

1. The means model and the effects model for two-way ANOVA are equivalent.

True

False

2. Consider the means model for two-way ANOVA as described in our video:

$$Y_{ijk} = \mu_{jk} + \varepsilon_{ijk}$$

where  $Y_{ijk}$  is the  $i^{th}$  measurement of the response in the  $j^{th}$  level of the  $\tau$  factor and the  $k^{th}$  level of the  $\alpha$  factor; and  $i = 1, \dots, n_{jk}$ .

$n_{jk}$  is the total number of observations in the study/experiment.

False

True

3. In the two-way ANOVA effects model,  $\tau_j$  can be interpreted as:

the true difference between the grand mean and the mean of the response in the  $j^{th}$  level of the  $\tau$  factor, holding the  $\alpha$  factor constant.

the true difference between the grand mean and the mean of the response in the  $j^{th}$  level of the  $\tau$  factor, holding the  $\alpha$  factor at its mean value.

The causal effect of the  $j^{th}$  level of the  $\tau$  factor, adjusting for the  $\alpha$  factor.

the true difference between the grand mean and the mean of the response in the  $j^{th}$  level of the  $\tau$  factor, adjusting for the  $\alpha$  factor.

4. The error term in the two-way ANOVA means model is assumed to be distributed as:

$$\varepsilon_{ijk} \overset{i}{\sim} N(0, \sigma_i^2).$$

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5. Consider the two-way ANOVA effects model:

$$Y_{ijk} = \mu + \tau_j + \alpha_k + \varepsilon_{ijk}$$

and suppose that, for all levels of  $\alpha$ , the mean response for units in  $\tau_1$  is greater than the mean response for units in  $\tau_2$ . Then, necessarily, the move from  $\tau_1$  to  $\tau_2$  causes the increase in the mean response.

True

False

6.

Factor A	factor B	Response
1	1	10.9
2	1	9.2
3	1	8.0
1	2	8.6
2	2	11.1
3	2	7.3
1	3	9.9
3	3	8.5

Suppose that the data frame above is an entire two-factor study. Does this data frame constitute a full factorial design?

Yes

No