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[Template] Duc.cpp

```
#include <bits/stdc++.h>
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace std;
using namespace __gnu_pbds;
#define sorted_array tree<int, null_type, less<int>, rb_tree_tag,
tree_order_statistics_node_update>
#define llong long long
#define long llong
int n_test;
void enter()
void solve()
void cleanup()
int main()
  ios::sync_with_stdio(false);
        if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());
        cin >> n_test;
        while (n_test--)
                 enter();
                 solve();
                 cleanup();
```

[Template] Duc.java

```
import java.util.*;
import java.awt.geom.*;
import java.io.*;
import java.math.*;
class Main
  static Scanner fi = new Scanner (System.in);
  static PrintWriter fo = new PrintWriter (System.out);
  static int n;
  static void enter()
  static void solve()
  public static void main(String[] args)
    try {fi = new Scanner (new File("test.inp"));}
    catch (FileNotFoundException e) {}
    enter ();
    solve ();
    fi.close(); fo.close();
```

Template [Viet].cpp

```
#include <bits/stdc++.h>
#define N
#define INF
#define rep(i, a, b) for(int i = a; i <= b; i++)
#define per(i, b, a) for(int i = b; i >= a; i--)
```

```
#define bitcount(S) __builtin_popcount(S)
#define II (long long)
#define db (double)
#define dbg(x) std::cout << #x << " " << x << std::endl
#define sz(x) x.size()
#define fi first
#define se second
using namespace std;
int main() {
    //freopen("input.txt", "r", stdin);
}</pre>
```

BufferedReader.cpp

```
#include <bits/stdc++.h>
using namespace std;
#define long int64_t
struct BufferedReader
  char Buf[1 << 16 | 1];
  int cur;
  void FillBuffer ()
    Buf[fread(Buf, 1, 1 << 16, stdin)] = 0;
    cur = 0;
  BufferedReader ()
    //freopen("test.inp","r",stdin);
    FillBuffer();
  void nextchar ()
    ++cur;
    if (!Buf[cur]) FillBuffer();
```

```
BufferedReader& operator >> (int &t)
    t = 0;
    while (!isdigit(Buf[cur])) nextchar();
    while (isdigit(Buf[cur])) t = t * 10 + Buf[cur] - '0', nextchar();
    return *this;
};
push-relabel.cpp
#include <bits/stdc++.h>
using namespace std;
#define llong long long
#define long llong
const int n_max = 1010;
bool in queue[n max];
long E[n_max];
int G[n_max][n_max], F[n_max][n_max];
int H[n max];
int n, xs, xt;
void push flow(int x, int y)
         int flow = min((long)G[x][y] - F[x][y], E[x]);
         F[x][y] += flow;
         F[y][x] = flow;
         E[x] = flow;
         E[y] += flow;
void enter()
         int m, x, y;
         cin >> n >> m >> xs >> xt;
         while (m--)
```

```
cin >> x >> y;
                  cin >> G[x][y];
void solve()
         list<int> P;
         H[xs] = n;
         E[xs] = LLONG MAX;
         for (int y = 1; y \le n; ++y)
         if (G[xs][y] > 0)
                  push flow(xs, y);
                  P.push_back(y);
                  in_queue[y] = true;
         while (!P.empty())
                  int x = P.front();
                  int h min = INT MAX;
                  for (int y = 1; y <= n; ++y)
                  if (G[x][y] > F[x][y])
                           if (H[y] >= H[x]) h_min = min(h_min, H[y]);
                           else
                                    push flow(x, y);
                                    if (!in_queue[y] && y != xs && y != xt)
P.push_back(y), in_queue[y] = true;
                  if (E[x] > 0) H[x] = h min + 1;
                  else
                           P.pop front();
                           in_queue[x] = false;
```

```
W[i->first] = i->second;
                                                                                                         dfs(i\rightarrow first, h + 1);
          cout << E[xt] << "\n";
                                                                                                         M[x] += M[i->first];
int main()
                                                                                                     void load path(int x)
  ios::sync with stdio(false); cin.tie(nullptr);
          if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());
                                                                                                       while (M[x] * 2 > M[P[x][0]]) I[x] = ++m, x = P[x][0];
          enter();
                                                                                                       int p = x;
          solve();
                                                                                                       while ((x = heavy child[x]) > 0) IE[x] = m, top node[x] = p;
                                                                                                     void upd edge (int u,int v,int x = 1,int l = 1,int r = m)
QTREE (HLD).cpp
#include <bits/stdc++.h>
                                                                                                       if (I == r) { T[x] = v; return; }
using namespace std;
                                                                                                       int k = x * 2, mid = (I + r) / 2;
#define llong long long
                                                                                                       if (u \le mid)
#define long llong
                                                                                                         upd_edge(u, v, k, l, mid);
#define ii pair<int,int>
                                                                                                       else
                                                                                                         upd edge(u, v, k + 1, mid + 1, r);
const int n max = 10010;
                                                                                                       T[x] = max(T[k], T[k + 1]);
struct edge { int x, y, c; } E[n max];
list<ii> G[n max];
                                                                                                     int get max (int u,int v,int x = 1,int l = 1,int r = m)
int M[n max], H[n max], I[n max], IE[n max], W[n max], top node[n max],
heavy_child[n_max], T[n_max * 4], P[n_max][16];
int n, m, n test;
                                                                                                       if (v < I \mid | r < u) return 0;
                                                                                                       if (u \le I \&\& r \le v) return T[x];
inline bool is_heavy (int x) { return M[x] * 2 > M[P[x][0]]; }
                                                                                                       int k = x * 2, mid = (l + r) / 2;
                                                                                                       return max(get max(u, v, k, l, mid),
void dfs (int x,int h)
                                                                                                             get_max(u, v, k + 1, mid + 1, r));
  H[x] = h; M[x] = 1;
  for (list<ii>::iterator i = G[x].begin(); i != G[x].end(); ++i)
                                                                                                     int lca (int x,int y)
  if (i\rightarrow first != P[x][0])
                                                                                                       if (H[x] < H[y]) swap(x, y);
     P[i->first][0] = x;
                                                                                                       for (int i = 15; i >= 0; --i)
```

```
if (H[P[x][i]] >= H[y]) x = P[x][i];
  if (x == y) return x;
  for (int i = 15; i >= 0; --i)
  if (P[x][i] != P[y][i]) x = P[x][i], y = P[y][i];
  return P[x][0];
int get max edge (int x,int p) // p is x's ancestor
  int s = 0;
  while (x != p)
     if (is heavy(x))
       if (H[top\_node[x]] >= H[p]) // p is not in heavy path
         s = max(s, get_max(I[x], IE[x]));
         x = top node[x];
       } else // p is in heavy path
         s = max(s, get max(I[x], I[p] - 1));
         x = p;
    else // advance normally
       s = max(s, W[x]);
       x = P[x][0];
  return s;
namespace query
  void change (int u,int v)
     int x = (H[E[u].x] > H[E[u].y] ? E[u].x : E[u].y);
     W[x] = v;
     if (is_heavy(x)) upd_edge(I[x], v);
```

```
void query (int x,int y)
    int p = lca(x, y);
    cout << max(get_max_edge(x, p), get_max_edge(y, p)) << "\n";</pre>
void enter ()
  cin >> n;
  for (int i = 1; i < n; ++i)
    cin >> E[i].x >> E[i].y >> E[i].c;
    G[E[i].x].push_back(ii (E[i].y, E[i].c));
    G[E[i].y].push_back(ii (E[i].x, E[i].c));
void init ()
  dfs(1, 1);
  for (int j = 1; j < 16; ++j)
  for (int i = 1; i <= n; ++i)
    P[i][j] = P[P[i][j-1]][j-1];
  M[0] = 3 * n;
  for (int x = 1; x <= n; ++x)
  if (is_heavy(x)) heavy_child[P[x][0]] = x;
  for (int x = 1; x <= n; ++x)
  if (is heavy(x) && heavy child[x] == 0) load path(x);
  for (int x = 1; x <= n; ++x)
  if (is_heavy(x)) upd_edge(I[x], W[x]);
void solve ()
  string s;
  int x, y;
```

```
while (true)
    cin >> s;
    if (s == "DONE") return;
    cin >> x >> y;
    if (s == "CHANGE") query::change(x, y);
    if (s == "QUERY") query::query(x, y);
void clean up ()
  fill n(heavy child + 1, n, 0);
  fill n(top node + 1, n, 0);
  fill_n(IE + 1, n, 0);
  fill n(l + 1, n, 0);
  for (int i = 1; i <= n; ++i) G[i].clear();
  m = 0;
int main ()
  ios::sync with stdio(false); cin.tie(NULL);
  if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());
  cin >> n test;
  while (n test--)
    enter();
    init();
    solve();
    clean up();
```

convex-hull-trick.java

public class ConvexHullOptimization {

```
long[] A = new long[1000000];
long[] B = new long[1000000];
int len;
int ptr;
// a descends
public void addLine(long a, long b) {
 // intersection of (A[len-2],B[len-2]) with (A[len-1],B[len-1]) must lie to the left of
intersection of (A[len-1],B[len-1]) with (a,b)
  while (len >= 2 && (B[len - 2] - B[len - 1]) * (a - A[len - 1]) >= (B[len - 1] - b) *
(A[len - 1] - A[len - 2])) {
   --len;
  A[len] = a;
  B[len] = b;
  ++len;
// x ascends
 public long minValue(long x) {
  ptr = Math.min(ptr, len - 1);
  while (ptr + 1 < len && A[ptr + 1] * x + B[ptr + 1] <= A[ptr] * x + B[ptr]) {
   ++ptr;
  return A[ptr] * x + B[ptr];
// Usage example
 public static void main(String[] args) {
  ConvexHullOptimization h = new ConvexHullOptimization();
  h.addLine(3, 0);
  h.addLine(2, 1);
  h.addLine(3, 2);
  h.addLine(0, 6);
  System.out.println(h.minValue(0));
  System.out.println(h.minValue(1));
  System.out.println(h.minValue(2));
  System.out.println(h.minValue(3));
```

Edmond Blossom.java

```
import java.util.*;
public class MaxMatchingEdmonds {
 static int lca(int[] match, int[] base, int[] p, int a, int b) {
  boolean[] used = new boolean[match.length];
  while (true) {
   a = base[a];
   used[a] = true;
   if (match[a] == -1) break;
   a = p[match[a]];
  while (true) {
   b = base[b];
   if (used[b]) return b;
   b = p[match[b]];
 static void markPath(int[] match, int[] base, boolean[] blossom, int[] p, int v, int b,
int children) {
  for (; base[v] != b; v = p[match[v]]) {
   blossom[base[v]] = blossom[base[match[v]]] = true;
   p[v] = children;
   children = match[v];
 static int findPath(List<Integer>[] graph, int[] match, int[] p, int root) {
  int n = graph.length;
  boolean[] used = new boolean[n];
  Arrays.fill(p, -1);
  int[] base = new int[n];
  for (int i = 0; i < n; ++i)
   base[i] = i;
  used[root] = true;
  int qh = 0;
  int at = 0;
  int[] q = new int[n];
```

```
a[at++] = root;
while (qh < qt) {
 int v = q[qh++];
  for (int to : graph[v]) {
  if (base[v] == base[to] | | match[v] == to) continue;
  if (to == root | | match[to] != -1 && p[match[to]] != -1) {
    int curbase = lca(match, base, p, v, to);
    boolean[] blossom = new boolean[n];
    markPath(match, base, blossom, p, v, curbase, to);
    markPath(match, base, blossom, p, to, curbase, v);
    for (int i = 0; i < n; ++i)
     if (blossom[base[i]]) {
      base[i] = curbase;
      if (!used[i]) {
       used[i] = true;
       q[qt++] = i;
   else if (p[to] == -1) {
    p[to] = v;
    if (match[to] == -1)
     return to;
    to = match[to];
    used[to] = true;
    q[qt++] = to;
return -1;
public static int maxMatching(List<Integer>[] graph) {
int n = graph.length;
int[] match = new int[n];
Arrays.fill(match, -1);
int[] p = new int[n];
for (int i = 0; i < n; ++i) {
 if (match[i] == -1) {
  int v = findPath(graph, match, p, i);
   while (v != -1) {
    int pv = p[v];
```

```
int ppv = match[pv];
    match[v] = pv;
    match[pv] = v;
    v = ppv;
 int matches = 0:
 for (int i = 0; i < n; ++i)
  if (match[i] != -1)
   ++matches;
 return matches / 2;
// Usage example
public static void main(String[] args) {
int n = 4;
 List<Integer>[] g = new List[n];
 for (int i = 0; i < n; i++) {
  g[i] = new ArrayList<>();
 g[0].add(1);
 g[1].add(0);
 g[1].add(2);
 g[2].add(1);
 g[2].add(3);
 g[3].add(2);
 g[0].add(3);
 g[3].add(0);
 System.out.println(2 == maxMatching(g));
```

mincost-matching.cpp

```
#include <algorithm>
#include <cstdio>
#include <cmath>
#include <vector>
```

```
using namespace std;
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
int n = int(cost.size());
// construct dual feasible solution
VD u(n);
VD v(n);
for (int i = 0; i < n; i++) {
  u[i] = cost[i][0];
 for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);
for (int j = 0; j < n; j++) {
  v[j] = cost[0][j] - u[0];
  for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);
// construct primal solution satisfying complementary slackness
Lmate = VI(n, -1);
Rmate = VI(n, -1);
int mated = 0;
for (int i = 0; i < n; i++) {
  for (int j = 0; j < n; j++) {
   if (Rmate[j] != -1) continue;
   if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
         Lmate[i] = j;
         Rmate[i] = i;
         mated++;
         break;
VD dist(n);
VI dad(n);
VI seen(n);
// repeat until primal solution is feasible
```

```
while (mated < n) {
 // find an unmatched left node
 int s = 0;
 while (Lmate[s] != -1) s++;
 // initialize Dijkstra
 fill(dad.begin(), dad.end(), -1);
 fill(seen.begin(), seen.end(), 0);
 for (int k = 0; k < n; k++)
  dist[k] = cost[s][k] - u[s] - v[k];
 int j = 0;
 while (true) {
  // find closest
  i = -1;
  for (int k = 0; k < n; k++) {
        if (seen[k]) continue;
        if (i == -1 | | dist[k] < dist[i]) i = k;
  seen[j] = 1;
  // termination condition
  if (Rmate[j] == -1) break;
  // relax neighbors
  const int i = Rmate[j];
  for (int k = 0; k < n; k++) {
        if (seen[k]) continue;
        const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
        if (dist[k] > new_dist) {
         dist[k] = new dist;
         dad[k] = j;
 // update dual variables
 for (int k = 0; k < n; k++) {
  if (k == j | | !seen[k]) continue;
  const int i = Rmate[k];
```

```
v[k] += dist[k] - dist[j];
  u[i] -= dist[k] - dist[j];
 u[s] += dist[j];
 // augment along path
 while (dad[i] >= 0) {
  const int d = dad[j];
  Rmate[j] = Rmate[d];
  Lmate[Rmate[i]] = i;
 j = d;
 Rmate[i] = s;
 Lmate[s] = j;
 mated++;
double value = 0;
for (int i = 0; i < n; i++)
 value += cost[i][Lmate[i]];
return value;
```

edmondskarp [Viet].cpp

```
#include <bits/stdc++.h>
#define N 1001
#define INF (int) 1e6 + 1
#define rep(i, a, b) for(int i = a; i <= b; i++)
#define per(i, b, a) for(int i = b; i >= a; i--)
#define bitcount(S) __builtin_popcount(S)
#define II (long long)
#define db (double)
#define dbg(x) std::cout << x << std::endl
#define sz(x) x.size()
#define se second
using namespace std;
int n, m, s, t;</pre>
```

```
vector<int> g[N];
int c[N][N], d[N], f[N][N];
long long res;
bool findPath() {
  queue<int> q;
  rep(i, 1, n)
     d[i] = 0;
  d[s] = -1;
  q.push(s);
  while (!q.empty()) {
    int u = q.front();
     q.pop();
     if (u == t)
       return true;
     for(auto v: g[u])
       if (!d[v] \&\& c[u][v] > f[u][v]) {
          d[v] = u;
          q.push(v);
  return false;
void enlarge() {
  int u, v, delta = INF;
  v = t;
  while (v != s) {
     u = d[v];
     delta = min(delta, c[u][v] - f[u][v]);
     v = u;
  v = t;
  while (v != s) {
     u = d[v];
     f[u][v] += delta;
     f[v][u] -= delta;
     v = u;
  res += delta;
int main() {
  //freopen("input.txt", "r", stdin);
  scanf("%d%d%d%d", &n, &m, &s, &t);
```

```
rep(i, 1, m) {
    int u, v, w;
    scanf("%d%d%d", &u, &v, &w);
    g[u].push_back(v);
    g[v].push_back(u);
    c[u][v] = w;
}
while (findPath())
    enlarge();
printf("%lld", res);
```

convexHull [Viet].cpp

```
#include <iostream>
#include <stack>
#include <stdlib.h>
using namespace std;
struct Point
  int x, y;
};
// A globle point needed for sorting points with reference
// to the first point Used in compare function of qsort()
Point p0;
// A utility function to find next to top in a stack
Point nextToTop(stack<Point> &S)
  Point p = S.top();
  S.pop();
  Point res = S.top();
  S.push(p);
  return res;
// A utility function to swap two points
int swap(Point &p1, Point &p2)
```

```
Point temp = p1;
  p1 = p2;
  p2 = temp;
// A utility function to return square of distance
// between p1 and p2
int distSq(Point p1, Point p2)
  return (p1.x - p2.x)*(p1.x - p2.x) +
      (p1.y - p2.y)*(p1.y - p2.y);
// To find orientation of ordered triplet (p, q, r).
// The function returns following values
// 0 --> p, q and r are colinear
// 1 --> Clockwise
// 2 --> Counterclockwise
int orientation(Point p, Point q, Point r)
  int val = (q.y - p.y) * (r.x - q.x) -
        (q.x - p.x) * (r.v - q.v);
  if (val == 0) return 0; // colinear
  return (val > 0)? 1: 2; // clock or counterclock wise
// A function used by library function qsort() to sort an array of
// points with respect to the first point
int compare(const void *vp1, const void *vp2)
  Point *p1 = (Point *)vp1;
  Point *p2 = (Point *)vp2;
  // Find orientation
 int o = orientation(p0, *p1, *p2);
 if (o == 0)
  return (distSq(p0, *p2) >= distSq(p0, *p1))? -1 : 1;
  return (o == 2)? -1: 1;
```

```
// Prints convex hull of a set of n points.
void convexHull(Point points[], int n)
 // Find the bottommost point
 int ymin = points[0].y, min = 0;
 for (int i = 1; i < n; i++)
  int y = points[i].y;
  // Pick the bottom-most or chose the left
  // most point in case of tie
  if ((y < ymin) | | (ymin == y &&
     points[i].x < points[min].x))
    ymin = points[i].y, min = i;
 // Place the bottom-most point at first position
 swap(points[0], points[min]);
 // Sort n-1 points with respect to the first point.
 // A point p1 comes before p2 in sorted ouput if p2
 // has larger polar angle (in counterclockwise
 // direction) than p1
 p0 = points[0];
 gsort(&points[1], n-1, sizeof(Point), compare);
 // If two or more points make same angle with p0,
 // Remove all but the one that is farthest from p0
 // Remember that, in above sorting, our criteria was
 // to keep the farthest point at the end when more than
 // one points have same angle.
 int m = 1; // Initialize size of modified array
 for (int i=1; i<n; i++)
    // Keep removing i while angle of i and i+1 is same
    // with respect to p0
    while (i < n-1 && orientation(p0, points[i],
                    points[i+1]) == 0
     i++;
    points[m] = points[i];
```

```
m++; // Update size of modified array
 // If modified array of points has less than 3 points,
  // convex hull is not possible
 if (m < 3) return;
 // Create an empty stack and push first three points
 // to it.
  stack<Point>S;
  S.push(points[0]);
  S.push(points[1]);
  S.push(points[2]);
  // Process remaining n-3 points
  for (int i = 3; i < m; i++)
   // Keep removing top while the angle formed by
   // points next-to-top, top, and points[i] makes
   // a non-left turn
   while (orientation(nextToTop(S), S.top(), points[i]) != 2)
     S.pop();
   S.push(points[i]);
  // Now stack has the output points, print contents of stack
  while (!S.empty())
    Point p = S.top();
    cout << "(" << p.x << ", " << p.y <<")" << endl;
    S.pop();
// Driver program to test above functions
int main()
  Point points[] = \{\{0, 3\}, \{1, 1\}, \{2, 2\}, \{4, 4\},
             \{0, 0\}, \{1, 2\}, \{3, 1\}, \{3, 3\}\};
  int n = sizeof(points)/sizeof(points[0]);
  convexHull(points, n);
  return 0;
```

mincost [Viet].cpp

```
#include <bits/stdc++.h>
#define N 502
#define INF 1000001
#define rep(i, a, b) for(int i = a; i \le b; i++)
#define per(i, b, a) for(int i = b; i >= a; i--)
#define bitcount(S) builtin popcount(S)
#define II (long long)
#define db (double)
#define dbg(x) std::cout << x << std::endl
#define sz(x) x.size()
#define fi first
#define se second
using namespace std;
int n, m, k, p[N], res, s, t, d[N];
string st, a[N];
struct edge {
  int v, cap, f, cost, i;
  edge(int v, int cap, int f, int cost, int i) {
    v = v; cap = cap; f = f; cost = cost; i = i;
};
vector<edge> g[N];
pair<int, int> pre[N];
bool in[N];
void addEdge(int u, int v, int cap, int cost) {
  edge a = edge(v, cap, 0, cost, g[v].size());
  edge b = edge(u, 0, 0, -cost, g[u].size());
  g[u].push_back(a);
  g[v].push back(b);
void buildGraph() {
  rep(i, 0, n)
    addEdge(i, i + 1, k, 0);
  rep(i, 1, m)
    rep(j, 0, n - a[i].length())
```

```
if (st.substr(j, a[i].length()) == a[i])
          addEdge(j, j + a[i].length(), 1, -p[i]);
  s = 0; t = n + 1;
bool fordBellman() {
  queue<int> q;
  rep(i, 1, n + 1) {
    d[i] = INF;
     in[i] = false;
  d[s] = 0;
  q.push(s);
  in[s] = true;
  while (!q.empty()) {
    int u = q.front(); q.pop(); in[u] = false;
    rep(i, 0, g[u].size() - 1) {
       edge e = g[u][i];
       if (e.cap > e.f \&\& d[e.v] > d[u] + e.cost) {
          d[e.v] = d[u] + e.cost;
          pre[e.v] = make_pair(u, i);
          if (!in[e.v]) {
            q.push(e.v);
            in[e.v] = true;
  return (d[t] < INF);
void enlarge() {
  int v = t, delta = INF;
  int u, i, j;
  while (v != s) {
     u = pre[v].fi;
    i = pre[v].se;
    delta = min(delta, g[u][i].cap - g[u][i].f);
     v = u;
  v = t;
  while (v != s) {
```

```
u = pre[v].fi;
    i = pre[v].se;
    j = g[u][i].i;
    g[u][i].f += delta;
    g[v][j].f -= delta;
    v = u;
  res -= d[t] * delta;
int main() {
  //freopen("input.txt", "r", stdin);
  cin >> n >> st >> m;
  rep(i, 1, m)
    cin >> a[i] >> p[i];
  cin >> k;
  buildGraph();
  while (fordBellman())
    enlarge();
  cout << res;
Treap.cpp
#include <bits/stdc++.h>
using namespace std;
struct Treap
  #define S(t) (t ? t->Sum : 0)
  #define W(t) (t?t->Weight:0)
  struct Node
    long Weight, Sum, Value, AssignValue, IncStart, IncRate;
    int Priority;
    Node *I, *r;
    Node (long x)
      Value = x;
```

```
Priority = (rand() << 15) | rand();
    I = r = NULL;
    IncRate = IncStart = 0;
    AssignValue = -1;
    Weight = 1;
    Sum = 0;
} *root;
void PushQuery (Node *t)
  Node *I = t->I, *r = t->r;
  if (t->AssignValue > -1)
    if (I)
      I->IncRate = I->IncStart = 0;
      I->Value = I->AssignValue = t->AssignValue;
      I->Sum = I->Value * I->Weight;
    if (r)
      r->IncRate = r->IncStart = 0;
      r->Value = r->AssignValue = t->AssignValue;
      r->Sum = r->Value * r->Weight;
    t->AssignValue = -1;
 if (t->IncStart | | t->IncRate)
    if (I)
      I->Sum += t->IncStart * I->Weight;
      I->Sum += t->IncRate * ((I->Weight * (I->Weight + 1)) >> 1);
      I->Value += t->IncStart + t->IncRate * (W(I->I) + 1);
      l->IncStart += t->IncStart;
```

```
l->IncRate += t->IncRate;
    if (r)
      long k = t->IncStart + t->IncRate * (W(I) + 1);
      r->Sum += k * r->Weight;
      r->Sum += t->IncRate * ((r->Weight * (r->Weight + 1)) >> 1);
      r->Value += k + t->IncRate * (W(r->l) + 1);
      r->IncStart += k;
      r->IncRate += t->IncRate;
    t->IncRate = t->IncStart = 0;
void PropertyUpdate (Node *t)
 if (t)
    t->Weight = W(t->1) + W(t->r) + 1;
    t->Sum = S(t->1) + S(t->r) + t->Value;
void Split (Node *t, Node *&l, Node *&r, int p)
 if (!t) I = r = NULL;
  else
    PushQuery(t);
    if (p \le W(t > I))
      r = t;
      Split(t->l, l, r->l, p);
    } else
      I = t;
      Split(t->r, l->r, r, p - W(t->l) - 1);
```

```
PropertyUpdate(t);
void Merge (Node *&t, Node *I, Node *r)
  if (I) PushQuery(I);
 if (r) PushQuery(r);
  if (!1) t = r;
  else
  if (!r) t = 1;
  else
 if (I->Priority > r->Priority)
    t = l;
    Merge(t->r, l->r, r);
  } else
    t = r;
    Merge(t->l, l, r->l);
  PropertyUpdate(t);
void Assign (int l,int r,long value)
  Node *t1, *t = root, *t2;
  Split(t, t, t2, r);
  Split(t, t1, t, l - 1);
  t->IncRate = t->IncStart = 0;
  t->AssignValue = t->Value = value;
 t->Sum = value * t->Weight;
  Merge(t, t1, t);
  Merge(t, t, t2);
  root = t;
```

```
void IncRange (int l,int r,long IncRate)
    Node *t1, *t = root, *t2;
    Split(t, t, t2, r);
    Split(t, t1, t, I - 1);
    t->IncRate += IncRate;
    t->Sum += IncRate * ((t->Weight * (t->Weight + 1)) >> 1);
    t->Value += IncRate * (W(t->l) + 1);
    Merge(t, t1, t);
    Merge(t, t, t2);
    root = t;
  void insert (int p,int v)
    Node *t1, *t2;
    Split(root, t1, t2, p - 1);
    Merge(t1, t1, new Node(v));
    Merge(root, t1, t2);
  long GetSum (int I,int r)
    Node *t1, *t = root, *t2;
    Split(t, t, t2, r);
    Split(t, t1, t, I - 1);
    long s = t->Sum;
    Merge(t, t1, t);
    Merge(t, t, t2);
    root = t;
    return s;
  #undef S
  #undef W
};
```

Math.cpp

```
#include "bits/stdc++.h"
const double PI = acos(-1);
struct point
         long x, y;
         point(long x, long y): x(x), y(y) {}
};
// = 0 -> parallel
// > 0 -> left
// < 0 \rightarrow right
inline long ccw(point a, point b, point c)
         return (b.x - a.x) * (c.y - a.y) - (b.y - a.y) * (c.x - a.x);
long euclid_extended(int nr, int r, int nt, int t)
         if (nr == 0) return t;
         return euclid_extended(r - r / nr * nr, nr, t - r / nr * nt, nt);
long inverse_mod(int x, int module)
         return euclid_extended(x, module, 1, 0);
```

Stirling number of the second kind

Number of ways to partition a set of n objects into k non-empty subsets:

$$\{\frac{n}{n}\} = 1$$

$$\{\frac{n}{1}\} = 1$$

$$\{\frac{n}{k}\} = \frac{1}{k!} \sum_{j=0}^{k} (-1)^{k-j} {k \choose j} j^{n}$$

Bell numbers

The sum over the values for k of the Stirling numbers of the second kind

$$B_n = \sum_{k=0}^n \{ \frac{n}{k} \}$$

$$B_{n+1} = \sum_{k=0}^{n} \binom{n}{k} B_k$$

Let
$$(x)_n = x(x-1)(x-2)...(x-n+1)$$

$$\sum_{k=0}^{n} \left\{\frac{n}{k}\right\} (x)_n = x^n$$

Recursion:

$$\{(n+1)/k\} = k\{n/k\} + \{n/(k-1)\}$$

For
$$k>0$$
: $\{0/0\} = 1$ and $\{n/0\} = \{0/n\} = 0$

Catalan number

$$C_n = \frac{(2n)!}{n! (n+1)!}$$

Motzkin number

$$M_n = \frac{2n+1}{n+2}M_{n-1} + \frac{3n-3}{n+2}M_{n-2}$$