## Bucket Sort When You Know The Distribution.

## David Ponarovsky

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## Abstract

We propose a new simple construction based on Tanner Codes, which yields a good LDPC code with testability query complexity of  $\Theta\left(n^{1-\varepsilon}\right)$  for any  $\varepsilon>0$ .

**The problem.** Let  $f:[0,1] \to [0,1]$  a fixed distribution function. Write an algorithm that sort n draws  $x_1...x_n$  at linear expectation time.

**Solution.** We will define a partition of the input into a seira of n buckets  $\mathcal{B} = \{B_k = [t_k, t_{k+1}] : k \in [n]\}$  such that  $\mathbf{Pr}[x \in B_i] = \frac{1}{n}$  for any bucket.

$$\mathbf{E}\left[B_{i}^{2}\right] = \mathbf{E}\left[\left(\sum_{j}X_{ij}\right)^{2}\right] = \mathbf{E}\left[\sum_{j,j'}X_{ij}X_{ij'}\right]$$

$$= \sum_{\{j,j'\}\mathbf{E}\left[X_{ij}\right]\mathbf{E}\left[X_{ij'}\right] = \sum_{\{j\neq j'\}\mathbf{E}\left[X_{ij}\right]\mathbf{E}\left[X_{ij'}\right] + \sum_{j}\mathbf{E}\left[X_{ij}\right] = \left(\frac{n}{2}\right) + 1 = O\left(1\right)$$