## Recursion Code.

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## Abstract

None

## 1 Construction.

**Definition 1.** Let  $\Delta$  be an integer greater than 2 and consider an alogrithm  $\mathcal{A}$  that for any n that is power of 3 construct a  $\Delta$ -regular graph over n vertices. Now, let G be  $\Delta$ -regular graph over n vertices generated by  $\mathcal{A}$ . Define the **third graph obtained by** G, labeled by  $G^{\sim}$  to be the graph which  $\mathcal{A}$  returns over  $\frac{1}{3}n$  such that any of the edges could be associate by puncturing a  $\frac{2}{3}$  fraction of the edges of each vertex.

The Code. Let  $C\left(\frac{1}{2}\Delta n\right)$  be the code defiend by the joining the parity check matrix of a Tanner code over  $\Delta$ -regular graph and