Polytopes.

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1 Basics.

Definition 1 (Convex Polygon). P will be said a convex polygon if for every $x, y \in P$ we have that any point z that lays on the line between x and y belongs to P.

1.1 Different Constructions.

Consider two different polytopes $P, Q \subset \mathbb{R}^d$ then we could construct a third polytop by:

- 1. Intersection, takeing the $P \cap Q \subset \mathbb{R}^d$
- 2. Minkeoski sum, $P+Q=\{p+q:p\in P,q\in Q\}\subset\mathbb{R}^d$
- 3. Product, $P \times Q = \{(p,q) : p \in P, q \in Q\} \subset \mathbb{R}^{2d}$