# Final Recitation – Information Theory, Application.

David Ponarovsky

June 19, 2025

### Introduction

- Brief overview of the topic
- ► Importance and relevance
- Objectives of the presentation

# **Key Points**

- ▶ Main point 1
- ► Main point 2
- ► Main point 3

#### Claim

Let Y be a bit given by moving X trough BSC(p). Then:

$$1 - H(Y) \le (1 - p^2) (1 - H(X))$$

#### Claim

Let  $Y = (Y_1, Y_2, ..., Y_m)$  be a bit given by moving each of  $X_i \in X = (X_1, X_2, ..., X_m)$  trough BSC(p). Then:

$$m - H(Y) \le (1 - p^2) (m - H(X))$$

$$m - H(Y_1, Y_2, ..., Y_m) = m - \sum_{i} H(Y_i | Y_1, Y_2, ..., Y_{i-1})$$

$$\leq m - \sum_{i} H(Y_i | X_1, X_2, ..., X_{i-1})$$

$$\leq \sum_{i} 1 - H(Y_i | X_1, X_2, ..., X_{i-1})$$

$$\leq \sum_{i} (1 - p^2) (1 - H(X_i | X_1, X_2, ..., X_{i-1}))$$

$$\leq (1 - p^2) \sum_{i} (1 - H(X_i | X_1, X_2, ..., X_{i-1})) = (1 - e^2)$$