Chapter 1 Problem 2:

1.

Constrained expression

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ln[1]:= y1[x_] := g[x] + (y0 - g[x0]) + (Sec[x0]Sin[x] - Tan[x0]) (yx0 - (D[g[x], x] /. x \rightarrow x0));

y1[x] // TraditionalForm
```

Out[2]//TraditionalForm=

$$(yx0 - g'(x0))(\sin(x)\sec(x0) - \tan(x0)) + g(x) - g(x0) + y0$$

Check the constraints

$$ln[3]:= y1[x0] - y0 == 0$$

 $(D[y1[x], x] /. x \rightarrow x0) - yx0 == 0$

Out[3]= True

Out[4]= True

2.

Constrained expression

Out[6]//TraditionalForm=

$$\sec(x0) (\sin(x) - \sin(xf)) (yx0 - g'(x0)) + g(x) - g(xf) + yf$$

Check the constraints

$$ln[7]:= (D[y2[x], x] /. x \rightarrow x0) - yx0 == 0$$

 $y2[xf] - yf == 0$

Out[7]= True

Out[8]= True

3.

Constrained expression

$$\log_{\mathbb{R}^n} y3[x_-] := g[x] + (y0 - g[x0]) + Sec[xf] (Sin[x] - Sin[x0]) (yxf - (D[g[x], x] /. x \rightarrow xf));$$

$$y3[x] \text{ // TraditionalForm}$$

Out[10]//TraditionalForm=

$$\sec(xf)(\sin(x) - \sin(x0))(yxf - g'(xf)) + g(x) - g(x0) + y0$$

Check the constraints

$$ln[11]:= y3[x0] - y0 == 0$$

(D[y3[x], x] /. x \rightarrow xf) - yxf == 0

Out[11]= True

Out[12]= True