Chapter 1 Problem 1:

1.

Constrained expression

$$ln[1]:= y1[x_] := g[x] + (y0 - g[x0]) + (x - x0) (yx0 - (D[g[x], x] /. x \rightarrow x0));$$

y1[x] // TraditionalForm

Out[2]//TraditionalForm=

$$(x - x0) (yx0 - g'(x0)) + g(x) - g(x0) + y0$$

Check the constraints

$$ln[3]:= y1[x0] - y0 == 0$$

 $(D[y1[x], x] /. x \rightarrow x0) - yx0 == 0$

Out[3]= True

Out[4]= True

2.

Constrained expression

Out[6]//TraditionalForm=

$$(x - xf)(yx0 - g'(x0)) + g(x) - g(xf) + yf$$

Check the constraints

$$ln[7]:= (D[y2[x], x] /. x \rightarrow x0) - yx0 == 0$$

y2[xf] - yf == 0

Out[7]= True

Out[8]= True

3.

Constrained expression

$$ln[9]:= y3[x_] := g[x] + (y0 - g[x0]) + (x - x0) (yxf - (D[g[x], x] /. x \rightarrow xf));$$

y3[x] // TraditionalForm

Out[10]//TraditionalForm=

$$(x - x0) (yxf - g'(xf)) + g(x) - g(x0) + y0$$

Check the constraints

$$ln[11]:= y3[x0] - y0 == 0$$

 $(D[y3[x], x] /. x \rightarrow xf) - yxf == 0$

Out[11]= True

Out[12]= True

4.

Constrained expression

y4[x] // TraditionalForm

Out[14]//TraditionalForm=

$$\frac{\left(x-x0\right)\left(x-xf\right)^{2}\left(yx0-g'(x0)\right)}{\left(x0-xf\right)^{2}}+\frac{\left(x-x0\right)^{2}\left(x-xf\right)\left(yxf-g'(xf)\right)}{\left(x0-xf\right)^{2}}+\\ \frac{\left(x-xf\right)^{2}\left(y0-g(x0)\right)\left(-2\,x+3\,x0-xf\right)}{\left(x0-xf\right)^{3}}+\frac{\left(x-x0\right)^{2}\left(yf-g(xf)\right)\left(2\,x+x0-3\,xf\right)}{\left(x0-xf\right)^{3}}+g(x)$$

Check the constraints

$$ln[15]:= y4[x0] - y0 == 0$$

$$(D[y4[x], x] /. x \rightarrow x0) - yx0 == 0$$

$$FullSimplify[y4[xf] - yf == 0]$$

$$FullSimplify[(D[y4[x], x] /. x \rightarrow xf) - yxf == 0]$$

Out[15]= True

Out[16]= True

Out[17]= True

Out[18]= True