

Hypothesis Testing

Null hypothesis \Rightarrow Treat everything same or equal.

Null Hypothesis \rightarrow It is default or well accepted already.

A hypothesis which has already been ~~done~~ ~~by~~ done by someone or Not done by someone, just assume between independent of one variable to depends of other variable has no relation.

It means, ~~just~~ we just assume no relationship between them, so someone just prof it and confidence level more than that so we accept the hypothesis, or ~~we~~ we are just ~~reject~~ reject it ~~basically~~ ~~basically~~ basis of Not proven at certain level.

e.g. The Null hypothesis states, there is no relationship between two population parameters.

e.g. Researchers reject or disprove the Null hypothesis to set the stage for further experimentation.

Null hypothesis is coin is fair coin

Null Hypothesis represented by H_0

e.g. $H_0 \rightarrow I_1$ & I_2 (variable)

both are same ($\mu_1 = \mu_2$)

(II) ALTERNATE Hypothesis \rightarrow (mean of other variable) (mean of other variable)

It is inverse of Null hypothesis and saying it is not true both of two ~~of~~ ~~two~~ variable. ~~Alternate hypothesis~~ is Rejected the Null hypothesis.

$H_a \rightarrow I_1 \& I_2$ (not same)

$\mu_1 \neq \mu_2$

Example \Rightarrow Null hypothesis (H_0) - The world is flat

Alternate hypothesis (H_a) - The world is round

Question	Null Hypothesis
Does taking aspirin every day reduce the chance of having a heart attack?	Taking aspirin daily does not affect heart attack risk.

P-Value = Probability value

P-Value \rightarrow or Two Tailed Test

Short name of P-value is Probability Value.

Definition \rightarrow It is defined as a probability of getting result that is either the same or more extreme than the actual observation.

The P-value is also known as level of marginal significance within the hypothesis-testing that represents the probability of occurrence of given event.

The P-value is used as a alternative to the rejection point to provide the least significance at which the Null Hypothesis is rejected,

If The P-value is small, then there is stronger evidence in favor of the Alternative hypothesis.

P-value \rightarrow It is the probability for the "Null hypothesis" to be true.

P-Value Table

P-value	Decision
P-value > 0.05	The result is not statistically significant and hence don't reject the null hypothesis.
P-value < 0.05	This result is significant. Reject the null hypothesis in favor of the Alternative hypothesis.
P-value < 0.01	The result is highly statistically significant, and thus rejects the null hypothesis in favor of the alternative hypothesis.

- P-value and the range between 0 and 1

- level of significance is denoted by α

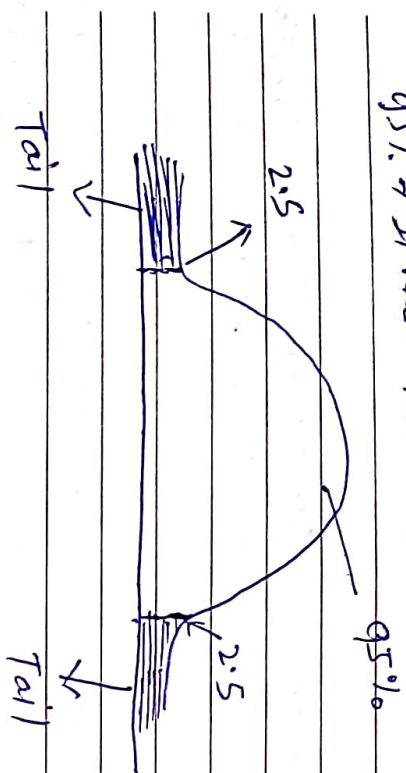
P-value formula \rightarrow

$$Z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$

\hat{p} = Sample proportion
 p_0 = Assumed population proportion in the null hypothesis
 n = Sample Size

2 Tailed Test

95% \rightarrow If mean null hypothesis come under this.



Example \rightarrow A statistician wants to test

the hypothesis $H_0: \mu = 120$ using

using the Alternative hypothesis ~~that~~

$H_a: \mu > 120$ and assuming

that $\alpha = 0.05$ for that, he took

The sample values as

$n = 40$, $\sigma = 32.17$ and $\bar{x} = 105.37$

determine the conclusion for this hypothesis?

Solution \rightarrow

$$\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}} = \frac{32.17}{\sqrt{40}}$$

$$\sigma_{\bar{x}} = 5.0865$$

Now, using the Test static formula, we get

$$t = \frac{(105.37 - 120)}{5.0865}$$

$$t = -2.8762$$

Using the ~~table~~ Z-Score table

We can find the value of $P(t > -2.8762)$

from the table, we get

$$P(t < -2.8762) = P(t > 2.8762)$$

$$= 0.003$$

Therefore,

$$\text{if } P(t > -2.8762) = 1 - 0.003$$

$$P\text{-value} = 0.997$$

$$P\text{-value} = 0.997 > 0.05$$

So, Null hypothesis is accepted

or

fail to Reject H_0 (Null hypothesis)

Type I error \rightarrow

Rejecting Null hypothesis when it is true

Type II error \rightarrow

Not Rejecting the Null hypothesis
when it is false

$P(\text{Type I error} / H_0 \text{ is true}) = \alpha$

$P(\text{Type II error} / H_0 \text{ is false}) = \beta$

$P(\text{Rejecting a false } H_0) = 1 - \beta$

	H_0	
	True	False
Reject H_0	Type I error	✓
Fail to Reject H_0	✓	Type II error

Z-Score or Z-Test \rightarrow

Z-Score says How many standard deviation you are away from the mean, if Z-score is equal to 0, then it is on mean

$$Z = \frac{x - \mu}{\sigma}$$

where Z = standard score

x = observed value

μ = mean of the sample

σ = standard deviation of the sample

if Z-score is higher than mean average

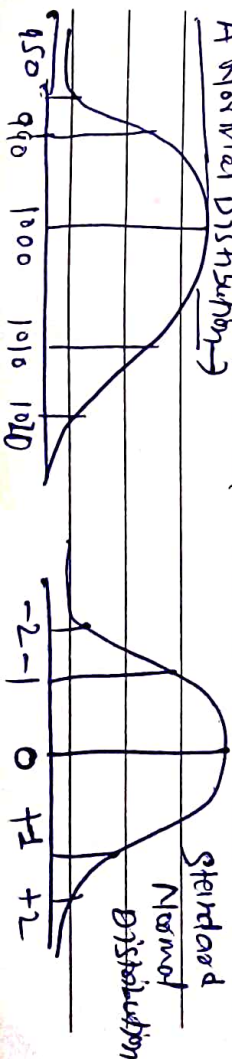
e.g. - if Z-score is equal to +1, it is 1 standard deviation above the mean

Z-score is negative the mean average is below

e.g. - Z-score is equal to -2 standard deviation below the mean

Z-scores is by creating standard

A normal distribution \rightarrow Normal distribution



Z-Score \rightarrow A Z-score measures exactly how many standard deviation above or below the mean a data point is.

- A positive Z-score says the data point is above average
- A Negative Z-score says the data point is below average
- A Z-score close to 0 says the data point is close to average
- A data point can be considered unusual if its Z-score is above 3 or below -3