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Command line programs from LatticeRepLib

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1. Introduction

In the study of various spaces for representing lattices, a number of software tools have been prepared. Some of those are available as simple commandline programs. Most of them have flexible input and output their processed results in a form that another can use that for processing. A few are terminal programs that produce analysis. A small number take no input and generate files for other uses.

2. Data Inputs:

Table 1. *All these are case-insensitive. If a particular input lattice is invalid, it is rejected with a message.*

<u>Vector Input:</u>	g (or v or g6) for G⁶ vectors d (or d7) for D⁷ vectors s (or s6) for S⁶ , Delone/Selling scalars C3 for C³ input (without parentheses or commas, “C” would be interpreted as a C-centered unit cell)
<u>RANDOM:</u>	Random (valid) unit cell generated
<u>Crystal Lattice Input:</u>	“A” , “B” , “C” , “P” , “R” , “F” , “I” followed by three axis lengths and three angles (in degrees)
<u>semicolon:</u>	lines beginning with a semicolon are treated as comments
<u>END:</u>	ends the data input section

2.1. Examples of unit cell inputs

```
P 10 20 30 90 111 90
G 100 400 900 0 -215.02 0
S6 0 -107.51 0 7.51 -400 -792.49
; this is a comment
```

3. Programs

Table 2. *Programs for convert lattice representations*

Name	in	out	param	Output
CmdToB4	y	\mathbf{B}^4		For each input, it produces the 4 vectors as a,b,c,d as E3 vectors, and also the lengths of each of those vectors.
CmdToC3	y	\mathbf{C}^3		For each input, produces the \mathbf{C}^3 representation in the form (#,#) (#,#) (#,#), which does not conform to the format for input to other programs.
CmdToCell	y	a,b,c, α,β,γ		Converts to the conventional unit cell representation.
CmdToD13	y	\mathbf{D}^{13}		Outputs the lengths of the 13 unique vectors describing the Dirichlet cell.
CmdToDC	y	y		
CmdToG6	y	\mathbf{G}^6		Converts the input to \mathbf{G}^6
CmdToS6	y	\mathbf{S}^6		Converts the input to \mathbf{S}^6

Table 3. *Summary of programs manipulating data*

Name	in	out	param	Output
CmdCmplx	NA	y		Currently, this just outputs some programmed examples.
CmdDelone	y	\mathbf{S}^6		Converts input to \mathbf{S}^6
CmdGen	NA	\mathbf{G}^6	ngen type -	- number of examples to generate (optional) lattice type to generate, many options (optional) c,t,h,o,r,h,m,a, cP, cF,cI, tP, tI, hP, hR, oP, oF, oI, oS, mP, mC, mS, aP, numeric Niggli types - 1-44, Delone types - C1,C3,C5, ... If no parameters are present, one each of the 44 Niggli types. If only a number is present, that is how many of each of the 44 Niggli types to generate. For usage examples, see Table 4
CmdLM	y	cy		Lattice Matching. The first input cell is used as the reference. Succeeding cells are matched as well as possible to the reference cell.
CmdNiggli	y	\mathbf{G}^6		Produces the Niggli reduced cell for each input
CmdPath	?	?		Clearly not working the way it should
CmdPerturb	y	y	n-number of perturbations, parts per thousand to perturb	n cells perturbed normal to the input \mathbf{S}^6 vector If a lattice centering (including P) is input, the output is in the same centering. Otherwise, the output is in \mathbf{S}^6 .
CmdS6Refl	y	\mathbf{S}^6		For each input, all 24 \mathbf{S}^6 reflections are produced.
CmdSella	y	y		
CmdSort	y	y	"C3" or "seq"	
CmdVolume	y	mod		Outputs the unit cell and the volume of each input cell.
MultiMetricDists	y	mod	"Y/y" (optional)	Parameter Y/y for maxima style output
PlotC3	y	mod	1,2,or 3 for which \mathbf{C}^3 coordinate to plot. "seq" or "C3"	Plot one of the 3 \mathbf{C}^3 coordinates, sorted by minimizing point to point distance for \mathbf{S}^6 reflections or sorting the \mathbf{C}^3 components to put them in the asymmetric unit.
Radial	y	as radial		Radial computes the polar distances in Angstroms from the first input cell. That is a, α , b, β , and c, γ as coordinates in complex space.
SELLA	y	mod		Outputs the distances from each of the Bravais lattice types (in s_6).
SVD	y	mod		Outputs the singular value decomposition vectors and eigenvalues for the input lattice. This is done in \mathbf{S}^6 .

- CmdGen

CmdGen is a program for creating examples of various types of lattice types.

There are two optional input parameters. The first is the count of how many samples of each type to generate. The second (if present) is the type of lattices

to generate. There is no input data other than the command line parameters.

For examples of using CmdGen, see table 4

There is considerable flexibility in the input types. However, they are case-sensitive.

- Niggli types by number 1-44 (see Table 6).
- Delone types by Delone's designation - C1,C3,C5, T1, T2, T5, R1, R3, O1A, O2, O3, O4, O5, O1B, M1A, M2A, M3, M4, M1B, M2B, A1, A2, A3, H4 (see Table 5).
- Crystal system - c,h,t,o,m,a
- SVD

On input to a number of lattices, SVD calculates a Singular Value Decomposition. The output consists of the eigenvalues and the six eigenvectors. It is important to check that the form of each cell is the same; for instance, monoclinic cell should have the unique interaxial angle in the same place (*e.g.* β)

As an example, consider using SVD to compute the information for one of the

Command line:

```
CmdGen 5 33 — CmdSort seq — SVD
```

```
; SVD
```

```
S6 from input cell 0.000 -31.196 0.000 -71.963 -109.653 -131.880
```

```
S6 from input cell 0.000 -23.060 0.000 -77.367 -110.398 -125.599
```

```
S6 from input cell 0.000 -28.898 0.000 -54.985 -106.336 -82.229
```

```
S6 from input cell 0.000 -56.133 0.000 -103.736 -177.343 -123.204
```

```
S6 from input cell 0.000 -10.111 0.000 -50.618 -91.57100 -98.102
```

```
eigenvalue 0 vector 1 0 0 0 0 0
```

```
eigenvalue 413.012 vector 0 -0.1728 00 -0.4007 -0.6616 -0.6097
```

```
eigenvalue 48.3869 vector 0 -0.4009 0 -0.1129 -0.5164 0.7482
```

eigenvalue 14.0785 vector 0 -0.7060 0 -0.4581 0.5344 -0.0786

eigenvalue 8.53435 vector 0 0.5576 0 -0.7853 0.1001 0.2494

eigenvalue 0 vector 0 0 -1 0 0 0


























The two zero eigenvalues correspond to the invariant interaxial angles (α and γ , in this case).

Table 4. *CmdGen examples*

CmdGen	generates a single example of each of the 44 Niggli types
CmdGen 2	generates two examples of each of the 44 Niggli types
CmdGen 4 aP	generates four examples of each of the two anorthic Niggli types
CmdGen 2 17	generates 2 examples of Niggli 17, which is mC Output: ; Niggli lattice type requested ; lattice type = 17 G6 90.428 90.428 142.222 83.992 83.992 22.888 IT# = 17 mC G6 79.033 79.033 111.127 -61.421 -73.872 -22.772 IT# = 17 mC
CmdGen 2 C5	generate two examples of Delone type "C5", which is primitive cubic. Output: ; Delone lattice type input ; lattice type = C5 G6 181.275 181.275 181.275 0.000 0.000 0.000 IT# = C5 cP G6 74.526 74.526 74.526 0.000 0.000 0.000 IT# = C5 cP
CmdGen 1 h	Generate a single example of each of the hexagonal (and rhombohedral) Bravais lattice (per Niggli). Output: ; Niggli lattice type input ; lattice type = 2 G6 119.828 119.828 119.828 -45.302 -45.302 -45.302 IT# = 2 hR ; ; lattice type = 4 G6 86.837 86.837 86.837 19.813 19.813 19.813 IT# = 4 hR ; ; lattice type = 9 G6 3.688 3.688 145.128 3.688 3.688 3.688 IT# = 9 hR ; ; lattice type = 12 G6 55.273 55.273 136.854 0.000 0.000 -55.273 IT# = 12 hP ; ; lattice type = 22 G6 73.578 73.578 149.339 0.000 0.000 -73.578 IT# = 22 hP ; ; lattice type = 24 G6 101.390 125.771 125.771 -91.974 -67.593 -67.593 IT# = 24 hR ;

Table 5. The table of ? describing the 24 Bravais types in \mathbf{S}^6 . It has been redone removing the images of the Dirichlet cells, the not-reduced cells, and adding the "lattice character", which describes the linear manifold of each type. The crystal family types have been renamed to modern usage: Q changed to T for tetrahedral, K changed to C for cubic, and T changed to A for anorthic. Where Delone in some places included two types in one table cell, they have been split into two (for example: "M1" becomes "M1A" and "M1B").

Note that five types ($O3$, $M3$, $M2B$, $A2$, and $A3$) are not normal crystallographic types. They are boundary types, and they have fewer free parameters than the generic type requires. For instance, $O3$ (character: $rs0\ rs0$) has only two free parameters (r and s), whereas an ordinary orthorhombic type requires three variables.

		1	2	3	4	5
C	C1  cl (rrr rrr)		C3  cF (rr0 rr0)		C5  cP(000 rrr)	
T	T1  tl (rrs rrs)	T2  tl (rr0 rrs)			T5  tP(000 rrs)	
R	R1  hR (rrr sss)		R3  hR (rr0 sr0)			
O	O1A  oF (rrs rrt)	O2  ol (rs0 srt)	O3 *  ol (rs0 rs0)	O4  oS (00r sst)	O5  oP (000 rst)	
O	O1B  ol (rst rst)					
M	M1A  mC (rrs ttu)	M2A  mC (rs0 stu)	M3 *  mC (rs0 ts0)	M4  mP (00r stu)		
M	M1B  mC (rst rsu)	M2B *  mC (rs0 rst)				
A	A1  aP (rst uvw)	A2 *  aP (rs0 tuv)	A3 *  aP (rs0 tu0)			
H				H4  hP (00r rrs)		

* The right angles have no relationship to symmetry.

Table 6. *Roof/Niggli symbol, International Tables (IT) lattice character, Bravais lattice type, unsorted DC⁷ subspace, boundary polytope. Note that the variables r , s and t are non-negative, and u , v and w may be positive, negative or zero as constrained below.*

Roof/ Niggli Symbol	IT Lattice Char	Bravais Lattice Type	Unsorted DC ⁷ Subspace	Bound- ary Polytope
44A	3	cP	$(r, r, r, 2r, 2r, 2r, 3r)$	$12345 = 12\hat{3} = 12\hat{4} = 12\hat{5}$
44C	1	cF	$(r, r, r, r, r, r, 2r)$	12679ACD
44B	5	cI	$(r, r, r, 4r/3, 4r/3, 4r/3, r)$	$12F2'F' = 12\hat{F}$
45A	11	tP	$(r, r, t, r + t, r + t, 2r, 2r + t)$	$1345 = 1\hat{3} = 1\hat{4} = 1\hat{5}$
45B	21	tP	$(r, s, s, 2s, r + s, r + s, r + 2s)$	$2345 = 2\hat{3} = 2\hat{4} = 2\hat{5}$
45D	6	tI	$(r, r, r, r - w/2, r - w/2, 2r + w, r),$ $-r \leq w \leq 0$	$12FF' = 12\hat{F}$
45D	7	tI	$[r, r, r, 2 * r + u, r - u/2, r - u/2, r],$ $-r \leq u \leq 0$	$12F2' = 12\hat{F}$
45C	15	tI	$(r, r, t, t, t, 2r, t)$	158BF
45E	18	tI	$(r, s, s, -r/2 + 2s, s, s, -r/2 + 2s)$	$2ADA' = 2\hat{A}\hat{D}$
48A	12	hP	$(r, r, t, r + t, r + t, r, r + t)$	134E
48B	22	hP	$(r, s, s, s, r + s, r + s, r + s)$	2458
49C	2	hR	$(r, r, r, 2r - u, 2r - u, 2r - u, 3r - u),$ $0 < u \leq r$	$121'2' = \hat{1}\hat{2}$
49D	4	hR	$(r, r, r, 2r + u, 2r + u, 2r + u, 3r + 3u),$ $-r \leq u \leq 0$	$121'2' = \hat{1}\hat{2}$
49B	9	hR	$(r, r, t, t, t, r, r + t)$	1679ACD
49E	24	hR	$(r, s, s, s + r/3, s + r/3, s + r/3, s)$	$2F2'F' = 2\hat{F}$
50C	32	oP	$(r, s, t, s + t, r + t, r + s, r + s + t)$	$345 = \hat{3} = \hat{4} = \hat{5}$
50D	13	oC	$(r, r, t, r + t, r + t, 2r + w, 2r + t + w),$ $-r \leq w \leq 0$	134
50E	23	oC	$(r, s, s, u + 2 * s, s + r, s + r, u + 2 * s + r),$ $-s \leq u \leq 0$	245
50A	36	oC	$(r, s, t, s + t, t, r + s, s + t)$	35B
50B	38	oC	$(r, s, t, s + t, r + t, s, s + t)$	34E
50F	40	oC	$[r, s, t, t, r + t, r + s, r + t)$	458
51A	16	oF	$(r, r, s, r + s + u, r + s + u, -2u, s),$ $-r \leq u \leq 0$	$1F1' = \hat{1}F$
51B	26	oF	$(r, s, t, -r/2 + s + t, t, s, -r/2 + s + t)$	$ADA' = \hat{A}\hat{D}$
52A	8	oI	$(r, r, r, 2r + u, 2r + v, -u - v, r),$ $-r \leq u \leq 0, -r \leq v \leq 0$	12F
52B	19	oI	$(r, s, s, 2s - u, s, s, -r + 2s + u),$ $0 < u \leq r$	
			$(r, s, s, 2s - u, s, s, r + 2s - u),$ $r < u \leq s$	29C = 2AD
52C	42	oI	$r, s, t, t, t, r + s, t$	58BF

4. Availability of code

The C^{++} code for C++ is available in github.com, in <https://github.com/duck10/LatticeRepLib.git>.

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Synopsis

Selling reduction and Delone reduction are considered in a space of complex variables.
