# $\mathbf{QNC}_1 \subset \mathbf{noisy}\mathbf{-BQP}$

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#### 1 Notations.

 $C_g$  - good qLDPC,  $C_{ft}$  - concatenation code (ft stands for fault tolerance). For a code  $C_y$  we use  $\Phi_y$ ,  $E_y$ ,  $D_y$  to denote the maps circuits into the circuits compute in the code space, the encoder, and the decoder. We use  $\Phi_U$  to denote the 'Bell'-state storing the gate U.

#### 2 The Noise Model

## 3 Fault Tolerance (With Resets gates) at Linear Depth.

**Claim 3.1.** There is  $p_{th} \in (0,1)$  such that if  $p < p_{th}$  then any quantum circuit C with depth D and width W can be computed by p-noisy, resets allowed, circuit C', with a depth at most  $\max \{D, \log(WD)\}$ .

### 3.1 Initializing Magic for Teleportation gates and encodes ancillaries.

The Protocol:

- 1. Initializing zeros. Divide the qubits into |B|-size blocks. Encodes each block in  $C_g$  via  $D_{ft}\Phi_{ft}[E_g]|0^{|B|}\rangle$ .
- 2. Initializing Magic for Teleportation gates encoded in  $C_g$  via  $D_{ft}\Phi_{ft}[E_g]|\Phi_U\rangle$  for each gate U in the original circit .
- 3. Each gate is replaced by gate teleportation.

4.

**Claim 3.2.** The gate  $D_{ft}\Phi_{ft}[E_g]$  initializes states encoded in  $C_g$  subject to p-noise channel.