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# AGRE: A knowledge graph recommendation algorithm based on multiple paths embeddings RNN encoder



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#### ABSTRACT

More and more researches have focused on the use of knowledge graphs (KG) to solve the sparsity problem of traditional collaborative filtering recommendation systems. Most KG based recommendation algorithms focus on independent paths connecting users and items, or iteratively propagate user preferences in KG. However, the current approachs that focus on indedpent paths ignore the association between paths. Therefore, in this study, we propose a knowledge graph recommendation system algorithm for the multiple paths RNN encoder (AGRE), which fully considers the association between paths. Specifically, the paths between the user and the item are coded by a specified RNN (MRNN) to accurately learn the user's preferences. Traditional RNNs can encode multiple paths without considering the association between paths, but our RNN can encode multiple paths with considering the association between paths. We have compared AGRE with other state-of-the-art algorithms on three real-world datasets, and achieved good results in terms of AUC and Precision@K. This indicates that AGRE could solve the problem of sparse interaction between users and items, and could make full use of the knowledge graph for recommendation.

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# 1. Introduction

With the rapid growth of data volume, the phenomenon of information overload becomes more and more common, and it is difficult for individual users to quickly find items and content of interest to them. As a technology to solve information overload, recommendation system has received more and more attention and has been applied in some practical application scenarios [1-4]. In order to achieve personalized recommendations, traditional collaborative filtering methods use various online unstructured data of users, such as the number of clicks, ratings, etc., and predict user preferences for items based on these historical information [5]. Generally speaking, a learnable collaborative filtering model consists of embedding and interactive data modeling [6]. Among them, embedding can transform users and items into vector forms, and interactive data modeling can reconstruct historical interactive information of users and items based on embedding vectors. For example, the matrix factorization model

directly expresses the IDs of users and items in vector form, and models their interaction through inner products [7]. The neural collaborative filtering model uses a nonlinear neural network instead of the inner product interaction function in the matrix factorization model [6,8]. The collaborative filtering model based on translation uses Euclidean distance as an interactive function to predict recommendation results [9].

In order to solve the problem that the traditional collaborative filtering system only considers descriptive features (user ID and item ID, attributes) to construct the embedding function, which may make it difficult for the collaborative filtering algorithm to generate a satisfactory embedding vector. In addition, when the number of interactions deeply digs into the complex useritem relationship, these methods tend to overfit, which makes the sparsity problem even more serious. Therefore, researchers propose to use auxiliary information in the recommendation system to enrich the semantic representation of items, such as social networks, attributes, and multimedia [10-16]. Recently, the knowledge graph (KG) has attracted more and more attention from the recommendation system research community because it contains more comprehensive and effective recommendation auxiliary data such as networks, item attributes and user information etc [17-24]. The recommendation algorithm considering the knowledge graph is generally considered from the following three

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aspects: direct relationship [18,25–30], semantic path [31,31–36] and propagation [37–42].

However, the above algorithms have some problems such as the following: (1) Since only the direct relationship between entities is considered, the method based on direct relationship cannot fully capture the complex semantics of the connection between the user and the item to enhance the embedding learning; (2) the method based on semantic path inevitably leads to information loss to decompose the complicated association between users and items into separate linear paths, so they ignore the association between paths; (3) Due to there is no constraint between the target entity and its neighbors, the propagationbased embedding learning process introduces noise (neighbors unrelated to specific interactions) and heavy computation (a large number of neighbors), thereby reducing the performance of the algorithm. In order to solve the above-mentioned problems, this study proposes a knowledge graph recommendation algorithm based on a multiple paths RNN encoder (AGRE).

AGRE can learn more accurate embedding by mining and connecting specific semantic paths from KG, and making use of the rich semantics of the connection between users and items in an automatic way through considering the association between paths. To sum up, our contribution are as follows: (1) We consider the association between paths (In addition to u and v, there are other common nodes in the path. For example, the path  $u \to a \to b \to v$  and the path  $u \to a \to c \to v$  have common node a); (2) We design an improved RNN encoder and apply it to encode multiple paths (MRNN). As far as we know, it is the first time that RNN has been applied to encode multiple paths between users and items with considering the association between paths; (3) We conduct experiments on three real datasets, and compared with other state-of-the-art algorithms. The experimental results indicate AGRE's rationality and effectiveness.

The remainder of this work is organized as follows: In Section 2, we introduce related work. In Section 3, we specify Framework of AGRE 3.1, and MRNN 3.2, attention mechanism 3.3, prediction 3.4, model optimization 3.5 and experimental setup 3.6. In Section 4, we conduct extensive experiments to evaluate the proposed method for AGRE. Finally, in Section 5, we discuss and conclude this work.

#### 2. Related work

Recommendation algorithms based on knowledge graphs are mainly considered from the following three aspects: methods based on direct relationships, methods based on semantic paths, and methods based on propagation. First, the method based on direct relationship is to use the relationship between directly connected entities in KG for embedding learning. For example, CKE [25] uses TransR [26] to learn items' embeddings with the participation of KG. DKN [27] uses KG to generate news embedding through TransD [28]. KTUP [18] complements recommended model and knowledge map through TransH [29] joint learning. MKR [30] uses KG embedding to standardize recommendation tasks. Additionally, the semantic path-based method measures the connectivity between users and items through the similarity of meta-paths [31], such as PER [31], HeteCF [32] and Sem-Rec [33]. Some researchers use random walk based on meta-path to achieve better embedding learning, such as Metapath2vec [34]. However, methods based on meta-path rely on manual features, which greatly hinders the universality of these methods. Therefore, RKGE [35] and KPRN [36] automatically extract the paths that have length constraints connecting users and items, and model these paths through recurrent neural network (RNN). Moreover, the strategy of the propagation-based method is to iteratively propagate across the entire KG to help recommendations. RippleNet [37], for example, expands user's interest along the edge in KG to discover user's potential interest. KGCN [38] and KGCN-LS [39] use Graph convolution Network (GCN [40]) to calculate items' embeddings through the propagation between neighbors in KG. KGAT [41] recursively performs propagation on KG through GNN to refine entity embedding. These methods, which take the whole KG as input, learn entities' embedding by aggregating the information from its neighbors.

# 3. Model

This section introduces the advantages of the ARGE algorithm and its detailed construction process. In this study, the knowledge graph is an directed graph. Its construction process is as follows: (1) Add all users, items and their attributes to the knowledge graph; (2) Connect items and their corresponding attributes; (3) Connect users and items that interact with users.

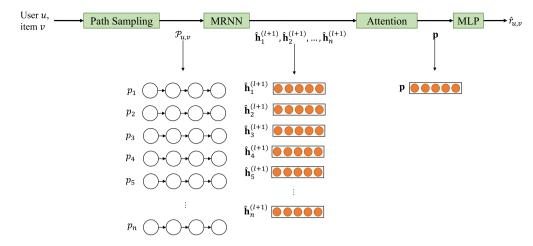
Compared with the traditional knowledge graph algorithms [35–41,43–46], we believe that multiple paths in the knowledge graph are beneficial for recommendation, mainly from the following two aspects. On the one hand, as a nonlinear combination of independent paths, multi-paths contain rich semantic and topological information and are more expressive than independent paths. On the other hand, the paths only retains the entities and relationships related to the specific (u, v) interaction, which can effectively avoid the noise caused by KG.

However, applying multiple paths to infer users' preferences is not an easy task, and it mainly faces the following two challenges. The first challenge is how to consider the associations between paths. Association is universal, and better results are usually obtained when association are taken into account. The GNN is a good example, which introduces the association between samples. But the current approachs ignore the association between paths. The second challenge is how to encode the extracted multiple paths in an efficient way to enhance user preference inference. In the literatures [35,36], RNN has been used to generate representation vectors for paths, but the first challenge prompted us to design a RNN model that could be used to encode multiple paths and take into account the associations between paths. The RNN generates multiple path representation vectors that consider the association between paths from each independent path representation.

Table 1 is a description of symbols commonly used in this study.

# 3.1. Framework

This section introduce the overall framework of AGRE, which applies an improved RNN to encode multiple paths. The entire working process of the model is shown in Fig. 1. AGRE mainly includes four modules, followed by Path Sampling, MRNN, Attention and MLP. The specific input and output of each module are shown in Fig. 1. Path sampling is to extract the paths between user u and item v. The length of the paths is l. We bring the paths in  $\mathcal{P}_{u,v}$  into the model, and this process incurs huge computational cost. Additionally, too many paths may introduce noise. In order to balance the computational cost and possible noise problems, we set a fixed number of paths to n during the calculation. These paths form the set  $\mathcal{P}_{u,v}$ . MRNN can encode multiple paths, taking into account the associations between paths. Attention can aggregate multiple pieces of information to obtain the embedding of multiple paths. The MLP outputs the predicted probability of user u interacting with the item v.



**Fig. 1.** The user u and item v are input into path sampling to obtain the paths between user u and item v. And the path set  $\mathcal{P}_{u,v}$  is input into MRNN to obtain the hidden state  $\hat{\mathbf{h}}_j^{(l+1)}$  that is the embedding of path. Attention aggregates information from multiple paths. Finally, the embedding  $\mathbf{p}$  of multiple paths is input into the MLP, and the probability  $\hat{\mathbf{r}}_{u,v}$  of the user u clicking on the item v is obtained.

Table 1
Model symbol introduction.

Model symbol introduction.			
Description			
Learnable parameter			
Learnable parameter			
Learnable parameter			
The set of path between $u$ and $v$			
$r_{u,v} = 1$ represents that user $u$ has interacted with item $v$ ,			
$r_{u,v} = 0$ indicates that user $u$ has not interacted with item $v$			
User			
Item			
The length of paths			
The size of $\mathcal{P}_{u,v}$			
The path in $\mathcal{P}_{u,v}$			
The relation-embedding of the $j$ -th node in path $p_i$			
The hidden state of the $j$ -th node in path $p_i$			
The path-association hidden state of the j-th node in ith path			
Sigmoid function			
The predicted probability of user $u$ interacting with item $v$			
Loss function			
The parameters of AGRE			
Training set			
L2 regularization coefficient			
Cross entropy			

### 3.2. MRNN

The traditional path-based method only encodes one path, and ignores the association between paths. In this work, we proposed a MRNN method, compared with RNN can only encode one path, MRNN considers the association between paths and can encode multiple paths. The MRNN is shown in Fig. 2.

# 3.2.1. Relation perception

Because relationships have different meanings for entities, relationships can help models express clearer semantics. For example, singing relationship and composition relationship have different meanings for a piece of music. And relationships between entities are used in many literatures [30,37,47].

Eq. (1) is the relation-embedding of the *j*-th node in the path  $p_i$ , where  $\mathbf{e}_i^j$  is the embedding of  $e_i^j$ , and  $\mathbf{r}_i^j$  is the embedding of  $r_i^j$ .

$$\mathbf{x}_{i}^{j} = \begin{bmatrix} \mathbf{e}_{i}^{j} \\ \mathbf{r}_{i}^{j} \end{bmatrix}, \tag{1}$$

For examples,  $\mathcal{P}_{u,v} = \{p_1, p_2, p_3, \dots, p_n\}, p_i = \{e_i^1, r_i^1, e_i^2, r_i^2, e_i^3, \dots, r_i^l, e_i^{(l+1)}\}$ , where  $\mathcal{P}_{u,v}$  is the set of the paths between

user u and item v,  $p_i$  is the path in  $\mathcal{P}_{u,v}$ ,  $e_i^j$  is the j-th node in the path  $p_i$ ,  $r_i^j$  is the relation between  $e_i^j$  and  $e_i^{(j+1)}$ . In particular,  $r_i^{(l+1)}$  is a relation that does not exist. For consistency with other entities, we give an empty relationship. An empty relationship means no relationship. The input of RNN is  $[\mathbf{x}_1^j, \mathbf{x}_2^j, \mathbf{x}_3^j, \dots \mathbf{x}_n^j]$ .

# 3.2.2. Path association

To effectively apply KGs for recommendation, obtaining embeddings for multiple paths is a key aspect to consider. Since there are also associations between different paths, in order to obtain a better embedding of multiple paths in the knowledge graph, we must add the association between paths in the AGRE algorithm. In traditional relation mining methods, semantic pathbased methods do not consider the associations among paths [35, 36,48]. Here, we comprehensively considered the associations between paths.

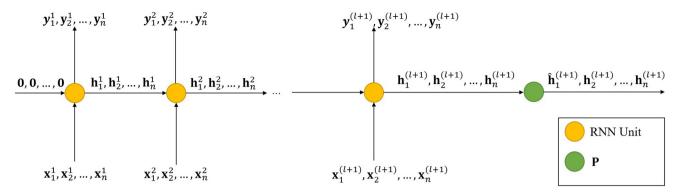
$$\mathbf{h}_{i}^{j} = \sigma(\mathbf{W}\mathbf{x}_{i}^{j} + \mathbf{H}\mathbf{h}_{i}^{(j-1)}), \tag{2}$$

$$[\hat{\mathbf{h}}_{1}^{(l+1)}, \hat{\mathbf{h}}_{2}^{(l+1)}, ..., \hat{\mathbf{h}}_{n}^{(l+1)}] = \sigma([\mathbf{h}_{1}^{(l+1)}, \mathbf{h}_{2}^{(l+1)}, ..., \mathbf{h}_{n}^{(l+1)}]\mathbf{P}), \tag{3}$$

In Eqs. (2) and (3),  $\mathbf{W} \in \mathbb{R}^{2d \times 2d}$  and  $\mathbf{H} \in \mathbb{R}^{2d \times 2d}$  are the learnable matrixes,  $\hat{\mathbf{h}}_i^{(j-1)} \in \mathbb{R}^{2d \times 1}$  is the hidden state of the (j-1)-th node in the path  $p_i$ .  $\mathbf{P} \in \mathbb{R}^{n \times n}$  is a learnable matrix, and  $\mathbf{h}_i^{(l+1)}$  is the embedding of the path  $p_i$ . We use a normal RNN to obtain embeddings for each path, and use the matrix  $\mathbf{P}$  to obtain path-association embeddings of the paths. The path-association embeddings fully considers the connections between paths. The path-association embeddings are generated by the embeddings of the paths, so path-association embeddings take into account the association between paths. The matrix  $\mathbf{P}$  can distinguish the influence of each path embedding, which acts as an attention mechanism.

# 3.3. Attention mechanism

The MRNN finally outputs the hidden states of node v in each path. It is the embeddings for these paths. In order to obtain embedding for multiple paths, these hidden states must be aggregated. There are two ways of aggregation. One is to add all hidden states and take the average. The other is to use an attention mechanism to distinguish the effects of these hidden states. Intuitively, different hidden states have different effects



**Fig. 2.** The difference between MRNN and ordinary RNN is the matrix **P**, we consider the association between paths through the learnable matrix **P**. To obtain the hidden state of each node, each node of the path is input into the RNN unit. The embedding of the path  $p_i$  is obtained. Finally, the path-association embeddings are obtained by the matrix **P**.

on the embedding of multiple paths, so the attention mechanism should be adopted.

$$a_i = \sigma(\mathbf{W}_a \hat{\mathbf{h}}_i^{l+1} + \mathbf{b}_a), \tag{4}$$

$$\mathbf{p} = \sum_{i=1}^{l=n} a_i \hat{\mathbf{h}}_i^{(l+1)},\tag{5}$$

In Eq. (4),  $a_i$  is the attention weight for *i*-th path in  $\mathcal{P}_{u,v}$ ,  $\mathbf{W}_a \in \mathbb{R}^{2d \times 1}$  and  $\mathbf{b}_a \in \mathbb{R}^{1 \times 1}$  are the learnable matrix. In Eq. (5),  $\mathbf{p} \in \mathbb{R}^{2d \times 1}$  is the embedding for multiple paths in  $\mathcal{P}_{u,v}$ .

# 3.4. Prediction

By applying AGRE, we can better learn the representation of multiple paths. The representation of multiple paths is further used to predict user's preference for item. We use a MLP to simulate the interaction between user and item [35], which is shown as Eq. (6):

$$\hat{r}_{uv} = \sigma(\mathbf{W}_{p}\mathbf{p} + \mathbf{b}_{p}), \tag{6}$$

Where  $\hat{r}_{uv}$  is the predicted probability of user u interacting with item v,  $\mathbf{W}_p \in \mathbb{R}^{2d \times 1}$  and  $\mathbf{b}_p \in \mathbb{R}^{1 \times 1}$  are learnable parameters. We use sigmoid function to control the predicted probability within the range of 0–1.

# 3.5. Model optimization

Objective function: Many studies [6,36,41,47–49] treat top-k recommendation as a binary classification task. Therefore, cross-entropy is the objective function, the formula is as follows Eq. (7)

$$\mathcal{J} = \sum_{(u,v) \in \mathcal{D}_{train}} \text{BCELOSS}(\hat{r}_{u,v}, r_{u,v}) + \lambda \|\mathcal{F}\|_2^2$$
 (7)

where  $\lambda$  is the L2 regularization coefficient,  $\mathcal{F}$  is the parameters of the model, and  $\mathcal{D}_{train}$  is training set. The first term represents cross-entropy, and the second term represents L2 regularization.

# 3.6. Experienment setup

# 3.6.1. Dateset

Datasets: (1) Last.FM [30] belongs to music recommendation. (2) Movielens-100K [35] is the record of user movies. (3) Yelp [35] is the record of user reviews for businesses.

Data processing: If an item is in a user's record, the user has interacted with the item. According to literature [27,37,38], the number of negative samples is the same as the number of positive samples. We randomly divide the records of each

Table 2
Dataset attributes

Butubet uttilbutesi			
Dataset	Last.FM	Movielens-100K	Yelp
#users	1876	943	16308
#items	3846	1674	11516
#interactions	21173	99974	199422
#entities	9366	6800	12088
#triples	15518	24686	85758
#relations	60	6	4
#items #interactions #entities #triples	3846 21173 9366 15518	1674 99974 6800 24686	11516 19942 12088

user into training set and test set according to 7:3. The number of attributes extracted from different data sets is displayed in Table 2, including: users, items, relations, triples, interactions and entities.

# 3.6.2. Evaluation

According to the literature [6,36,50], To reduce the complexity of evaluating the algorithm, we randomly select 100 users, and we randomly select 100 items that have not interacted with each user, and then randomly select 1 item in the test set. The recommendation list for each user consists of 101 items.

AUC [51] measures the extent to which a recommender system can distinguish items that users like from items they do not like. Precision@K [51] is the proportion of items that users like among the multiple items recommended by the system ( $K=\{1, 2, 5, 6, 7, 8, 9, 10\}$ ). The higher these metrics, the better the performance of the algorithm.

# 3.6.3. Baselines

Some state-of-the-art algorithms recently proposed are baselines. These algorithms include methods based on direct relationships, methods based on semantic paths and methods based on propagation.

- Methods based on direct relationships: CKE applies TransR and has no text and image data. MKR [30] applies TransH [29] to combine recommendation module and KG embedding module. For MKR, we search for best L in {1, 2, 3}, best T in {1, 2, 3, 4, 5}. According the code of MKR, the KGE weight is fixed to  $10^{-6}$ .
- Methods based on semantic paths: MCRec [48] uses metapath. We design two meta-paths: user → item → attribute → item and user → item → user → item. The number of paths is set by the original paper. RKGE [35] automatically extracts the paths that have length constraints connecting users and items. RKGE encodes the paths by RNN. The number of paths is set by the code of RKGE and the length of path is set by the original paper. KARN [44] integrates the user click history sequence and

**Table 3**The setting of some hyper parameters

THE SETTING OF SOME	he setting of some hyper parameters.				
Dataset	n	d	l	η	
Last.FM	30	20	3	0.001	
Movielens-100K	30	40	3	0.01	
Yelp	20	20	3	0.001	

the path connectivity between the user and the recommended items. Except for the embedding dimension, other parameters follow the original paper settings.

Methods based on propagation: RippleNet [37], KGCN [38] and CKAN [47] iteratively propagate across the KG to improve recommendation. We search best H or L in {1, 2, 3, 4}, and the size of set or neighbors in {5, 10, 20, 30, 40, 50}. The KGE weight in RippleNet is set by the code of RippleNet.

For all algorithms, the optimizer is Adam, and mini-batch gradient descent algorithm is applied for model optimization. They are widely used optimization strategies [37,38,41]. The batch size is fixed to 1024, the L2 regularization coefficient is fixed to 10<sup>-5</sup>, and the learning rate adjusted based on experience. We search for best embedding dimension in {5, 10, 20, 30, 40, 50}.

# 3.6.4. Parameter settings

For AGRE, d (the embedding dimension of entity) and n (the number of paths between user and item), l(the length of path) are important hyperparameters. Initially, We search for the best n in  $\{5, 10, 20, 30, 40, 50\}$  and search for the best d in  $\{5, 10, 20, 30, 40, 50\}$ , search for the best d in  $\{3, 4, 5\}$ . The roles of these hyperparameters are discussed in Section 4.3. For comparison with other state-of-the-art algorithms, other parameters are the same as these algorithms. Table 3 shows the hyperparameters in this work, where  $\eta$  is the learning rate.

# 4. Experiment and analysis

In this section, the following three questions are answered through experiments on Last.FM, Movielens-100K and Yelp datasets: (1) Does the AGRE outperforms state-of-the-art algorithms? (2) Do some modules of AGRE affect the model? (3) How does the AGRE is affected by the hyperparameters?

# 4.1. Compare to baselines

In order to better understand the performance of the AGRE algorithm, we compare the performance of the eight different state-of-the-art algorithms on three different datasets, and Fig. 3 shows the results. It is apparent that in majority of cases, the performance of the AGRE is better than other eight different algorithms. Comparing Figs. 3(a), 3(b) and 3(c), it can be observed that as K increases, the precision decreases. The performance of the AGRE algorithm is generally better than other algorithms. For example, in Last.FM, when K={1, 2, 5, 6, 7, 8, 9, 10}, compared with the best results of state-of-the-art algorithms, AGRE outperforms by 8.91% on average. Additionally, compared with the worst case of these algorithms, when K={1, 2, 5, 6, 7, 8, 9, 10}, AGRE outperforms by up to 65.02% on average. Compared with the average values of other algorithms when K={1, 2, 5, 6, 7, 8, 9, 10}, AGRE outperforms by 34.27%, 34.55%, 24.59%, 25.13%, 27.54%, 22.51%, 21.43% and 18.45%, respectively. These results demonstrate that the competitive prediction precision of the AGRE algorithm. It should, however, be noted that K could affect the precision of AGRE and other algorithms.

Generally speaking, AUC is one of the most important evaluation metrics for measuring the performance of model. Table 4

**Table 4**The comparison of AUC in different model.

Model	Dataset		
	Last.FM	Movielens-100K	Yelp
AGRE	0.853	0.886	0.878
MKR	0.796	0.812	0.858
CKE	0.828	0.845	0.842
RKGE	0.802	0.839	0.858
MCRec	0.839	0.845	0.869
CKAN	0.763	0.797	0.806
Ripplenet	0.805	0.873	0.825
KGCN	0.781	0.865	0.812
KARN	0.842	0.856	0.872

**Table 5**The results for AGRE comparing to variants.

	Last.FM	Movielens-100K	Yelp
AGRE	0.853	0.886	0.878
AGRE-P	0.846	0.872	0.873
AGRE-a	0.846	0.879	0.873
AGRE-r	0.827	0.884	0.875

illustrates the AUC values of each model on the three datasets. As can be seen in Table 4, in the majority of cases, the AGRE is revealed a considerably higher AUC values than other algorithms. For instance, compared with all other 8 top algorithms, the AUC value of the AGRE algorithm has achieved good performance in three different datasets.

Yelp is the most sparse of all datasets. However, AGRE can still outperform other algorithms. This shows that AGRE can solve the data sparsity problem very well.

These results indicate that the effectiveness of MRNN in the AGRE algorithm. Beacause MRNN takes into account the association between paths.

# 4.2. Compare to variants

To investigate the underlying reasons for the performance advantages of the AGRE algorithm, we study the role of relation perception and attention mechanism, the matrix  ${\bf P}$  in detail in this section.

- (1) AGRE-r removes relation perception:  $\mathbf{x}_i^j = \mathbf{e}_i^j$ ;
- (2) AGRE-a removes attention mechanism:  $\mathbf{p} = \frac{\hat{\mathbf{h}}_i^{(l+1)}}{n}$ ;
- (3) AGRE-P removes the matrix **P**:  $\hat{\mathbf{h}}_{i}^{(l+1)} = \mathbf{h}_{i}^{(l+1)}$ .

The Table 5 shows the result for AGRE comparing to its variants. AGRE outperforms three variants, which shows that relation perception, attention mechanism and the matrix **P** are important roles for AGRE.

# 4.3. Parameter sensitivity analysis

In order to explore the role of some hyperparameters in the AGRE algorithm, here we study the impact of the following three parameter changes on the performance of the AGRE algorithm on Last.FM. These parameters are: d (the embedding dimension of entity), n (the number of paths between user and item), and l (the length of path). We take the Last.FM dataset as an example to illustrate the impact of these hyperparameters.

It is known from the literature [49] that the number of paths between user and item is a significant influencing factor. It is evident from the results that the number of paths between user and item cannot be too large or too small, too large is easy to introduce noise, too small is easy to make MRNN become a RNN that encodes paths. As shown in Fig. 4(a), we observe that as n increases, the performance of the model is greatly improved at

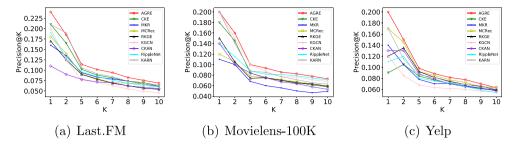
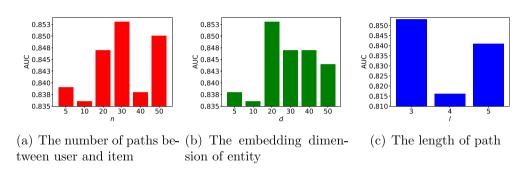


Fig. 3. These figures show Precision@K of different algorithms in 3 datasets. We get the values of Precision@K by taking K in {1, 2, 5, 6, 7, 8, 9, 10}. Figure (a) is the Precision@K in Last.FM. Figure (b) is the Precision@K in Movielens-100K. Figure (c) is the Precision@K in Yelp. The meaning of each curve is shown in the upper right corner of each subfigure.



**Fig. 4.** AUC reach max value when n = 30, d = 20, l = 3. AUC increases then decrease as d and n increase.

the beginning. Because more paths can help to encode the rich knowledge from KG. At the same time, the paths collected at the beginning may be independent (the nodes of each path do not have the same node except u and v). However, as n increases further, it gradually tends to a stable value in Last.FM, which means that too much semantic path integration introduce noise [49]. The results seem to indicate that the more paths between the user and the item, the more useful it is to improve the performance of the knowledge graph in terms of recommendation performance in a certain range.

It is known from the literature [37,41,49] that the appropriate embedding dimension is a significant influencing factor. Generally speaking, the embedding dimension cannot be too large or too small, too large is easy to overrepresent the entity, too small is easy to encode less useful information. Fig. 4(b) illustrate the findings of the impact of entity embedding dimension d on model performance. As can be seen, in the cases of data Last.FM, the performance of the AGRE starts to improve with the increase of d, reaches the best performance when d reaches a certain value, and then decreases as *d* continues to increase. This demonstrates that a larger embedding dimension significantly help to encode more useful information, but too large embedding dimensions may overrepresent the entity and thereby introducing noise [37, 41.49]. In addition, we should also note that the change of AUC value and d is a fluctuating trend. These results imply that more underlying complex mechanisms need to be explored in future.

We also study the effect of path length on AGRE. The results are shown in Fig. 4(c). As can be seen from it, AGRE performs best when the path length is 3. Because shorter paths contain clearer and interpretable semantics [35].

# 5. Conclusion and discussion

Due to the knowledge graph (KG) contains recommendation auxiliary data such as network, item attributes and user information, it has received more and more attention from the recommendation system research community. In order to solve the problem that the methods based on semantic path ignore the association between paths, this work proposes AGRE, a knowledge graph recommendation algorithm based on multiple paths RNN encoder. It integrates the structured information of the knowledge graph into the algorithm. The improved RNN is conducive to encoding the multiple paths between users and items at the same time. This considers the association between paths. In addition, AGRE effectively alleviates the sparsity problem and improves the accuracy of recommendations. Experimental results on three real-world datasets indicate that AGRE is generally better than other state-of-the-art algorithms in AUC and Precision@K. Meanwhile, AGRE provides users with more accurate recommendation results, and it also has strong flexibility in fusing heterogeneous data.

The AGRE algorithm uses the paths between user and item. Therefore, the algorithm relies heavily on the degree of association between sampling paths. For example, if there is no association in the sampling paths, the AGRE algorithm degenerate into an algorithm for encoding one path. Future research should adopt universally relevant sampling strategies, and consider users' online ratings [42], temporal information [52] and Artificial intelligence [53] etc.

# **CRediT authorship contribution statement**

**Na Zhao:** Conceptualization, Data curation, Formal analysis, Investigation, Methodology, Funding acquisition, Roles/Writing – original draft. **Zhen Long:** Data curation, Formal analysis, Methodology, Roles/Writing – original draft. **Jian Wang:** Formal analysis, Methodology, Roles/Writing – original draft, Funding acquisition. **Zhi-Dan Zhao:** Conceptualization, Data curation, Formal analysis, Investigation, Methodology, Funding acquisition, Roles/Writing – original draft, Writing – review & editing.

#### **Declaration of competing interest**

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

# Data availability

Movielens-100K and Yelp are RKGE dataset, which can be obtained from the following website. If you want to use this data, please refer to the official instructions https://github.com/sunzhuntu/Recurrent-Knowledge-Graph-Embedding. The Last.FM is MKR dataset, which is available from the https://github.com/hwwang55/MKR.

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