#### Scheme Notes 01

Geoffrey Matthews

Department of Computer Science Western Washington University

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#### Resources

- The software:
  - https://racket-lang.org/
- Texts:
  - https://mitpress.mit.edu/sicp/
  - http://www.scheme.com/tsp13/ (make sure you use the 3rd edition and not the 4th)
  - http://ds26gte.github.io/tyscheme/

### Running the textbook examples

- Using the racket language is usually best, the examples from The Scheme Programming Language should run without modification.
- ▶ The examples from SICP are a little more idiosyncratic. Most of them can be run by installing the sicp package as in these instructions:

```
http://stackoverflow.com/questions/19546115/which-lang-packet-is-proper-for-sicp-in-dr-racket
```

## Every powerful language has

- primitive expressions: the simplest entities, such as 3 and +
- means of combination: building compound elements from simpler ones such as (+ 3 4)
  - In Scheme combinations are always parentheses, with the operator first and the operands following.
- means of abstraction: a way for naming compound elements
  and then manipulating them as units such as
  (define pi 3.14159)
  (define square (lambda (x) (\* x x)))

# The REPL does the following three things:

- Reads an expression
- Evaluates it to produce a value
- Prints the value

The returned value has a small set of types, including number, boolean and procedure. (Later, we'll see symbol, pair, vector, and promise (stream).)

### There are 4 types of expressions:

- Constants: numbers, booleans. Examples: 4 3.141592 #t #f
- ► Variables: names for values. We create these using the special form define
- Special forms: have special rules for evaluation. In addition, you may not redefine a special form.
- Combinations: (<operator> <operands>). These are sometimes called "function calls" or "procedure applications."

The first two types of expressions (constants and variables) are primitive expressions – they have no parentheses. The second two types are called compound expressions – they have parentheses.

#### **Mantras**

- Every expression has a value
  - (except for errors, infinite loops and the define special form)
- ► To find the value of a combination:
  - Find values of all subexpressions in any order
  - Apply the value of the first to the values of the rest
- ▶ The value of a lambda expression is a procedure

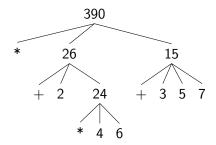
# Finding the value of a combination

- Find values of all subexpressions in any order
- Apply the value of the first to the values of the rest

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#### Program Evaluation In Lisp

A process of tree accumulation.



## Introducing Local Variables

#### Beware! This will NOT work.

```
(let ((x 3)
	(y (* 2 x))
	(z (* 3 x)))
	(+ x (* y z))) => 57
```

#### But this will.

```
(let* ((x 3)
	(y (* 2 x))
	(z (* 3 x)))
	(+ x (* y z))) => 57
```

### **Defining Procedures**

Two equivalent ways:

```
(define (square x) (* x x))
(define square (lambda (x) (* x x)))
```

The first one is more in line with the procedure call:

```
(square 5) => 25
```

### **Defining Procedures**

Two equivalent ways:

```
(define (square x) (* x x))
(define square (lambda (x) (* x x)))
```

The second one is more in line with defining other things:

```
(define x (* 3 4))
(define y (list 'a 'b 'c))
```

The action of define is simply to give a *name* to the result of an expression.

### **Defining Procedures**

Two equivalent ways:

```
(define (square x) (* x x))
(define square (lambda (x) (* x x)))
```

The result of a lambda-expression is an anonymous function. We can name it, as above, or use it without any name at all:

```
(square 5) => 25
((lambda (x) (* x x)) 5) => 25
```

## Solving problems

#### Newton's method:

If y is a guess for  $\sqrt{x}$ , then the average of y and x/y is an even better guess.

X	guess	quotient	average
2	1.0	2.0	1.5
2	1.5	1.3333333333333333	1.416666666666665
2	1.416666666666665	1.411764705882353	1.4142156862745097
2	1.4142156862745097	1.41421143847487	1.4142135623746899

. . .

Evidently, we want to iterate, and keep recomputing these things until we find a value that's close enough.

#### Newton's Method in Scheme

```
(define sqrt-iter
  (lambda (guess x)
    (if (good-enough? guess x)
        guess
        (sqrt-iter (improve guess x) x))))
(define improve
  (lambda (guess x)
    (average guess (/ x guess))))
(define average
  (lambda (x y) (/ (+ x y) 2)))
(define good-enough?
  (lambda (guess x)
    (< (abs (- (square guess) x)) 0.00001)))</pre>
(define square
  (lambda (x) (* x x)))
(define sqrt
  (lambda (x) (sqrt-iter 1.0 x)))
```

Decompose big problems into smaller problems.

#### Definitions can be nested

```
(define sqrt
  (lambda (x)
    (define good-enough?
      (lambda (guess x)
        (< (abs (- (square guess) x)) 0.001)))</pre>
    (define improve
      (lambda (guess x)
        (average guess (/ x guess))))
    (define sqrt-iter
      (lambda (guess x)
        (if (good-enough? guess x)
            guess
            (sqrt-iter (improve guess x) x))))
    (sqrt-iter 1.0 x)))
```

#### Parameters need not be repeated

```
(define sqrt
  (lambda (x))
    (define good-enough?
      (lambda (guess)
        (< (abs (- (square guess) x)) 0.001)))
    (define improve
      (lambda (guess)
        (average guess (/ x guess))))
    (define sqrt-iter
      (lambda (guess)
        (if (good-enough? guess)
            guess
            (sqrt-iter (improve guess)))))
    (sqrt-iter 1.0)))
```

#### Introducing local functions with letrec

```
(define sqrt
  (lambda (x)
    (letrec ((good-enough?
              (lambda (guess)
                (< (abs (- (square guess) x)) 0.001)))
             (improve
              (lambda (guess)
                (average guess (/ x guess))))
             (sqrt-iter
              (lambda (guess)
                (if (good-enough? guess)
                    guess
                     (sqrt-iter (improve guess)))))
             (sqrt-iter 1.0))))
```

#### Procedures as parameters

Summation notation:

$$\sum_{i=a}^{b} f(i) = f(a) + \ldots + f(b)$$

In scheme:

# Finding fixed points

```
x is a fixed point of f if x = f(x)
For some functions you can find fixed points by iterating: x, f(x), f(f(x)), f(f(f(x))), \dots
```

#### Fixed points in scheme:

```
(define fixed-point
  (lambda (f)
    (let
        ((tolerance 0.0001)
         (max-iterations 10000))
      (letrec
          ((close-enough?
            (lambda (a b) (< (abs (- a b)) tolerance)))
           (try
            (lambda (guess iterations)
              (let ((next (f guess)))
                (cond ((close-enough? guess next) next)
                      ((> iterations max-iterations) #f)
                      (else (try next (+ iterations 1)))))))
        (try 1.0 0)))))
(fixed-point cos) => 0.7390547907469174
(fixed-point sin) => 0.08420937654137994
(fixed-point (lambda (x) x)) => 1.0
(fixed-point (lambda (x) (+ x 1))) => #f
```

#### Remember Newton's Method?

```
(define sqrt
  (lambda (x)
        (fixed-point (lambda (y) (/ (+ y (/ x y)) 2)))))
```

#### Procedures as Returned Values

```
(define average-damp
  (lambda (f)
      (lambda (x) (/ (+ x (f x)) 2))))

(define sqrt
  (lambda (x)
      (fixed-point (average-damp (lambda (y) (/ x y))))))
```