

Homework 1 Writeup

Instructions

- Describe any interesting decisions you made to write your algorithm.
- Show and discuss the results of your algorithm.
- Feel free to include code snippets, images, and equations.
- There is no page limit.

In the beginning...

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$$a = b + c \tag{1}$$

Interesting Implementation Detail

```
1 for k = 1:numView
2     [~, ~, V] = svd(L(:, :, k));
3     h = V(:, 9);
4     h = h / h(9);
5     homography(:, :, k) = reshape(h, [3, 3])';
6 end
```

In homography calculation part, I calculate smallest right singular vector of L and normalize h33 to be 1, at each view

```
1 function [objective] = func_calibration(imagePoints,
2     worldPoints, x)
3 numView = size(imagePoints, 3);
4 hat_m = zeros(size(imagePoints));
5
6 % ----- Your code here (9) -----
7
```

```

8 K = [1, 0, 0
9       0, 1, 0
10      0, 0, 1];
11
12 K(1,1) = x(1);
13 K(1,2) = x(2);
14 K(1,3) = x(3);
15 K(2,2) = x(4);
16 K(2,3) = x(5);
17
18 for view = 1:numView
19     rvec = x(6*view+3:6*view+5);
20     tvec = x(6*view:6*view+2);
21     R = rotationVectorToMatrix(rvec);
22     R = R';
23     P = K * [R(:,1), R(:,2), reshape(tvec,[3,1])];
24     points = worldPoints;
25     points = [points, ones(size(imagePoints,1), 1)];
26     hat = P * points';
27     hat(1,:) = hat(1,:) ./ hat(3,:);
28     hat(2,:) = hat(2,:) ./ hat(3,:);
29     hat_m(:,:,view) = hat(1:2,:);
30 end
31
32 objective = imagePoints - hat_m;

```

In optimizing function used to MLE, first, I reconstruct K and Projection matrix from x. Then I add ones vector to worldPoints matrix, because of making homogenous coord. And I calculate $q(\hat{h})_{ij}$.

```

1 cost_vol = zeros(m, n, max_disparity);
2
3 pad_right = padarray(rightImageGray, [0 max_disparity], '
    replicate', 'pre');
4
5 block_pad = round(w/2) - 1;
6
7 pad_left = padarray(leftImageGray, [block_pad block_pad],
    'replicate', 'both');
8 padded_right = padarray(pad_right, [block_pad block_pad],
    'replicate', 'both');
9
10
11 filter = zeros(w);
12 filter(1:w, 1:w) = 1 / (w^2);
13
14 avg_right = imfilter(pad_right, filter, 'replicate');

```

```

15 avg_left = imfilter(leftImageGray, filter, 'replicate');
16
17 for i=1:m
18     for j=1:n
19         for d = 1:max_disparity
20             j2 = j -d + max_disparity;
21             avg_l = avg_left(i, j);
22             avg_r = avg_right(i, j2);
23             A = pad_left(i:i+w-1, j:j+w-1);
24             a = A(:) - avg_l;
25             B = padded_right(i:i+w-1, j2:j2+w-1);
26             b = B(:) - avg_r;
27             cost_vol(i, j, d) = -dot(a, b) / (norm(a) * norm
                (b));
28         end
29     end
30 end

```

In cost volume with a cost function and cost aggregation part, first, because of boundary I do padding image, then I used average filter to calculate average of all [window size * window size] subarray first. These average values are used when get NCC score. NCC score's range is [-1, 1]. When NCC score is 1, I can say this is matched. So I multiple -1 to NCC score for change min score mean matching

```

1 cost_vol2 = zeros(m, n, max_disparity);
2 parent = zeros(m, n, max_disparity);
3 min_dis = 10;
4 dis = min_dis:max_disparity;
5 dis_size = max_disparity - min_dis + 1;
6
7 rob = @(x) x.^2 ./ (1 + x.^2);
8 cost_vol2(:, n, :) = cost_vol(:, n, :);
9 for i=1:m
10     for j=n-1:-1:1
11         for d = min_dis:max_disparity
12             r = rob(d - dis);
13             cost = reshape(cost_vol2(i, j + 1, min_dis:
                max_disparity), [dis_size, 1]) ...
                + reshape(r, [dis_size, 1]);
14             [value, idx] = min(cost);
15             cost_vol2(i, j, d) = cost_vol(i, j, d) + value;
16             parent(i, j, d) = idx + min_dis - 1;
17         end
18     end
19 end
20 end
21 [~, idx] = min(cost_vol2(:, 1, min_dis:max_disparity), [], 3)
    ;

```

```

22 for i=1:m
23     disparityMap(i,1) = idx(i) + min_dis - 1;
24     idx_next = parent(i,1,idx(i) + min_dis - 1);
25     for j=2:n
26         disparityMap(i,j) = idx_next;
27         idx_next = parent(i,j,idx_next);
28     end
29 end

```

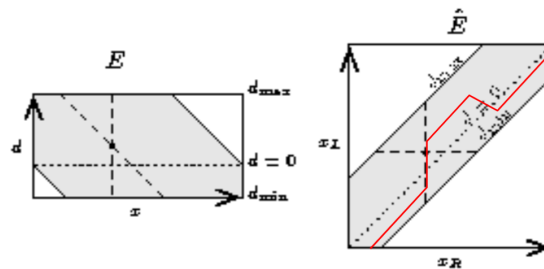
In constructing Disparity map part, I use Energy minimization and Dynamic Programming algorithm learned in class, and described below. First triplication for loop is the process of updating the entire cost volume using DP algorithm that considers the disparity of the neighboring pixels, and second double for loop is the process of backtracking which disparity should be given to each pixel.

Dynamic programming

- 1-D cost function

$$E_{\text{data}}(\mathbf{d}) = \sum_{x,y} \rho_P(d_{x+1,y} - d_{x,y}) + \sum_{x,y} E_0(x,y;d)$$

$$\tilde{E}(x,y,d) = E_0(x,y;d) + \min_{d'} (\tilde{E}(x-1,y,d') + \rho_P(d_{x,y} - d'_{x-1,y}))$$



Lect1

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Figure 1: Energy minimization + DP algorithm

A Result

```
>> main
Starting parallel pool (parpool) using the 'local' profile ...
Connected to the parallel pool (number of workers: 4).
```

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Evaluation [01]

Original y coordinate mean difference: 11.9712

Rectified y coordinate mean difference: 0.0559

Evaluation [02]

Original y coordinate mean difference: 14.7440

Rectified y coordinate mean difference: 0.0278

Start depth estimation [scene1]

Depth mean difference: 375.29

Start depth estimation [scene2]

Depth mean difference: 1425.72

IdleTimeout has been reached.

Parallel pool using the 'local' profile is shutting down.

Figure 2: Output result of entire code

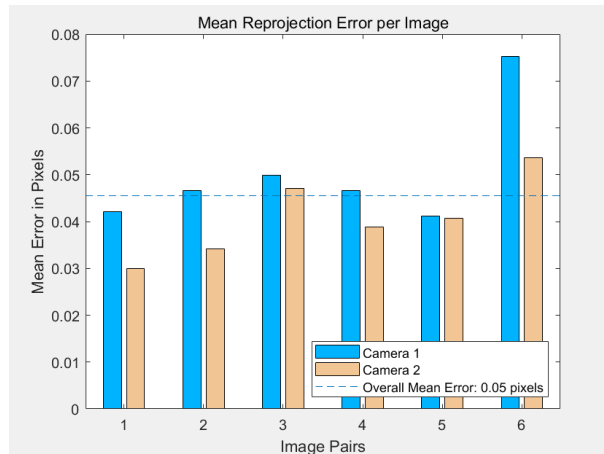


Figure 3: Reprojection error of camera parameters

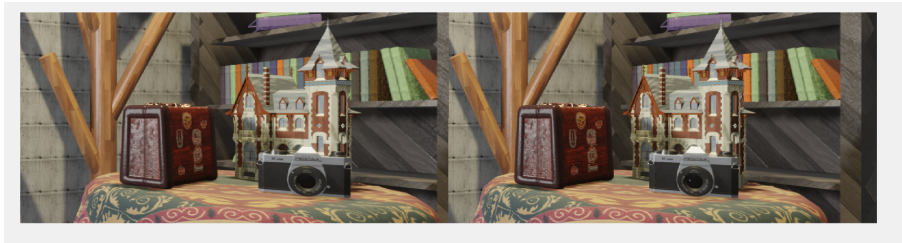


Figure 4: Reprojection result of scene1



Figure 5: Reprojection result of scene2

Reprojection error is 0.0x pixel units, so it can be said it I got very good result. I guess that some error can be caused by inaccuracy of input value and svd function.

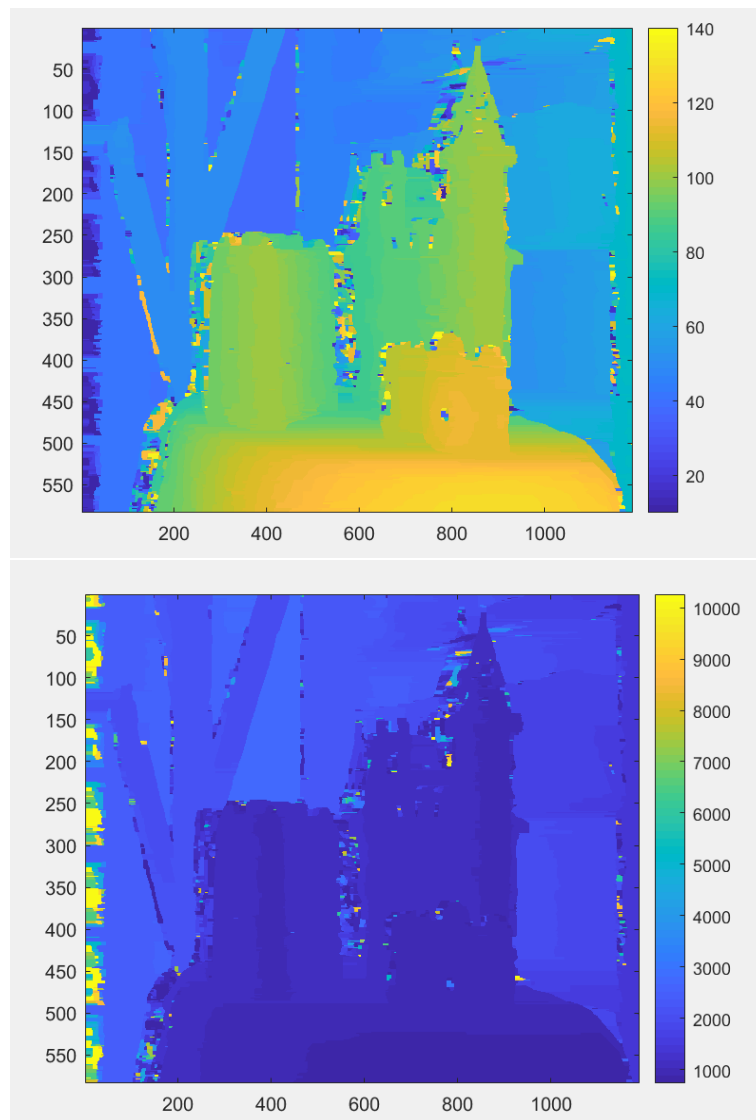


Figure 6: up : disparity image of scene1, down : depth image of scene1

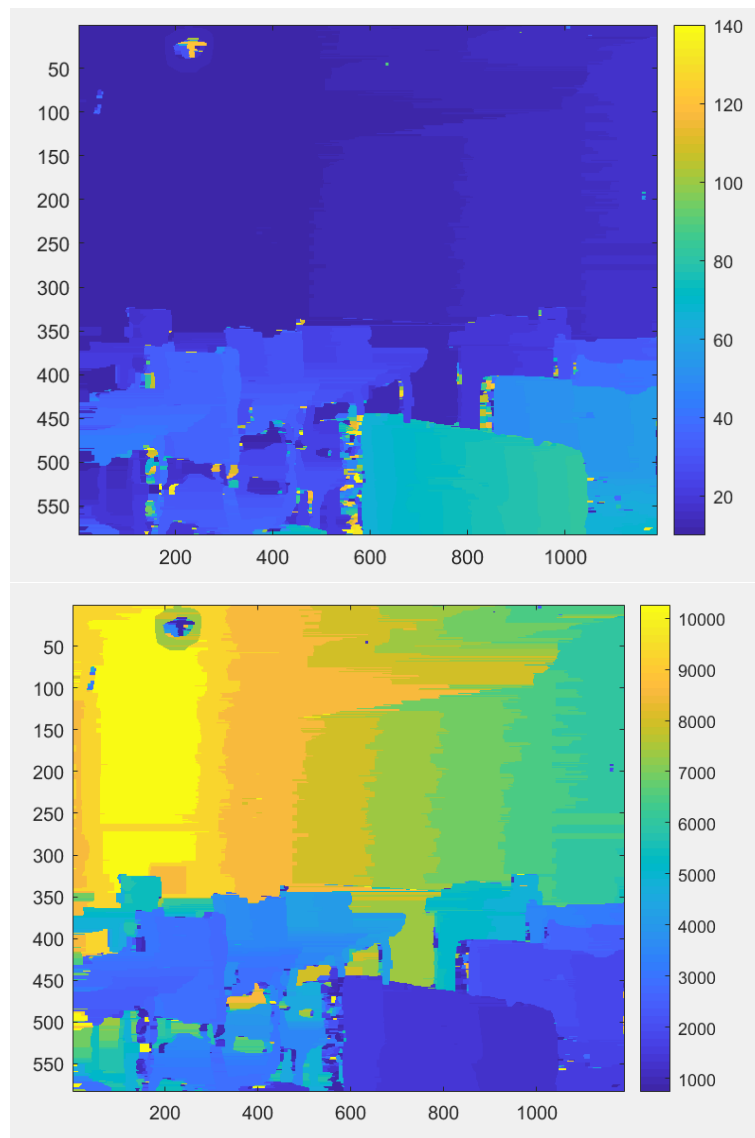


Figure 7: up : disparity image of scene2, down : depth image of scene2

I think error of disparity and depth can be caused by lack of parameter tuning and boundary condition. In addition, when low disparity case, small error of disparity cause large error of depth , so there was a high error on the part of the blackboard with relatively low disparity.