

## H infinity homework2

108061578 高振晏

In this homework, we try to plot the state trajectory of a linear stochastic system with sin and cosine external disturbance. We first write down the state-space representation of the augmented system with  $x$  and the error of  $x$  and  $\hat{x}$ . Then we solve the riccati-like equation which is a BMI, so we separate the BMI matrix into 2 LMI problem and solve them respectively. Also since we want to reach the H2 performance, so we also consider minimizing the effect of the initial state, so then we need to solve the LMI of both H infinity and H2 constraint.

By assuming the initial state to be  $[10, 20]$ , we minimize the for  $\rho$  H infinity and  $\gamma$  for H2. And we get  $\rho=4008.1$   $\gamma=4008.1$ . Then we use Runge-Kutta 4<sup>th</sup> method to plot the state trajectory.

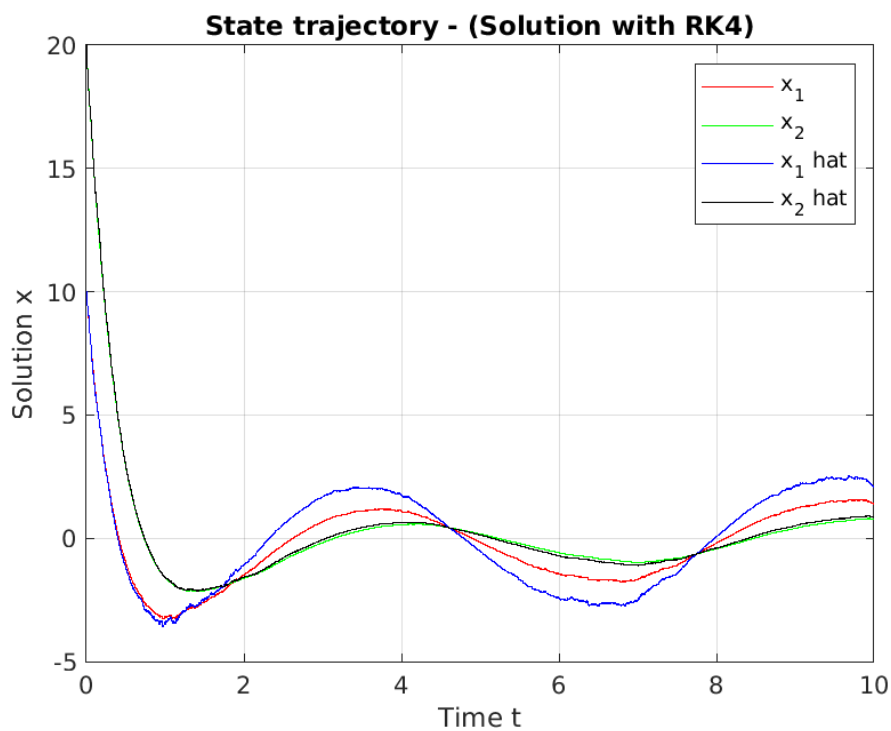


Fig.1 state trajectory with Runge-Kutta.

We can see that due to the smoothing method, the effect of wiener process is not obvious. Also we can see that  $x_1$  isn't tracing very well. The  $\hat{x}_1$  is overshoot too much. However,  $\hat{x}_2$  is tracing  $x_1$  very well.

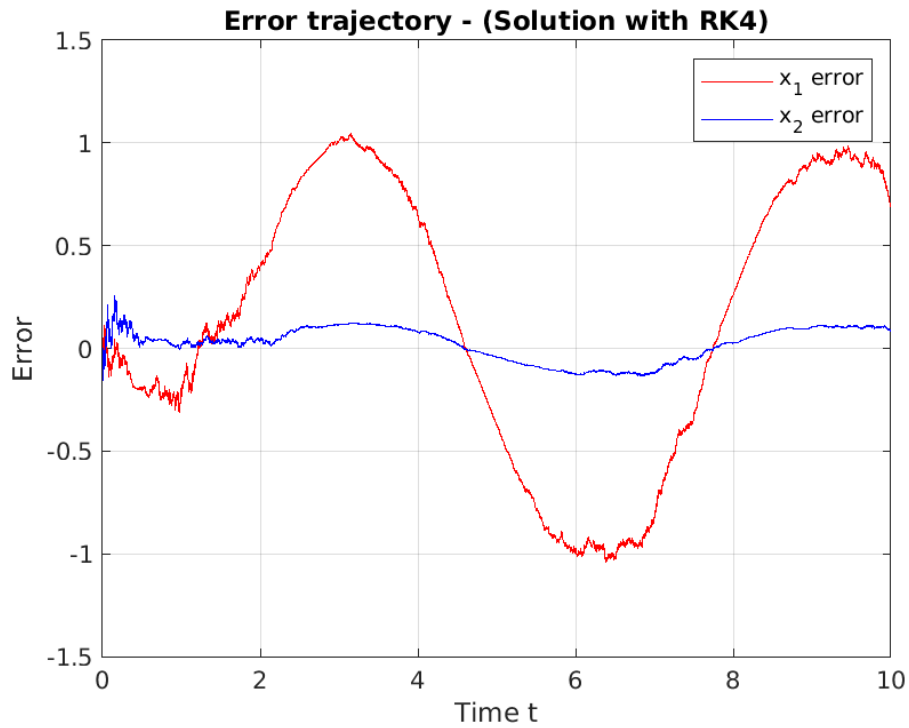


Fig.2 Error trajectory with Runge-Kutta

We can see that the error of  $x_2$  is quite small and only fluctuating around zero. However, error of  $x_1$  is quite large, and seems to follow the sin wave shape. Since we can see  $x_2$  from our output measurement, we can control  $x_2$  better and also the  $\rho$  that we try to minimize is still quite large, so the effect of  $H$  infinity is not that obvious.

**State trajectory - (Solution without RK4 and external disturbance)**

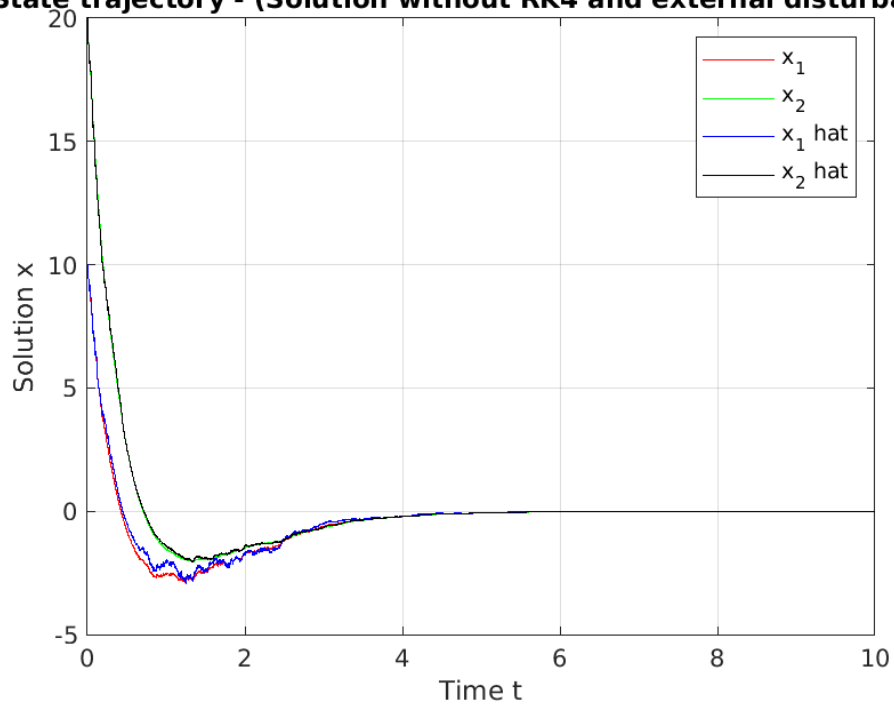


Fig.3 State trajectory without Runge-Kutta and external disturbance.

We can see that since we consider mix H2/H infinity performance, so when we eliminate external disturbance, it can be stable. Also, we can see that without the external disturbance both  $x_1$  and  $x_2$  can be traced very well. However, since we have large  $\gamma$  so out transient affects quite long. If we only try to minimize  $\gamma$  the for H2 performance, we may can have very small  $\gamma$ .

**Error trajectory - (Solution without RK4 and external disturbance)**

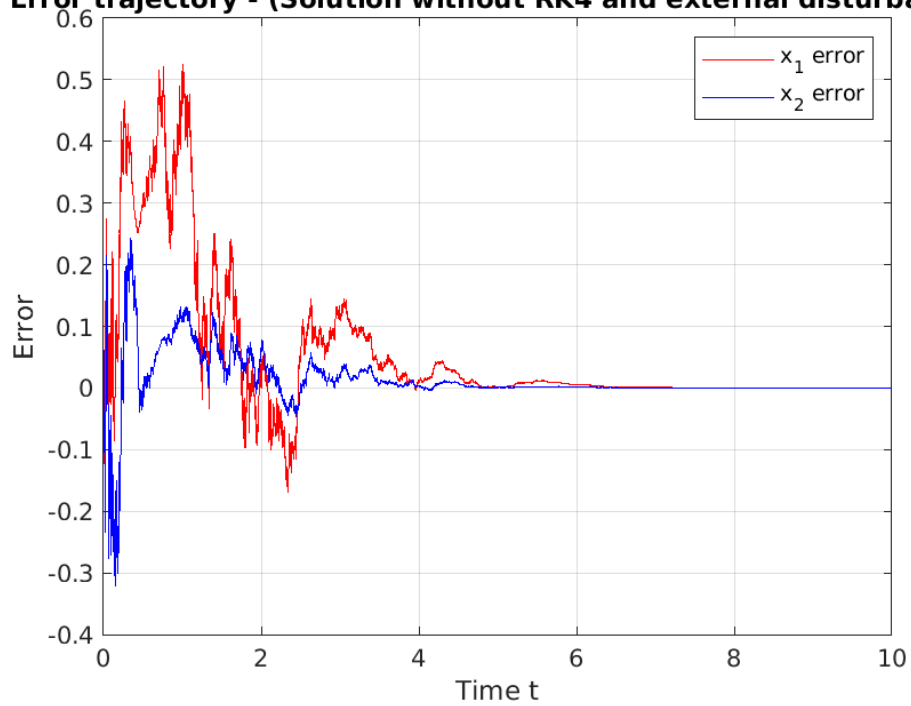


Fig.4 Error trajectory without Runge-Kutta and external disturbance.

We can see that mostly the error is due to the system uncertain (i.e. the wiener process), the uncertainty error tends to reduce to 0 when our system becomes more stable.