

## Contents

[Template] Duc.cpp.....	1
[Template] Duc.java .....	2
Template [Viet].cpp .....	2
BufferedReader.cpp .....	2
push-relabel.cpp .....	3
QTREE (HLD).cpp .....	4
convex-hull-trick.java .....	6
Edmond Blossom.java .....	7
mincost-matching.cpp .....	8
Hungarian.java .....	9
edmondskarp [Viet].cpp .....	10
convexHull [Viet].cpp .....	11
mincost [Viet].cpp .....	13
Treap.cpp .....	14
Math.cpp .....	16
Stirling number of the second kind .....	17
Bell numbers .....	17
Catalan number .....	17
Motzkin number .....	17

## [Template] Duc.cpp

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
#define sorted_array tree<int, null_type, less<int>, rb_tree_tag,
tree_order_statistics_node_update>
#define llong long long
#define long llong

int n_test;

void enter()
{
}

void solve()
{
}

void cleanup()
{
}

int main()
{
    ios::sync_with_stdio(false);
    if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());

    cin >> n_test;
    while (n_test--)
    {
        enter();
        solve();
        cleanup();
    }
}
```

```
}
```

## [Template] Duc.java

```
import java.util.*;
import java.awt.geom.*;
import java.io.*;
import java.math.*;

class Main
{
    static Scanner fi = new Scanner (System.in);
    static PrintWriter fo = new PrintWriter (System.out);
    static int n;

    static void enter()
    {
    }

    static void solve()
    {
    }

    public static void main(String[] args)
    {
        try {fi = new Scanner (new File("test.inp"));}
        catch (FileNotFoundException e) {}

        enter ();
        solve ();

        fi.close(); fo.close();
    }
}
```

## Template [Viet].cpp

```
#include <bits/stdc++.h>
#define N
#define INF
```

```
#define rep(i, a, b) for(int i = a; i <= b; i++)
#define per(i, b, a) for(int i = b; i >= a; i--)
#define bitcount(S) __builtin_popcount(S)
#define ll (long long)
#define db (double)
#define dbg(x) std::cout << #x << " " << x << std::endl
#define sz(x) x.size()
#define fi first
#define se second
using namespace std;
int main() {
    //freopen("input.txt", "r", stdin);
}
```

## BufferedReader.cpp

```
#include <bits/stdc++.h>
using namespace std;
#define long int64_t

struct BufferedReader
{
    char Buf[1 << 16 | 1];
    int cur;

    void FillBuffer ()
    {
        Buf[fread(Buf, 1, 1 << 16, stdin)] = 0;
        cur = 0;
    }

    BufferedReader ()
    {
        //freopen("test.inp", "r", stdin);
        FillBuffer();
    }

    void nextchar ()
    {
        ++cur;
        if (!Buf[cur]) FillBuffer();
    }
}
```

```

}

BufferedReader& operator >> (int &t)
{
    t = 0;
    while (!isdigit(Buf[cur])) nextchar();
    while (isdigit(Buf[cur])) t = t * 10 + Buf[cur] - '0', nextchar();

    return *this;
}
};

```

## push-relabel.cpp

```

#include <bits/stdc++.h>
using namespace std;
#define ll long long long
#define long llong

const int n_max = 1010;

bool in_queue[n_max];
long E[n_max];
int G[n_max][n_max], F[n_max][n_max];
int H[n_max];
int n, xs, xt;

void push_flow(int x, int y)
{
    int flow = min((long)G[x][y] - F[x][y], E[x]);
    F[x][y] += flow;
    F[y][x] -= flow;
    E[x] -= flow;
    E[y] += flow;
}

void enter()
{
    int m, x, y;
    cin >> n >> m >> xs >> xt;

```

```

while (m--)
{
    cin >> x >> y;
    cin >> G[x][y];
}

void solve()
{
    list<int> P;

    H[xs] = n;
    E[xs] = LLONG_MAX;
    for (int y = 1; y <= n; ++y)
        if (G[xs][y] > 0)
        {
            push_flow(xs, y);
            P.push_back(y);
            in_queue[y] = true;
        }

    while (!P.empty())
    {
        int x = P.front();
        int h_min = INT_MAX;

        for (int y = 1; y <= n; ++y)
            if (G[x][y] > F[x][y])
            {
                if (H[y] >= H[x]) h_min = min(h_min, H[y]);
                else
                {
                    push_flow(x, y);
                    if (!in_queue[y] && y != xs && y != xt)
                        P.push_back(y), in_queue[y] = true;
                }
            }

        if (E[x] > 0) H[x] = h_min + 1;
        else
        {
            P.pop_front();

```

```

        in_queue[x] = false;
    }
}

cout << E[xt] << "\n";
}

int main()
{
    ios::sync_with_stdio(false); cin.tie(nullptr);
    if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());

    enter();
    solve();
}

```

## QTREE (HLD).cpp

```

#include <bits/stdc++.h>
using namespace std;
#define ll long long
#define long ll long
#define ii pair<int,int>

const int n_max = 10010;

struct edge { int x, y, c; } E[n_max];

list<ii> G[n_max];
int M[n_max], H[n_max], l[n_max], IE[n_max], W[n_max], top_node[n_max],
heavy_child[n_max], T[n_max * 4], P[n_max][16];
int n, m, n_test;

inline bool is_heavy (int x) { return M[x] * 2 > M[P[x][0]]; }

void dfs (int x,int h)
{
    H[x] = h; M[x] = 1;

    for (list<ii>::iterator i = G[x].begin(); i != G[x].end(); ++i)
        if (i->first != P[x][0])

```

```

        {
            P[i->first][0] = x;
            W[i->first] = i->second;
            dfs(i->first, h + 1);
            M[x] += M[i->first];
        }
}

void load_path(int x)
{
    while (M[x] * 2 > M[P[x][0]]) l[x] = ++m, x = P[x][0];

    int p = x;
    while ((x = heavy_child[x]) > 0) IE[x] = m, top_node[x] = p;
}

void upd_edge (int u,int v,int x = 1,int l = 1,int r = m)
{
    if (l == r) { T[x] = v; return; }

    int k = x * 2, mid = (l + r) / 2;
    if (u <= mid)
        upd_edge(u, v, k, l, mid);
    else
        upd_edge(u, v, k + 1, mid + 1, r);

    T[x] = max(T[k], T[k + 1]);
}

int get_max (int u,int v,int x = 1,int l = 1,int r = m)
{
    if (v < l || r < u) return 0;
    if (u <= l && r <= v) return T[x];

    int k = x * 2, mid = (l + r) / 2;
    return max(get_max(u, v, k, l, mid),
               get_max(u, v, k + 1, mid + 1, r));
}

int lca (int x,int y)
{
    if (H[x] < H[y]) swap(x, y);

```

```

for (int i = 15; i >= 0; --i)
if (H[P[x][i]] >= H[y]) x = P[x][i];

if (x == y) return x;

for (int i = 15; i >= 0; --i)
if (P[x][i] != P[y][i]) x = P[x][i], y = P[y][i];

return P[x][0];
}

int get_max_edge (int x,int p) // p is x's ancestor
{
    int s = 0;

    while (x != p)
        if (is_heavy(x))
            if (H[top_node[x]] >= H[p]) // p is not in heavy path
            {
                s = max(s, get_max(l[x], lE[x]));
                x = top_node[x];
            } else // p is in heavy path
            {
                s = max(s, get_max(l[x], l[p] - 1));
                x = p;
            }
        else // advance normally
        {
            s = max(s, W[x]);
            x = P[x][0];
        }

    return s;
}

namespace query
{
    void change (int u,int v)
    {
        int x = (H[E[u].x] > H[E[u].y] ? E[u].x : E[u].y);

```

```

        W[x] = v;
        if (is_heavy(x)) upd_edge(l[x], v);
    }

    void query (int x,int y)
    {
        int p = lca(x, y);
        cout << max(get_max_edge(x, p), get_max_edge(y, p)) << "\n";
    }
}

void enter ()
{
    cin >> n;
    for (int i = 1; i < n; ++i)
    {
        cin >> E[i].x >> E[i].y >> E[i].c;
        G[E[i].x].push_back(ii (E[i].y, E[i].c));
        G[E[i].y].push_back(ii (E[i].x, E[i].c));
    }
}

void init ()
{
    dfs(1, 1);
    for (int j = 1; j < 16; ++j)
    for (int i = 1; i <= n; ++i)
        P[i][j] = P[P[i][j - 1]][j - 1];

    M[0] = 3 * n;
    for (int x = 1; x <= n; ++x)
    if (is_heavy(x)) heavy_child[P[x][0]] = x;

    for (int x = 1; x <= n; ++x)
    if (is_heavy(x) && heavy_child[x] == 0) load_path(x);

    for (int x = 1; x <= n; ++x)
    if (is_heavy(x)) upd_edge(l[x], W[x]);
}

void solve ()
{

```

```

string s;
int x, y;

while (true)
{
    cin >> s;
    if (s == "DONE") return;
    cin >> x >> y;

    if (s == "CHANGE") query::change(x, y);
    if (s == "QUERY") query::query(x, y);
}

void clean_up ()
{
    fill_n(heavy_child + 1, n, 0);
    fill_n(top_node + 1, n, 0);
    fill_n(IE + 1, n, 0);
    fill_n(I + 1, n, 0);
    for (int i = 1; i <= n; ++i) G[i].clear();
    m = 0;
}

int main ()
{
    ios::sync_with_stdio(false); cin.tie(NULL);
    if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());

    cin >> n_test;
    while (n_test--)
    {
        enter();
        init();
        solve();
        clean_up();
    }
}

```

## convex-hull-trick.java

```

public class ConvexHullOptimization {

    long[] A = new long[1000000];
    long[] B = new long[1000000];
    int len;
    int ptr;

    // a descends
    public void addLine(long a, long b) {
        // intersection of (A[len-2],B[len-2]) with (A[len-1],B[len-1]) must lie to the left of
        // intersection of (A[len-1],B[len-1]) with (a,b)
        while (len >= 2 && (B[len - 2] - B[len - 1]) * (a - A[len - 1]) >= (B[len - 1] - b) *
            (A[len - 1] - A[len - 2])) {
            --len;
        }
        A[len] = a;
        B[len] = b;
        ++len;
    }

    // x ascends
    public long minValue(long x) {
        ptr = Math.min(ptr, len - 1);
        while (ptr + 1 < len && A[ptr + 1] * x + B[ptr + 1] <= A[ptr] * x + B[ptr]) {
            ++ptr;
        }
        return A[ptr] * x + B[ptr];
    }

    // Usage example
    public static void main(String[] args) {
        ConvexHullOptimization h = new ConvexHullOptimization();
        h.addLine(3, 0);
        h.addLine(2, 1);
        h.addLine(3, 2);
        h.addLine(0, 6);
        System.out.println(h.minValue(0));
        System.out.println(h.minValue(1));
        System.out.println(h.minValue(2));
        System.out.println(h.minValue(3));
    }
}

```

```

}
}

```

## Edmond Blossom.java

```
import java.util.*;
```

```
public class MaxMatchingEdmonds {
```

```

    static int lca(int[] match, int[] base, int[] p, int a, int b) {
        boolean[] used = new boolean[match.length];
        while (true) {
            a = base[a];
            used[a] = true;
            if (match[a] == -1) break;
            a = p[match[a]];
        }
        while (true) {
            b = base[b];
            if (used[b]) return b;
            b = p[match[b]];
        }
    }

```

```

    static void markPath(int[] match, int[] base, boolean[] blossom, int[] p, int v, int b,
int children) {
        for (; base[v] != b; v = p[match[v]]) {
            blossom[base[v]] = blossom[base[match[v]]] = true;
            p[v] = children;
            children = match[v];
        }
    }

```

```

    static int findPath(List<Integer>[] graph, int[] match, int[] p, int root) {
        int n = graph.length;
        boolean[] used = new boolean[n];
        Arrays.fill(p, -1);
        int[] base = new int[n];
        for (int i = 0; i < n; ++i)
            base[i] = i;

```

```

        used[root] = true;
        int qh = 0;
        int qt = 0;
        int[] q = new int[n];
        q[qt++] = root;
        while (qh < qt) {
            int v = q[qh++];

            for (int to : graph[v]) {
                if (base[v] == base[to] || match[v] == to) continue;
                if (to == root || match[to] != -1 && p[match[to]] != -1) {
                    int curbase = lca(match, base, p, v, to);
                    boolean[] blossom = new boolean[n];
                    markPath(match, base, blossom, p, v, curbase, to);
                    markPath(match, base, blossom, p, to, curbase, v);
                    for (int i = 0; i < n; ++i)
                        if (blossom[base[i]]) {
                            base[i] = curbase;
                            if (!used[i]) {
                                used[i] = true;
                                q[qt++] = i;
                            }
                        }
                } else if (p[to] == -1) {
                    p[to] = v;
                    if (match[to] == -1)
                        return to;
                    to = match[to];
                    used[to] = true;
                    q[qt++] = to;
                }
            }
        }
        return -1;
    }

```

```

    public static int maxMatching(List<Integer>[] graph) {
        int n = graph.length;
        int[] match = new int[n];
        Arrays.fill(match, -1);
        int[] p = new int[n];
        for (int i = 0; i < n; ++i) {

```

```

    if (match[i] == -1) {
        int v = findPath(graph, match, p, i);
        while (v != -1) {
            int pv = p[v];
            int ppv = match[pv];
            match[v] = pv;
            match[pv] = v;
            v = ppv;
        }
    }
}

int matches = 0;
for (int i = 0; i < n; ++i)
    if (match[i] != -1)
        ++matches;
return matches / 2;
}

// Usage example
public static void main(String[] args) {
    int n = 4;
    List<Integer>[] g = new List[n];
    for (int i = 0; i < n; i++) {
        g[i] = new ArrayList<>();
    }
    g[0].add(1);
    g[1].add(0);
    g[1].add(2);
    g[2].add(1);
    g[2].add(3);
    g[3].add(2);
    g[0].add(3);
    g[3].add(0);
    System.out.println(2 == maxMatching(g));
}
}

```

## mincost-matching.cpp

```
#include <algorithm>
```

```

#include <cstdio>
#include <cmath>
#include <vector>

using namespace std;

typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;

double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
    int n = int(cost.size());

    // construct dual feasible solution
    VD u(n);
    VD v(n);
    for (int i = 0; i < n; i++) {
        u[i] = cost[i][0];
        for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);
    }
    for (int j = 0; j < n; j++) {
        v[j] = cost[0][j] - u[0];
        for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);
    }

    // construct primal solution satisfying complementary slackness
    Lmate = VI(n, -1);
    Rmate = VI(n, -1);
    int mated = 0;
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++) {
            if (Rmate[j] != -1) continue;
            if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
                Lmate[i] = j;
                Rmate[j] = i;
                mated++;
                break;
            }
        }
    }

    VD dist(n);

```



```

VI dad(n);
VI seen(n);

// repeat until primal solution is feasible
while (mated < n) {

    // find an unmatched left node
    int s = 0;
    while (Lmate[s] != -1) s++;

    // initialize Dijkstra
    fill(dad.begin(), dad.end(), -1);
    fill(seen.begin(), seen.end(), 0);
    for (int k = 0; k < n; k++)
        dist[k] = cost[s][k] - u[s] - v[k];

    int j = 0;
    while (true) {

        // find closest
        j = -1;
        for (int k = 0; k < n; k++) {
            if (seen[k]) continue;
            if (j == -1 || dist[k] < dist[j]) j = k;
        }
        seen[j] = 1;

        // termination condition
        if (Rmate[j] == -1) break;

        // relax neighbors
        const int i = Rmate[j];
        for (int k = 0; k < n; k++) {
            if (seen[k]) continue;
            const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
            if (dist[k] > new_dist) {
                dist[k] = new_dist;
                dad[k] = j;
            }
        }
    }
}

```

```

// update dual variables
for (int k = 0; k < n; k++) {
    if (k == j || !seen[k]) continue;
    const int i = Rmate[k];
    v[k] += dist[k] - dist[j];
    u[i] -= dist[k] - dist[j];
}
u[s] += dist[j];

// augment along path
while (dad[j] >= 0) {
    const int d = dad[j];
    Rmate[j] = Rmate[d];
    Lmate[Rmate[j]] = j;
    j = d;
}
Rmate[j] = s;
Lmate[s] = j;

mated++;
}

double value = 0;
for (int i = 0; i < n; i++)
    value += cost[i][Lmate[i]];

return value;
}

```

## Hungarian.java

```
import java.util.*;
```

```

class Hungarian {

    // a[1..n][1..m] >= 0, n <= m
    public static int solveAssignmentProblem(int[][] a) {
        int n = a.length - 1;
        int m = a[0].length - 1;
        int[] u = new int[n + 1];
        int[] v = new int[m + 1];
    }
}

```

```

int[] p = new int[m + 1];
int[] way = new int[m + 1];
for (int i = 1; i <= n; ++i) {
    p[0] = i;
    int j0 = 0;
    int[] minv = new int[m + 1];
    Arrays.fill(minv, Integer.MAX_VALUE);
    boolean[] used = new boolean[m + 1];
    do {
        used[j0] = true;
        int i0 = p[j0];
        int delta = Integer.MAX_VALUE;
        int j1 = 0;
        for (int j = 1; j <= m; ++j)
            if (!used[j]) {
                int cur = a[i0][j] - u[i0] - v[j];
                if (cur < minv[j]) {
                    minv[j] = cur;
                    way[j] = j0;
                }
                if (minv[j] < delta) {
                    delta = minv[j];
                    j1 = j;
                }
            }
        for (int j = 0; j <= m; ++j)
            if (used[j]) {
                u[p[j]] += delta;
                v[j] -= delta;
            } else
                minv[j] -= delta;
        j0 = j1;
    } while (p[j0] != 0);
    do {
        int j1 = way[j0];
        p[j0] = p[j1];
        j0 = j1;
    } while (j0 != 0);
}
return -v[0];
}

```

```

// random test
public static void main(String[] args) {
    Random rnd = new Random(1);
    for (int step = 0; step < 1000; step++) {
        int n = rnd.nextInt(8) + 1;
        int m = n + rnd.nextInt(9 - n);
        int[][] a = new int[n + 1][m + 1];
        for (int i = 1; i <= n; i++) {
            for (int j = 1; j <= m; j++) {
                a[i][j] = rnd.nextInt(100000);
            }
        }
        int res1 = solveAssignmentProblem(a);
        System.out.println(res1);
    }
}

```

## edmondskarp [Viet].cpp

```

#include <bits/stdc++.h>
#define N 1001
#define INF (int) 1e6 + 1
#define rep(i, a, b) for(int i = a; i <= b; i++)
#define per(i, b, a) for(int i = b; i >= a; i--)
#define bitcount(S) __builtin_popcount(S)
#define ll (long long)
#define db (double)
#define dbg(x) std::cout << x << std::endl
#define sz(x) x.size()
#define fi first
#define se second
using namespace std;
int n, m, s, t;
vector<int> g[N];
int c[N][N], d[N], f[N][N];
long long res;
bool findPath() {
    queue<int> q;
    rep(i, 1, n)
        d[i] = 0;
    d[s] = -1;
}

```

```

q.push(s);
while (!q.empty()) {
    int u = q.front();
    q.pop();
    if (u == t)
        return true;
    for(auto v: g[u])
        if (!d[v] && c[u][v] > f[u][v]) {
            d[v] = u;
            q.push(v);
        }
}
return false;
}

void enlarge() {
    int u, v, delta = INF;
    v = t;
    while (v != s) {
        u = d[v];
        delta = min(delta, c[u][v] - f[u][v]);
        v = u;
    }
    v = t;
    while (v != s) {
        u = d[v];
        f[u][v] += delta;
        f[v][u] -= delta;
        v = u;
    }
    res += delta;
}

int main() {
    //freopen("input.txt", "r", stdin);
    scanf("%d%d%d%d", &n, &m, &s, &t);
    rep(i, 1, m) {
        int u, v, w;
        scanf("%d%d%d", &u, &v, &w);
        g[u].push_back(v);
        g[v].push_back(u);
        c[u][v] = w;
    }
    while (findPath())

```

```

        enlarge();
        printf("%lld", res);
    }
}

```

## convexHull [Viet].cpp

```

#include <iostream>
#include <stack>
#include <stdlib.h>
using namespace std;

struct Point
{
    int x, y;
};

// A global point needed for sorting points with reference
// to the first point Used in compare function of qsort()
Point p0;

// A utility function to find next to top in a stack
Point nextToTop(stack<Point> &S)
{
    Point p = S.top();
    S.pop();
    Point res = S.top();
    S.push(p);
    return res;
}

// A utility function to swap two points
int swap(Point &p1, Point &p2)
{
    Point temp = p1;
    p1 = p2;
    p2 = temp;
}

// A utility function to return square of distance
// between p1 and p2
int distSq(Point p1, Point p2)

```

```

{
    return (p1.x - p2.x)*(p1.x - p2.x) +
           (p1.y - p2.y)*(p1.y - p2.y);
}

// To find orientation of ordered triplet (p, q, r).
// The function returns following values
// 0 --> p, q and r are colinear
// 1 --> Clockwise
// 2 --> Counterclockwise
int orientation(Point p, Point q, Point r)
{
    int val = (q.y - p.y) * (r.x - q.x) -
              (q.x - p.x) * (r.y - q.y);

    if (val == 0) return 0; // colinear
    return (val > 0)? 1: 2; // clock or counterclock wise
}

// A function used by library function qsort() to sort an array of
// points with respect to the first point
int compare(const void *vp1, const void *vp2)
{
    Point *p1 = (Point *)vp1;
    Point *p2 = (Point *)vp2;

    // Find orientation
    int o = orientation(p0, *p1, *p2);
    if (o == 0)
        return (distSq(p0, *p2) >= distSq(p0, *p1))? -1 : 1;

    return (o == 2)? -1: 1;
}

// Prints convex hull of a set of n points.
void convexHull(Point points[], int n)
{
    // Find the bottommost point
    int ymin = points[0].y, min = 0;
    for (int i = 1; i < n; i++)
    {
        int y = points[i].y;
        // Pick the bottom-most or chose the left
        // most point in case of tie
        if ((y < ymin) || (ymin == y &&
            points[i].x < points[min].x))
            ymin = points[i].y, min = i;
    }

    // Place the bottom-most point at first position
    swap(points[0], points[min]);

    // Sort n-1 points with respect to the first point.
    // A point p1 comes before p2 in sorted output if p2
    // has larger polar angle (in counterclockwise
    // direction) than p1
    p0 = points[0];
    qsort(&points[1], n-1, sizeof(Point), compare);

    // If two or more points make same angle with p0,
    // Remove all but the one that is farthest from p0
    // Remember that, in above sorting, our criteria was
    // to keep the farthest point at the end when more than
    // one points have same angle.
    int m = 1; // Initialize size of modified array
    for (int i=1; i<n; i++)
    {
        // Keep removing i while angle of i and i+1 is same
        // with respect to p0
        while (i < n-1 && orientation(p0, points[i],
            points[i+1]) == 0)
            i++;

        points[m] = points[i];
        m++; // Update size of modified array
    }

    // If modified array of points has less than 3 points,
    // convex hull is not possible
    if (m < 3) return;

    // Create an empty stack and push first three points

```

```

// to it.
stack<Point> S;
S.push(points[0]);
S.push(points[1]);
S.push(points[2]);

// Process remaining n-3 points
for (int i = 3; i < m; i++)
{
    // Keep removing top while the angle formed by
    // points next-to-top, top, and points[i] makes
    // a non-left turn
    while (orientation(nextToTop(S), S.top(), points[i]) != 2)
        S.pop();
    S.push(points[i]);
}

// Now stack has the output points, print contents of stack
while (!S.empty())
{
    Point p = S.top();
    cout << "(" << p.x << ", " << p.y << ")" << endl;
    S.pop();
}
}

// Driver program to test above functions
int main()
{
    Point points[] = {{0, 3}, {1, 1}, {2, 2}, {4, 4},
                     {0, 0}, {1, 2}, {3, 1}, {3, 3}};
    int n = sizeof(points)/sizeof(points[0]);
    convexHull(points, n);
    return 0;
}

```

## mincost [Viet].cpp

```

#include <bits/stdc++.h>
#define N 502
#define INF 1000001

```

```

#define rep(i, a, b) for(int i = a; i <= b; i++)
#define per(i, b, a) for(int i = b; i >= a; i--)
#define bitcount(S) __builtin_popcount(S)
#define ll (long long)
#define db (double)
#define dbg(x) std::cout << x << std::endl
#define sz(x) x.size()
#define fi first
#define se second
using namespace std;
int n, m, k, p[N], res, s, t, d[N];
string st, a[N];
struct edge {
    int v, cap, f, cost, i;
    edge(int _v, int _cap, int _f, int _cost, int _i) {
        v = _v; cap = _cap; f = _f; cost = _cost; i = _i;
    }
};
vector<edge> g[N];
pair<int, int> pre[N];
bool in[N];

void addEdge(int u, int v, int cap, int cost) {
    edge a = edge(v, cap, 0, cost, g[v].size());
    edge b = edge(u, 0, 0, -cost, g[u].size());
    g[u].push_back(a);
    g[v].push_back(b);
}

void buildGraph() {
    rep(i, 0, n)
        addEdge(i, i + 1, k, 0);
    rep(i, 1, m)
        rep(j, 0, n - a[i].length())
            if (st.substr(j, a[i].length()) == a[i])
                addEdge(j, j + a[i].length(), 1, -p[i]);
    s = 0; t = n + 1;
}

bool fordBellman() {
    queue<int> q;
    rep(i, 1, n + 1) {

```

```

    d[i] = INF;
    in[i] = false;
}
d[s] = 0;
q.push(s);
in[s] = true;
while (!q.empty()) {
    int u = q.front(); q.pop(); in[u] = false;
    rep(i, 0, g[u].size() - 1) {
        edge e = g[u][i];
        if (e.cap > e.f && d[e.v] > d[u] + e.cost) {
            d[e.v] = d[u] + e.cost;
            pre[e.v] = make_pair(u, i);
            if (!in[e.v]) {
                q.push(e.v);
                in[e.v] = true;
            }
        }
    }
}
return (d[t] < INF);
}

```

```

void enlarge() {
    int v = t, delta = INF;
    int u, i, j;
    while (v != s) {
        u = pre[v].fi;
        i = pre[v].se;
        delta = min(delta, g[u][i].cap - g[u][i].f);
        v = u;
    }
    v = t;
    while (v != s) {
        u = pre[v].fi;
        i = pre[v].se;
        j = g[u][i].i;
        g[u][i].f += delta;
        g[v][j].f -= delta;
        v = u;
    }
    res -= d[t] * delta;
}

```

```

}

int main() {
    //freopen("input.txt", "r", stdin);
    cin >> n >> st >> m;
    rep(i, 1, m)
        cin >> a[i] >> p[i];
    cin >> k;
    buildGraph();
    while (fordBellman())
        enlarge();
    cout << res;
}

```

## Treap.cpp

```

#include <bits/stdc++.h>
using namespace std;

```

```

struct Treap
{
    #define S(t) (t ? t->Sum : 0)
    #define W(t) (t ? t->Weight : 0)
}

```

```

struct Node
{
    long Weight, Sum, Value, AssignValue, IncStart, IncRate;
    int Priority;
    Node *l, *r;
}

```

```

Node (long x)
{
    Value = x;

    Priority = (rand() << 15) | rand();
    l = r = NULL;
    IncRate = IncStart = 0;
    AssignValue = -1;
    Weight = 1;
    Sum = 0;
}

```

```

} *root;

void PushQuery (Node *t)
{
    Node *l = t->l, *r = t->r;

    if (t->AssignValue > -1)
    {
        if (l)
        {
            l->IncRate = l->IncStart = 0;
            l->Value = l->AssignValue = t->AssignValue;
            l->Sum = l->Value * l->Weight;
        }

        if (r)
        {
            r->IncRate = r->IncStart = 0;
            r->Value = r->AssignValue = t->AssignValue;
            r->Sum = r->Value * r->Weight;
        }

        t->AssignValue = -1;
    }

    if (t->IncStart || t->IncRate)
    {
        if (l)
        {
            l->Sum += t->IncStart * l->Weight;
            l->Sum += t->IncRate * ((l->Weight * (l->Weight + 1)) >> 1);
            l->Value += t->IncStart + t->IncRate * (W(l->l) + 1);

            l->IncStart += t->IncStart;
            l->IncRate += t->IncRate;
        }

        if (r)
        {
            long k = t->IncStart + t->IncRate * (W(l) + 1);
            r->Sum += k * r->Weight;
            r->Sum += t->IncRate * ((r->Weight * (r->Weight + 1)) >> 1);
        }
    }
}

```

```

r->Value += k + t->IncRate * (W(r->l) + 1);

r->IncStart += k;
r->IncRate += t->IncRate;
}

t->IncRate = t->IncStart = 0;
}

void PropertyUpdate (Node *t)
{
    if (t)
    {
        t->Weight = W(t->l) + W(t->r) + 1;
        t->Sum = S(t->l) + S(t->r) + t->Value;
    }
}

void Split (Node *t, Node *&l, Node *&r, int p)
{
    if (!t) l = r = NULL;
    else
    {
        PushQuery(t);

        if (p <= W(t->l))
        {
            r = t;
            Split(t->l, l, r->l, p);
        } else
        {
            l = t;
            Split(t->r, l->r, r, p - W(t->l) - 1);
        }
    }

    PropertyUpdate(t);
}

void Merge (Node *&t, Node *l, Node *r)
{
}

```

```

if (l) PushQuery(l);
if (r) PushQuery(r);

if (!l) t = r;
else
if (!r) t = l;
else
if (l->Priority > r->Priority)
{
    t = l;
    Merge(t->r, l->r, r);
} else
{
    t = r;
    Merge(t->l, l, r->l);
}

PropertyUpdate(t);
}

void Assign (int l,int r,long value)
{
    Node *t1, *t = root, *t2;
    Split(t, t, t2, r);
    Split(t, t1, t, l - 1);

    t->IncRate = t->IncStart = 0;
    t->AssignValue = t->Value = value;
    t->Sum = value * t->Weight;

    Merge(t, t1, t);
    Merge(t, t, t2);
    root = t;
}

void IncRange (int l,int r,long IncRate)
{
    Node *t1, *t = root, *t2;
    Split(t, t, t2, r);
    Split(t, t1, t, l - 1);

    t->IncRate += IncRate;

```

```

t->Sum += IncRate * ((t->Weight * (t->Weight + 1)) >> 1);
t->Value += IncRate * (W(t->l) + 1);

Merge(t, t1, t);
Merge(t, t, t2);
root = t;
}

void insert (int p,int v)
{
    Node *t1, *t2;
    Split(root, t1, t2, p - 1);
    Merge(t1, t1, new Node(v));
    Merge(root, t1, t2);
}

long GetSum (int l,int r)
{
    Node *t1, *t = root, *t2;
    Split(t, t, t2, r);
    Split(t, t1, t, l - 1);

    long s = t->Sum;
    Merge(t, t1, t);
    Merge(t, t, t2);
    root = t;

    return s;
}

#undef S
#undef W
};

```

[Math.cpp](#)

```
#include "bits/stdc++.h"
```

```
const double PI = acos(-1);
```

```
struct point
```



```

{
    long x, y;
    point(long x, long y): x(x), y(y) {}
};

// = 0 -> parallel
// > 0 -> left
// < 0 -> right
inline long ccw(point a, point b, point c)
{
    return (b.x - a.x) * (c.y - a.y) - (b.y - a.y) * (c.x - a.x);
}

long euclid_extended(int nr, int r, int nt, int t)
{
    if (nr == 0) return t;
    return euclid_extended(r - r / nr * nr, nr, t - r / nr * nt, nt);
}

long inverse_mod(int x, int module)
{
    return euclid_extended(x, module, 1, 0);
}

```

### Stirling number of the second kind

Number of ways to partition a set of n objects into k non-empty subsets:

$$\left\{ \begin{matrix} n \\ n \end{matrix} \right\} = 1$$

$$\left\{ \begin{matrix} n \\ 1 \end{matrix} \right\} = 1$$

$$\left\{ \begin{matrix} n \\ k \end{matrix} \right\} = \frac{1}{k!} \sum_{j=0}^k (-1)^{k-j} \binom{k}{j} j^n$$

### Bell numbers

The sum over the values for k of the Stirling numbers of the second kind

$$B_n = \sum_{k=0}^n \left\{ \begin{matrix} n \\ k \end{matrix} \right\}$$

$$B_{n+1} = \sum_{k=0}^n \binom{n}{k} B_k$$

$$\text{Let } (x)_n = x(x-1)(x-2) \dots (x-n+1)$$

$$\sum_{k=0}^n \left\{ \begin{matrix} n \\ k \end{matrix} \right\} (x)_k = x^n$$

Recursion:

$$\{(n+1)/k\} = k\{n/k\} + \{n/(k-1)\}$$

$$\text{For } k > 0: \{0/0\} = 1 \text{ and } \{n/0\} = \{0/n\} = 0$$

### Catalan number

$$C_n = \frac{(2n)!}{n! (n+1)!}$$

### Motzkin number

$$M_n = \frac{2n+1}{n+2} M_{n-1} + \frac{3n-3}{n+2} M_{n-2}$$