Memory.

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0.1 Definitions.

0.2 Idea.

Given -
$$\rho$$
 \longrightarrow Decoding \longrightarrow p -depololraized \downarrow \downarrow \downarrow E_1 E_2 E_3

 $\mathbf{Pr}\left[S\subset E_2\right] \leq \mathbf{Pr}\left[\text{any bit }v\in S_{c_1} \text{ sees majority of unstatisfied stabilizers }\right] \leq q^{\Delta|S|_{c_1}}$

$$\mathbf{Pr}[S \subset E_{3}] = \sum_{S' \subset S} \mathbf{Pr}[S' \subset E_{2} \cap S/S' \in E_{3}/E_{2}]$$

$$\leq \sum_{S' \subset S} q^{\Delta |S'_{c_{1}}|} p^{|S/S'_{c_{1}}|} \leq \sum_{S' \subset S} q^{\Delta |S'_{c_{1}}|} p^{|S_{c_{1}}| - |S'_{c_{1}}|}$$

$$\leq (q^{\Delta} + p)^{|S_{c_{1}}|} \leq \begin{cases} (q^{\Delta} + p)^{\frac{1}{4}|S|} & \text{if } |S_{c_{1}}| \geq \frac{1}{4}|S| \\ \star & \text{else} \end{cases}$$