# **Final Examination**

Date: 16/06/2021; Duration: 120 minutes

Online, Open-book

SUBJECT: Algorithms & Data Structures (IT013IU)								
Approval by The SCSE	Lecturer:							
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Full name:	Full name:							
STUDENT INFO								
Student name:								
Student ID:								

# INSTRUCTIONS: the total point is 100 (equivalent to 40% of the course)

#### 1. Purpose:

- Test your knowledge on data structures and algorithms in the following topics: Binary Tree,
  Hash Table, Graphs, Advanced graph algorithms
- Examine your skill in analysis and design algorithms

#### 2. Requirement:

- Read carefully each question and answer it following the requirements
- Write the answers and draw models CLEAN and TIDY directly in a WORD file
- You can draw your trees, graphs by hand or by any tool (like draw.io)
- Include the SETTING session below in your answer file.

Note: For all calculations in this subject, the following rounding convention is used: 7/2 = 4

#### 0. Setting - TO INSERT TO YOUR ANSWER FILE

a. Write the last 2 digits of your student ID (called is x):\_\_\_\_\_ (TO FILL IN)

**b.** Compute your **OFFSET** = x % 5 = \_\_\_\_\_ (TO FILL IN)

c. Using the table below to compute your Starting node: \_\_\_\_\_ (TO FILL IN)

OFFSET	0	1	2	3	4
STARTING	A	В	С	D	E
NODE					

#### Your list iteration procedure:

For all lists of items in the following sessions, take items from left to right starting from your **OFFSET.** If the end of the list is reached before all items are taken, continue from index 0 (wrap around).

#### 1. Binary search tree (25pts)

Given a list of items, take items one by one using your list iteration procedure.

Table 1 - Items

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
45	30	80	20	35	70	90	25	21	39	37	38	75	78	76	90

- 1.a. Insert all items into a binary search tree and draw the tree (15pts)
- 1.b. Delete the root node and redraw the tree (10pts)

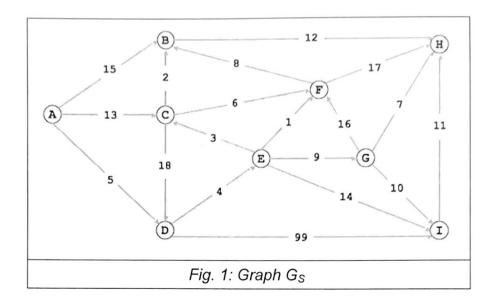
## 2. Hash table (20pts)

Given a list of items in table 1, take items using your list iteration procedure.

- 2.a. Insert all items into the hash table of size 27 by using the linear probing algorithm to solve collisions (10pts).
- 2.b. Change the hash table's size to 31, redraw it (10pts)

## 3. Graph - Elementary Algorithms (30pts)

- 3.a Given the graph  $G_S$  in Fig. 1, run the DFS algorithm from your **STARTING NODE** and redraw the graph with the discovery time and the finishing time for each node. (15pts)
- 3.b. Find all strongly connected components in  $G_s$  and draw the  $G_s^{-1}$  with the finishing time for each node(15pts)



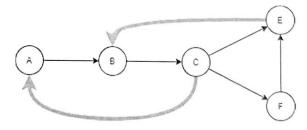
### 4. Graph – Shortest path algorithm (15pts)

Run the Dijkstra's algorithm on the graph G<sub>s</sub> in Fig.1 <u>from your starting node</u>, and fill the following table with corresponding values after each step of the algorithm

### 5. Algorithm to find backward edges (10pts)

While traversing a graph using the DFS algorithm, backward edges are edges that link a node to another node in the path from the source node to the node.

For example, in the graph below, colored edges are backward edges.



 (10pts) Propose an algorithm (write a pseudo-code) based on the DFS algorithm to print out all the backward edges of a given graph starting from a source node.

DFS(G, u)

--- The end ---