

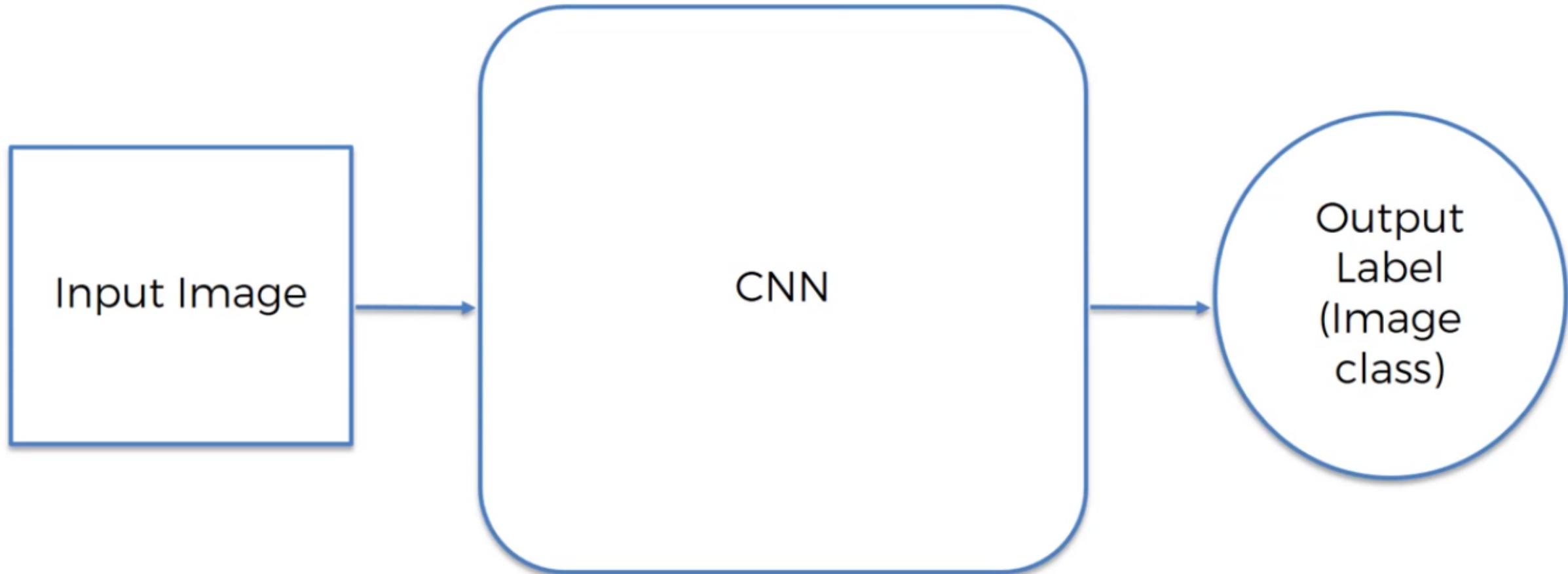
# Convolutional Neural Networks

# Plan of Attack

What we will learn in this section:

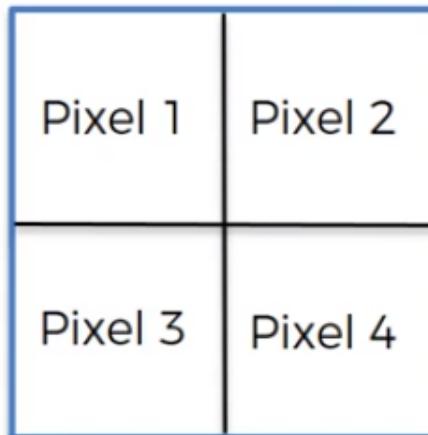
- What are Convolutional Neural Networks?
- Step 1 - Convolution Operation
- Step 1(b) - ReLU Layer
- Step 2 - Pooling
- Step 3 - Flattening
- Step 4 - Full Connection
- Summary
- EXTRA: Softmax & Cross-Entropy

# Convolutional Neural Networks

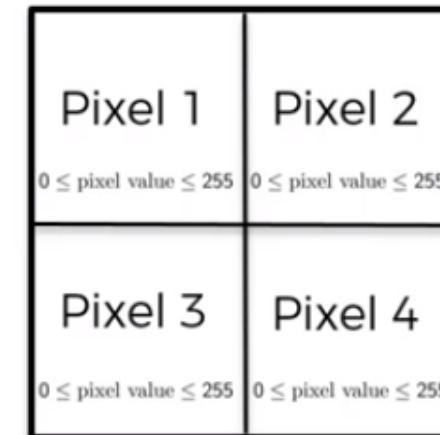


# Convolutional Neural Networks

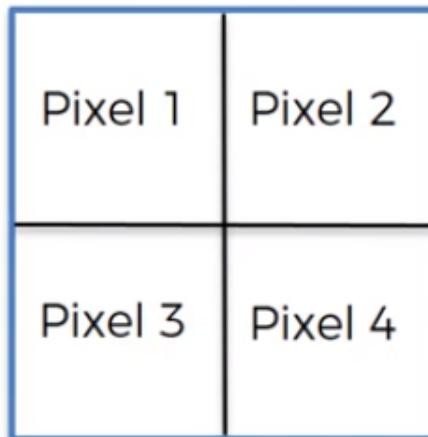
B / W Image 2x2px



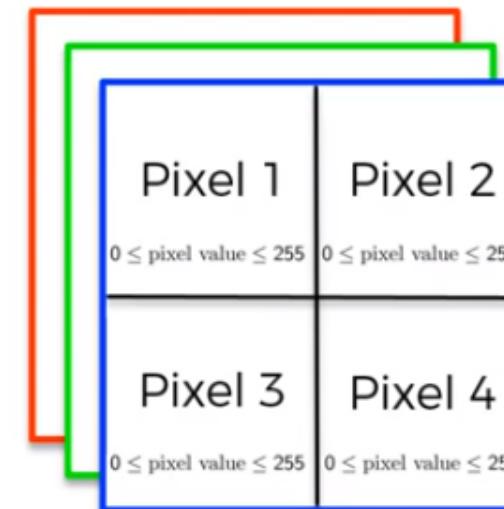
2d array



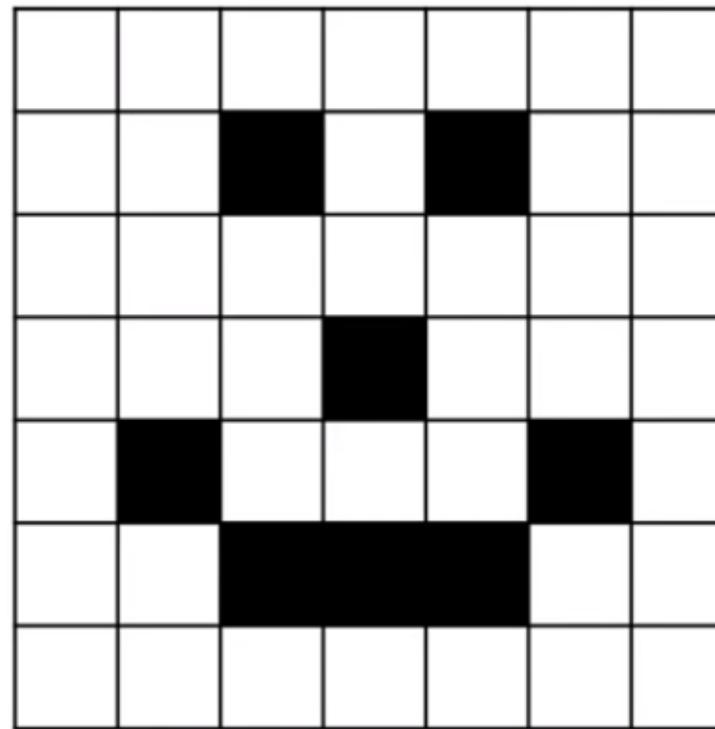
Colored Image 2x2px



3d array



# Convolutional Neural Networks



0	0	0	0	0	0	0	0
0	1	0	0	0	1	0	0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	1	0	0	0	0	1	0
0	0	1	1	1	0	0	0
0	0	0	0	0	0	0	0

# Convolutional Neural Networks

STEP 1: Convolution



STEP 2: Max Pooling



STEP 3: Flattening



STEP 4: Full Connection

# Step 1 – Convolution

# Step 1 - Convolution

$$(f * g)(t) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} f(\tau) g(t - \tau) d\tau$$

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image

0	0	1
1	0	0
0	1	1

Feature Detector

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



0				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0	0
0	1	0	0	0	1	0	0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	1	0	0	0	1	0	0
0	0	1	1	1	0	0	0
0	0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



0	1			

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0	0
0	1	0	0	0	1	0	0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	1	0	0	0	1	0	0
0	0	1	1	1	0	0	0
0	0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0		

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



0	1	0	0	0
0				

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0



Input Image

0	0	1
1	0	0
0	1	1

Feature Detector



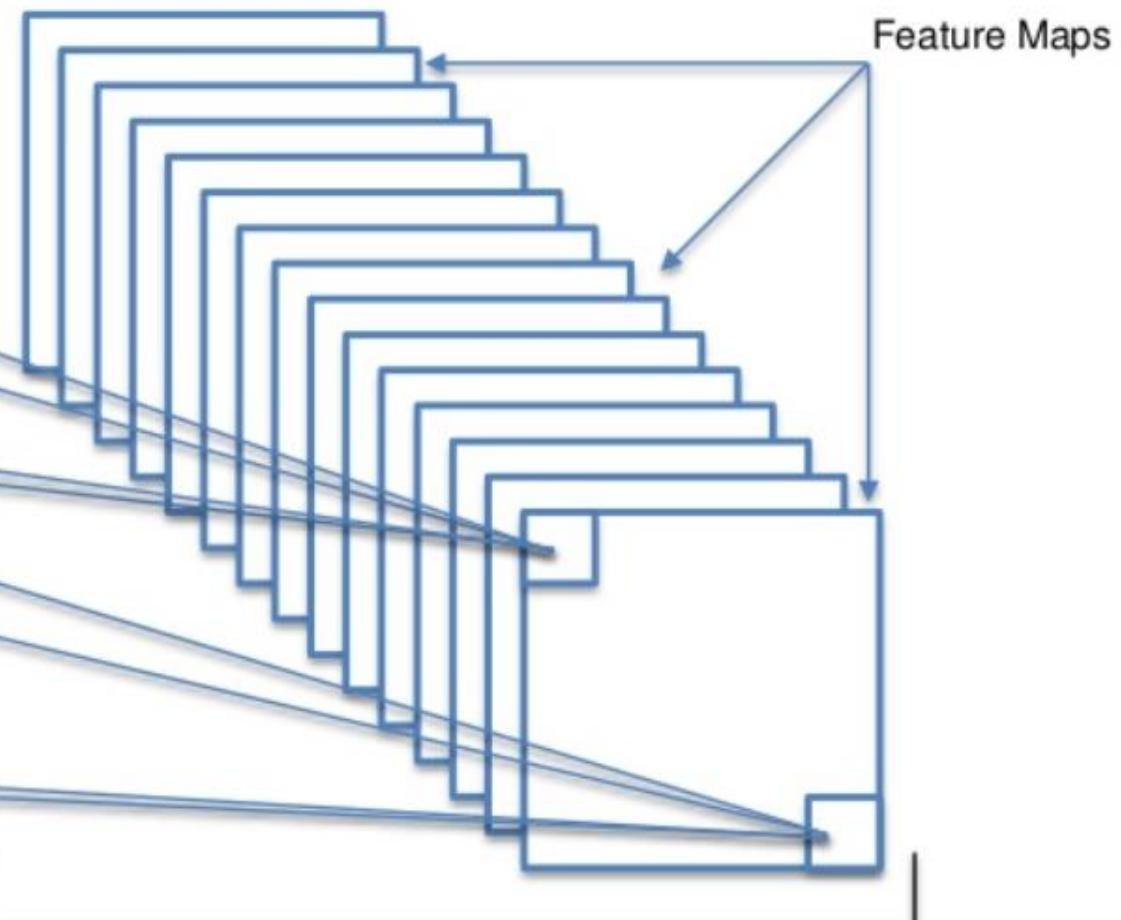
0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

# Step 1 - Convolution

0	0	0	0	0	0	0	0
0	1	0	0	0	1	0	0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	1	0	0	0	1	0	0
0	0	1	1	1	0	0	0
0	0	0	0	0	0	0	0

We create many feature maps to obtain our first convolution layer



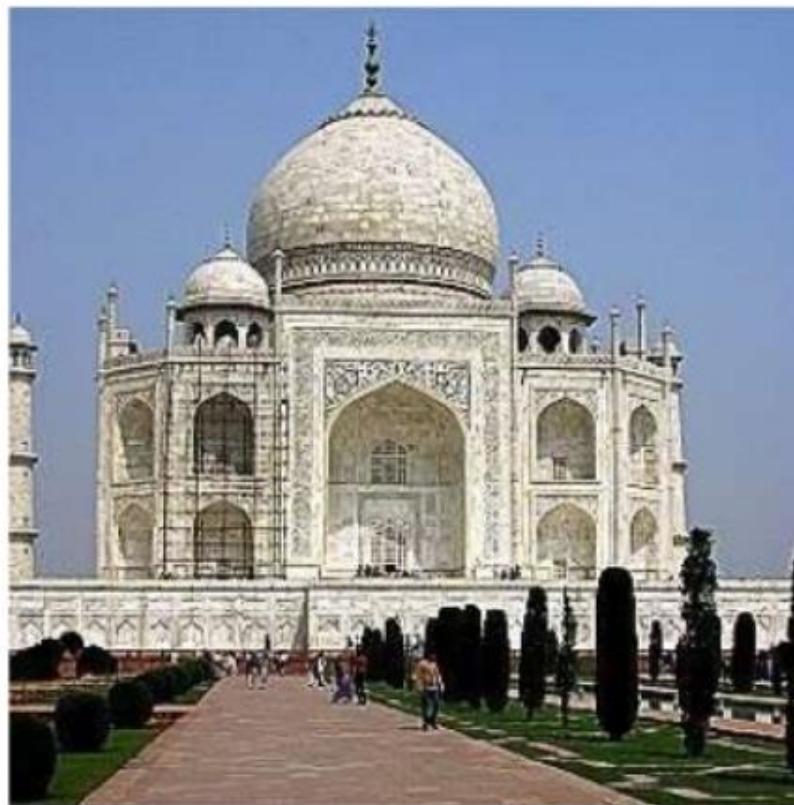
Input Image

Convolutional Layer

# Step 1 - Convolution

Sharpen:

0	0	0	0	0
0	0	-1	0	0
0	-1	5	-1	0
0	0	-1	0	0
0	0	0	0	0



*Image Source: docs.gimp.org/en/plug-in-convmatrix.html*

# Step 1 - Convolution

Blur:

0	0	0	0	0
0	1	1	1	0
0	1	1	1	0
0	1	1	1	0
0	0	0	0	0



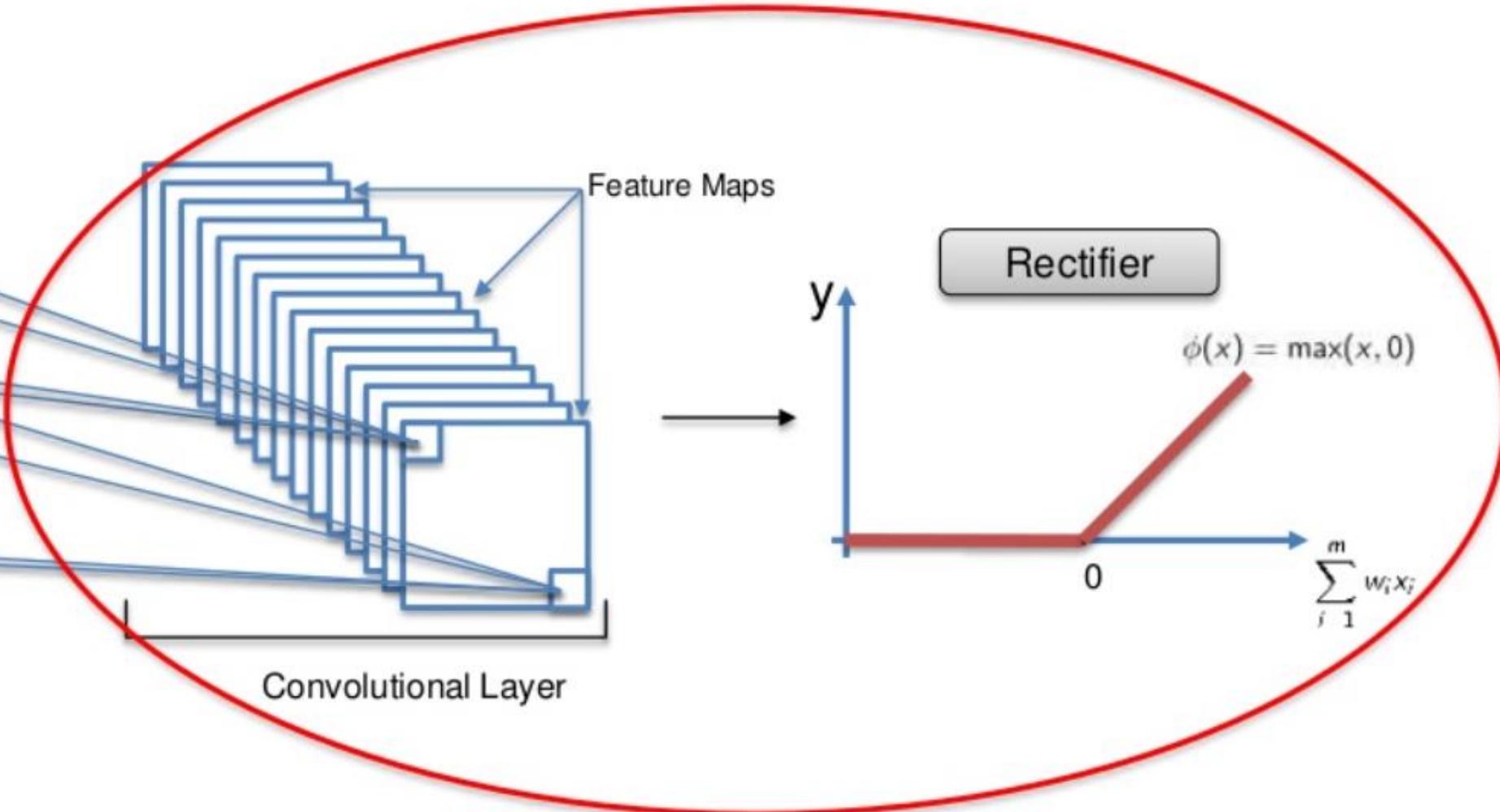
*Image Source: docs.gimp.org/en/plug-in-convmatrix.html*

# **Step 1(B) – ReLU Layer**

# Step 1(B) – ReLU Layer

0	0	0	0	0	0	0	0
0	1	0	0	0	1	0	
0	0	0	0	0	0	0	
0	0	0	1	0	0	0	
0	1	0	0	0	1	0	
0	0	1	1	1	0	0	
0	0	0	0	0	0	0	

Input Image



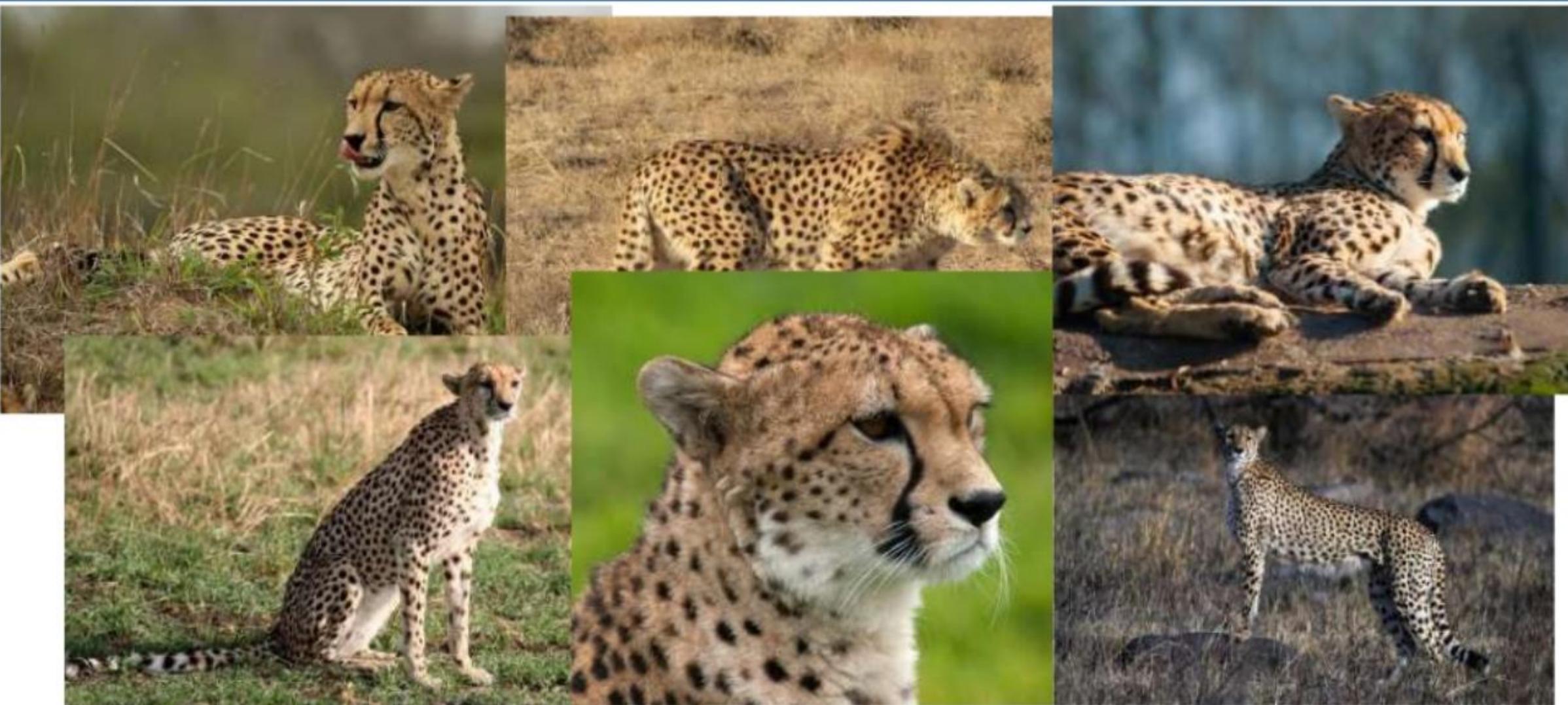
## **Step 2 – Max Pooling**

## Step 2 - Max Pooling



*Image Source: Wikipedia*

## Step 2 - Max Pooling



*Image Source: Wikipedia*

## Step 2 - Max Pooling

0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

## Step 2 - Max Pooling

0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

Max Pooling




Pooled Feature Map

## Step 2 - Max Pooling

0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

Max Pooling



1		

Pooled Feature Map

## Step 2 - Max Pooling

0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

Max Pooling



1	1	

Pooled Feature Map

# Step 2 - Max Pooling

Full screen

0	1	0	0	0	
0	1	1	1	0	
1	0	1	2	1	
1	4	2	1	0	
0	0	1	2	1	

Feature Map

Max Pooling

1	1	0

Pooled Feature Map

## Step 2 - Max Pooling

0	1	0	0	0
0	1	1	1	0
1	0	1	2	1
1	4	2	1	0
0	0	1	2	1

Feature Map

Max Pooling

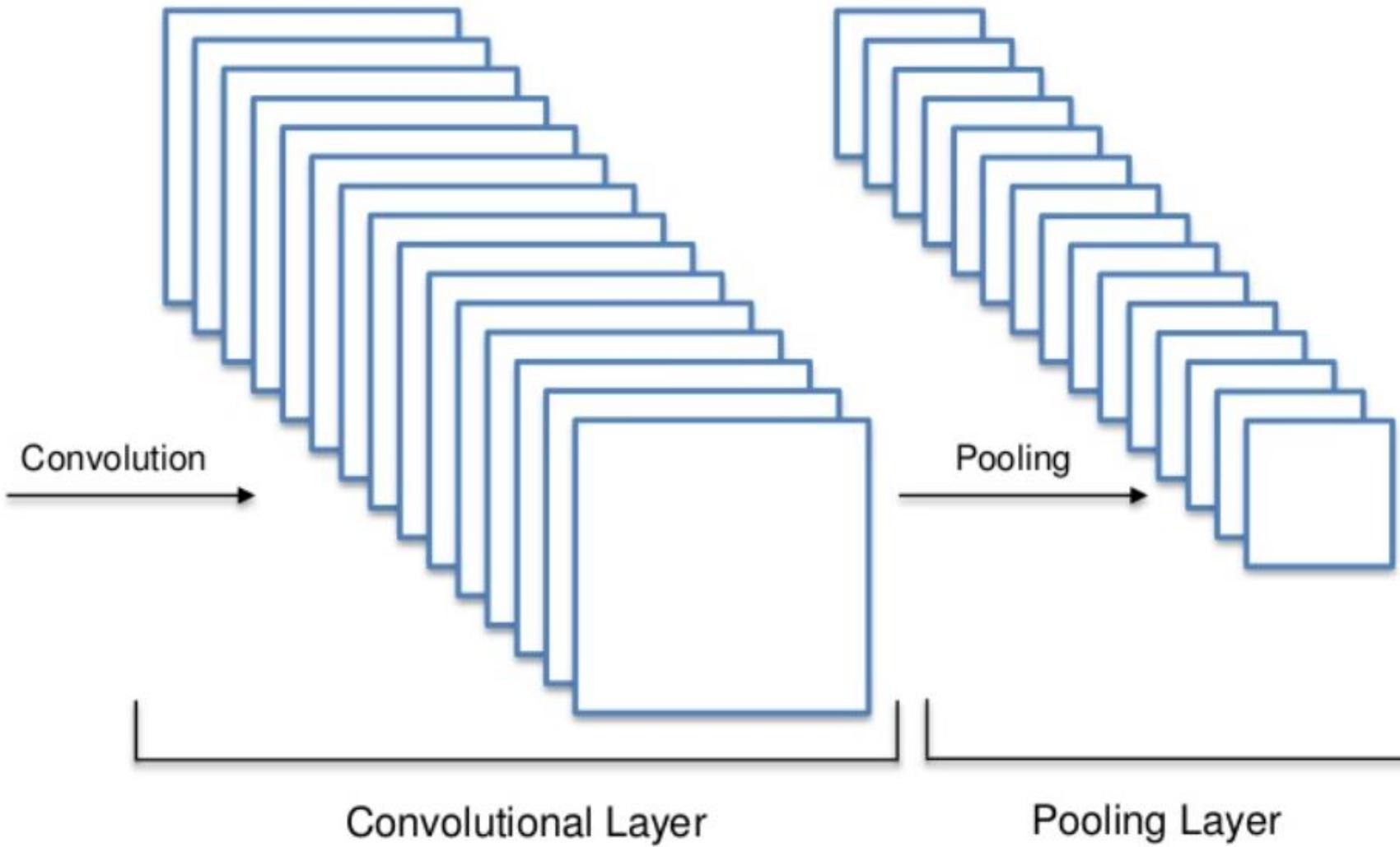
1	1	0
4	2	1
0	2	1

Pooled Feature Map

## Step 2 - Max Pooling

0	0	0	0	0	0	0
0	1	0	0	0	1	0
0	0	0	0	0	0	0
0	0	0	1	0	0	0
0	1	0	0	0	1	0
0	0	1	1	1	0	0
0	0	0	0	0	0	0

Input Image



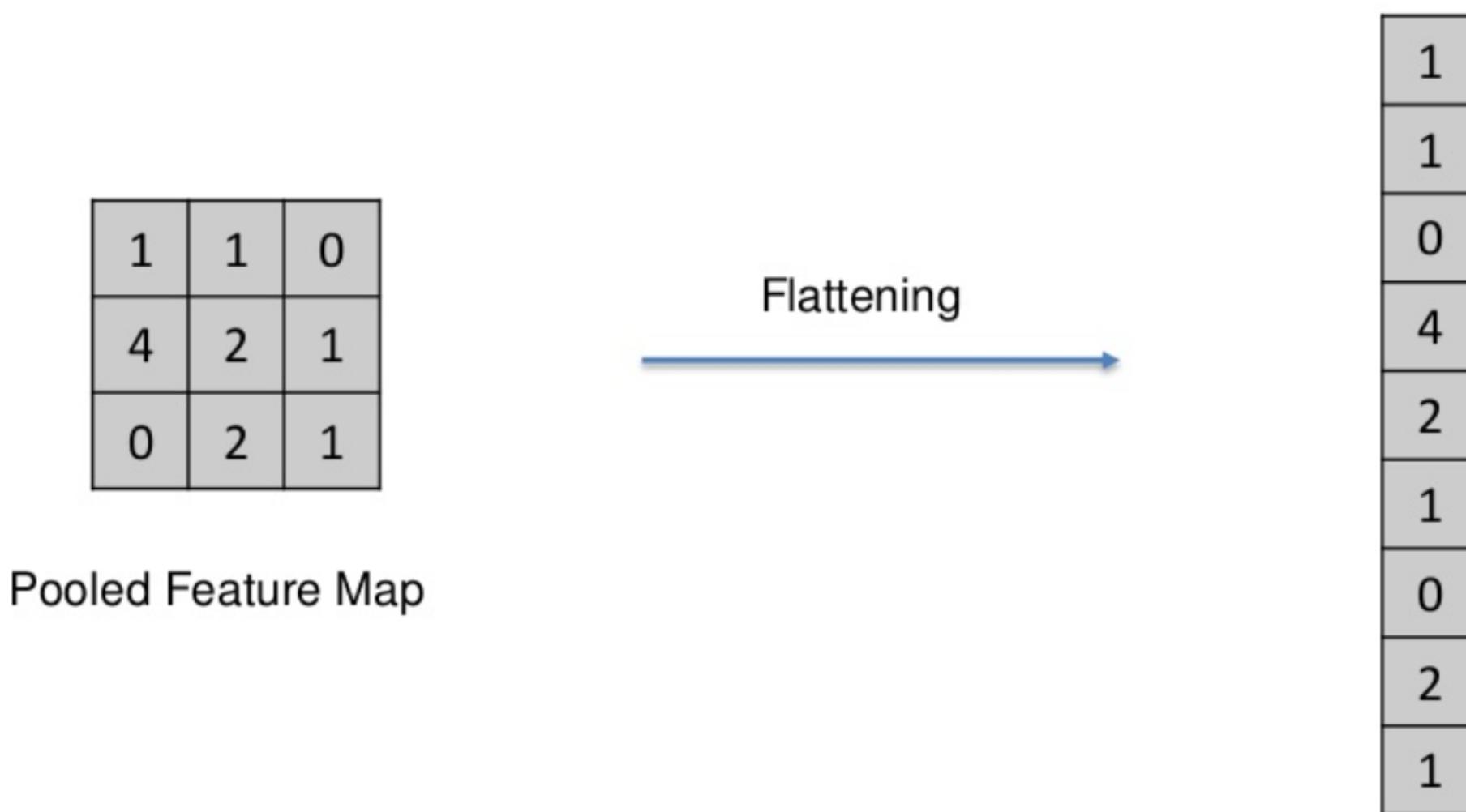
# **Step 3 – Flattening**

# Step 3 - Flattening

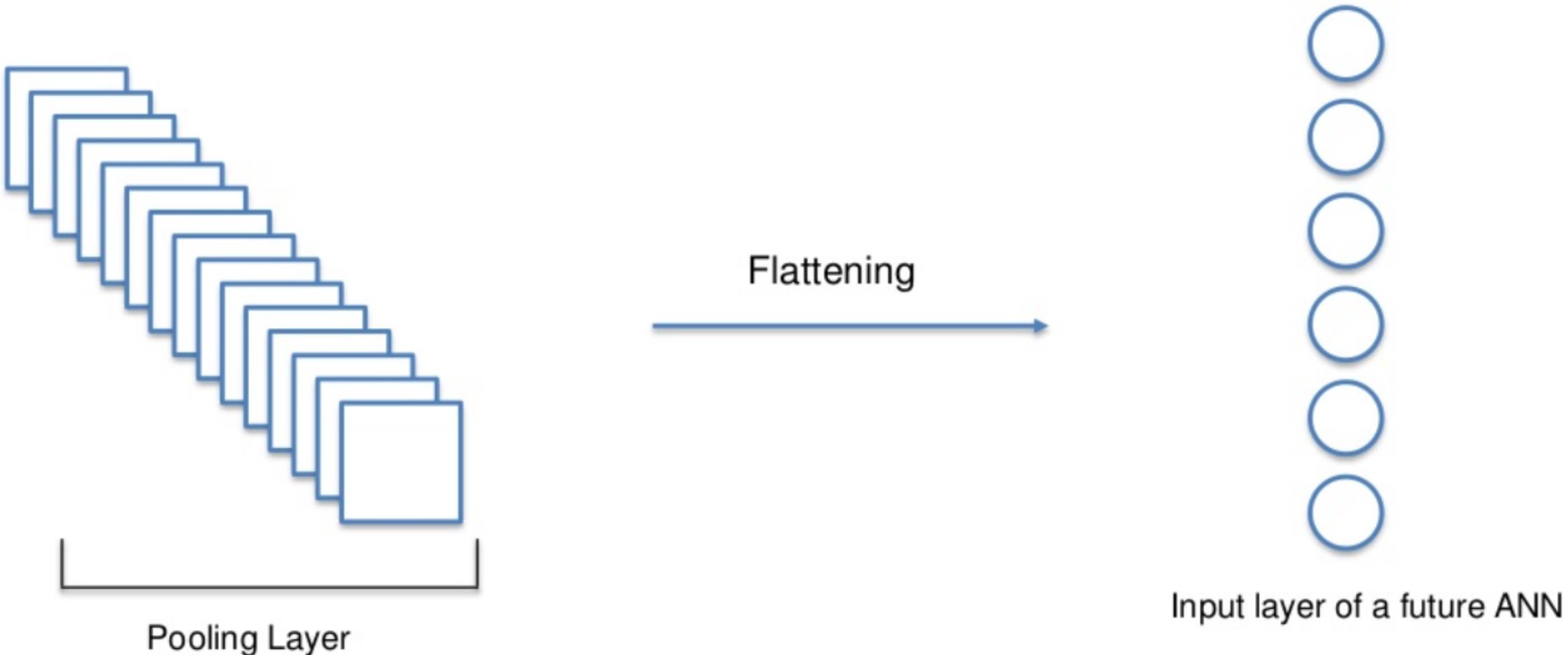
1	1	0
4	2	1
0	2	1

Pooled Feature Map

# Step 3 - Flattening



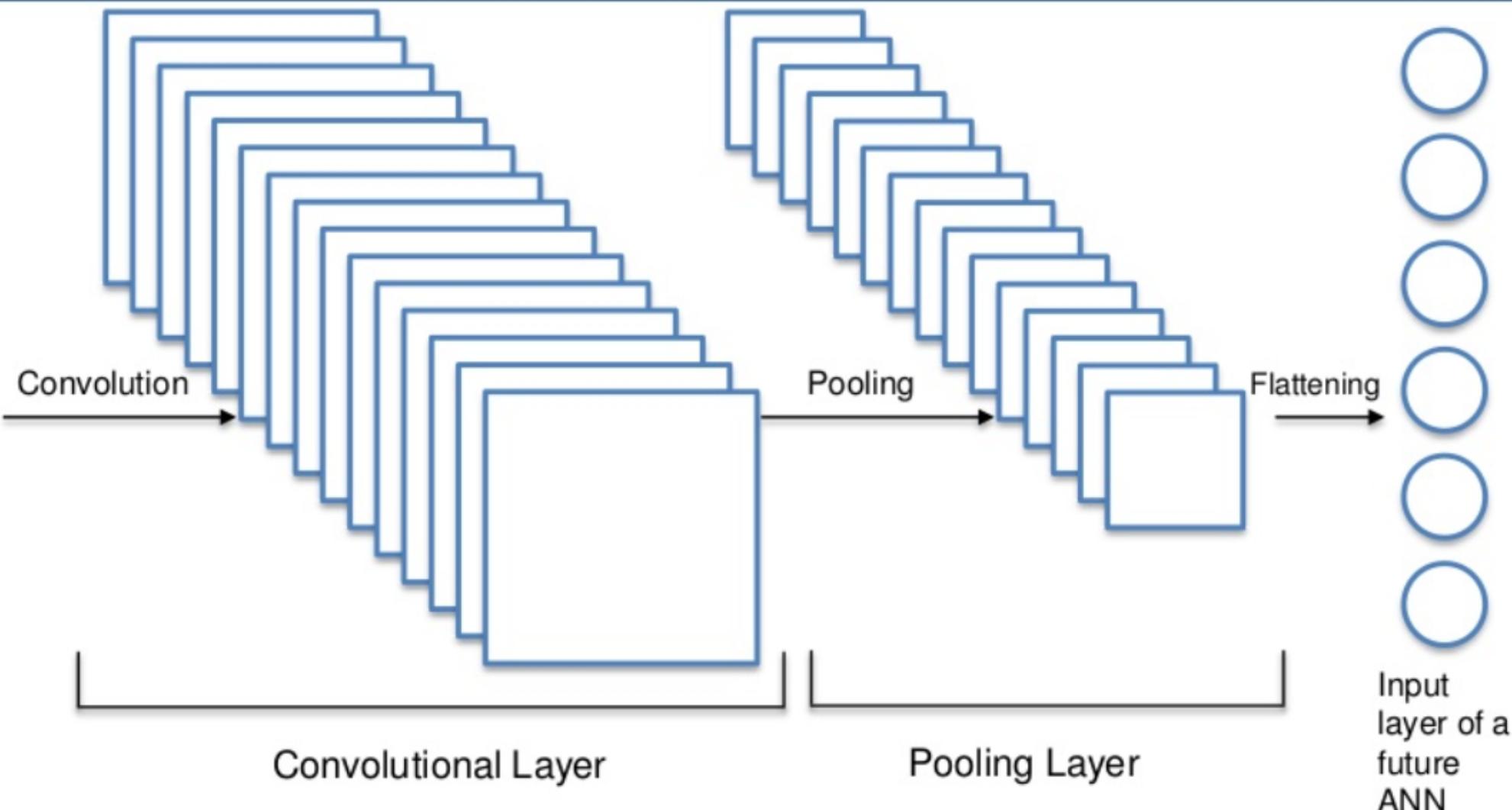
# Step 3 - Flattening



# Step 3 - Flattening

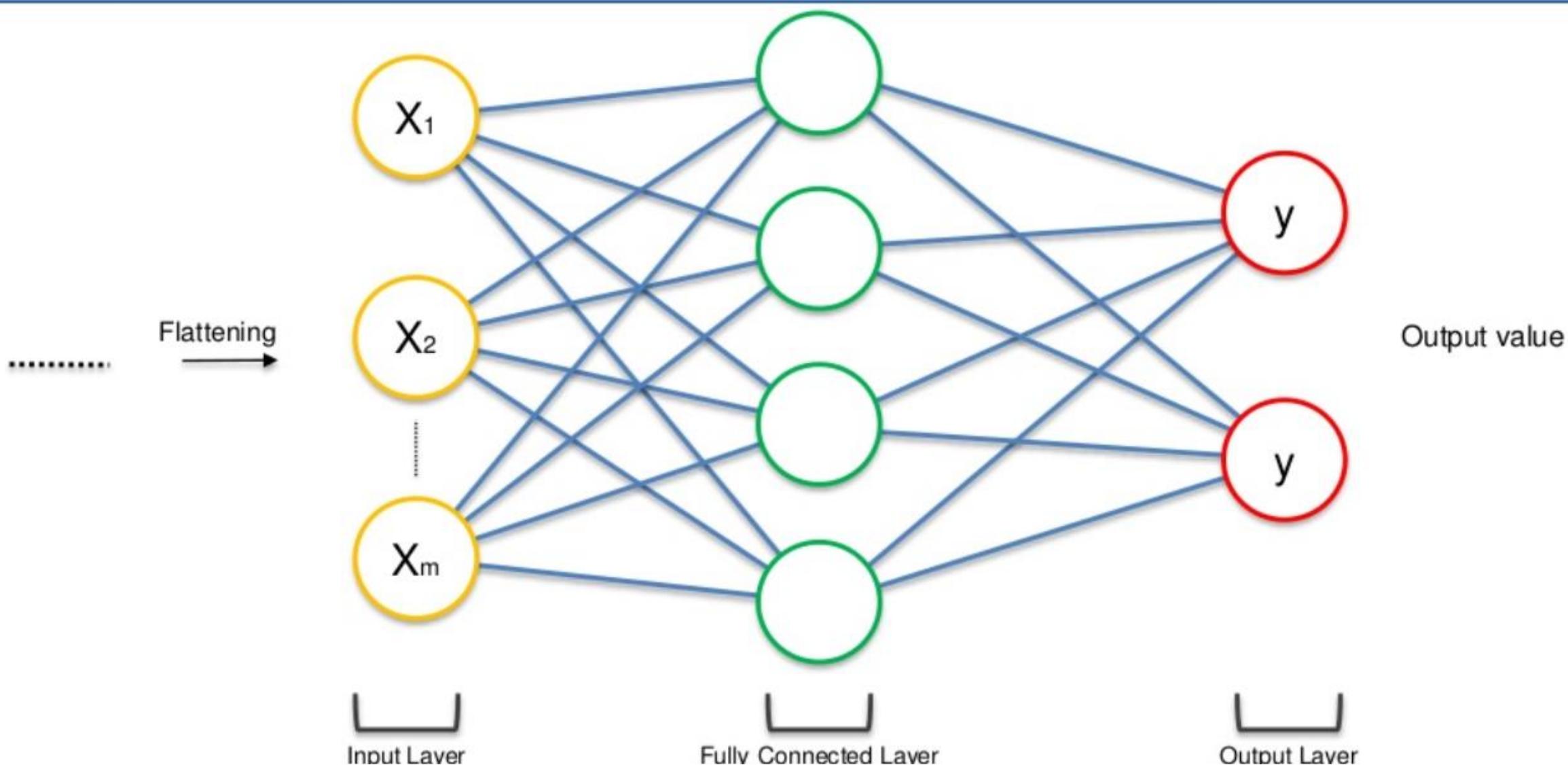
0	0	0	0	0	0	0	0
0	1	0	0	0	1	0	0
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	1	0	0	0	1	0	0
0	0	1	1	1	0	0	0
0	0	0	0	0	0	0	0

Input Image

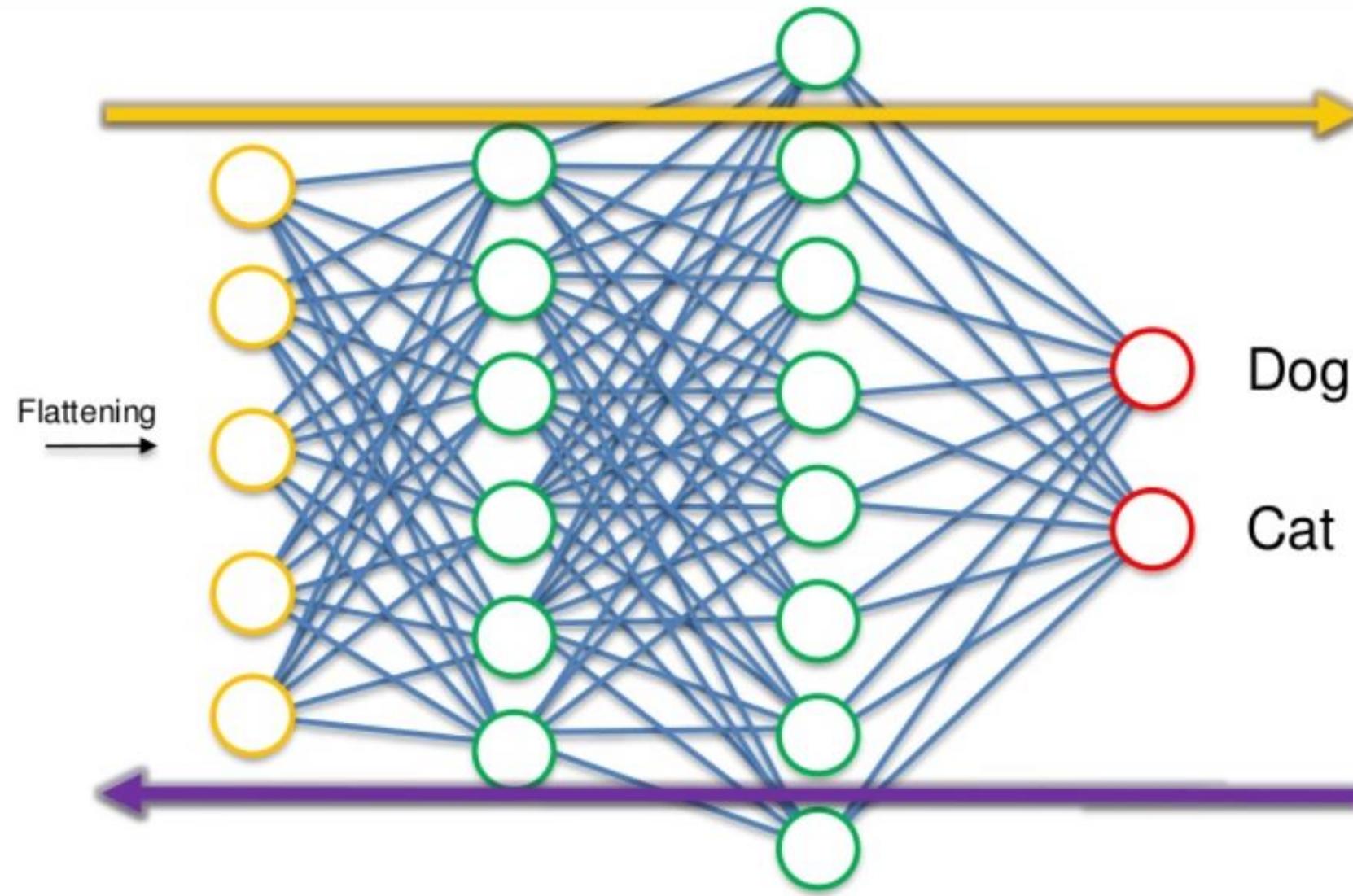


# **Step 4 – Full Connection**

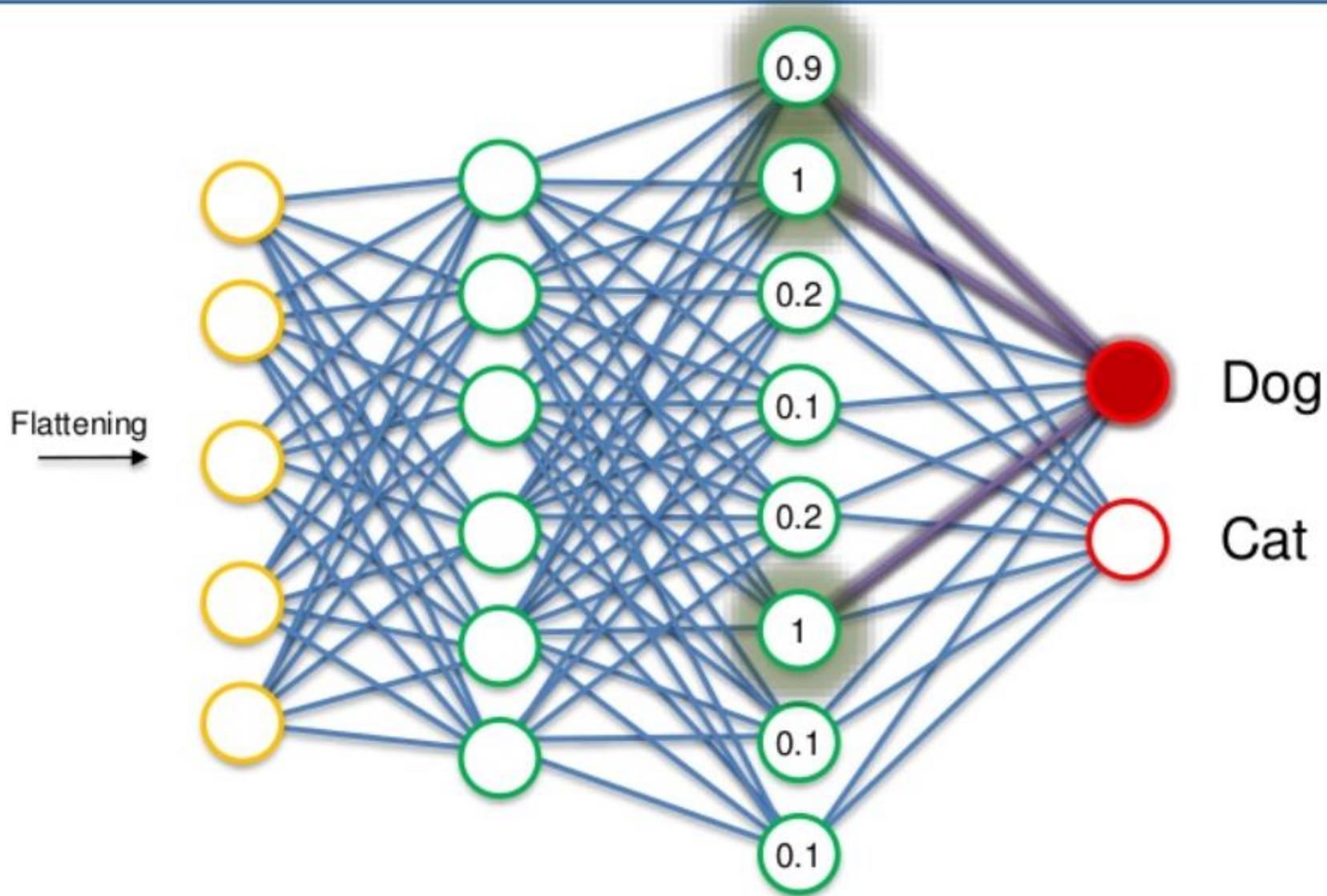
# Step 4 - Full Connection



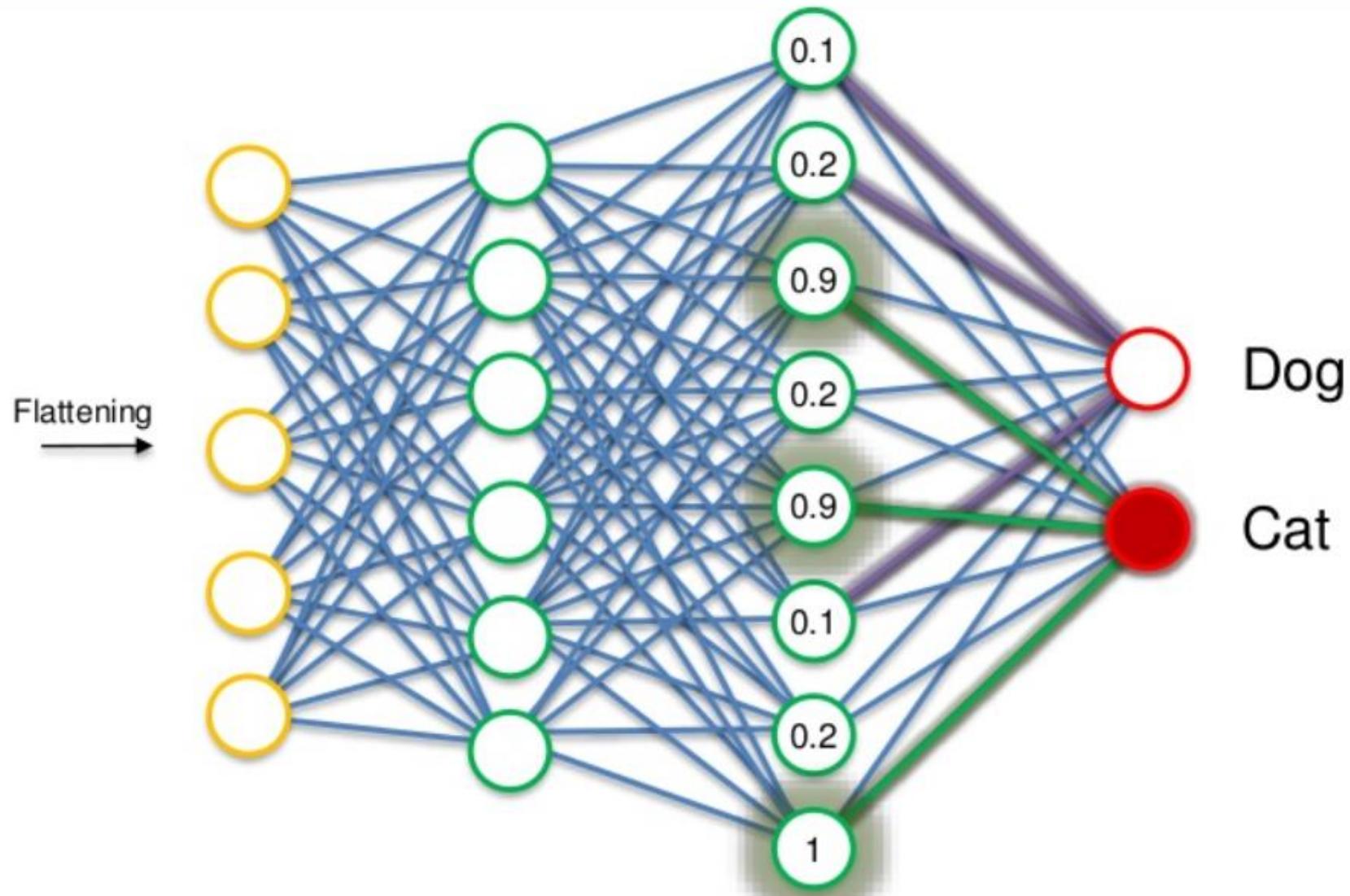
## Step 4 - Full Connection



# Step 4 - Full Connection



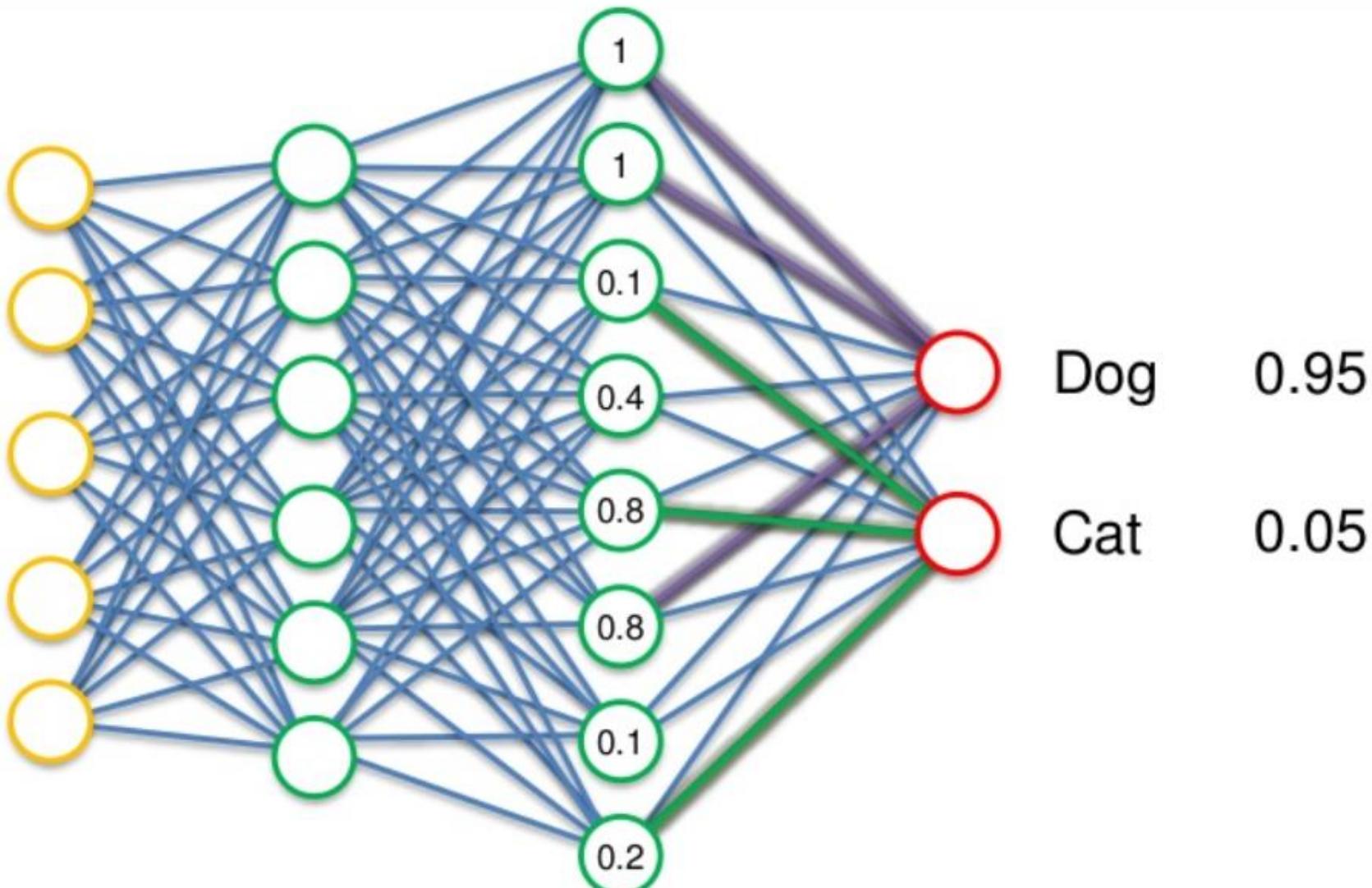
# Step 4 - Full Connection



# Step 4 - Full Connection



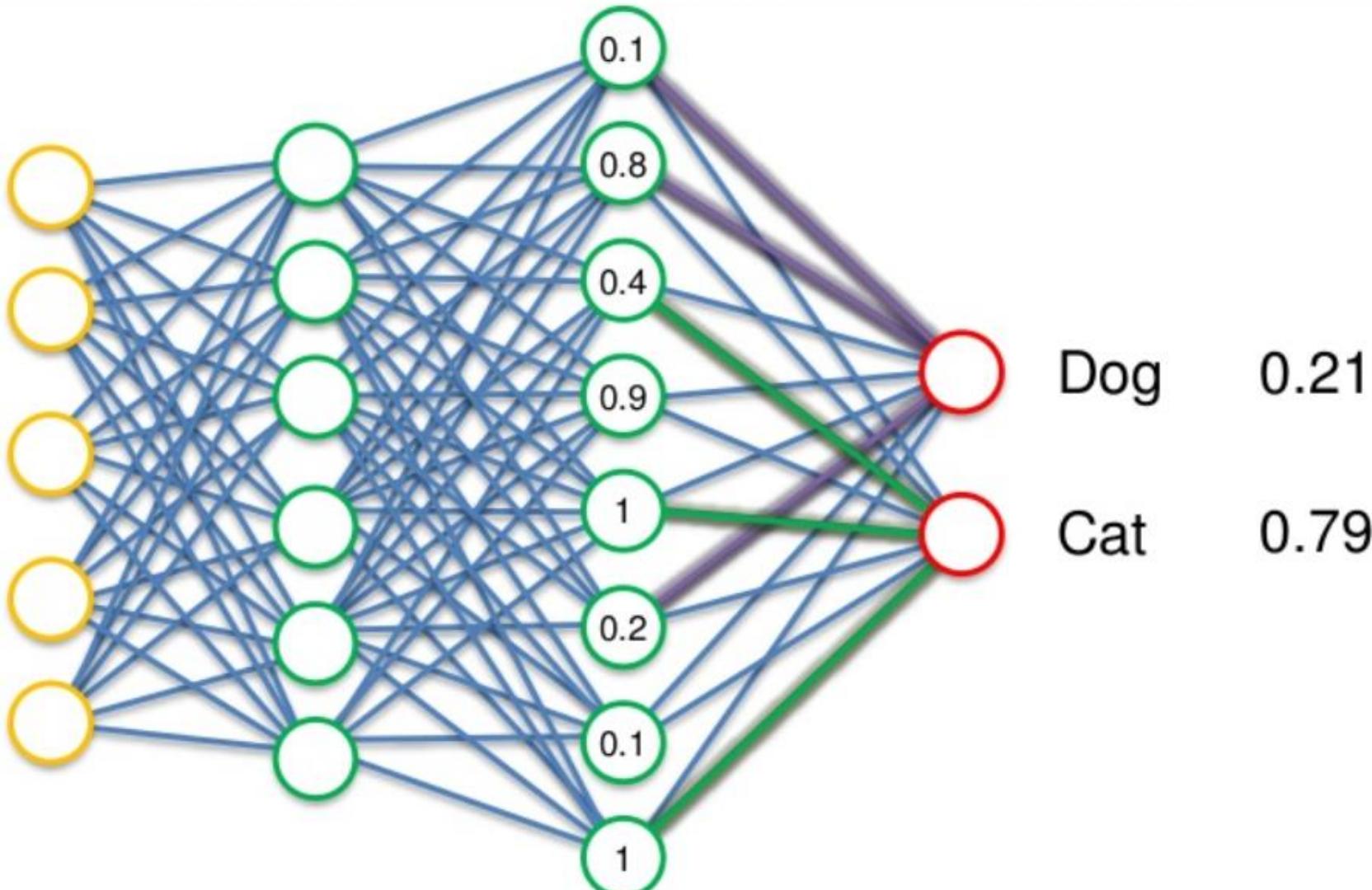
Flattening  
→



# Step 4 - Full Connection



Flattening  
→



# Softmax & Cross-Entropy



Flattening  
→

