## Mục Lục:

## **[Template] Duc.cpp**

#include <bits/stdc++.h>

#include <ext/pb\_ds/assoc\_container.hpp>

#include <ext/pb\_ds/tree\_policy.hpp>

using namespace std;

using namespace \_\_gnu\_pbds;

#define sorted\_array tree<int, null\_type, less<int>, rb\_tree\_tag, tree\_order\_statistics\_node\_update>

#define llong long long

#define long llong

int n\_test;

void enter()

{

}

void solve()

{

}

void cleanup()

{

}

int main()

{

ios::sync\_with\_stdio(false);

if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());

cin >> n\_test;

while (n\_test--)

{

enter();

solve();

cleanup();

}

}

## **[Template] Duc.java**

import java.util.\*;

import java.awt.geom.\*;

import java.io.\*;

import java.math.\*;

class Main

{

static Scanner fi = new Scanner (System.in);

static PrintWriter fo = new PrintWriter (System.out);

static int n;

static void enter()

{

}

static void solve()

{

}

public static void main(String[] args)

{

try {fi = new Scanner (new File("test.inp"));}

catch (FileNotFoundException e) {}

enter ();

solve ();

fi.close(); fo.close();

}

}

## **Template [Viet].cpp**

#include <bits/stdc++.h>

#define N

#define INF

#define rep(i, a, b) for(int i = a; i <= b; i++)

#define per(i, b, a) for(int i = b; i >= a; i--)

#define bitcount(S) \_\_builtin\_popcount(S)

#define ll (long long)

#define db (double)

#define dbg(x) std::cout << #x << " " << x << std::endl

#define sz(x) x.size()

#define fi first

#define se second

using namespace std;

int main() {

//freopen("input.txt", "r", stdin);

}

## **BufferedReader.cpp**

#include <bits/stdc++.h>

using namespace std;

#define long int64\_t

struct BufferedReader

{

char Buf[1 << 16 | 1];

int cur;

void FillBuffer ()

{

Buf[fread(Buf, 1, 1 << 16, stdin)] = 0;

cur = 0;

}

BufferedReader ()

{

//freopen("test.inp","r",stdin);

FillBuffer();

}

void nextchar ()

{

++cur;

if (!Buf[cur]) FillBuffer();

}

BufferedReader& operator >> (int &t)

{

t = 0;

while (!isdigit(Buf[cur])) nextchar();

while (isdigit(Buf[cur])) t = t \* 10 + Buf[cur] - '0', nextchar();

return \*this;

}

};

## **push-relabel.cpp**

#include <bits/stdc++.h>

using namespace std;

#define llong long long

#define long llong

const int n\_max = 1010;

bool in\_queue[n\_max];

long E[n\_max];

int G[n\_max][n\_max], F[n\_max][n\_max];

int H[n\_max];

int n, xs, xt;

void push\_flow(int x, int y)

{

int flow = min((long)G[x][y] - F[x][y], E[x]);

F[x][y] += flow;

F[y][x] -= flow;

E[x] -= flow;

E[y] += flow;

}

void enter()

{

int m, x, y;

cin >> n >> m >> xs >> xt;

while (m--)

{

cin >> x >> y;

cin >> G[x][y];

}

}

void solve()

{

list<int> P;

H[xs] = n;

E[xs] = LLONG\_MAX;

for (int y = 1; y <= n; ++y)

if (G[xs][y] > 0)

{

push\_flow(xs, y);

P.push\_back(y);

in\_queue[y] = true;

}

while (!P.empty())

{

int x = P.front();

int h\_min = INT\_MAX;

for (int y = 1; y <= n; ++y)

if (G[x][y] > F[x][y])

{

if (H[y] >= H[x]) h\_min = min(h\_min, H[y]);

else

{

push\_flow(x, y);

if (!in\_queue[y] && y != xs && y != xt) P.push\_back(y), in\_queue[y] = true;

}

}

if (E[x] > 0) H[x] = h\_min + 1;

else

{

P.pop\_front();

in\_queue[x] = false;

}

}

cout << E[xt] << "\n";

}

int main()

{

ios::sync\_with\_stdio(false); cin.tie(nullptr);

if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());

enter();

solve();

}

## **QTREE (HLD).cpp**

#include <bits/stdc++.h>

using namespace std;

#define llong long long

#define long llong

#define ii pair<int,int>

const int n\_max = 10010;

struct edge { int x, y, c; } E[n\_max];

list<ii> G[n\_max];

int M[n\_max], H[n\_max], I[n\_max], IE[n\_max], W[n\_max], top\_node[n\_max], heavy\_child[n\_max], T[n\_max \* 4], P[n\_max][16];

int n, m, n\_test;

inline bool is\_heavy (int x) { return M[x] \* 2 > M[P[x][0]]; }

void dfs (int x,int h)

{

H[x] = h; M[x] = 1;

for (list<ii>::iterator i = G[x].begin(); i != G[x].end(); ++i)

if (i->first != P[x][0])

{

P[i->first][0] = x;

W[i->first] = i->second;

dfs(i->first, h + 1);

M[x] += M[i->first];

}

}

void load\_path(int x)

{

while (M[x] \* 2 > M[P[x][0]]) I[x] = ++m, x = P[x][0];

int p = x;

while ((x = heavy\_child[x]) > 0) IE[x] = m, top\_node[x] = p;

}

void upd\_edge (int u,int v,int x = 1,int l = 1,int r = m)

{

if (l == r) { T[x] = v; return; }

int k = x \* 2, mid = (l + r) / 2;

if (u <= mid)

upd\_edge(u, v, k, l, mid);

else

upd\_edge(u, v, k + 1, mid + 1, r);

T[x] = max(T[k], T[k + 1]);

}

int get\_max (int u,int v,int x = 1,int l = 1,int r = m)

{

if (v < l || r < u) return 0;

if (u <= l && r <= v) return T[x];

int k = x \* 2, mid = (l + r) / 2;

return max(get\_max(u, v, k, l, mid),

get\_max(u, v, k + 1, mid + 1, r));

}

int lca (int x,int y)

{

if (H[x] < H[y]) swap(x, y);

for (int i = 15; i >= 0; --i)

if (H[P[x][i]] >= H[y]) x = P[x][i];

if (x == y) return x;

for (int i = 15; i >= 0; --i)

if (P[x][i] != P[y][i]) x = P[x][i], y = P[y][i];

return P[x][0];

}

int get\_max\_edge (int x,int p) // p is x's ancestor

{

int s = 0;

while (x != p)

if (is\_heavy(x))

if (H[top\_node[x]] >= H[p]) // p is not in heavy path

{

s = max(s, get\_max(I[x], IE[x]));

x = top\_node[x];

} else // p is in heavy path

{

s = max(s, get\_max(I[x], I[p] - 1));

x = p;

}

else // advance normally

{

s = max(s, W[x]);

x = P[x][0];

}

return s;

}

namespace query

{

void change (int u,int v)

{

int x = (H[E[u].x] > H[E[u].y] ? E[u].x : E[u].y);

W[x] = v;

if (is\_heavy(x)) upd\_edge(I[x], v);

}

void query (int x,int y)

{

int p = lca(x, y);

cout << max(get\_max\_edge(x, p), get\_max\_edge(y, p)) << "\n";

}

}

void enter ()

{

cin >> n;

for (int i = 1; i < n; ++i)

{

cin >> E[i].x >> E[i].y >> E[i].c;

G[E[i].x].push\_back(ii (E[i].y, E[i].c));

G[E[i].y].push\_back(ii (E[i].x, E[i].c));

}

}

void init ()

{

dfs(1, 1);

for (int j = 1; j < 16; ++j)

for (int i = 1; i <= n; ++i)

P[i][j] = P[P[i][j - 1]][j - 1];

M[0] = 3 \* n;

for (int x = 1; x <= n; ++x)

if (is\_heavy(x)) heavy\_child[P[x][0]] = x;

for (int x = 1; x <= n; ++x)

if (is\_heavy(x) && heavy\_child[x] == 0) load\_path(x);

for (int x = 1; x <= n; ++x)

if (is\_heavy(x)) upd\_edge(I[x], W[x]);

}

void solve ()

{

string s;

int x, y;

while (true)

{

cin >> s;

if (s == "DONE") return;

cin >> x >> y;

if (s == "CHANGE") query::change(x, y);

if (s == "QUERY") query::query(x, y);

}

}

void clean\_up ()

{

fill\_n(heavy\_child + 1, n, 0);

fill\_n(top\_node + 1, n, 0);

fill\_n(IE + 1, n, 0);

fill\_n(I + 1, n, 0);

for (int i = 1; i <= n; ++i) G[i].clear();

m = 0;

}

int main ()

{

ios::sync\_with\_stdio(false); cin.tie(NULL);

if (ifstream("test.inp")) cin.rdbuf((new ifstream("test.inp"))->rdbuf());

cin >> n\_test;

while (n\_test--)

{

enter();

init();

solve();

clean\_up();

}

}

## **convex-hull-trick.java**

public class ConvexHullOptimization {

long[] A = new long[1000000];

long[] B = new long[1000000];

int len;

int ptr;

// a descends

public void addLine(long a, long b) {

// intersection of (A[len-2],B[len-2]) with (A[len-1],B[len-1]) must lie to the left of intersection of (A[len-1],B[len-1]) with (a,b)

while (len >= 2 && (B[len - 2] - B[len - 1]) \* (a - A[len - 1]) >= (B[len - 1] - b) \* (A[len - 1] - A[len - 2])) {

--len;

}

A[len] = a;

B[len] = b;

++len;

}

// x ascends

public long minValue(long x) {

ptr = Math.min(ptr, len - 1);

while (ptr + 1 < len && A[ptr + 1] \* x + B[ptr + 1] <= A[ptr] \* x + B[ptr]) {

++ptr;

}

return A[ptr] \* x + B[ptr];

}

// Usage example

public static void main(String[] args) {

ConvexHullOptimization h = new ConvexHullOptimization();

h.addLine(3, 0);

h.addLine(2, 1);

h.addLine(3, 2);

h.addLine(0, 6);

System.out.println(h.minValue(0));

System.out.println(h.minValue(1));

System.out.println(h.minValue(2));

System.out.println(h.minValue(3));

}

}

## **Edmond Blossom.java**

import java.util.\*;

public class MaxMatchingEdmonds {

static int lca(int[] match, int[] base, int[] p, int a, int b) {

boolean[] used = new boolean[match.length];

while (true) {

a = base[a];

used[a] = true;

if (match[a] == -1) break;

a = p[match[a]];

}

while (true) {

b = base[b];

if (used[b]) return b;

b = p[match[b]];

}

}

static void markPath(int[] match, int[] base, boolean[] blossom, int[] p, int v, int b, int children) {

for (; base[v] != b; v = p[match[v]]) {

blossom[base[v]] = blossom[base[match[v]]] = true;

p[v] = children;

children = match[v];

}

}

static int findPath(List<Integer>[] graph, int[] match, int[] p, int root) {

int n = graph.length;

boolean[] used = new boolean[n];

Arrays.fill(p, -1);

int[] base = new int[n];

for (int i = 0; i < n; ++i)

base[i] = i;

used[root] = true;

int qh = 0;

int qt = 0;

int[] q = new int[n];

q[qt++] = root;

while (qh < qt) {

int v = q[qh++];

for (int to : graph[v]) {

if (base[v] == base[to] || match[v] == to) continue;

if (to == root || match[to] != -1 && p[match[to]] != -1) {

int curbase = lca(match, base, p, v, to);

boolean[] blossom = new boolean[n];

markPath(match, base, blossom, p, v, curbase, to);

markPath(match, base, blossom, p, to, curbase, v);

for (int i = 0; i < n; ++i)

if (blossom[base[i]]) {

base[i] = curbase;

if (!used[i]) {

used[i] = true;

q[qt++] = i;

}

}

} else if (p[to] == -1) {

p[to] = v;

if (match[to] == -1)

return to;

to = match[to];

used[to] = true;

q[qt++] = to;

}

}

}

return -1;

}

public static int maxMatching(List<Integer>[] graph) {

int n = graph.length;

int[] match = new int[n];

Arrays.fill(match, -1);

int[] p = new int[n];

for (int i = 0; i < n; ++i) {

if (match[i] == -1) {

int v = findPath(graph, match, p, i);

while (v != -1) {

int pv = p[v];

int ppv = match[pv];

match[v] = pv;

match[pv] = v;

v = ppv;

}

}

}

int matches = 0;

for (int i = 0; i < n; ++i)

if (match[i] != -1)

++matches;

return matches / 2;

}

// Usage example

public static void main(String[] args) {

int n = 4;

List<Integer>[] g = new List[n];

for (int i = 0; i < n; i++) {

g[i] = new ArrayList<>();

}

g[0].add(1);

g[1].add(0);

g[1].add(2);

g[2].add(1);

g[2].add(3);

g[3].add(2);

g[0].add(3);

g[3].add(0);

System.out.println(2 == maxMatching(g));

}

}

## **edmondskarp [Viet].cpp**

#include <bits/stdc++.h>

#define N 1001

#define INF (int) 1e6 + 1

#define rep(i, a, b) for(int i = a; i <= b; i++)

#define per(i, b, a) for(int i = b; i >= a; i--)

#define bitcount(S) \_\_builtin\_popcount(S)

#define ll (long long)

#define db (double)

#define dbg(x) std::cout << x << std::endl

#define sz(x) x.size()

#define fi first

#define se second

using namespace std;

int n, m, s, t;

vector<int> g[N];

int c[N][N], d[N], f[N][N];

long long res;

bool findPath() {

queue<int> q;

rep(i, 1, n)

d[i] = 0;

d[s] = -1;

q.push(s);

while (!q.empty()) {

int u = q.front();

q.pop();

if (u == t)

return true;

for(auto v: g[u])

if (!d[v] && c[u][v] > f[u][v]) {

d[v] = u;

q.push(v);

}

}

return false;

}

void enlarge() {

int u, v, delta = INF;

v = t;

while (v != s) {

u = d[v];

delta = min(delta, c[u][v] - f[u][v]);

v = u;

}

v = t;

while (v != s) {

u = d[v];

f[u][v] += delta;

f[v][u] -= delta;

v = u;

}

res += delta;

}

int main() {

//freopen("input.txt", "r", stdin);

scanf("%d%d%d%d", &n, &m, &s, &t);

rep(i, 1, m) {

int u, v, w;

scanf("%d%d%d", &u, &v, &w);

g[u].push\_back(v);

g[v].push\_back(u);

c[u][v] = w;

}

while (findPath())

enlarge();

printf("%lld", res);

}

## **convexHull [Viet].cpp**

#include <iostream>

#include <stack>

#include <stdlib.h>

using namespace std;

struct Point

{

int x, y;

};

// A globle point needed for sorting points with reference

// to the first point Used in compare function of qsort()

Point p0;

// A utility function to find next to top in a stack

Point nextToTop(stack<Point> &S)

{

Point p = S.top();

S.pop();

Point res = S.top();

S.push(p);

return res;

}

// A utility function to swap two points

int swap(Point &p1, Point &p2)

{

Point temp = p1;

p1 = p2;

p2 = temp;

}

// A utility function to return square of distance

// between p1 and p2

int distSq(Point p1, Point p2)

{

return (p1.x - p2.x)\*(p1.x - p2.x) +

(p1.y - p2.y)\*(p1.y - p2.y);

}

// To find orientation of ordered triplet (p, q, r).

// The function returns following values

// 0 --> p, q and r are colinear

// 1 --> Clockwise

// 2 --> Counterclockwise

int orientation(Point p, Point q, Point r)

{

int val = (q.y - p.y) \* (r.x - q.x) -

(q.x - p.x) \* (r.y - q.y);

if (val == 0) return 0; // colinear

return (val > 0)? 1: 2; // clock or counterclock wise

}

// A function used by library function qsort() to sort an array of

// points with respect to the first point

int compare(const void \*vp1, const void \*vp2)

{

Point \*p1 = (Point \*)vp1;

Point \*p2 = (Point \*)vp2;

// Find orientation

int o = orientation(p0, \*p1, \*p2);

if (o == 0)

return (distSq(p0, \*p2) >= distSq(p0, \*p1))? -1 : 1;

return (o == 2)? -1: 1;

}

// Prints convex hull of a set of n points.

void convexHull(Point points[], int n)

{

// Find the bottommost point

int ymin = points[0].y, min = 0;

for (int i = 1; i < n; i++)

{

int y = points[i].y;

// Pick the bottom-most or chose the left

// most point in case of tie

if ((y < ymin) || (ymin == y &&

points[i].x < points[min].x))

ymin = points[i].y, min = i;

}

// Place the bottom-most point at first position

swap(points[0], points[min]);

// Sort n-1 points with respect to the first point.

// A point p1 comes before p2 in sorted ouput if p2

// has larger polar angle (in counterclockwise

// direction) than p1

p0 = points[0];

qsort(&points[1], n-1, sizeof(Point), compare);

// If two or more points make same angle with p0,

// Remove all but the one that is farthest from p0

// Remember that, in above sorting, our criteria was

// to keep the farthest point at the end when more than

// one points have same angle.

int m = 1; // Initialize size of modified array

for (int i=1; i<n; i++)

{

// Keep removing i while angle of i and i+1 is same

// with respect to p0

while (i < n-1 && orientation(p0, points[i],

points[i+1]) == 0)

i++;

points[m] = points[i];

m++; // Update size of modified array

}

// If modified array of points has less than 3 points,

// convex hull is not possible

if (m < 3) return;

// Create an empty stack and push first three points

// to it.

stack<Point> S;

S.push(points[0]);

S.push(points[1]);

S.push(points[2]);

// Process remaining n-3 points

for (int i = 3; i < m; i++)

{

// Keep removing top while the angle formed by

// points next-to-top, top, and points[i] makes

// a non-left turn

while (orientation(nextToTop(S), S.top(), points[i]) != 2)

S.pop();

S.push(points[i]);

}

// Now stack has the output points, print contents of stack

while (!S.empty())

{

Point p = S.top();

cout << "(" << p.x << ", " << p.y <<")" << endl;

S.pop();

}

}

// Driver program to test above functions

int main()

{

Point points[] = {{0, 3}, {1, 1}, {2, 2}, {4, 4},

{0, 0}, {1, 2}, {3, 1}, {3, 3}};

int n = sizeof(points)/sizeof(points[0]);

convexHull(points, n);

return 0;

}

**convexHull [Viet].cpp**

#include <bits/stdc++.h>

#define N 502

#define INF 1000001

#define rep(i, a, b) for(int i = a; i <= b; i++)

#define per(i, b, a) for(int i = b; i >= a; i--)

#define bitcount(S) \_\_builtin\_popcount(S)

#define ll (long long)

#define db (double)

#define dbg(x) std::cout << x << std::endl

#define sz(x) x.size()

#define fi first

#define se second

using namespace std;

int n, m, k, p[N], res, s, t, d[N];

string st, a[N];

struct edge {

int v, cap, f, cost, i;

edge(int \_v, int \_cap, int \_f, int \_cost, int \_i) {

v = \_v;cap = \_cap;f = \_f;cost = \_cost; i = \_i;

}

};

vector<edge> g[N];

pair<int, int> pre[N];

bool in[N];

void addEdge(int u, int v, int cap, int cost) {

edge a = edge(v, cap, 0, cost, g[v].size());

edge b = edge(u, 0, 0, -cost, g[u].size());

g[u].push\_back(a);

g[v].push\_back(b);

}

void buildGraph() {

rep(i, 0, n)

addEdge(i, i + 1, k, 0);

rep(i, 1, m)

rep(j, 0, n - a[i].length())

if (st.substr(j, a[i].length()) == a[i])

addEdge(j, j + a[i].length(), 1, -p[i]);

s = 0; t = n + 1;

}

bool fordBellman() {

queue<int> q;

rep(i, 1, n + 1) {

d[i] = INF;

in[i] = false;

}

d[s] = 0;

q.push(s);

in[s] = true;

while (!q.empty()) {

int u = q.front(); q.pop(); in[u] = false;

rep(i, 0, g[u].size() - 1) {

edge e = g[u][i];

if (e.cap > e.f && d[e.v] > d[u] + e.cost) {

d[e.v] = d[u] + e.cost;

pre[e.v] = make\_pair(u, i);

if (!in[e.v]) {

q.push(e.v);

in[e.v] = true;

}

}

}

}

return (d[t] < INF);

}

void enlarge() {

int v = t, delta = INF;

int u, i, j;

while (v != s) {

u = pre[v].fi;

i = pre[v].se;

delta = min(delta, g[u][i].cap - g[u][i].f);

v = u;

}

v = t;

while (v != s) {

u = pre[v].fi;

i = pre[v].se;

j = g[u][i].i;

g[u][i].f += delta;

g[v][j].f -= delta;

v = u;

}

res -= d[t] \* delta;

}

int main() {

//freopen("input.txt", "r", stdin);

cin >> n >> st >> m;

rep(i, 1, m)

cin >> a[i] >> p[i];

cin >> k;

buildGraph();

while (fordBellman())

enlarge();

cout << res;

}

**convexHull [Viet].cpp**

#include <bits/stdc++.h>

using namespace std;

struct Treap

{

#define S(t) (t ? t->Sum : 0)

#define W(t) (t ? t->Weight : 0)

struct Node

{

long Weight, Sum, Value, AssignValue, IncStart, IncRate;

int Priority;

Node \*l, \*r;

Node (long x)

{

Value = x;

Priority = (rand() << 15) | rand();

l = r = NULL;

IncRate = IncStart = 0;

AssignValue = -1;

Weight = 1;

Sum = 0;

}

} \*root;

void PushQuery (Node \*t)

{

Node \*l = t->l, \*r = t->r;

if (t->AssignValue > -1)

{

if (l)

{

l->IncRate = l->IncStart = 0;

l->Value = l->AssignValue = t->AssignValue;

l->Sum = l->Value \* l->Weight;

}

if (r)

{

r->IncRate = r->IncStart = 0;

r->Value = r->AssignValue = t->AssignValue;

r->Sum = r->Value \* r->Weight;

}

t->AssignValue = -1;

}

if (t->IncStart || t->IncRate)

{

if (l)

{

l->Sum += t->IncStart \* l->Weight;

l->Sum += t->IncRate \* ((l->Weight \* (l->Weight + 1)) >> 1);

l->Value += t->IncStart + t->IncRate \* (W(l->l) + 1);

l->IncStart += t->IncStart;

l->IncRate += t->IncRate;

}

if (r)

{

long k = t->IncStart + t->IncRate \* (W(l) + 1);

r->Sum += k \* r->Weight;

r->Sum += t->IncRate \* ((r->Weight \* (r->Weight + 1)) >> 1);

r->Value += k + t->IncRate \* (W(r->l) + 1);

r->IncStart += k;

r->IncRate += t->IncRate;

}

t->IncRate = t->IncStart = 0;

}

}

void PropertyUpdate (Node \*t)

{

if (t)

{

t->Weight = W(t->l) + W(t->r) + 1;

t->Sum = S(t->l) + S(t->r) + t->Value;

}

}

void Split (Node \*t, Node \*&l, Node \*&r, int p)

{

if (!t) l = r = NULL;

else

{

PushQuery(t);

if (p <= W(t->l))

{

r = t;

Split(t->l, l, r->l, p);

} else

{

l = t;

Split(t->r, l->r, r, p - W(t->l) - 1);

}

}

PropertyUpdate(t);

}

void Merge (Node \*&t, Node \*l, Node \*r)

{

if (l) PushQuery(l);

if (r) PushQuery(r);

if (!l) t = r;

else

if (!r) t = l;

else

if (l->Priority > r->Priority)

{

t = l;

Merge(t->r, l->r, r);

} else

{

t = r;

Merge(t->l, l, r->l);

}

PropertyUpdate(t);

}

void Assign (int l,int r,long value)

{

Node \*t1, \*t = root, \*t2;

Split(t, t, t2, r);

Split(t, t1, t, l - 1);

t->IncRate = t->IncStart = 0;

t->AssignValue = t->Value = value;

t->Sum = value \* t->Weight;

Merge(t, t1, t);

Merge(t, t, t2);

root = t;

}

void IncRange (int l,int r,long IncRate)

{

Node \*t1, \*t = root, \*t2;

Split(t, t, t2, r);

Split(t, t1, t, l - 1);

t->IncRate += IncRate;

t->Sum += IncRate \* ((t->Weight \* (t->Weight + 1)) >> 1);

t->Value += IncRate \* (W(t->l) + 1);

Merge(t, t1, t);

Merge(t, t, t2);

root = t;

}

void insert (int p,int v)

{

Node \*t1, \*t2;

Split(root, t1, t2, p - 1);

Merge(t1, t1, new Node(v));

Merge(root, t1, t2);

}

long GetSum (int l,int r)

{

Node \*t1, \*t = root, \*t2;

Split(t, t, t2, r);

Split(t, t1, t, l - 1);

long s = t->Sum;

Merge(t, t1, t);

Merge(t, t, t2);

root = t;

return s;

}

#undef S

#undef W

};

# **Stirling numbers of the second kind**

Number of ways to partition a set of n objects into k non-empty subsets:

{} = 1

{} = 1

{} =

**Bell numbers**

The sum over the values for k of the Stirling numbers of the second kind

=

Let = x(x-1)(x-2)…(x-n+1)

=

Recursion:

{(n+1)/k} = k{n/k} + {n/(k-1)}

For k>0: {0/0] = 1 and {n/0} = {0/n} = 0