

# Evaluating the policy gradient

$$\text{recall: } J(\theta) = E_{\tau \sim p_{\theta}(\tau)} \left[ \sum_t r(\mathbf{s}_t, \mathbf{a}_t) \right] \approx \frac{1}{N} \sum_i \sum_t r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t})$$

$$\nabla_{\theta} J(\theta) = E_{\tau \sim \pi_{\theta}(\tau)} \left[ \left( \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t) \right) \left( \sum_{t=1}^T r(\mathbf{s}_t, \mathbf{a}_t) \right) \right]$$

$$\nabla_{\theta} J(\theta) \approx \underbrace{\frac{1}{N} \sum_{i=1}^N}_{\text{orange line}} \left( \sum_{t=1}^T \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_{i,t} | \mathbf{s}_{i,t}) \right) \underbrace{\left( \sum_{t=1}^T r(\mathbf{s}_{i,t}, \mathbf{a}_{i,t}) \right)}_{\text{green line}}$$

$$\underline{\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)}$$

REINFORCE algorithm:

- 1. sample  $\{\tau^i\}$  from  $\pi_{\theta}(\mathbf{a}_t | \mathbf{s}_t)$  (run the policy)
- 2.  $\nabla_{\theta} J(\theta) \approx \sum_i \left( \sum_t \nabla_{\theta} \log \pi_{\theta}(\mathbf{a}_t^i | \mathbf{s}_t^i) \right) \left( \sum_t r(\mathbf{s}_t^i, \mathbf{a}_t^i) \right)$
- 3.  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$

