

Lista de Exercícios: Derivadas e Integrais.

Calcule a derivada das funções:

$$1. f(x) = \frac{x^3}{1+x^2} \quad \text{resp. } f'(x) = \frac{3x^2(1+x^2) - x^3 \cdot 2x}{(1+x^2)^2}$$

$$2. f(x) = \frac{\ln x}{1+x} \quad \text{resp. } f'(x) = \frac{\left(\frac{1}{x}(1+x) - \ln x \cdot 1\right)}{(1+x)^2}$$

$$3. f(x) = \sec x + \operatorname{tg} x + \operatorname{sen} x \cos x$$

$$\text{Resp. } f'(x) = \sec x \operatorname{tg} x + \sec^2 x + \cos x \cos x - \operatorname{sen} x \operatorname{sen} x$$

$$4. f(x) = e^{x^2+x} \quad \Rightarrow \quad f'(x) = e^{x^2+x}(2x+1)$$

$$5. f(x) = \operatorname{sen}(3x^2 - 1) \quad \Rightarrow \quad f'(x) = \cos(3x^2 - 1)(6x)$$

$$6. f(x) = \ln(3x^3 - 2x) \quad \Rightarrow \quad f'(x) = \frac{9x^2 - 2}{3x^3 - 2x}$$

$$7. f(x) = \operatorname{tg}(4x + 3) \quad \Rightarrow \quad f'(x) = 4 \sec^2(4x + 3)$$

$$8. f(x) = (x^3 - 3x^2)^5 \quad \Rightarrow \quad f'(x) = 5(x^3 - 3x^2)^4(3x^2 - 6x)$$