposed by Amphion Ltd [4], CAST.Inc [5] and ALMA.Tech [6]. Another such converter is presented in [7]. It has been implemented on a hybrid system which consists of the TriMedia processor augmented with FPGA-based reconfigurable functional units.

As part of an on going research project to develop a hardware accelerator for image and signal processing algorithms based on matrix computations at Queens University of Belfast [8–11], This paper proposes the use of FPGA as a low cost accelerator for two RGB to YCrCb Colour Space Conversion based architectures using DA principles, which is a bit level rearrangement of a multiply accumulate to hide the multiplications. The two proposed

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architectures are based on serial and parallel manipulation of pixels.

The target hardware for the implementation and verification of the proposed architectures is Celoxica RC1000 PCI based FPGA development board equipped with a Xilinx XCV2000E Virtex FPGA [12,13]. The composition of the rest of the paper is as follows. A review for the conversion from  $R'G'B'$  to  $Y'CrCb$  is given in Section 2. Sections 3 and 4 are concerned with the mathematical backgrounds and the descriptions of the two proposed architectures. Then the hardware implementations and the results and analysis are presented in Sections 5 and 6, respectively. Finally concluding remarks are given in Section 6.

## 2. Color space conversion: a review

As mentioned in the introduction, many color models have been proposed, each oriented towards supporting a specific task or solving a particular problem. Described below are the two colour systems selected for our study which are used in many image processing applications.

### 2.1. RGB colour space

RGB colour space is a simple and robust colour definition. RGB uses three numerical components to represent a colour. This colour space can be thought of as a three-dimensional coordinate system whose axes correspond to the three components, R or Red, G or Green, and B or Blue. RGB is the colour space that computer displays use. It corresponds most closely to the behavior of the human eye [1]. RGB is an additive colour system. The three primary colours red, green, and blue are added to form the desired colour. For a true colour image, the red, green, and blue components of a pixel are each with eight bits width. In total, it may have 16 million ( $2^{24}$ ) possible colours. Each component has a range of 0–255, with all three 0s producing black and all three 255s producing white [1]. In the rest of this paper, the gamma-corrected RGB values are noted  $R'G'B'$ .

### 2.2. $Y'CrCb$ colour space

$Y'CrCb$  is a scaled and offset version of the YUV colour space based on luminance and chrominance, which correspond to brightness and colour. In this color space  $R'G'B'$  is separated into a luminance part ( $Y'$ ) and two chrominance parts (Cb and Cr).  $Y'$  is defined to have a range of 16–235, Cb and Cr have a range of 16–240 [1,2].

### 2.3. Converting from $R'G'B'$ to $Y'CrCb$

Decomposing an  $R'G'B'$  colour image into one luminance image and two chrominance images is the

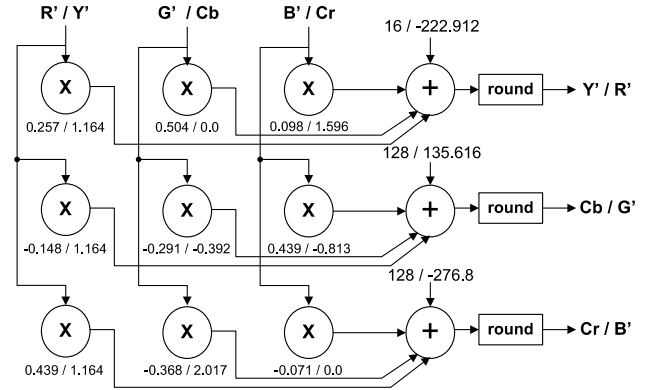


Fig. 1. General block diagram for  $R'G'B' \leftrightarrow Y'CrCb$  CSC.

method that has been used in most commercial applications such as face detection [14,15], as well as the JPEG and MPEG imaging standards [16–18].

The calculation of  $Y'CrCb$  colour components from  $R'G'B'$  components consumes up to 40% of the processing power in a highly optimized decoder [16]. Accelerating this operation would be useful for the acceleration of the whole process. A colour in the  $R'G'B'$  colour space is converted to the  $Y'CrCb$  colour space using the following equation

$$\begin{pmatrix} Y' \\ Cr \\ Cb \end{pmatrix} = \begin{pmatrix} 0.257 & 0.504 & 0.098 & 16 \\ 0.439 & -0.368 & -0.071 & 128 \\ -0.148 & -0.291 & 0.439 & 128 \end{pmatrix} \begin{pmatrix} R' \\ G' \\ B' \\ 1 \end{pmatrix} \quad (1)$$

while the inverse conversion can be carried out using the following equation:

$$\begin{pmatrix} R' \\ G' \\ B' \end{pmatrix} = \begin{pmatrix} 1.164 & 1.596 & 0.0 & -222.912 \\ 1.164 & -0.813 & -0.392 & 135.616 \\ 1.164 & 0.0 & 2.017 & -276.8 \end{pmatrix} \begin{pmatrix} Y' \\ Cr \\ Cb \\ 1 \end{pmatrix} \quad (2)$$

Fig. 1 shows the direct mapping of Eqs. (1) and (2).

## 3. Proposed architecture based serial manipulation approach

### 3.1. Mathematical background

Since colour space conversion can be expressed as a Matrix-Vector (MV) multiplication, a novel algorithm based DA is presented in this section.

DA distributes arithmetic operations rather than grouping them as multipliers do. Conventional DA, called ROM-based DA, decomposes the variable input of the inner product to bit level in order to generate precomputed data.

ROM-based DA uses a ROM table to store the precomputed data, which makes it regular and efficient in the use of the silicon area, in a VLSI implementation. The advantage of a DA-based ROM approach is its efficiency of implementation. The basic operations required are a sequence of ROMs, addition, subtraction and shift operations of the input data sequence [19]. Examples for the use of DA can be found in these Refs. [19–21].

Consider the matrix-vector product given by the following equation

$$C_i = \sum_{k=0}^{N-1} A_{ik} B_k \quad (3)$$

where  $\{A_{ik}\}$ 's are L-bits constants and  $\{B_k\}$ 's are written in the unsigned binary representation as shown in Eq. (4)

$$B_k = \sum_{m=0}^{W-1} b_{k,m} 2^m \quad (4)$$

where  $b_{k,l}$  is the  $m$ th bit of  $B_k$ , which is zero or one,  $W$  is the word-length used which represents the resolution for each colour component of a pixel.

Substituting (4) in (3)

$$C_i = \sum_{k=0}^{N-1} A_{ik} \left( \sum_{m=0}^{W-1} b_{k,m} 2^m \right) = \sum_{m=0}^{W-1} \left( \sum_{k=0}^{N-1} A_{ik} (b_{k,m} 2^m) \right) \quad (5)$$

define

$$Z_m = \sum_{k=0}^{N-1} A_{ik} b_{k,m} \quad (6)$$

therefore,  $C_i$  can be computed as:

$$C_i = \sum_{m=0}^{W-1} Z_m 2^m \quad (7)$$

The idea is that since the term  $Z_m$  depends on the  $b_{k,m}$  values and has only  $2^N$  possible values, it is possible to precompute and store them in ROMs. An input set of  $N$  bits ( $b_{0,m}, b_{1,m}, \dots, b_{(N-1),m}$ ) is used as an address to retrieve the corresponding  $Z_m$  values. The ROM's content is different and depends on the constant matrix  $A$  coefficients. These intermediate results are accumulated in  $W$  clock cycles to produce  $C_i$  coefficients.

### 3.2. Case study: converting from $R'G'B' \leftrightarrow Y'CrCb$

The CSC core implements the following mathematical formula to convert from one space to another

$$\begin{pmatrix} C_0 \\ C_1 \\ C_2 \end{pmatrix} = \begin{pmatrix} A_{00} & A_{01} & A_{02} & A_{03} \\ A_{10} & A_{11} & A_{12} & A_{13} \\ A_{20} & A_{21} & A_{22} & A_{23} \end{pmatrix} \begin{pmatrix} B_0 \\ B_1 \\ B_2 \\ 1 \end{pmatrix} \quad (8)$$

where  $C_i$  ( $0 \leq i \leq 2$ ) and  $B_i$  ( $0 \leq i \leq 3$ ) represent the input and output colour components, respectively. Since all the components are in the range of 0–255, eight bits are enough to represent them. In our application ( $N=4$  and  $W=8$ ),  $C_i$  can be computed as

$$C_i = \sum_{m=0}^7 Z_m 2^m \quad (9)$$

where

$$Z_m = \sum_{k=0}^3 A_{ik} b_{k,m} \quad (10)$$

$$\begin{array}{ccccccc} & k=0 & k=1 & k=2 & k=3 & & \\ & (A_{i0} \times b_{0,0} + & A_{i1} \times b_{1,0} + & A_{i2} \times b_{2,0} + & A_{i3} \times b_{3,0}) & \times 2^0 + & m=0 \\ C_i = & (A_{i0} \times b_{0,1} + & A_{i1} \times b_{1,1} + & A_{i2} \times b_{2,1} + & A_{i3} \times b_{3,1}) & \times 2^1 + & m=1 \\ & (A_{i0} \times b_{0,2} + & A_{i1} \times b_{1,2} + & A_{i2} \times b_{2,2} + & A_{i3} \times b_{3,2}) & \times 2^2 + & m=2 \\ & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ & (A_{i0} \times b_{0,7} + & A_{i1} \times b_{1,7} + & A_{i2} \times b_{2,7} + & A_{i3} \times b_{3,7}) & \times 2^7 + & m=7 \end{array} \quad (11)$$

Three ROMs (one for each matrix  $A$  row) with the size of  $2^N = 2^4 = 16$  are needed in order to store the precompute  $2^4$  possible partial products values. Since the last element of the vector  $B$  is equal to 1:

$$b_{3,m} = \begin{cases} 1 & \text{for } m = 0 \\ 0 & \text{for } m \neq 0 \end{cases} \quad (12)$$

Eq. (9) can be rewritten as

$$C_i = \sum_{m=0}^7 Z_i^* 2^m + A_{i3} \quad (13)$$

where

$$Z_i^* = \sum_{k=0}^2 A_{ik} b_{k,m} \quad (14)$$

$$\begin{array}{ccccccc} & k=0 & k=1 & k=2 & & & \\ & (A_{i0} \times b_{0,0} + & A_{i1} \times b_{1,0} + & A_{i2} \times b_{2,0}) & \times 2^0 + & m=0 \\ & (A_{i0} \times b_{0,1} + & A_{i1} \times b_{1,1} + & A_{i2} \times b_{2,1}) & \times 2^1 + & m=1 \\ C_i = & (A_{i0} \times b_{0,2} + & A_{i1} \times b_{1,2} + & A_{i2} \times b_{2,2}) & \times 2^2 + & m=2 \\ & \vdots & \vdots & \vdots & \vdots & \vdots \\ & A_{i0} \times b_{0,7} & A_{i1} \times b_{1,7} & A_{i2} \times b_{2,7} & \times 2^7 + & m=7 \\ & A_{i3} & & & & \end{array} \quad (15)$$

It is worth mentioning that the size of the ROMs has been reduced to  $2^3$ . Table 1 gives the content of each ROM.

### 3.3. Proposed architecture

Since our objective is to implement a core which performs two different colour conversions ( $R'G'B' \leftrightarrow Y'CrCb$ ), six ROMs are needed (three for each

Table 1  
Content of the ROM  $i$  ( $0 \leq i \leq 2$ )

$b_{0,m}$	$b_{1,m}$	$b_{2,m}$	The content of the ROM $i$
0	0	0	0
0	0	1	$A_{i2}$
0	1	0	$A_{i1}$
0	1	1	$A_{i1} + A_{i2}$
1	0	0	$A_{i0}$
1	0	1	$A_{i0} + A_{i2}$
1	1	0	$A_{i0} + A_{i1}$
1	1	1	$A_{i0} + A_{i1} + A_{i2}$

conversion). Figs. 2 and 3 show the proposed core pins and its internal architecture, respectively.

The pins description is given in Table 2.

The proposed architecture consists of three identical Processing Elements (PEs) and two memory blocks. Each PE comprises a parallel ACCumulator (ACC) and a right shifter and each memory block consists of three ROMs with the size of  $2^3$  each (see Fig. 4). The ROM's content is different and depends on the matrix  $A$  coefficients, which depend on the conversion type.

It is worth mentioning that our architecture is scalable, however, it can be used to perform  $n$  conversions by adding every time  $3 \times n$  ROMs in order to store the matrix conversion coefficients and keeping always the same PEs. An  $N \times M$  image can be converted using the proposed architecture by setting the inputs every eight clock cycles

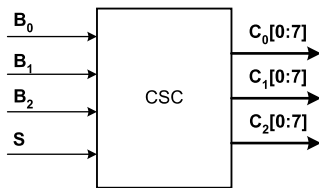


Fig. 2. Symbol of the CSC core.

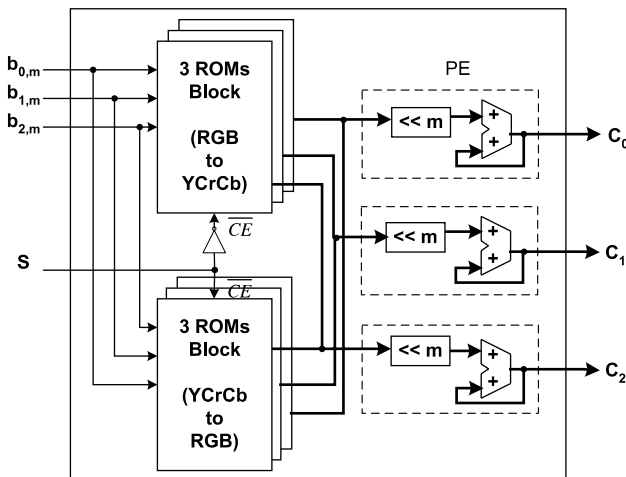


Fig. 3. Serial CSC based DA architecture.

Table 2  
Pins description

Name	Dir	Description
$B_0$	I	First input colour space component
$B_1$	I	Second input colour space component
$B_2$	I	Third input colour space component
$C_0$	O	First output colour space component
$C_1$	O	Second output colour space component
$C_2$	O	Third output colour space component
S	I	Colour space conversion type selection

using the  $R'G'B'$ ; components of a new pixel ( $Y'CrCb$  for the inverse conversion) Fig. 5.

#### 4. Proposed architecture based parallel manipulation approach

##### 4.1. Mathematical background

Consider an  $N \times M$  image ( $N$ : image height,  $M$ : image width).

Let represent each image pixel by  $b_{ijk}$ , ( $0 \leq i \leq N-1$ ,  $0 \leq j \leq M-1$ ,  $0 \leq k \leq 2$ ), where

$$\begin{cases} b_{ij0} = R_{ij} / \text{the red component of the pixel in row } i \\ \text{and column } j \\ b_{ij1} = G_{ij} / \text{the green component of the pixel in row } i \\ \text{and column } j \\ b_{ij2} = B_{ij} / \text{the blue component of the pixel in row } i \\ \text{and column } j \end{cases} \quad (16)$$

The image can be converted using the following mathematical formula

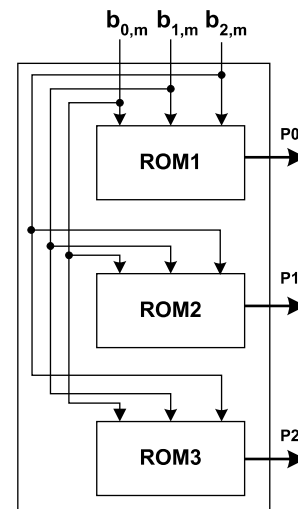


Fig. 4. Memory block structure.

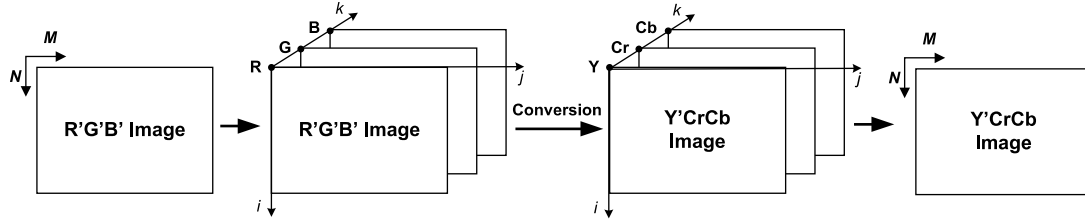


Fig. 5. R'G'B' to Y'CrCb conversion.

$$\begin{pmatrix} \begin{pmatrix} c_{000} \\ c_{001} \\ c_{002} \end{pmatrix} & \cdots & \begin{pmatrix} c_{0(M-1)0} \\ c_{0(M-1)1} \\ c_{0(M-1)2} \end{pmatrix} \\ \begin{pmatrix} c_{100} \\ c_{101} \\ c_{102} \end{pmatrix} & \cdots & \begin{pmatrix} c_{1(M-1)0} \\ c_{1(M-1)1} \\ c_{1(M-1)2} \end{pmatrix} \\ \vdots & \cdots & \vdots \\ \begin{pmatrix} c_{(N-1)00} \\ c_{(N-1)01} \\ c_{(N-1)02} \end{pmatrix} & \cdots & \begin{pmatrix} c_{(N-1)(M-1)0} \\ c_{(N-1)(M-1)1} \\ c_{(N-1)(M-1)2} \end{pmatrix} \end{pmatrix} \\ = \begin{pmatrix} A_{00} & A_{01} & A_{02} & A_{03} \\ A_{10} & A_{11} & A_{12} & A_{13} \\ A_{20} & A_{21} & A_{22} & A_{23} \end{pmatrix}$$

$$\otimes \begin{pmatrix} \begin{pmatrix} b_{000} \\ b_{001} \\ b_{002} \\ 1 \end{pmatrix} & \cdots & \begin{pmatrix} b_{0(M-1)0} \\ b_{0(M-1)1} \\ b_{0(M-1)2} \\ 1 \end{pmatrix} \\ \begin{pmatrix} b_{100} \\ b_{101} \\ b_{102} \\ 1 \end{pmatrix} & \cdots & \begin{pmatrix} b_{1(M-1)0} \\ b_{1(M-1)1} \\ b_{1(M-1)2} \\ 1 \end{pmatrix} \\ \vdots & \cdots & \vdots \\ \begin{pmatrix} b_{(N-1)00} \\ b_{(N-1)01} \\ b_{(N-1)02} \\ 1 \end{pmatrix} & \cdots & \begin{pmatrix} b_{(N-1)(M-1)0} \\ b_{(N-1)(M-1)1} \\ b_{(N-1)(M-1)2} \\ 1 \end{pmatrix} \end{pmatrix} \quad (17)$$

where the operation  $\otimes$  can be defined as follows: each vector

$$\begin{pmatrix} c_{ij0} \\ c_{ij1} \\ c_{ij2} \end{pmatrix}$$

is the result of the product

$$\begin{pmatrix} A_{00} & A_{01} & A_{02} & A_{03} \\ A_{10} & A_{11} & A_{12} & A_{13} \\ A_{20} & A_{21} & A_{22} & A_{23} \end{pmatrix} \begin{pmatrix} b_{ij0} \\ b_{ij1} \\ b_{ij2} \\ 1 \end{pmatrix},$$

where  $c_{ijk}$  represent the output image colour space components and

$$A = \begin{pmatrix} A_{00} & A_{01} & A_{02} & A_{03} \\ A_{10} & A_{11} & A_{12} & A_{13} \\ A_{20} & A_{21} & A_{22} & A_{23} \end{pmatrix}$$

represents one of the constant matrices in Eqs. (1) and (2).

The  $c_{ijk}$  elements (the output image colour space components) can be computed using the following equation

$$c_{ijk} = \sum_{m=0}^3 A_{km} b_{ijm} \quad (0 \leq i \leq N-1, 0 \leq j \leq M-1, 0 \leq k \leq 2) \quad (18)$$

where  $\{A_{km}\}$ 's are L-bits constants and  $\{b_{ijm}\}$ 's are written in the unsigned binary representation as shown in Eq. (17):

$$b_{ijm} = \sum_{l=0}^{W-1} b_{ijm,l} 2^l \quad (0 \leq i \leq N-1, 0 \leq j \leq M-1, 0 \leq m \leq 2) \quad (19)$$

Using the same development in Section 4.1, Eq. (16) can be rewritten as

$$c_{ijk} = \sum_{l=0}^7 Z_l^* 2^l + A_{k3} \quad (20)$$

where

$$Z_l^* = \sum_{m=0}^2 A_{km} b_{ijm,l} \quad (21)$$

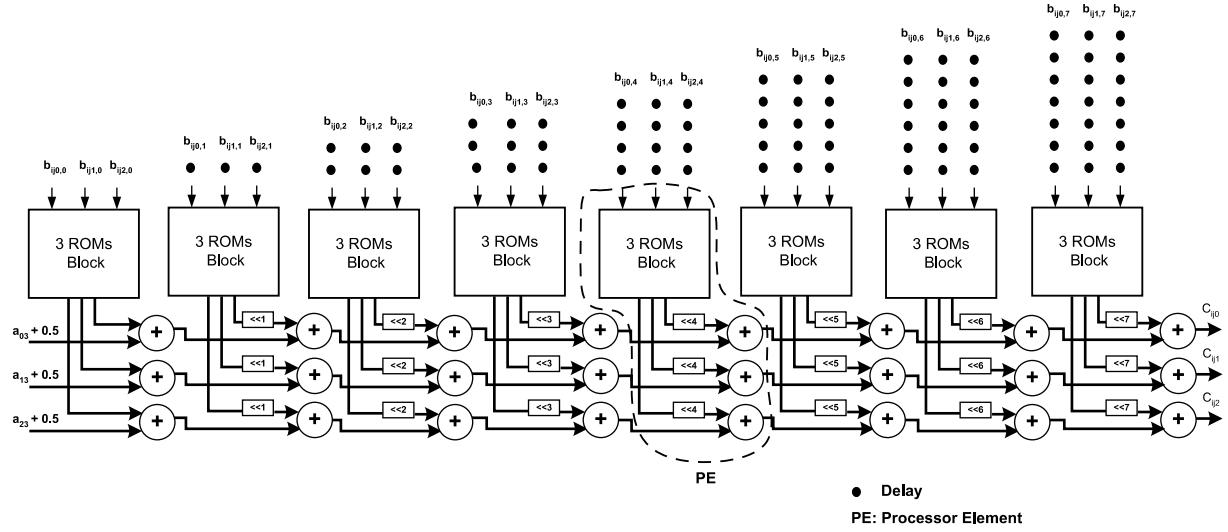


Fig. 6. Proposed parallel architecture based on DA principles clock cycles, where  $(3 \times 4)$  is the constant matrix  $A$  size.

$$\begin{aligned}
 & m=0 \quad m=1 \quad m=1 \\
 & (A_{k0} \times b_{ij0,0} + A_{k1} \times b_{ij1,0} + A_{k2} \times b_{ij2,0}) \times 2^0 + l=0 \\
 & (A_{k0} \times b_{ij0,1} + A_{k1} \times b_{ij1,1} + A_{k2} \times b_{ij2,1}) \times 2^1 + l=1 \\
 & c_{ijk} = (A_{k0} \times b_{ij0,2} + A_{k1} \times b_{ij1,2} + A_{k2} \times b_{ij2,2}) \times 2^2 + l=2 \\
 & \vdots \quad \vdots \quad \vdots \quad \vdots \quad \vdots \\
 & (A_{k0} \times b_{ij0,7} + A_{k1} \times b_{ij1,7} + A_{k2} \times b_{ij2,7}) \times 2^7 + l=7 \quad (22) \\
 & A_{k3} \\
 & PP_{ijk0} + PP_{ijk1} + PP_{ijk2} + PP_{ijk3} + \\
 & = PP_{ijk4} + PP_{ijk5} + PP_{ijk6} + PP_{ijk7} + \\
 & A_{k3}
 \end{aligned}$$

Likewise the first proposed architecture, the ROM's content is different and depends on the matrix  $A$  coefficients, which depend on the conversion type.

#### 4.2. Proposed architecture

Eq. (18) can be mapped into the proposed architecture as shown in Fig. 6.

The architecture consists of eight identical  $PE_n$  ( $0 \leq n \leq 7$ ). Each  $PE_n$  comprises three parallel signed integer adders, three  $n$  right shifters and one ROMs block, which have the structure as shown in Fig. 4. It is worth noting that the architecture has a latency of  $W$  and a throughput rate equal to 1. The entire image conversion can be carried out in  $(\text{Latency} + (NM)\text{Throughput}) = 8 + (NM)$  clock cycles,

```

for i ← 1 to L do // scanning image rows
  for j ← 1 to M do // scanning image columns
    for k ← 1 to 3 do // scanning the three RGB value of a pixel
      for l ← 1 to 3 do // scanning columns of the constant conversion matrix
        cijk += akm x bijm
      end for
    end for
  end for
end for

```

Fig. 7. Pseudo code for the standard algorithm.

while using the standard algorithm (Fig. 7), the conversion can be carried out in  $(3 \times 4 \times N \times M)$  clock cycles, where  $(3 \times 4)$  is the constant matrix  $A$  size.

Fig. 8 shows the functional analysis diagram of the proposed architecture.

#### 5. Hardware implementation

The two proposed architectures based on DA technique have been implemented and verified using the Celoxica RC1000-PP FPGA development board. The RC1000-PP board used is a standard PCI bus card equipped with the Virtex-E2000 FPGA chip (package: bg560, speed grade 6). Tables 3 and 4 give the content of the ROMs used for  $R'G'B'$  to  $Y'CrCb$  and  $Y'CrCb$  to  $R'G'B'$  conversions for both architectures, respectively.

The second proposed architecture can be used for the inverse conversion ( $Y'CrCb$  to  $R'G'B'$ ) by:

- Duplicating the ROMs using the same implementation approach used for the first architecture (with a selector signal which allows the user to choose the appropriate converter); or
- Setting the contents of the ROMs in advance, depending on the desired conversion.

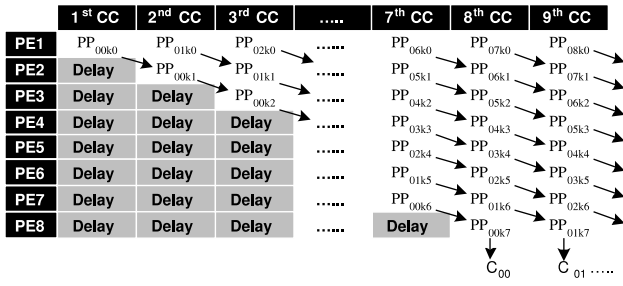


Fig. 8. Functional analysis diagram.

The precomputed partial products are stored in the ROMs using 13 bits fixed point representation (eight bits for integer part and five bits for fractional part). 13-bit arithmetic is used inside the architecture. The input and output soft betwo architectures are presented using eight bits and the outputs are rounded. Rounding usually looks at the decimal value and if it is greater than or equal to 0.5, then the result is increased by one. This implies a condition of verifying followed by another arithmetic operation. A more efficient way to round a number is to add 0.5 to the result and truncate the decimal value. This technique has been applied in our proposed architecture. The initial value for each PE's ACC (for the serial architecture) and for the first PEs adder (for the parallel architecture) is set in advance to  $(A_{i3} + 0.5)$ , where  $(0 \leq i \leq 2)$ . The MACs and parallel signed adders have been implemented using Xilinx CoreGen utility, which contains many efficient designs that can often save time for a programmer [22]. The shifters and ROMs initialisation have been implemented using VHDL. All design components have been connected together using Handel-C, a C-like language supporting parallelism, flexible data size and compilation of high-level programs directly into FPGA hardware [23].

## 6. Result and analysis

In order to make a fair and consistent comparison with the existing FPGA based CSCs, the XCV50E-8 FPGA device has been targeted. Table 5 illustrates the performances obtained for the proposed architecture in terms of area consumed and speed which can be achieved.

The proposed architecture based serial manipulation approach shows significant improvements in comparison

Table 3  
The content of the ROMs ( $R'/G'/B'$  to  $Y'/CrCb$ )

$R'_m/R'_{ij0,l}$	$G'_m/G'_{ij1,l}$	$B'_m/B'_{ij2,l}$	ROM1	ROM2	ROM3
0	0	0	0	0	0
0	0	1	0.098	−0.071	0.439
0	1	0	0.504	−0.368	−0.291
0	1	1	0.602	−0.439	0.148
1	0	0	0.257	0.439	−0.148
1	0	1	0.355	0.368	0.291
1	1	0	0.761	0.071	−0.439
1	1	1	0.859	0	0

Table 4  
The content of the ROMs ( $Y'/CrCb$  to  $R'/G'/B'$ )

$Y'_m/Y'_{ij0,l}$	$Cr_m/Cr_{ij1,l}$	$Cb_m/Cb_{ij2,l}$	ROM1	ROM2	ROM3
0	0	0	0	0	0
0	0	1	0	−0.392	0
0	1	0	1.596	−0.813	1.596
0	1	1	1.596	−1.025	1.596
1	0	0	1.164	1.164	1.164
1	0	1	1.164	0.772	1.164
1	1	0	2.76	0.351	2.76
1	1	1	2.76	−0.041	2.76

with the existing implementations [4–6], which perform the  $R'/G'/B'$  to  $Y'/CrCb$  conversion, in terms of the area consumed and the maximum running clock frequency, while the second architecture outperforms the existing ones in term of the number of conversions per second.

It is worth nothing that the existing cores used the same number of bit representation for the input and output data used in our design.

In addition a software based approach to perform the same operation has been implemented on a 2.0 GHz Intel®Pentium 4 processor with 1 GB of SDR RAM using Borland C++ Builder V6.0.

Table 6 illustrates the hardware/software implementations comparison in terms of the RMS error-due to the use of difference data representation in the two implementations,

$$\left( \text{RMS}_{\text{Error}} = \sqrt{\frac{1}{NM} \sum_{i=0}^{N-1} \sum_{j=0}^{M-1} (I_{\text{soft}}(i,j) - I_{\text{hard}}(i,j))^2} \right)$$

and the computation time, when using the second proposed DA architecture. Table 6 shows the test results for two different images (Baboon image ( $512 \times 512$ ) and Pepper image ( $256 \times 256$ )). It can be seen that the same converted image can be obtained fastly when using the FPGA implementation, with a minimum error (due to the use of difference data representation in the two implementations).

## 7. Conclusion

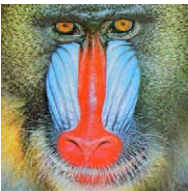





Processing an image in the RGB color space, with a set of RGB values for each pixel is not the most efficient method. To speed up some processing steps many broadcast, video and imaging standards use luminance and color difference

Table 5  
Performance comparison with existing CSC cores

Design parameters	Slices	Speed (MHz)	Throughput (vector/clock cycle)
Proposed architecture (1)	70	128	8
Proposed architecture (2)	193	234	1
CAST.Inc [5]	222	112	1
ALMA.Tech [6]	222	105	1
Amphion Ltd [4]	204	90	1



Table 6  
Software/hardware implementations for RGB to YCrCb CSC comparisons

Original image	Software implementation	Hardware implementation	RMS error	Computation time (ms)	
				Software	Hardware
			Y Cr Cb	0.487 0.630 0.461	126 1.2
			Y Cr Cb	0.684 0.830 0.396	43 0.28

video signals, such as YCrCb, making a mechanism for converting between formats necessary.  $R'G'B' \leftrightarrow Y'CrCb$  conversions require enormous computing power. However, novel, scalable and efficient architectures based on DA principles have been reported in this paper. The implementation result shows the effectiveness of the DA approach. The performance in terms of the area used and the maximum running frequency of the proposed architectures has been assessed and has shown that the proposed systems requires less area and can be run with a higher frequency when compared with existing systems.

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