## Problem

## October 5, 2023

## 1 Problem.

Let  $G = (L, R_0 \cup R_1, E)$  be bipartite graph. We think about the  $R_i$  vertices as the vertics that should applay 'logical-gate'  $X_i$  and a 'fake-gate'  $X_{\bar{i}}$ . Now let L' be additional vertices set at size  $\Theta(|L|)$ .

Claim 1.1. There is a way to connect  $R_0, R_1$  to L' such that:

- 1. Any vertex of R is connected by exactly single edge to L'.
- 2. (Strong.) The obtained graph is expnder. (Weak.) The expnasion of the new graph is not far way form the expnasion of the original graph.
- 3. (Computinal.) The reduction takes polynomial time.