

np Charts: Control Charts for Proportions / Percentages

**Data Science for Quality Management:
Control Charts for Discrete Data**
with **Wendy Martin**

Learning objectives:

Calculate Control Limits for the np chart using the normal approximation

Calculate Control Limits for the np chart using the exact calculation

Generate the np chart using R software

Control Limits (Normal Approximation)

$$UCL = \bar{np} + 3\sqrt{\bar{np}(1 - \bar{p})} = 17.69$$

For the Total

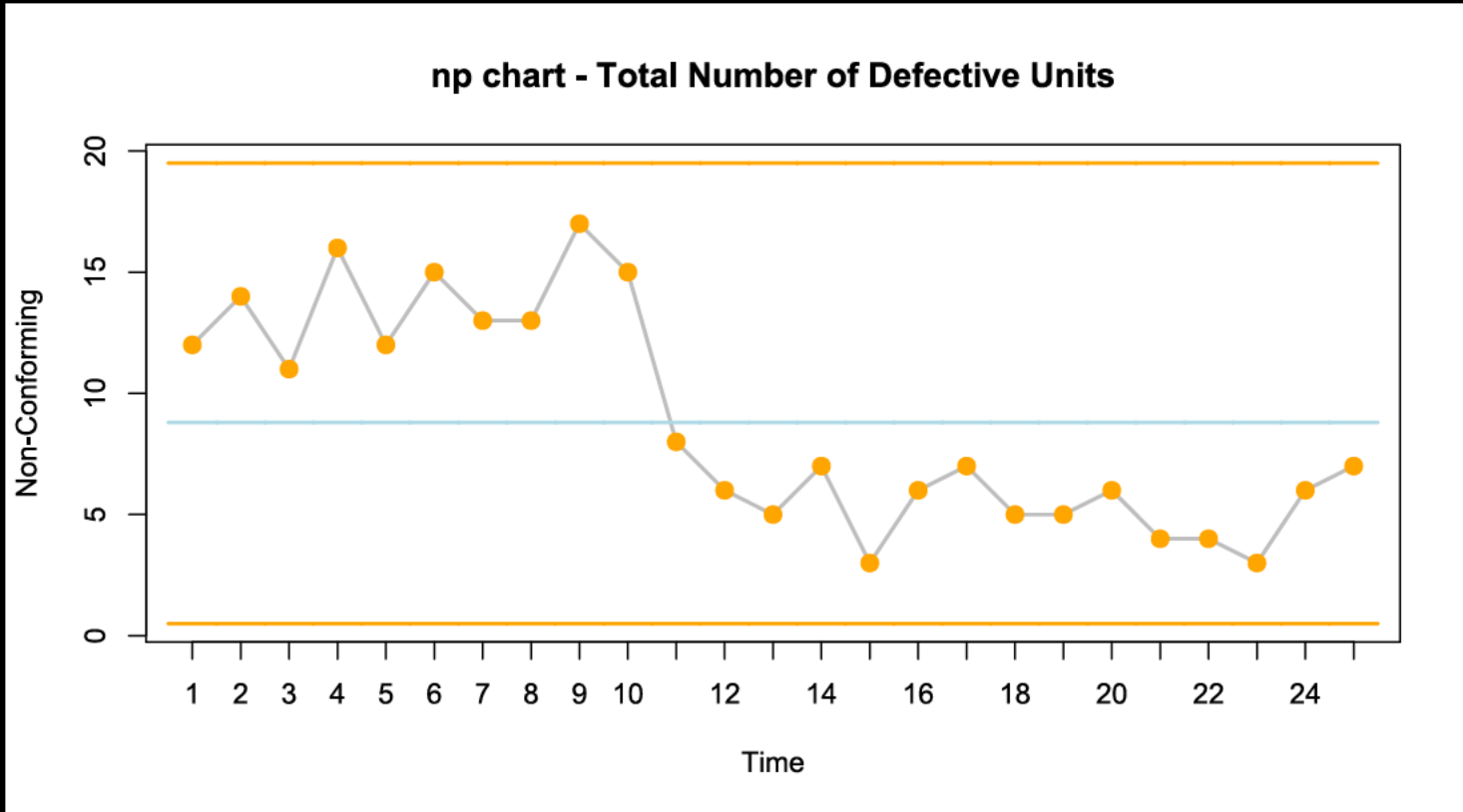
$$LCL = \bar{np} - 3\sqrt{\bar{np}(1 - \bar{p})} = \text{none}$$

For the Total

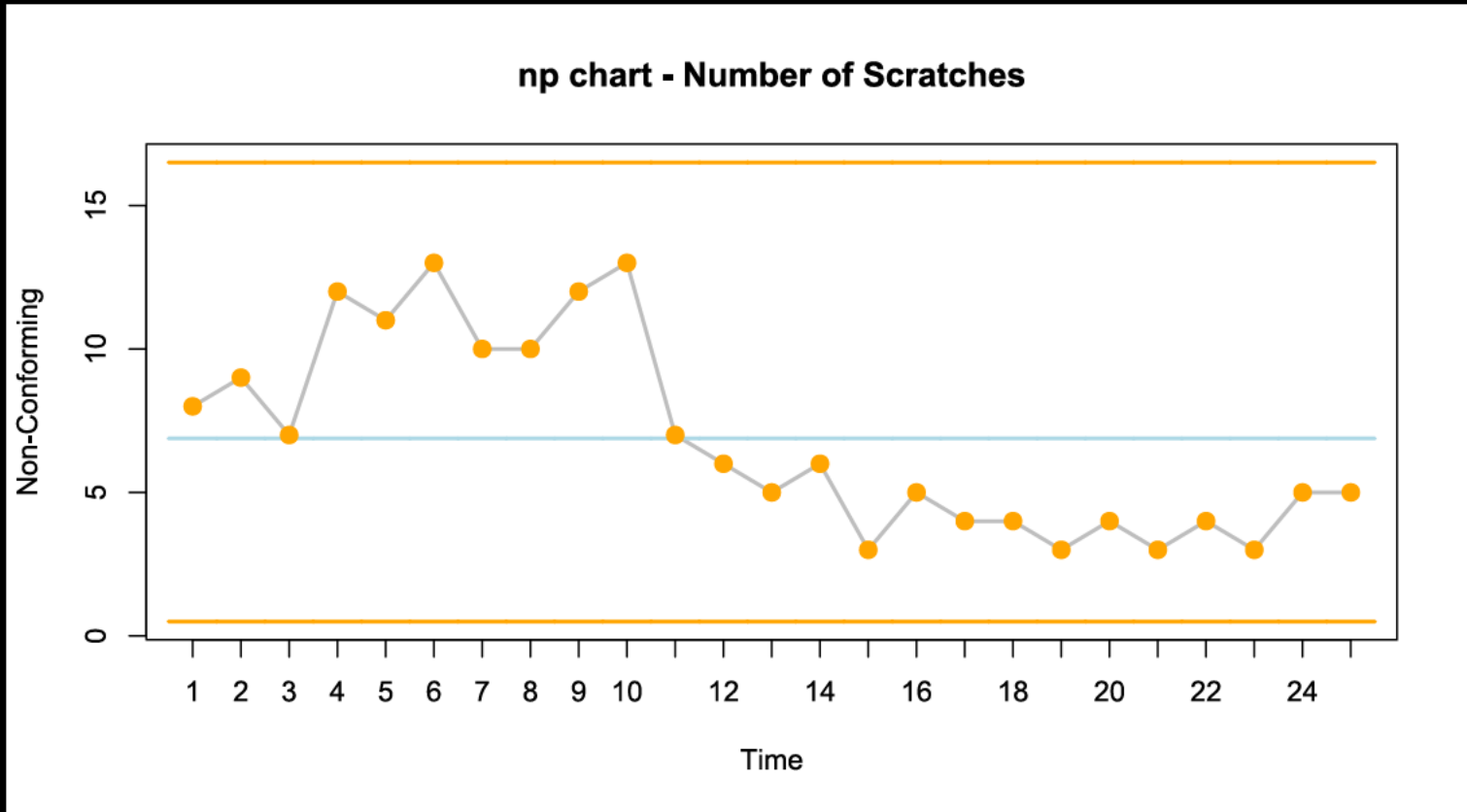
Exact Binomial Control Limits

- Using the binomial distribution
 - Calculate \bar{p} by dividing the average number of defects (8.8) by the sample of 5000 = 0.00176 for Total
 - Find UCL where $P(r \text{ and above}) \leq 0.00135$ and use $(r - 0.5)$ for the UCL = **19.5**
 - Find LCL where $P(r \text{ and below}) \leq 0.00135$ and use $(r + 0.5)$ for the LCL = **0.5**

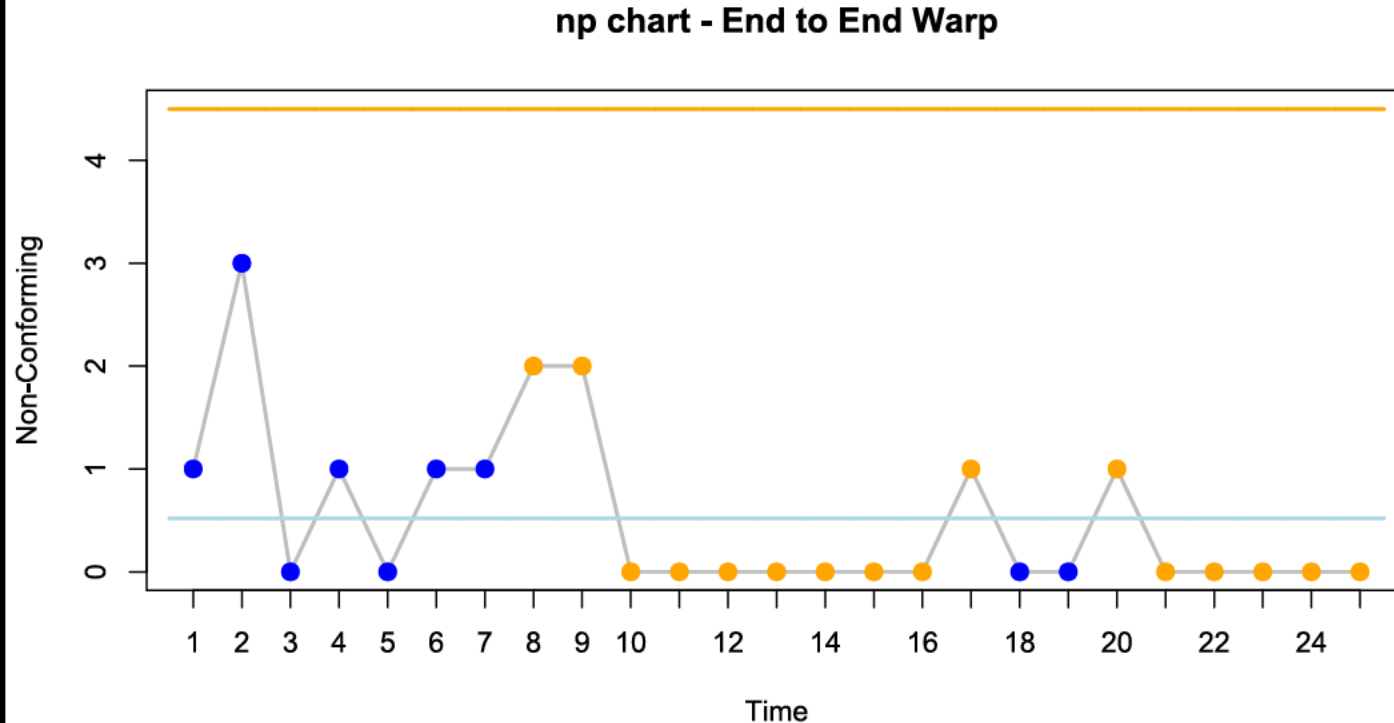
Control Chart Total



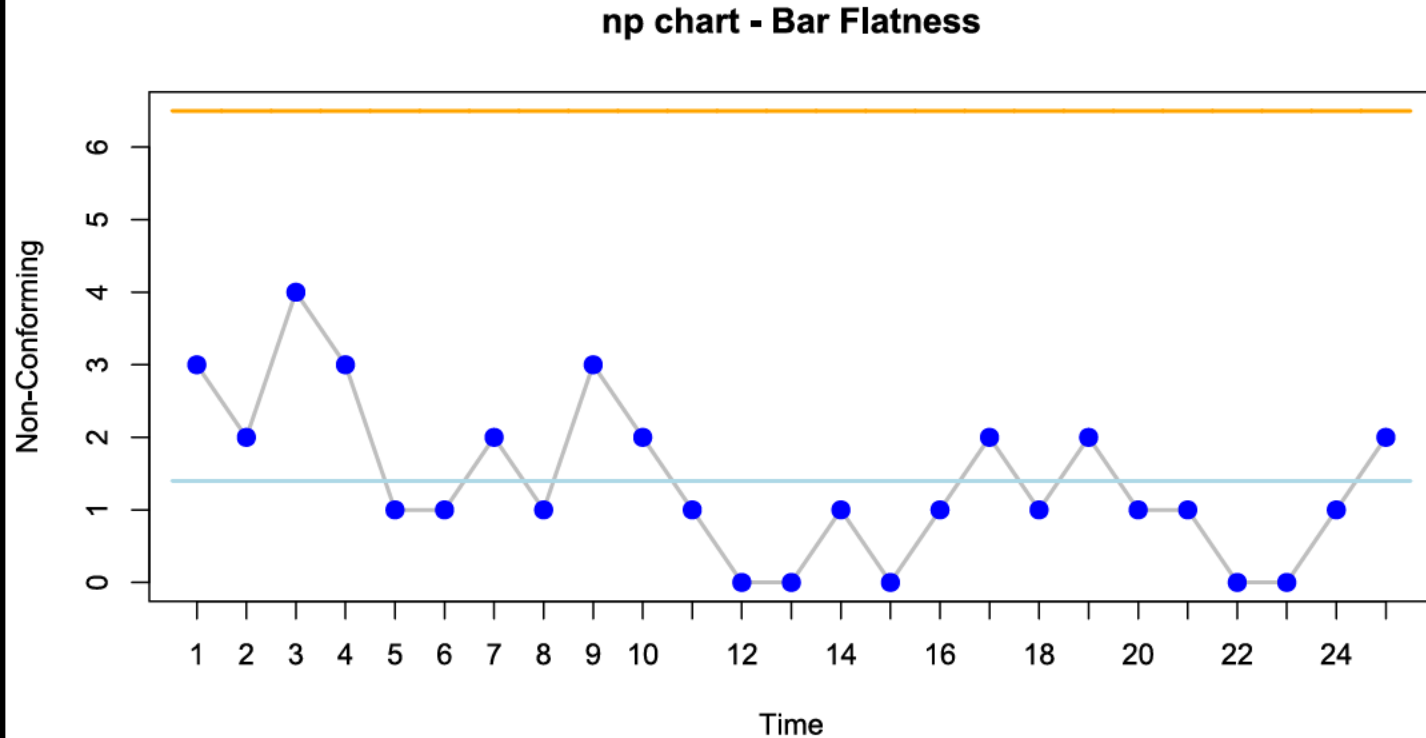
Control Chart Scratches



Control Chart Warp



Control Chart Flatness



Step 6: Assess the Process for Control

- Assess the process for: points outside the limits, runs, trends, cycles, and unusual patterns of variation.
- Can you provide an explanation as to why it was important not to just look at the 'Total'?

Sources

The material used in the PowerPoint presentations associated with this course was drawn from a number of sources. Specifically, much of the content included was adopted or adapted from the following previously-published material:

- Luftig, J. An Introduction to Statistical Process Control & Capability. Luftig & Associates, Inc. Farmington Hills, MI, 1982
- Luftig, J. Advanced Statistical Process Control & Capability. Luftig & Associates, Inc. Farmington Hills, MI, 1984.
- Luftig, J. A Quality Improvement Strategy for Critical Product and Process Characteristics. Luftig & Associates, Inc. Farmington Hills, MI, 1991
- Luftig, J. Guidelines for Reporting the Capability of Critical Product Characteristics. Anheuser-Busch Companies, St. Louis, MO. 1994
- Spooner-Jordan, V. Understanding Variation. Luftig & Warren International, Southfield, MI 1996
- Luftig, J. and Petrovich, M. Quality with Confidence in Manufacturing. SPSS, Inc. Chicago, IL 1997
- Littlejohn, R., Ouellette, S., & Petrovich, M. Black Belt Business Improvement Specialist Training, Luftig & Warren International, 2000
- Ouellette, S. Six Sigma Champion Training, ROI Alliance, LLC & Luftig & Warren, International, Southfield, MI 2005