

## Q1 Big-O Justification

12 Points

**Indicate whether the following assertions are true or false, and give a justification.**

If you are justifying the positive direction, give choices of  $n_0$  and  $C$ . For big- $\Theta$ , make sure to justify both big- $O$  and big- $\Omega$ , or big- $O$  in both directions.

If you are justifying the negative direction, indicate which term(s) can't work because one is guaranteed to grow faster or slower than the other.

### Q1.1 $n + 5n^2 + 8n^4$ is $O(n^3)$

2 Points

☐ True

☒ False

Justification

$n^3$  is a slower growing function than  $8n^4$ . The correct statement would be  $n + 5n^2 + 8n^4$  is  $O(n^4)$ .

### Q1.2 $n! + n$ is $O(n * \log n)$

2 Points

☐ True

☒ False

Justification

$n * \log n$  is a slower growing function than  $n!$ . The correct statement would be  $n! + n$  is  $O(n!)$

**Q1.3**  $\log n + n \cdot \log n + \log(\log n)$  is  $\Omega(n)$ 

2 Points

☒ True☐ False

Justification

Suppose  $n_0 = 0$  and  $C = 1$

**Q1.4**  $n^2 + n/4 + 6$  is  $\Theta(n^2)$ 

2 Points

☒ True☐ False

Justification

big-O justification: suppose  $n_0 = 0$  and  $C = 1/10$

big- $\Omega$  justification: suppose  $n_0 = 0$  and  $C = 500$

**Q1.5**  $1/(n^{50}) + \log 32$  is  $\Omega(1)$ 

2 Points

☐ True☒ False

Justification

The constant function is a faster growing function than  $1/(n^{50})$ .

The correct statement would be  $1/(n^{50}) + \log 32$  is  $\Omega(1/n^{51})$

**Q1.6**  $1/(n^{50}) + \log 2$  is  $O(1)$

2 Points

☒ True☐ False

Justification

Suppose  $x_0 = 0$  and  $C = 1000000$

## Q2 List Analysis

16 Points

**Answer the following questions, and justify them with one or two sentences. Unless specified otherwise, all runtime is the worst-case runtime.**

*Format Instructions. Please read the following instructions carefully.*

For your runtime, do not write  $\Theta()$ , only what is inside of  $()$ .

Only give the most relevant terms. For example, if you arrived at the answer  $\Theta(4n + 2)$ , then this would simplify to  $\Theta(n)$ . Your answer would just be  $n$ .

For answers with exponential terms, you should format it using  $^$ . For example, if your answer is  $\Theta(n^2)$ , your answer would be  $n^2$ .

For answers that involve log, you should explicitly write “log” with parentheses. For example, if your answer is  $\Theta(\log(n))$ , your answer would be  $\log(n)$ . You don’t have to write the base of the log.

For answers with multiple terms, do not include spaces. For example, if your answer is  $\Theta(n*m)$ , your answer would be  $m*n$ . Additionally, order them alphabetically.

### Q2.1 Did you read the format instructions?

0 Points

☒ I have read and understood the format requirements

**Q2.2** Give a tight big-O bound for the best case running time of prepend in ArrayList

2 Points

Big O bound

1

Justification

The number of computations will always be the same. The best case is if there are no elements in the array and no need to `expandCapacity()`. The for loop runs a fixed number of times (constant).

**Q2.3** Give a tight big-O bound for the worst case running time of prepend in ArrayList

2 Points

Big O bound

n

Justification

The worst case would occur if it would be necessary to `expandCapacity()` while the prepend method called the insert method. `expandCapacity` runs a for loop for n number of times in order to copy every single element into a new array.

**Q2.4** Give a tight big-O bound for the best case running time of prepend in LinkedList

2 Points

Big O bound

1

## Justification

If the String `s` was the first node, then this would be the best case. A new node would be created and added to the front. This is a constant function.

**Q2.5** Give a tight big-O bound for the worst case running time of `prepend` in `LinkedListStringList`

2 Points

Big O bound

1

## Justification

Even if the linked list contained nodes before `newFront`, calling `prepend` would create a new `Node`, assign it to the front, and would point to the node that was previously in the front. This would only take one step (constant function).

**Q2.6** Give a tight big-O bound for the best case running time of `add` in `ArrayStringList`

2 Points

Big O bound

1

## Justification

The best case is if the array size does not have to be increased with `expandCapacity()`. In this case there are no for loops, and there would only be a fixed amount of steps which makes it a constant function.

**Q2.7** Give a tight big-O bound for the worst case running time of add in ArrayList

2 Points

Big O bound

$n$

Justification

The worst case is if there is a for loop to run that runs the method `expandCapacity()`. `expandCapacity` runs a for loop for  $n$  number of times in order to copy every single element into a new array.

**Q2.8** Give a tight big-O bound for the best case running time of add in LinkedList

2 Points

Big O bound

$n$

Justification

Since this method has a while loop, the method has to run  $n$  number of times to iterate through the entire list of size  $n$ .

**Q2.9** Give a tight big-O bound for the worst case running time of add in LinkedList

2 Points

Big O bound

$n$

Justification

Since this method has a while loop, the method has to run  $n$  number of times to iterate through the entire list of size  $n$ .

## Q3 Mystery Functions and Measuring

26 Points

Determine which mystery method A-F corresponds to the implementations above by measuring against provided (but hidden) implementation.

Determine the tightest big-O bound for each function, and justify it with a few sentences. Give only the most relevant term, so use, for example  $O(n)$ , not  $O(4n + 2)$ .

Describe how you measured your functions.

Submit 3 relevant graphs that display your measurements.

### Q3.1 Function Matching - Mystery A

1 Point

- ☐ f1
- ☒ f2
- ☐ f3
- ☐ f4
- ☐ f5
- ☐ f6

### Q3.2 Function Matching - Mystery B

1 Point

☒ f1☐ f2☐ f3☐ f4☐ f5☐ f6**Q3.3** Function Matching - Mystery C

1 Point

☐ f1☐ f2☐ f3☐ f4☒ f5☐ f6**Q3.4** Function Matching - Mystery D

1 Point

☐ f1☐ f2☐ f3☒ f4☐ f5☐ f6



**Q3.5** Function Matching - Mystery E

1 Point

- ☐ f1
- ☐ f2
- ☐ f3
- ☐ f4
- ☐ f5
- ☒ f6

**Q3.6** Function Matching - Mystery F

1 Point

- ☐ f1
- ☐ f2
- ☒ f3
- ☐ f4
- ☐ f5
- ☐ f6

**Q3.7** Big-O bound for f1

2 Points

Big O bound

n

Justification

As seen by the graph for the mystery function B, the function illustrated is linear. Therefore, the runtime is  $n$ .

**Q3.8** Big-O bound for f2

2 Points

Big O bound

 $n$ 

Justification

As seen by the graph for the mystery function A, the function illustrated is linear. Therefore, the runtime is  $n$ .

**Q3.9** Big-O bound for f3

2 Points

Big O bound

 $\log(n)$ 

Justification

As seen by the graph for the mystery function F, the function illustrated is logarithmic. Therefore, the runtime is  $\log(n)$ .

**Q3.10** Big-O bound for f4

2 Points

Big O bound

 $n^2$ 

Justification

As seen by the graph for the mystery function D, the function illustrated is a square function. Therefore, the runtime is  $n^2$ .

**Q3.11** Big-O bound for f5

2 Points

Big O bound

 $n^3$ 

Justification

As seen by the graph for the mystery function C, the function illustrated is a cube function. Therefore, the runtime is  $n^3$ .

**Q3.12** Big-O bound for f6

2 Points

Big O bound

 $2^n$ 

Justification

As seen by the graph for the mystery function E, the function illustrated is an exponential function. Therefore, the runtime is  $2^n$ .

**Q3.13** Description of measuring process

2 Points

The public class Measure had a method called measure which produced a list of measurements for a particular function. The arguments passed in were a String array of mystery function names, as well as a start and end number in order to run the mystery method. I first created a new list that would store the values of the measurements. Next, I looped through the passed in array if the length was greater than 1. After, I would iterate through the mystery function starting at the start value of n and ending at the end value of n (inclusive). I would also call the System.nanoTime() method at the start and end times. The result

of the end-start times would be recorded as a new Measurement and added to the list.

**Q3.14** Graphs

6 Points

▼ A and B.pdf

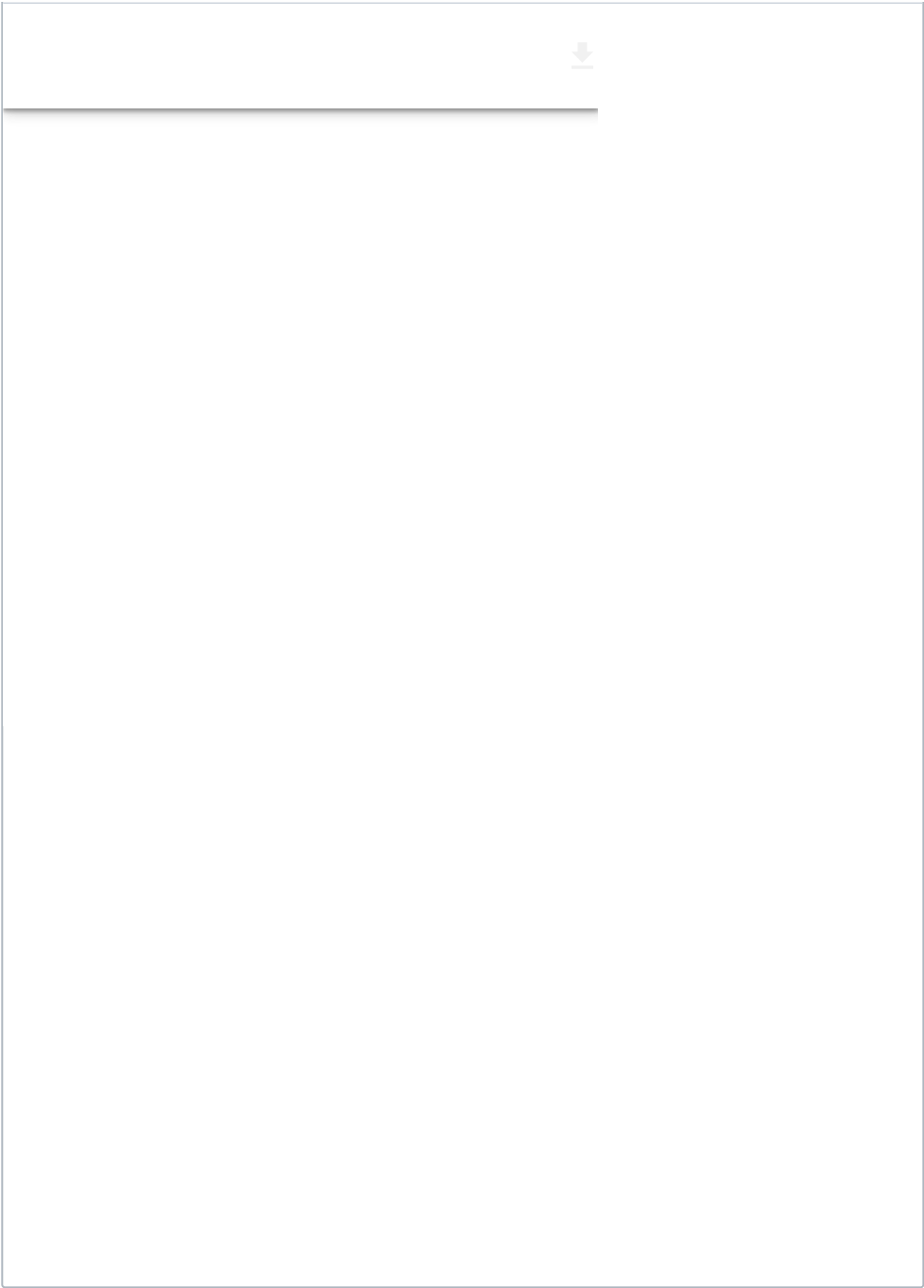
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▼ C and D.pdf

Download



▼ E and F.pdf

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1 / 1



## Q4 Collaborators

0 Points

You are required to indicate whether or not you had collaborators on this assignment. If you did not have collaborators, type "I did not collaborate with anyone". Otherwise list the name of your collaborators.

I did not collaborate with anyone.

## Programming Assignment 4 - questions - Late/Resubmit

**GRADED****STUDENT**

Sophia Yermolenko

**TOTAL POINTS****49 / 54 pts****QUESTION 1**

Big-O Justification

**11 / 12 pts**

- |     |   |           |
|-----|---|-----------|
| 1.1 | $n + 5n^2 + 8n^4$ is $O(n^3)$                       | 2 / 2 pts |
| 1.2 | $n! + n$ is $O(n * \log n)$                         | 2 / 2 pts |
| 1.3 | $\log n + n * \log n + \log(\log n)$ is $\Omega(n)$ | 2 / 2 pts |
| 1.4 | $n^2 + n/4 + 6$ is $\Theta(n^2)$                    | 2 / 2 pts |
| 1.5 | $1/(n^{50}) + \log 32$ is $\Omega(1)$               | 1 / 2 pts |
| 1.6 | $1/(n^{50}) + \log 2$ is $O(1)$                     | 2 / 2 pts |

**QUESTION 2**

List Analysis

**15 / 16 pts**

- |     |   |           |
|-----|---|-----------|
| 2.1 | Did you read the format instructions?   | 0 / 0 pts |
| 2.2 | Give a tight big-O bound for the best case running time of prepend in ArrayList   | 1 / 2 pts |
| 2.3 | Give a tight big-O bound for the worst case running time of prepend in ArrayList  | 2 / 2 pts |
| 2.4 | Give a tight big-O bound for the best case running time of prepend in LinkedList  | 2 / 2 pts |
| 2.5 | Give a tight big-O bound for the worst case running time of prepend in LinkedList | 2 / 2 pts |
| 2.6 | Give a tight big-O bound for the best case running time of add in ArrayList       | 2 / 2 pts |
| 2.7 | Give a tight big-O bound for the worst case running time of add in ArrayList      | 2 / 2 pts |
| 2.8 | Give a tight big-O bound for the best case running time of add in LinkedList      | 2 / 2 pts |

2.9 Give a tight big-O bound for the worst case running time of add in LinkedList 2 / 2 pts

**QUESTION 3**

Mystery Functions and Measuring 23 / 26 pts

3.1 Function Matching - Mystery A 1 / 1 pt

3.2 Function Matching - Mystery B 1 / 1 pt

3.3 Function Matching - Mystery C 1 / 1 pt

3.4 Function Matching - Mystery D 1 / 1 pt

3.5 Function Matching - Mystery E 1 / 1 pt

3.6 Function Matching - Mystery F 1 / 1 pt

3.7 Big-O bound for f1 2 / 2 pts

3.8 Big-O bound for f2 2 / 2 pts

3.9 Big-O bound for f3 2 / 2 pts

3.10 Big-O bound for f4 2 / 2 pts

3.11 Big-O bound for f5 2 / 2 pts

3.12 Big-O bound for f6 2 / 2 pts

3.13 Description of measuring process 2 / 2 pts

3.14 Graphs 3 / 6 pts

**QUESTION 4**

Collaborators 0 / 0 pts