

## Technical Aspects of Multimodal Systems Department of Informatics

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## Introduction to Robotics Assignment #1

**Due:** 23.04.2019, 23:59

Task 1.1 (8 points) Pyramid: A pyramid (square base  $AB = BC = CD = DA = 42 \, mm$ ; plumbline  $ME = 12 \, mm$ , with vertex E located at the top and point M located at the center of the base) is held by a robot so that its square base ABCD is located in the xy-plane of a cartesian world coordinate frame  $M_{xyz}$ , with point M at its origin, the edges AB and CD parallel to the x-axis and the edged BC and AD parallel to the y-axis. Attached to the pyramid is an object coordinate frame  $M_{uvw}$ , which initially coincides with  $M_{xyz}$ . Write down the general formula for each rotation.

- 1.1.1 (4 points): Determine the locations of the vertices A through E, after the following sequence of rotations has been performed by the robot:
  - 1. Rotation by  $\psi=50^\circ$  around  $M_w$
  - 2. Rotation by  $\phi = -35^{\circ}$  around  $M_u$
  - 3. Rotation by  $\theta=340^{\circ}$  around  $M_v$
- 1.1.2 (4 points): Same sequence of rotations, but using the rotation axes  $M_z$ ,  $M_x$  and  $M_y$  instead.

Task 1.2 (6 points) Homogeneous transformations: Given are three frames A, B and C as well as the following two homogeneous transformations:

$$^{A}T_{B} = \begin{bmatrix} 1/\sqrt{2} & 1/\sqrt{2} & 0 & 1 \\ -1/\sqrt{2} & 1/\sqrt{2} & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

and

$${}^{B}T_{C} = \begin{bmatrix} \sqrt{3}/2 & -1/2 & 0 & 2 \\ 1/2 & \sqrt{3}/2 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- **1.2.1 (3 points):** Can the interpretation of the transformation  ${}^AT_C$  be considered to be unambiguous? Explain your answer.
- 1.2.2 (3 points): Visualize the three coordinate systems with a tool of your choice.

## Task 1.3 (6 points) Euler angles:

- **1.3.1 (4 points):** Give four examples of Euler angle combinations  $(\phi, \theta, \psi)$  and interpret their geometric meaning using natural language.
- "This is a rotation around x by  $\phi$ " is not sufficient. Explain the properties of the transformation.
- **1.3.2 (2 points):** There are 12 possible sequences of rotations with Euler-angles around the axes (see slide 29). Explain why there are exactly 12!