

Bucket Sort When You Know The Distribution.

David Ponnarovsky

January 20, 2023

Abstract

We propose a new simple construction based on Tanner Codes, which yields a good LDPC code with testability query complexity of $\Theta(n^{1-\varepsilon})$ for any $\varepsilon > 0$.

The problem. Let $f : [0, 1] \rightarrow [0, 1]$ a fixed distribution function. Write an algorithm that sort n draws $x_1 \dots x_n$ at linear expectation time.

Solution. We will define a partition of the input into a seira of n buckets $\mathcal{B} = \{B_k = [t_k, t_{k+1}] : k \in [n]\}$ such that $\Pr[x \in B_i] = \frac{1}{n}$ for any bucket.

$$\begin{aligned} \mathbf{E}[B_i^2] &= \mathbf{E}\left[\left(\sum_j X_{ij}\right)^2\right] = \mathbf{E}\left[\sum_{j,j'} X_{ij} X_{ij'}\right] \\ &= \sum_{j,j'} \mathbf{E}[X_{ij}] \mathbf{E}[X_{ij'}] = \sum_{j \neq j'} \mathbf{E}[X_{ij}] \mathbf{E}[X_{ij'}] + \sum_j \mathbf{E}[X_{ij}] = \end{aligned}$$