

Notebook

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2.0.1 3. Jump Up, Fall Down

Consider a Markov Chain with state space $0, 1, 2, \dots, 12$ and transition behavior given by: - For $0 \leq i \leq 11$, the distribution of X_{n+1} given $X_n = i$ is uniform on $i+1, i+2, \dots, 12$. - $P(12, 0) = 1$.

a) Complete the cell below to construct the transition matrix of this chain and assign it to the name `jump_fall`.

In [8]: *#Answer to 3a*

```
s = np.arange(13)
def transition_probs(i, j):
    if i == 12:
        if j == 0:
            return(1)
        else:
            return(0)
    else:
        if j > i:
            return(1 / (12 - i))
        else:
            return(0)
jump_fall = MarkovChain.from_transition_function(s, transition_probs)
jump_fall
```

Out[8]:

	0	1	2	3	4	5	6	7	\
0	0.0	0.083333	0.083333	0.083333	0.083333	0.083333	0.083333	0.083333	
1	0.0	0.000000	0.090909	0.090909	0.090909	0.090909	0.090909	0.090909	
... Omitting 22 lines ...									
10	0.000000	0.000000	0.000000	0.500000	0.500000				
11	0.000000	0.000000	0.000000	0.000000	1.000000				
12	0.000000	0.000000	0.000000	0.000000	0.000000				

In [10]: *#Answer to 3c*

```
jump_fall.steady_state()
```

Out[10]:

Value	Probability
0	0.243712
1	0.0203093
... Omitting 5 lines ...	
8	0.0487423
9	0.0609279
... (3 rows omitted)	

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In []: