

COSMOLOGICAL FRAMEWORKS

FOR TESTING GRAVITY



TESSA BAKER

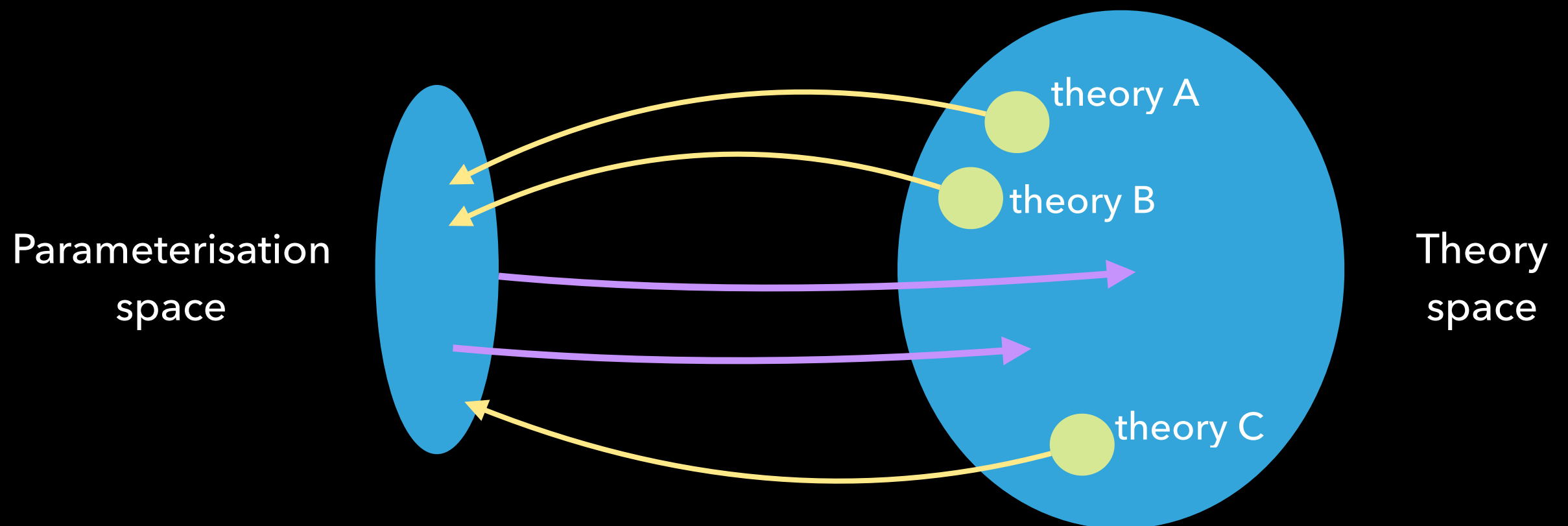
U. OXFORD & U. PENN.

OUTLINE

- ✦ A few remarks.
- ✦ Frameworks version 1: simple / data-friendly
- ✦ Frameworks version 2: EFT-inspired / theory-friendly
 - Formalism
 - Current constraints
- ✦ Forecast constraints on version 2.

PHILOSOPHY

- Cosmology driver: accelerated expansion.
- Dissatisfaction with current models on offer.
- Historical precedent set by PPN is encouraging.



CAVEAT EMPTOR

- **Not** directly analogous to PPN in implementation.
- **Not** a true EFT à la particle physics.
- Linear regime only — screening not manifest.
- Important to balance mathematical rigour with observational usefulness.
- Still under development.



SIMPLE TREATMENT



$$ds^2 = -dt^2 (1 + 2\Psi) + a^2(t) (1 - 2\Phi) dx^2$$

Poisson eq.: $2\nabla^2\Psi = 8\pi G \mu(a, k) \rho_M a^2 \Delta_M$

‘Slip’ ratio: $\gamma(a, k) = \frac{\Phi}{\Psi}$

Lensing potential: $\Phi + \Psi = \Sigma(a, k) (\Phi_{GR} + \Psi_{GR})$

SIMPLE TREATMENT



$$ds^2 = -dt^2 (1 + 2\Psi) + a^2(t) (1 - 2\Phi) dx^2$$

What's happening behind the scenes?

1) Use of the **quasi-static approximation (QSA)**:

$$|\dot{\Phi}| \ll |\nabla\Phi|, \quad |\ddot{\Phi}| \ll |\nabla^2\Phi| \quad + \text{ similar for } \Psi$$

⇒ OK well below cosmological horizon.

$$|\delta\dot{\phi}| \ll |\nabla\delta\phi|, \quad |\delta\ddot{\phi}| \ll |\nabla^2\delta\phi|$$

⇒ OK below the *sound horizon* of the new scalar.

SIMPLE TREATMENT



$$ds^2 = -dt^2 (1 + 2\Psi) + a^2(t) (1 - 2\Phi) dx^2$$

Checks of the QSA in specific theories:

<i>Galileons</i>	<i>1208.0600</i>	<i>f(R)</i>	<i>1411.6128</i>
<i>DGP</i>	<i>0906.0858</i>	<i>Symmetron</i>	<i>1312.6026</i>

2) The QSA reduces Poisson, slip and e.o.m. to **algebraic** relations between Φ , Ψ and $\delta\varphi$.

3) Combine equations to eliminate $\delta\varphi$.

SIMPLE TREATMENT



$$ds^2 = -dt^2 (1 + 2\Psi) + a^2(t) (1 - 2\Phi) dx^2$$

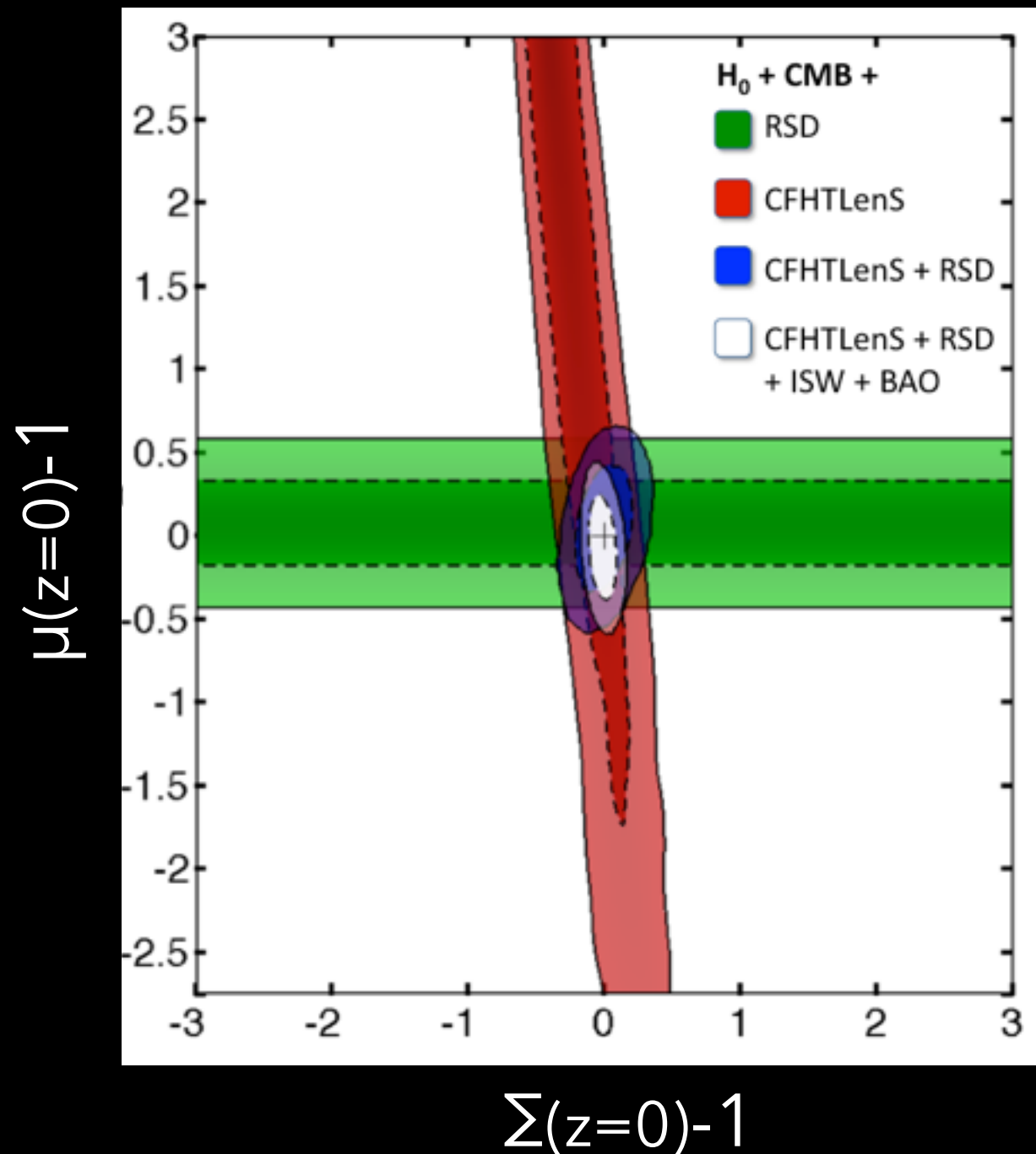
Poisson eq.: $2\nabla^2\Psi = 8\pi G \mu(a, k) \rho_M a^2 \Delta_M$

‘Slip’ ratio: $\gamma(a, k) = \frac{\Phi}{\Psi}$

Lensing potential: $\Phi + \Psi = \Sigma(a, k) (\Phi_{GR} + \Psi_{GR})$

\Rightarrow All properties of new scalar folded into μ and Σ (or Υ).

SIMPLE TREATMENT



Simpson et al. (2012)
Leonard et al. (2015)
Coming soon: KiDS.

Good: Simple to test.

Bad: All interesting behaviour folded away into μ, Σ .

(BRIEFLY: PPF)



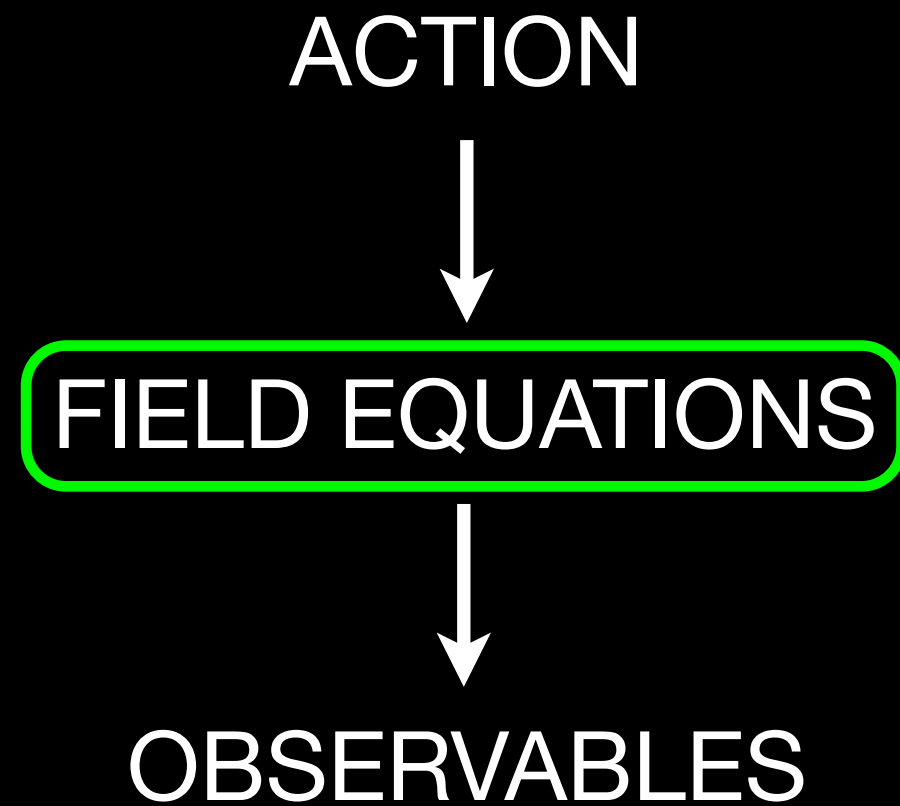
PPF = Post-Parameterised Friedmann formalism.

Tried to keep track of the new scalar d.o.f. more explicitly.

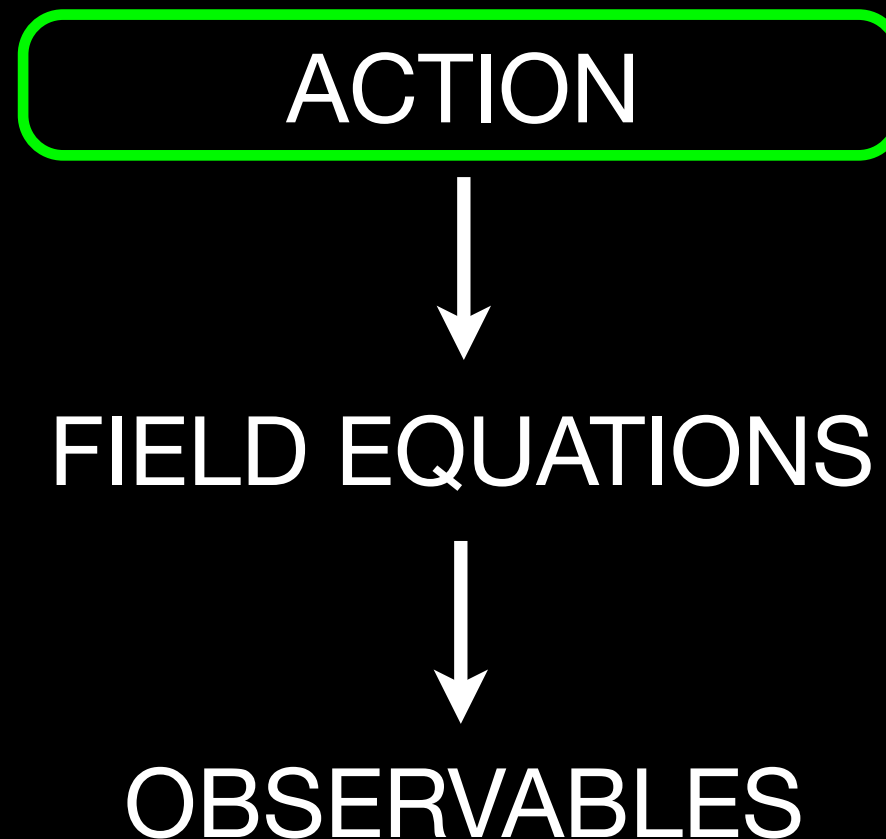
$$\begin{aligned} 2\nabla^2\Psi = & 8\pi G_N a^2 \rho_M \Delta_M \\ & + A(k, a)\Phi + B(k, a)\Psi + C(k, a)\dot{\Phi} \\ & + D(k, a)\delta\phi + E(k, a)\delta\dot{\phi} \end{aligned}$$

Too many free slots / 'parameters' to be constrainable.

WHAT'S GONE WRONG?



WHAT'S GONE WRONG?



We want to parameterise linear cosmological perturbation theory.
⇒ Need an action quadratic in perturbations.

Good: Reflects mathematical structure of MG theories better.

Bad: A step further away from observables.

EFT-INSPIRED APPROACHES



Specify the field content and symmetries.



Construct most general quadratic action from allowed building blocks.



Enforce symmetries \Rightarrow fix relationships between new terms.



Maximal set of 'parameters' to be constrained.

EFT-INSPIRED APPROACHES



Specify the field content and symmetries.

- Do we want to add new scalar, vector or tensor fields to gravity?

E.g.

Horndeski

bigravity

Einstein-Aether

- Isotropic + homogeneous cosmological background.

$\Rightarrow a(t), H(t)$

- Linear diffeomorphism invariance.

i.e. Reparameterisation invariance of manifold.

EFT-INSPIRED APPROACHES



Specify the field content and symmetries.



Construct most general quadratic action from allowed building blocks.

EFT-INSPIRED APPROACHES



Construct most general quadratic action from allowed building blocks.

$$\begin{aligned} \delta_2 S = & \int dt d^3x N \sqrt{-h} \left[L_{hR}(t) \delta h_j^i \delta R_i^j + L_{NK}(t) \delta N \delta K \right. \\ & + L_{h\partial N^i}(t) \delta h_{ij} \partial^i \delta \dot{N}^j + L_{\partial N \partial N}(t) \partial^i \delta N \partial_i \delta N + \dots \\ & + L_{\partial \phi \partial \phi}(t) \partial^i \delta \phi \partial_i \delta \phi + L_{\phi R}(t) \delta \phi \delta R + \dots \\ & \left. + \text{usual fluid matter sector} \right] \end{aligned}$$

EFT-INSPIRED APPROACHES



Specify the field content and symmetries.



Construct most general quadratic action from allowed building blocks.



Enforce symmetries \Rightarrow fix relationships between new terms.

EFT-INSPIRED APPROACHES



Enforce symmetries \Rightarrow fix relationships between new terms.

► i.e. the following must vanish:

$$\begin{aligned} & \left[(\dots) \delta N + (\dots) \partial_i \delta N^i + (\dots) \partial^i \partial^j (\delta h_{ij}) + (\dots) \delta \phi \right] \pi \\ & \quad + \\ & \left[(\dots) \delta N + (\dots) \partial_i \delta N^i + (\dots) \partial^i \partial^j (\delta h_{ij}) + (\dots) \delta \phi \right] \epsilon \\ & \quad + \text{(many terms not shown)} \end{aligned}$$

EFT-INSPIRED APPROACHES



Q: What's sitting inside those (...) ?

Ans: Linear combinations of the 'Taylor' coefficients, e.g.

$$4\dot{H}L_{KK\times} + \rho_M + P_M = 0$$

$$2L_{hh\times} - \dot{L}_{hK\times} - 3HL_{hK\times} = 0$$

$$L_{\dot{N}^i\dot{N}^j} = L_{K\dot{N}} = L_{\dot{N}\dot{N}} = 0$$

Complicated (but doable) elimination of variables.

⇒ Reduce action down to maximum set of 'true' free coeffs.

EFT-INSPIRED APPROACHES



Gauge invariance is **seriously** powerful.

Fields	# Naive coeffs.	# True free functions	Theory family
$g_{\mu\nu}$	32	1	GR
$g_{\mu\nu}, \phi$	72	5	Horndeski
$g_{\mu\nu}, A^\mu$	66	10	Vector-tensor
$g_{\mu\nu}, A^\mu, \lambda$	67	4	Einstein-Aether
$g_{\mu\nu}, q_{\mu\nu}$?	? (in progress)	Bigravity

1-SCALAR CASE (HORNDESKI)



$$\delta_2 S = \int d^3x dt a^3 \frac{M(t)^2}{2} \left[R^{(4D)} + \alpha_T(t) \delta_2 \left(\sqrt{h} R / a^3 \right) \right. \\ \left. + \alpha_K(t) H^2 \delta N^2 + 4\alpha_B(t) H \delta K \delta N \right]$$

$\alpha_T(t)$: speed of gravitational waves, $c_T^2 = 1 + \alpha_T$.

$\alpha_K(t)$: kinetic term of scalar field.

$\alpha_B(t)$: ‘braiding’ – mixing of scalar + metric kinetic terms.

$\alpha_M(t) = \frac{1}{H} \frac{d \ln M^2(t)}{dt}$: running of effective Planck mass.

1-SCALAR CASE (HORNDESKI)



$$\begin{aligned}
 S_G^{(2)} = \int d^4x a^3 M^2 \Bigg\{ & \frac{1}{2} H^2 (\alpha_K - 12\alpha_B - 6) \Phi^2 - 6H (1 + \alpha_B) \Phi \dot{\Psi} + 2(1 + \alpha_H) \Psi \partial^2 \Phi \\
 & - 3\dot{\Psi}^2 - (1 + \alpha_T) \Psi \partial^2 \Psi + 2a^2 H (1 + \alpha_B) \Phi \partial^2 \dot{E} - 2H (1 + \alpha_B) \Phi \partial^2 B + 2a^2 \Psi \partial^2 \dot{E} \\
 & - 2\dot{\Psi} \partial^2 B - 3 \left(\frac{\rho_m + P_m}{M^2} + 2\dot{H} \right) \dot{\Psi} \delta\chi + 2\alpha_H \dot{\Psi} \partial^2 \delta\chi + 6H\alpha_B \dot{\Psi} \delta\dot{\chi} + H^2 (6\alpha_B - \alpha_K) \Phi \delta\dot{\chi} \\
 & - 2H \left[\alpha_T - \alpha_H - \frac{d \ln M^2}{d \ln a} (\alpha_H + 1) - \frac{d\alpha_H}{d \ln a} \right] \Psi \partial^2 \delta\chi - 2H (\alpha_B - \alpha_H) \Phi \partial^2 \delta\chi \\
 & - 3H \left[\frac{(\rho_m + P_m)}{M^2} + 2\dot{H} (1 + \alpha_B) \right] \Phi \delta\chi - \left[\frac{(\rho_m + P_m)}{M^2} + 2\dot{H} \right] \delta\chi (\partial^2 B - a^2 \partial^2 \dot{E}) \\
 & + 2H\alpha_B \delta\dot{\chi} (\partial^2 B - a^2 \partial^2 \dot{E}) - \left[3 \left(\dot{H}^2 + H\ddot{H} + 3H^2 \dot{H} + H^2 \dot{H} \frac{d \ln M^2}{d \ln a} \right) \alpha_B + 3H\dot{H} \dot{\alpha}_B \right. \\
 & + \left. \frac{3}{2} \dot{H} \frac{(\rho_m + P_m)}{M^2} + 3\dot{H}^2 \right] \delta\chi^2 - \left[\left(\dot{H} + H^2 + H^2 \frac{d \ln M^2}{d \ln a} \right) (\alpha_B - \alpha_H) + H (\dot{\alpha}_B - \dot{\alpha}_H) \right. \\
 & + \left. H^2 \alpha_T + \dot{H} - H^2 \frac{d \ln M^2}{d \ln a} + \frac{1}{2} \frac{(\rho_m + P_m)}{M^2} \right] \delta\chi \partial^2 \delta\chi + \frac{1}{2} H^2 \alpha_K \delta\dot{\chi}^2 \\
 & \left. - P_m \left(\frac{3}{2} \Psi^2 - a^2 \Psi \partial^2 E - \frac{a^4}{2} \partial^2 E \partial^2 E \right) - \rho_m \left(\frac{1}{2} \Phi^2 + \frac{1}{2} B \partial^2 B + 3\Phi \Psi - a^2 \Phi \partial^2 E \right) \right\}, \tag{4.15}
 \end{aligned}$$

CONSTRAINTS:



- $\alpha_K(z)$ ('kineticity') drops out of e.o.m.s on small scales.
- $\alpha_T(z)$ (tensor speed) has little impact on scalar perturbations.

\Rightarrow Focus on $\alpha_B(z)$ and $\alpha_M(z)$.

- Need an ansatz for redshift dependence of the $\alpha_i(z)$.

Common choice:

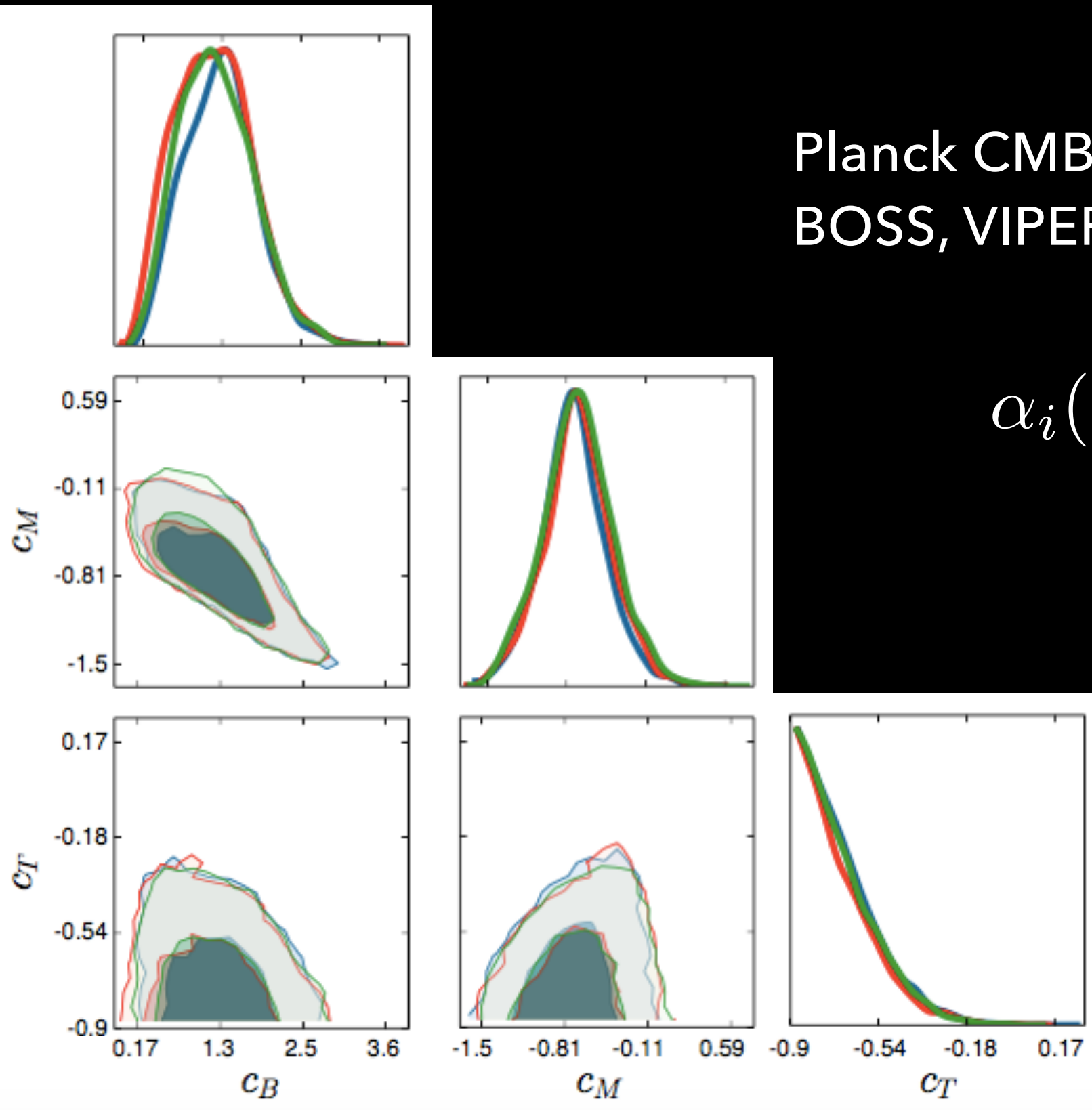
$$\alpha_i(z) = c_i \Omega_\Lambda(z)$$

CONSTRAINTS: CURRENT



Planck CMB data + galaxy surveys:
BOSS, VIPERS, WiggleZ.

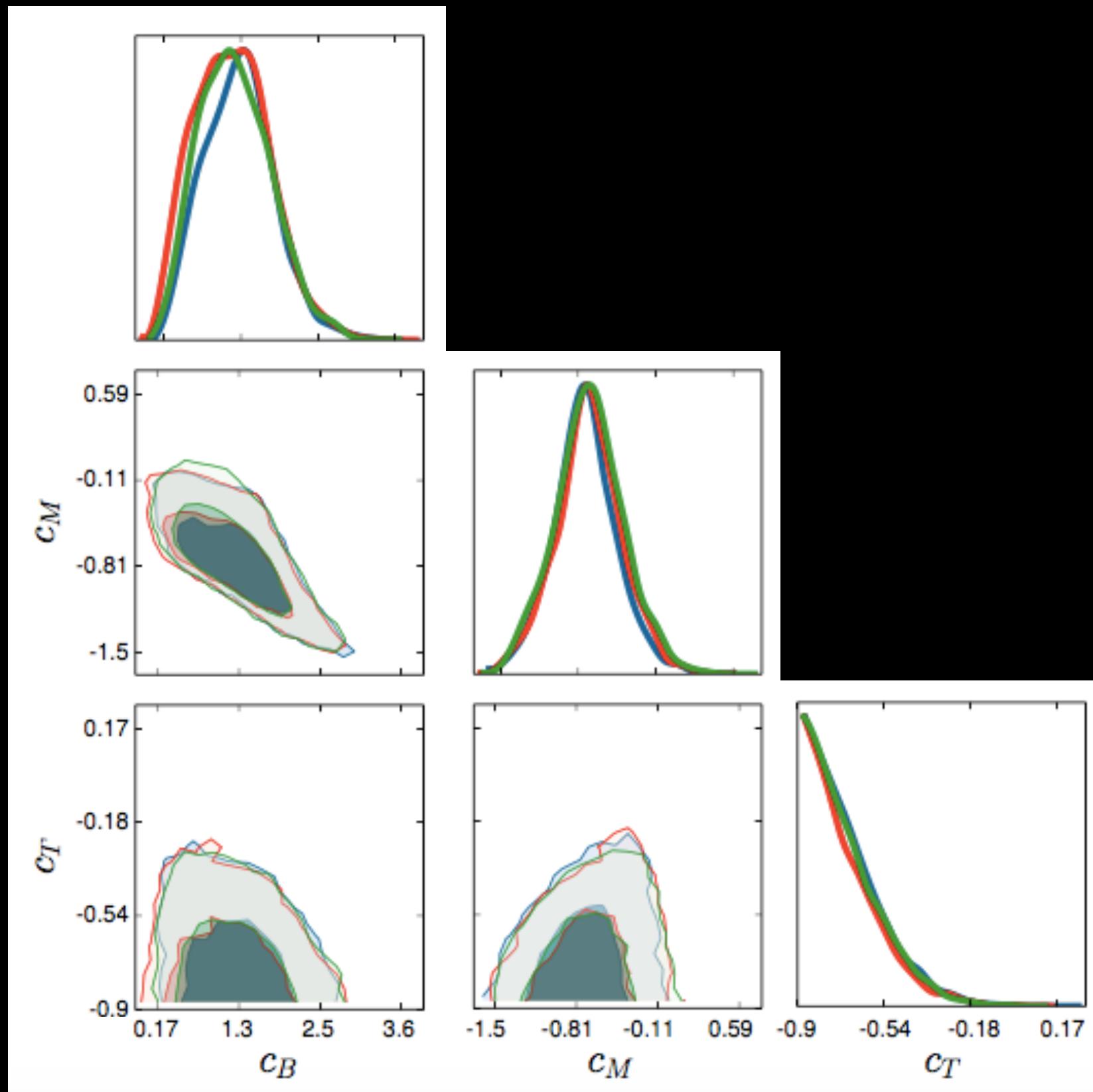
$$\alpha_i(z) = c_i \Omega_\Lambda(z)$$



— $c_K = 0$
— $c_K = 1$
— $c_K = 10$

Bellini et al., 2015.

CONSTRAINTS: CURRENT

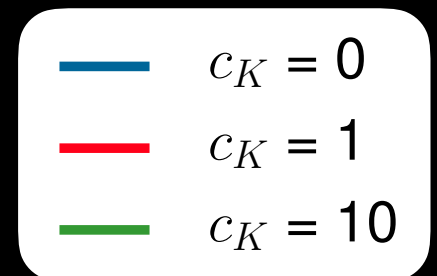


2σ constraints:

$$0.24 < c_B < 2.32$$

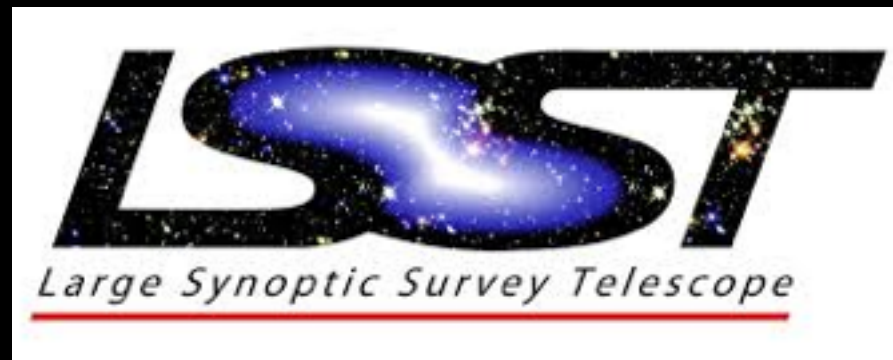
$$-1.36 < c_M < -0.13$$

$$-0.90 < c_T < -0.39$$



Bellini et al., 2015.

CONSTRAINTS:FUTURE

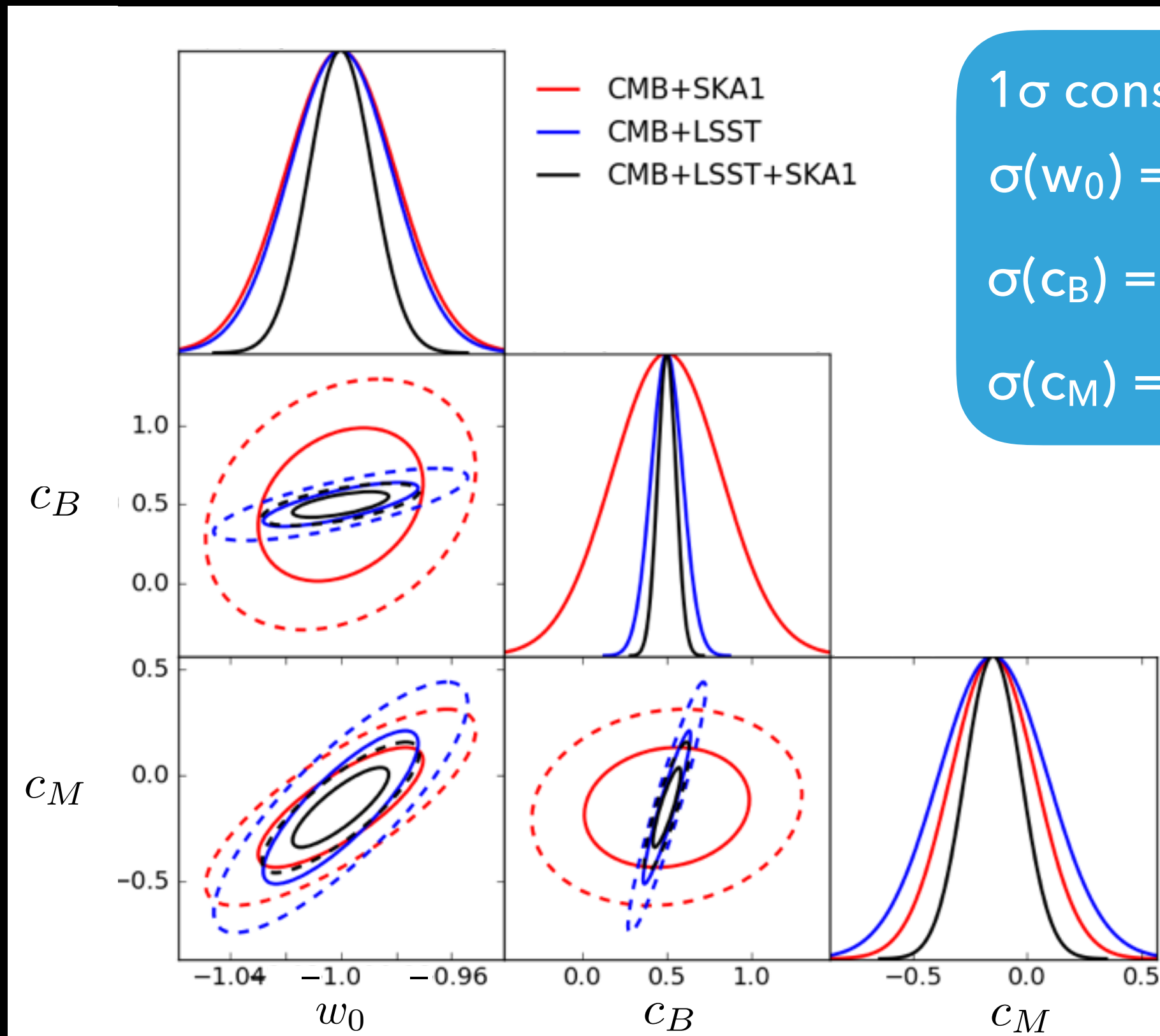


- ▶ ~ 20,000 deg² visited ~ 1000 times over 10 years.
- ▶ Focus areas:
 - weak+strong lensing
 - large-scale structure
 - galaxy clusters
 - supernovae
- ▶ Lensing + clustering power spectrum cross-correlations.



- ▶ Phase 1 2020.
- ▶ Survey types:
 - H1 intensity mapping (IM)
 - H1 galaxy survey
 - continuum survey
- ▶ Fine redshift resolution .
- ▶ Different systematics to optical surveys.

CONSTRAINTS:FUTURE



1 σ constraints:

$$\sigma(w_0) = 0.011$$

$$\sigma(c_B) = 0.054$$

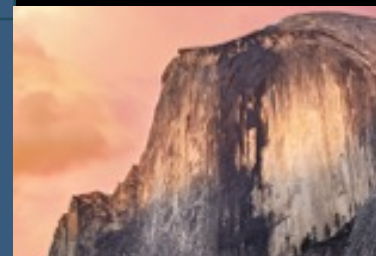
$$\sigma(c_M) = 0.124$$

Plots courtesy of
David Alonso.

CONCLUSIONS



Version 1: μ, Σ	Version 2: EFT
Simple	More theoretical baggage
Sub-horizon scales only (due to quasi-static approx.)	All linear scales , incl. near-horizon.
2 free functions (time, scale)	Depends on field content (5 for 1 scalar)



We have code!

xIST – Mathematica routines for **l**inear **S**calar **T**ensor theories.

CoPPer – **C**osmological **P**arameterised **P**erturbations.

Available from <https://github.com/noller/xIST>.

CONCLUSIONS

- ◆ Full formalism:

Lagos, TB, Ferreira & Noller — 1604.01396

- ◆ EFT of DE / Horndeski:

Gleyzes, Langlois, Mancarella & Vernizzi — 1509.02191
+ references therein.

- ◆ Connecting EFT & (μ, Σ) :

Pogosian & Silvestri — 1606.05339

- ◆ hi_class \Rightarrow Horndeski EFT in CLASS:

Zumalacárregui, Bellini, Sawicki & Lesgourges — 1605.06102

WHY THE 3+1 SPLIT?

- ▶ Makes the constraint structure manifest.
E.g. Lapse (N) and shift (N^i) are usually non-dynamical fields.
- ▶ Makes Lorentz violation and higher-derivative theories easier to write down.
- ▶ We have a preferred timelike vector in cosmology.
- ▶ Easier to compare to existing literature.