

<p>Quantum Information Theory - 67749</p> <p>Exercise 2, May 18, 2025</p>

1 Submission Guidelines.

- Due date - May 29, 2025.
- Make sure your submission is clear. Unreadable assignments will get zero score.
- Using any Generative AI tool is forbidden but not enforced. Yet, please keep in mind that we might call you for an interview about your assignment.

2 AEP.

1. Reformulate the classical AEP using the density matrices notation.

3 Fidelity.

1. When ρ and σ commute.
2. Between the mixed state and any pure state.
3. Use the construction presented in the proof of Uhlman's to calculate the fidelity between: $p|0\rangle\langle 0| + (1-p)|+\rangle\langle +|$ and $(1-p)|0\rangle\langle 0| + p|+\rangle\langle +|$.

4 Entropy.

Compute the entropy of the following density matrices.

1. The super position over linear subspace. (purestate).
2. The uniform distribution over linear subspace.

5 Coding Theorem.

Let ρ be the density matrix: $p|\beta_{00}\rangle\langle\beta_{00}| + \frac{1}{3}(1-p)\sum_{i\neq 00}|\beta_{ij}\rangle\langle\beta_{ij}|$.

6 Quantum Teleportation.

Give a quantum circuit that compute the gate $\begin{bmatrix} 1 & 0 \\ 0 & e^{i\frac{\pi}{8}} \end{bmatrix}$ up to global phase using only pauli, clifford, and measurements.