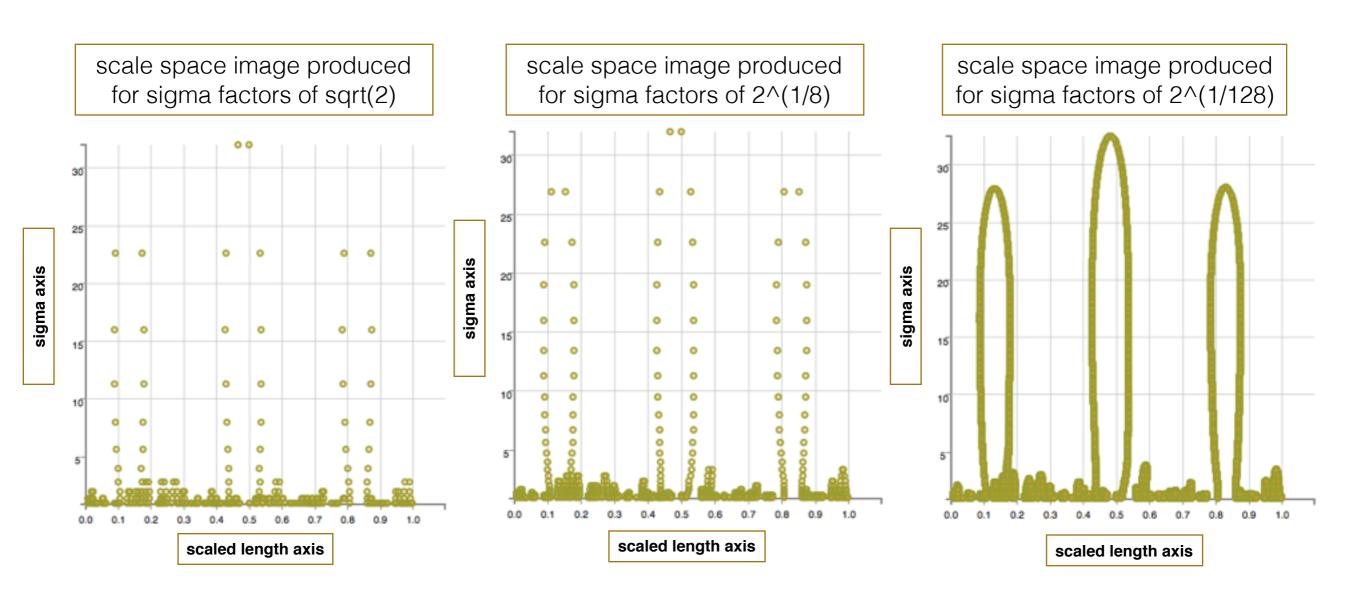
# contour finder



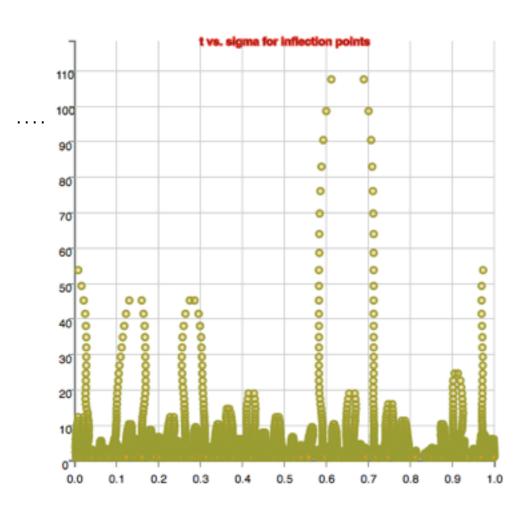


There is an error in estimating the peak of a contour for fastest creation of scale space images (<= sqrt(2)). That error can be reduced overall, by having more contours in the final solution. For an error < 10% in determining a contour's peak height, one should choose a sigma factor of  $2^{(1/8)}$  or smaller. It takes  $2^{3}$  more convolutions if the smaller sigma factor of  $2^{(1/8)}$  is used instead of  $2^{(1/2)}$ .

## Inflection points for sigma > 0

# Scale-Based Description and Recognition of Planar Curves and Two-Dimensional Shapes

FARZIN MOKHTARIAN AND ALAN MACKWORTH



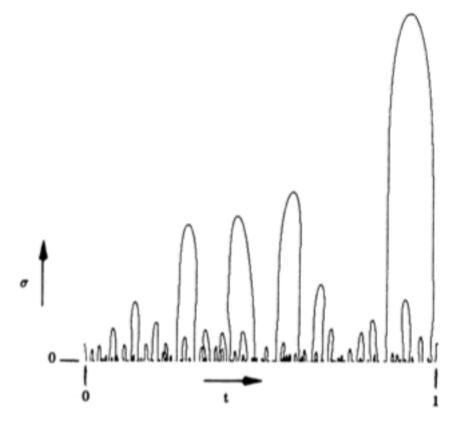
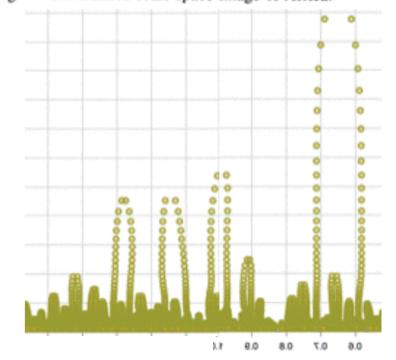
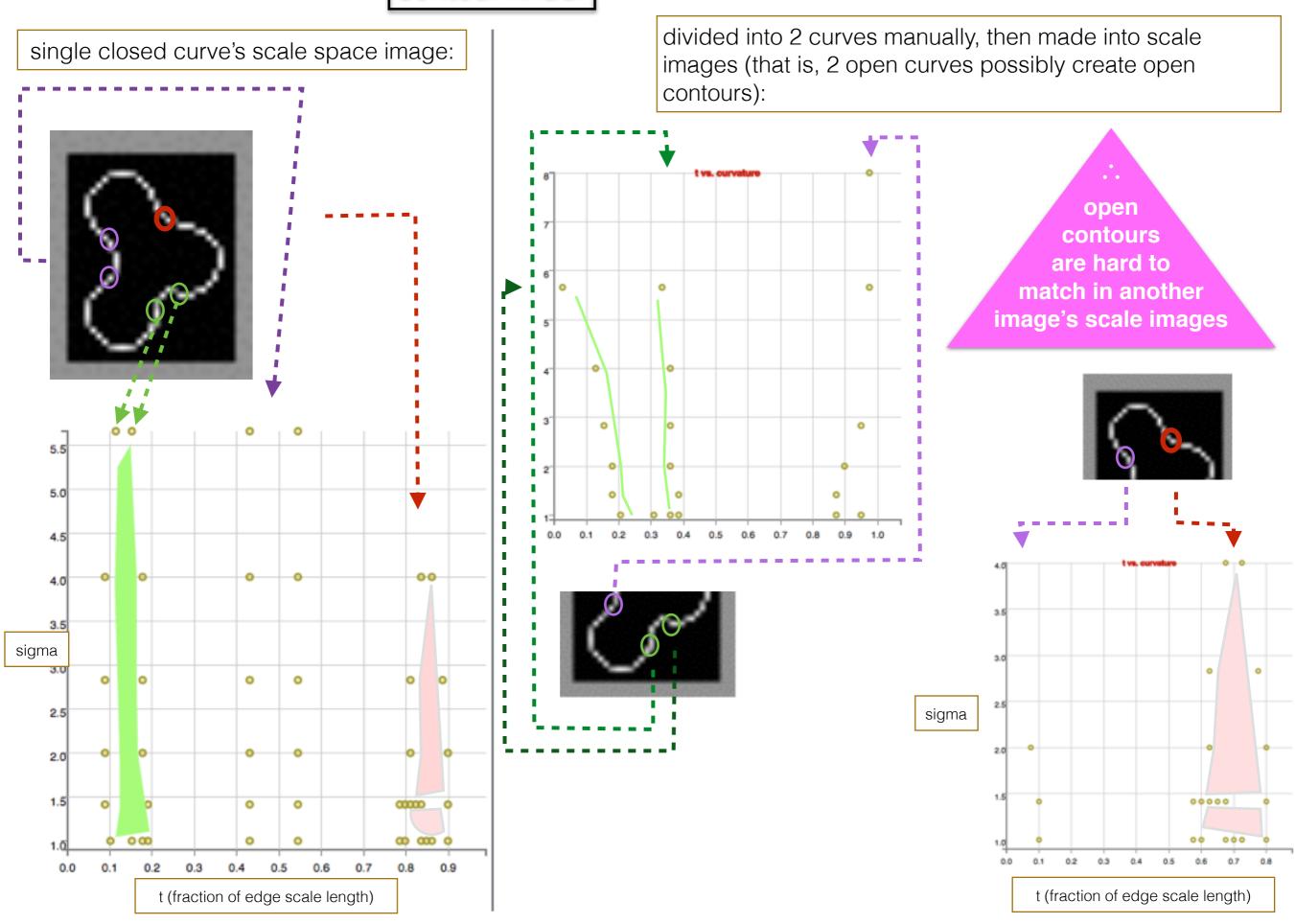


Fig. 3. Generalized scale space image of Africa.

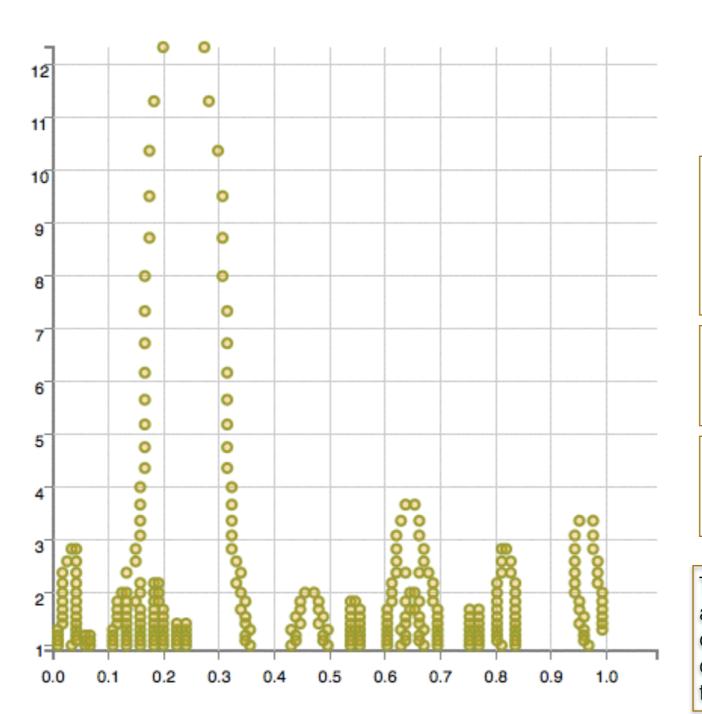


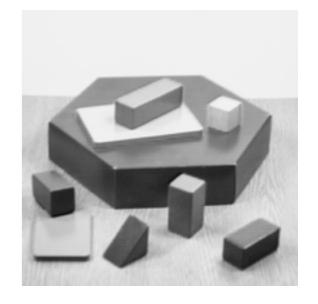
my scale space image agrees with theirs

## contour finder



## contour finder



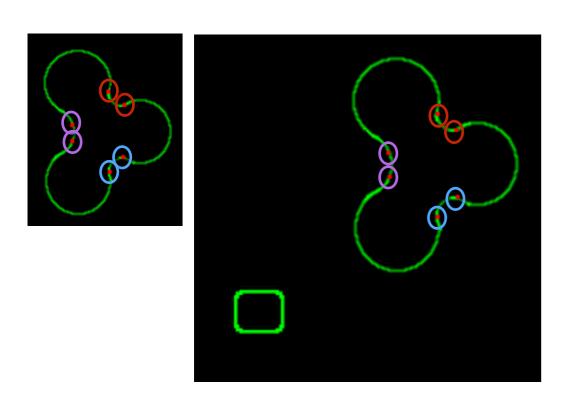


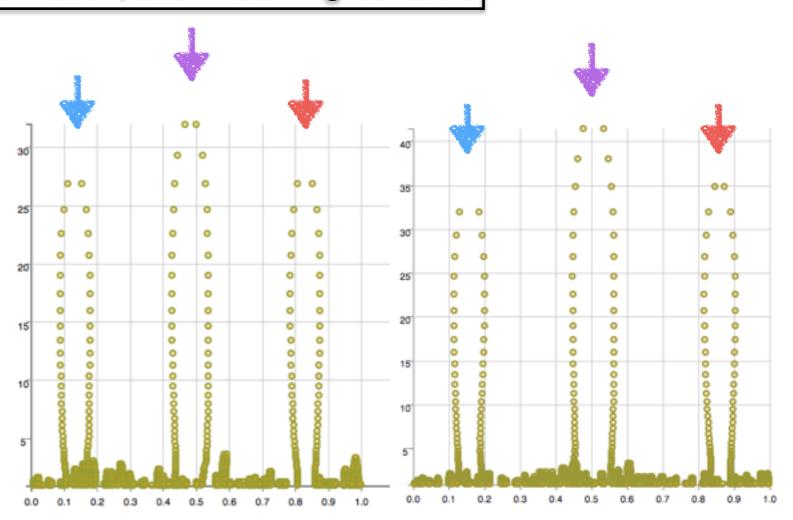
The contour finder looks for the peaks at the highest sigma and then follows the left and right branches down, subtracting that contour from the scale space image. each contour is found that way and subtracted to a lower threshold.

Then contours from one image are matched with the contours of another image (an image having the same content, that is).

Then euclidean transformation parameters rotation, scale, and translation are calculated from the matched contour peak coordinates.

Then, the parameters are refined with small changes and applied to the edges in image 1. The transformed closed curve edges from image 1 are compared to the closest matches in image 2 to find the best fitting transformation parameters.



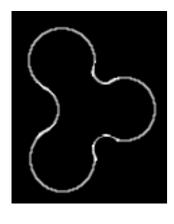


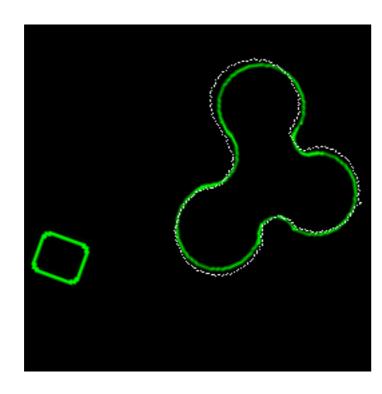
scale should be 1.3 rotation should be 360 - 20

Contour matcher solution scale=1.354256510734558
Contour matcher solution shift=-0.1688411384820938
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (43.336529, 0.504396) (157, 108) (159, 101)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.148750, 0.157143) (190, 143) (177, 150)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.859341) (200, 85) (209, 97)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=1 offsetImgY2=26
rotationInRadians=6.0030236
rotationInDegrees=343.94791799660214

scale=1.3542565

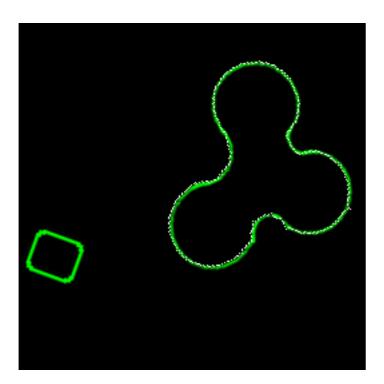
translationX=108.1361 translationY=15.72716





rotationInRadians=6.0030236
rotationInDegrees=343.94791799660214
scale=1.3542565
translationX=108.1361
translationY=15.72716

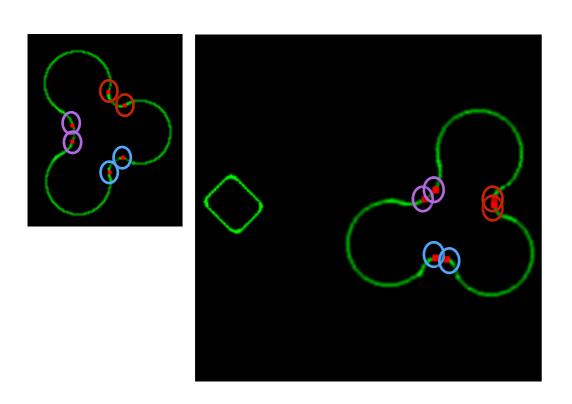
scale should be 1.3 rotation should be 360-20

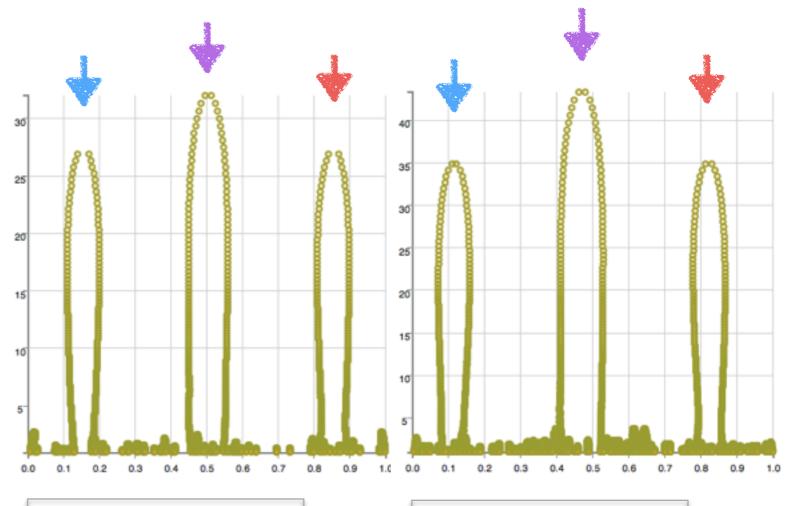


This shows that it's difficult to estimate scale unless some of the inflection points are further from the center of the shape

#### **After Refinement**

rotationInRadians=5.915757
rotationInDegrees=338.94791899582935
scale=1.3042566
translationX=111.0
translationY=20.0





reversed to have CCW ordering

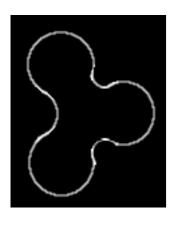
reversed to have CCW ordering

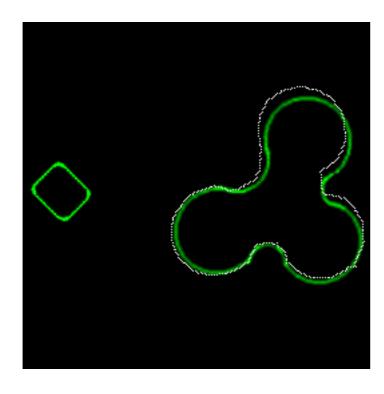
scale should be 1.3 rotation should be 360 - 45

```
Ala, li
```

```
Contour matcher solution scale=1.354256510734558
Contour matcher solution shift=-0.1425349861383438
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (43.336529, 0.530702) (172, 123) (180, 116)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.179825) (188, 168) (180, 167)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.884868) (224, 122) (224, 127)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=3 offsetImgY2=52
rotationInRadians=5.5627766
rotationInDegrees=318.7236195803948
```

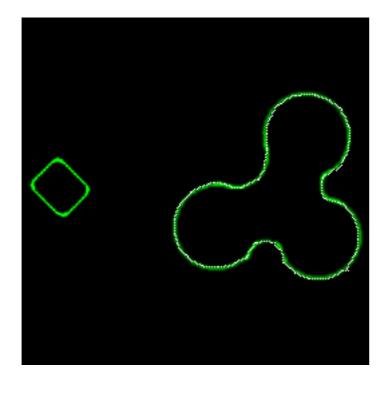
scale=1.3542565
translationX=119.984764
translationY=39.13688





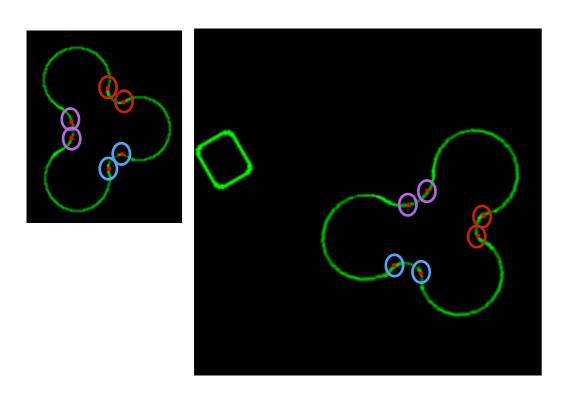
offsetImgX1=10 offsetImgY1=10 offsetImgX2=3 offsetImgY2=52 rotationInRadians=5.5627766 rotationInDegrees=318.7236195803948 scale=1.3542565 translationX=119.984764 translationY=39.13688

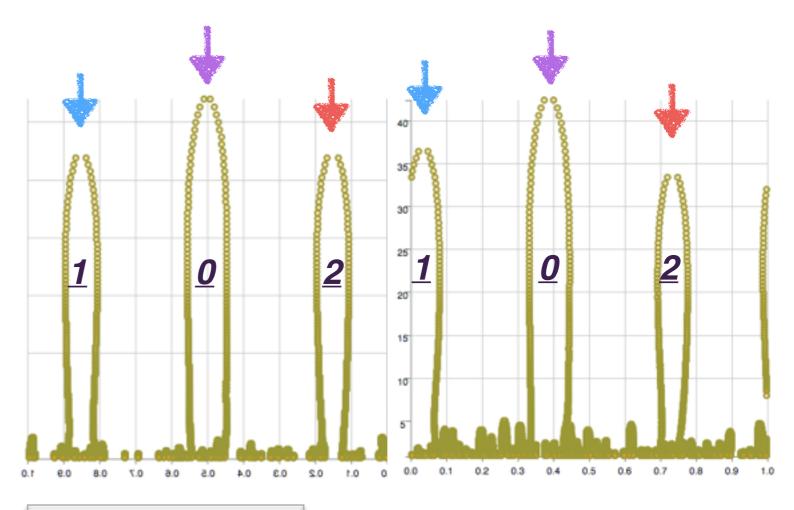
scale should be 1.3 rotation should be 360-45



#### **After Refinement**

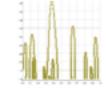
rotationInRadians=5.47551
rotationInDegrees=313.72362057962204
scale=1.3042566
translationX=124.0
translationY=47.0





reversed to have CCW ordering

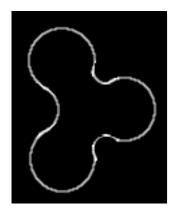
scale should be 1.3 rotation should be 360 - 60

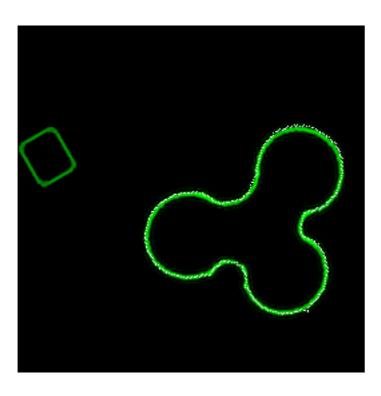


```
Contour matcher solution scale=1.325237512588501
Contour matcher solution shift=-0.2715021073818207
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (42.407913, 0.387309) (161, 133) (172, 126)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (36.441517, 0.035011) (168, 182) (157, 176)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (33.417011, 0.734136) (215, 143) (213, 156)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=0 offsetImgY2=71
rotationInRadians=5.2398615
rotationInDegrees=300.2219485151509
```

scale=1.3252375 translationX=107.96625

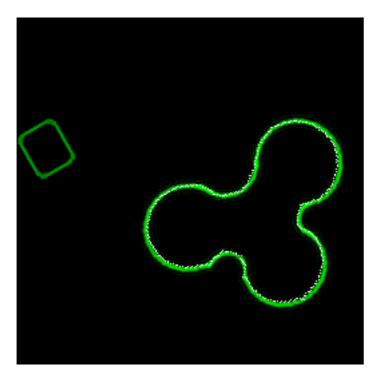
translationY=59.87517





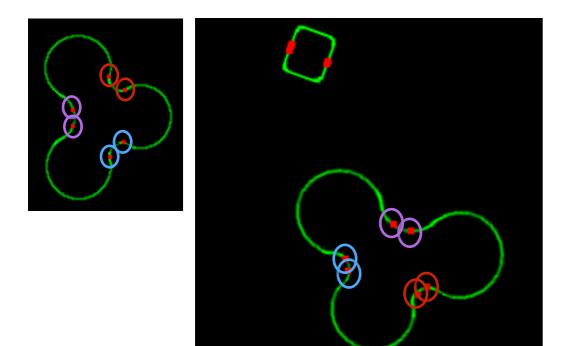
Contour matcher solution scale=1.325237512588501
Contour matcher solution shift=-0.2715021073818207
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72)
 CONTOUR PEAK2: (42.407913, 0.387309) (161, 133) (172, 126)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99)
 CONTOUR PEAK2: (36.441517, 0.035011) (168, 182) (157, 176)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54)
 CONTOUR PEAK2: (33.417011, 0.734136) (215, 143) (213, 156)
 offsetImgX1=10 offsetImgY1=10
 offsetImgX2=0 offsetImgY2=71
 rotationInRadians=5.2398615
 rotationInDegrees=300.2219485151509
 scale=1.3252375
 translationX=107.96625
 translationY=59.87517

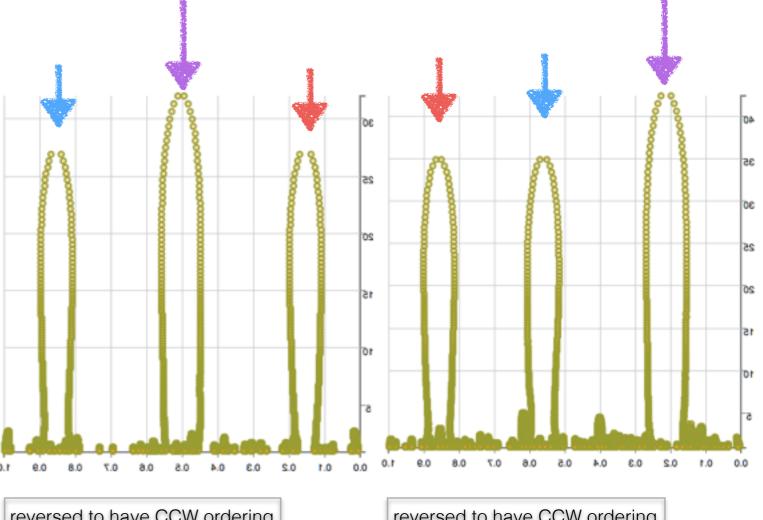
scale should be 1.3 rotation should be 360 - 60



#### **After Refinement**

rotationInRadians=5.2398615
rotationInDegrees=300.2219485151509
scale=1.2752376
translationX=110.0
translationY=63.0





reversed to have CCW ordering

reversed to have CCW ordering

scale should be 1.3 rotation should be 360 -110

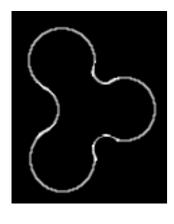


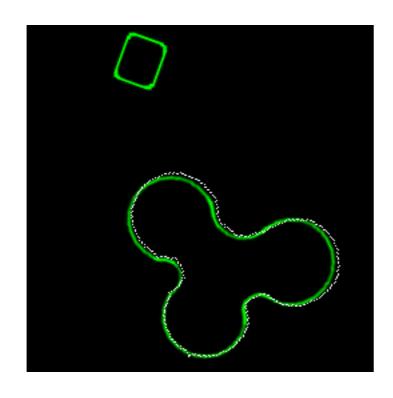
```
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (42.407913, 0.787445) (148, 154) (161, 159)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.439427) (114, 189) (112, 180)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.142070) (173, 201) (166, 207)
```

offsetImgX1=10 offsetImgY1=10 offsetImgX2=62 offsetImgY2=1 rotationInRadians=4.336784 rotationInDegrees=248.47941332561248

scale=1.3252375

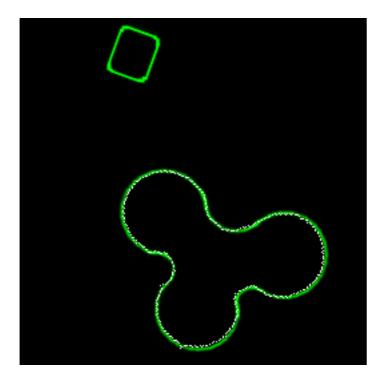
translationX=70.99721 translationY=91.054344





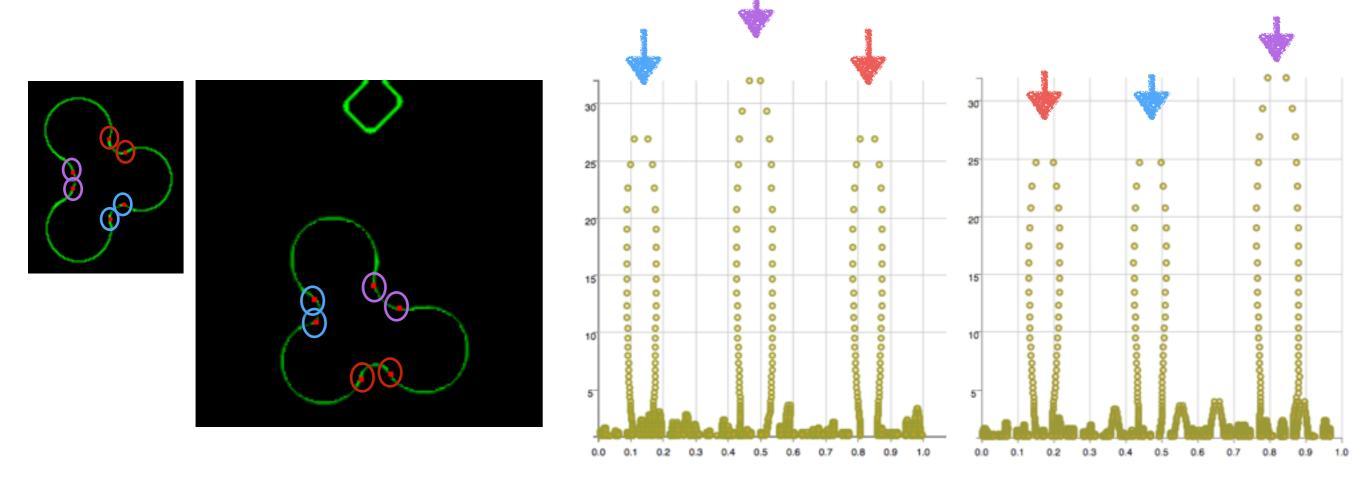
```
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (42.407913, 0.787445) (148, 154) (161, 159) CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.439427) (114, 189) (112, 180) CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.142070) (173, 201) (166, 207) offsetImgX1=10 offsetImgY1=10 offsetImgY2=1 rotationInRadians=4.336784 rotationInDegrees=248.47941332561248 scale=1.3252375 translationX=70.99721 translationY=91.054344
```

scale should be 1 rotation should be 360 - 110 (250)



#### **After Refinement**

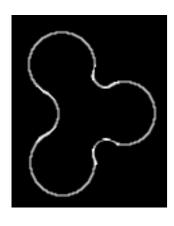
rotationInRadians=4.354237
rotationInDegrees=249.4794076616157
scale=1.2752376
translationX=71.0
translationY=95.0

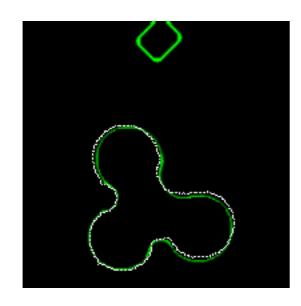


scale should be 1.3 rotation should be 360 - 135

translationY=70.68979

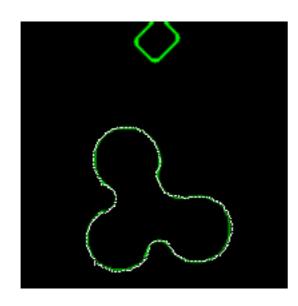
Contour matcher solution scale=1.0218971967697144
Contour matcher solution shift=0.3104316294193268
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (32.700951, 0.818444) (103, 120) (115, 132)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (25.768024, 0.468300) (69, 136) (69, 127)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (25.768024, 0.175793) (105, 164) (97, 166)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=46 offsetImgY2=0
rotationInRadians=3.9818497
rotationInDegrees=228.14318077005984
scale=1.0218972
translationX=32.712353





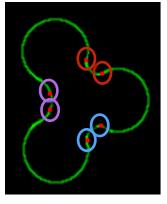
offsetImgX1=10 offsetImgY1=10 offsetImgX2=46 offsetImgY2=0 rotationInRadians=3.9818497 rotationInDegrees=228.14318077005984 scale=1.0218972 translationX=32.712353 translationY=70.68979

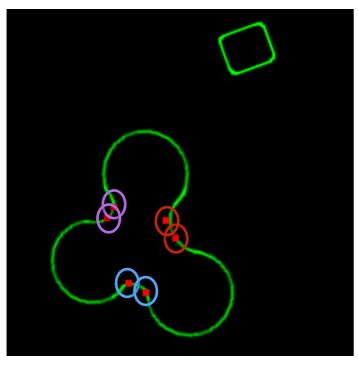
scale should be 1 rotation should be 360 - 135

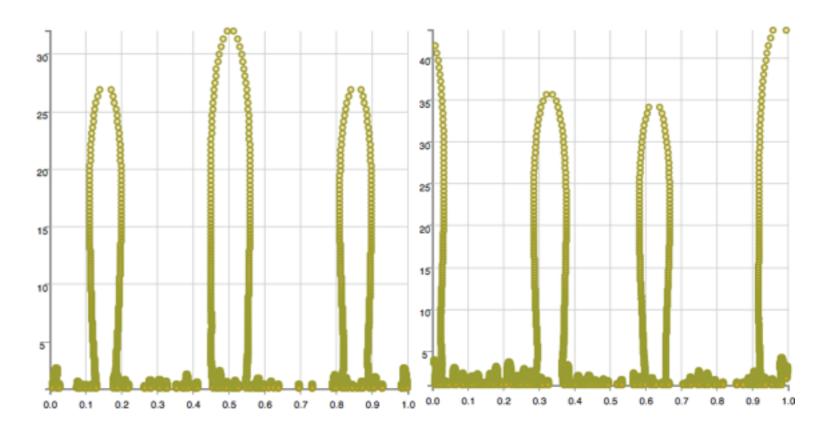


#### **After Refinement**

rotationInRadians=3.9406004
rotationInDegrees=225.77977139269535
scale=1.0218972
translationX=33.0
translationY=72.0







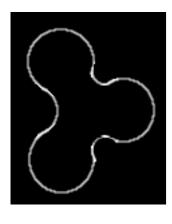
reversed to have CCW ordering

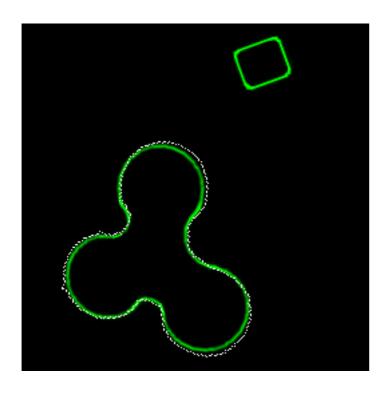
scale should be 1.3 rotation should be 360 - 160

Contour matcher solution shift=-0.648127555847168
Contour matcher solution cost=3.0

CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (43.336529, 0.025109) (119, 158) (126, 171)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (35.660648, 0.672489) (75, 156) (80, 148)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.148750, 0.377729) (104, 212) (91, 205)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=29 offsetImgY2=6
rotationInRadians=3.4556763
rotationInDegrees=197.995668339729
scale=1.3542565

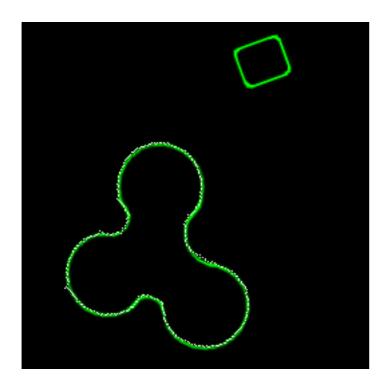
translationX=17.566353 translationY=81.42969





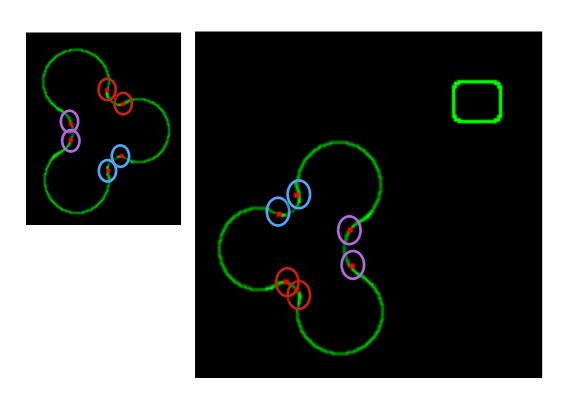
rotationInRadians=3.4556763 rotationInDegrees=197.995668339729 scale=1.3542565 translationX=17.566353 translationY=81.42969

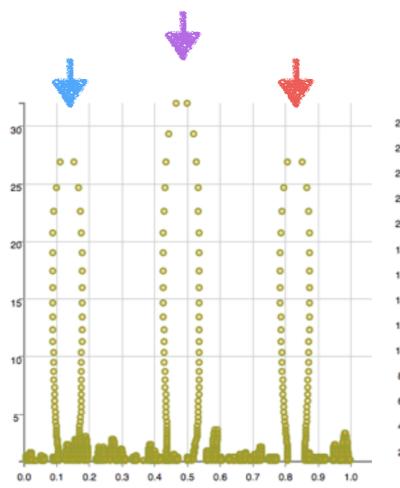
scale should be 1 rotation should be 360 - 160

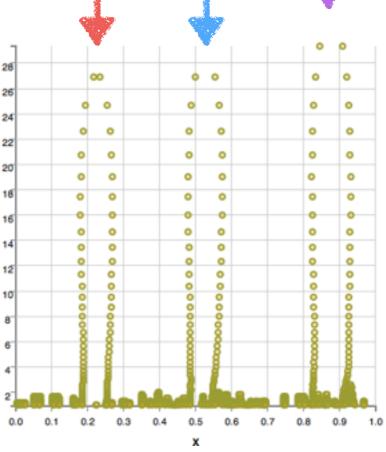


#### **After Refinement**

rotationInRadians=3.4993095 rotationInDegrees=200.49566784011543 scale=1.3042566 translationX=20.0 translationY=84.0





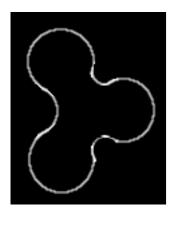


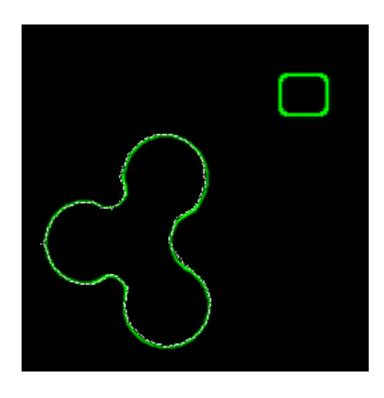
reversed to have CCW ordering

scale should be 1.3 rotation should be 180

translationY=70.504585

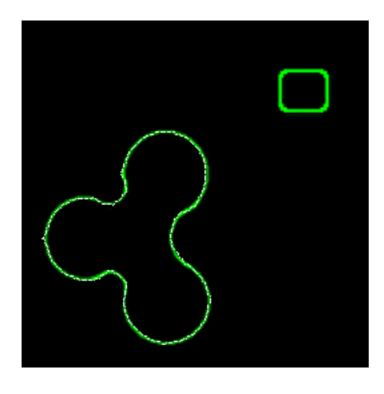
```
Contour matcher solution scale=1.2968404293060303
Contour matcher solution shift=0.22837476432323456
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (41.499199, 0.873068) (111, 158) (112, 167)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (35.660648, 0.522075) (67, 137) (77, 127)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.222958) (75, 194) (69, 188)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=14 offsetImgY2=33
rotationInRadians=3.1657186
rotationInDegrees=181.38231235356184
scale=1.2968404
translationX=5.891382
```





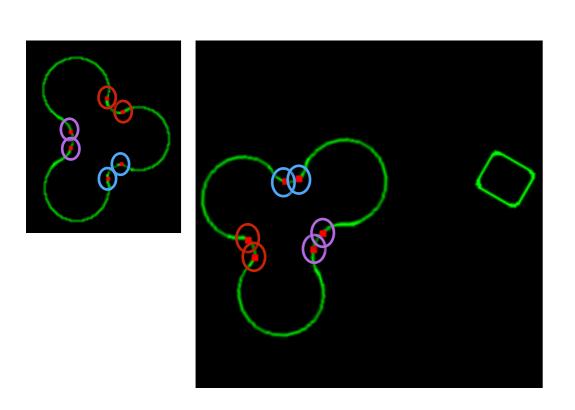
offsetImgX1=10 offsetImgY1=10 offsetImgX2=14 offsetImgY2=33 rotationInRadians=3.1657186 rotationInDegrees=181.38231235356184 scale=1.2968404 translationX=5.891382 translationY=70.504585

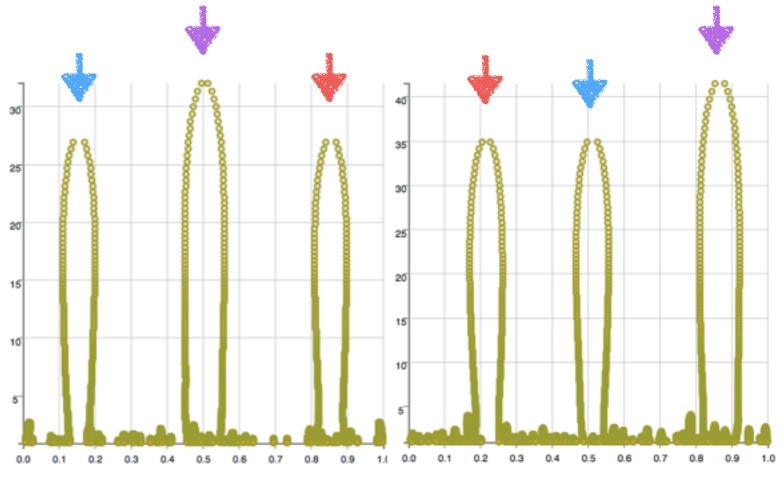
scale should be 1.3 rotation should be 180



#### **After Refinement**

rotationInRadians=3.1482654 rotationInDegrees=180.38231801755862 scale=1.2968404 translationX=6.0 translationY=71.0





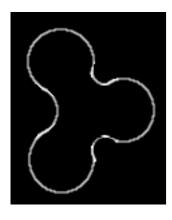
reversed to have CCW ordering

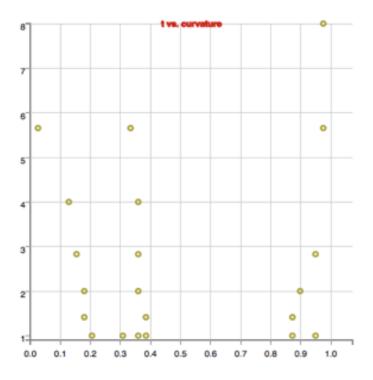
reversed to have CCW ordering

scale should be 1.3 rotation should be 360 - 210

translationY=41.450577

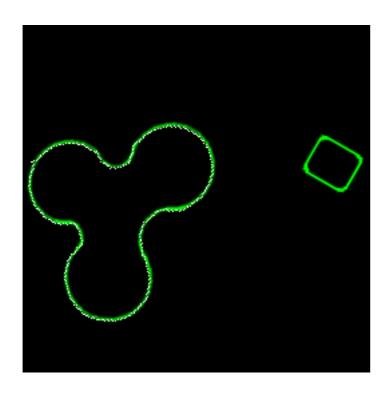
```
Contour matcher solution scale=1.2968404293060303
Contour matcher solution shift=-0.5097379088401794
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (41.499199, 0.134956) (95, 144) (88, 156)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.785398) (67, 105) (77, 103)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.490044) (44, 162) (39, 149)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=1 offsetImgY2=70
rotationInRadians=2.6591716
rotationInDegrees=152.3593086078036
scale=1.2968404
translationX=-10.876109
```





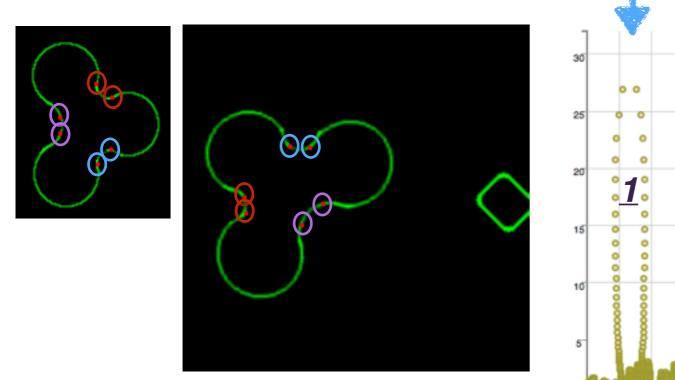
offsetImgX1=10 offsetImgY1=10 offsetImgX2=1 offsetImgY2=70 rotationInRadians=2.6591716 rotationInDegrees=152.3593086078036 scale=1.2968404 translationX=-10.876109 translationY=41.450577

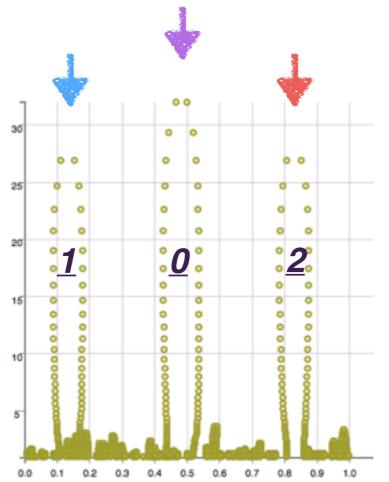
scale should be 1.3 rotation should be 360 - 210

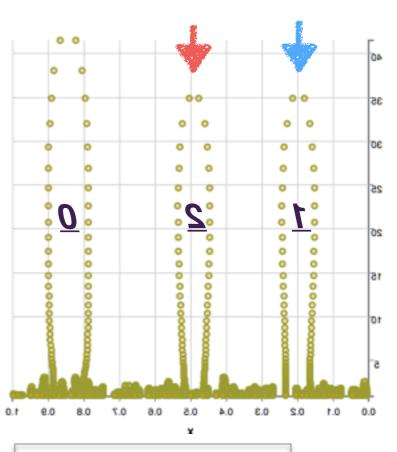


#### **After Refinement**

rotationInRadians=2.6155384
rotationInDegrees=149.85930910741718
scale=1.2968404
translationX=-12.0
translationY=43.0





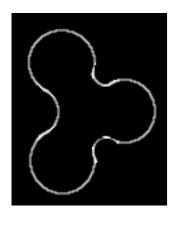


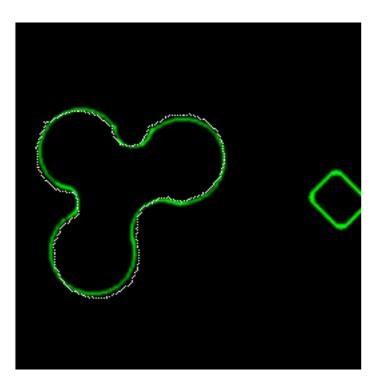
reversed to have CCW ordering

scale should be 1.3 rotation should be 360 - 225

translationX=-5.8268623 translationY=25.13414

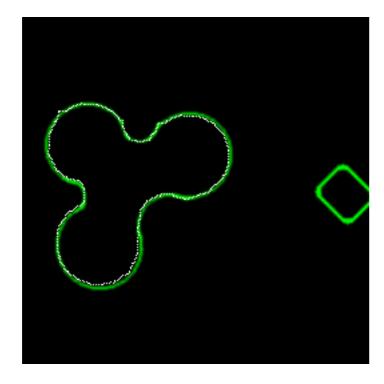
Contour matcher solution scale=1.325237512588501 Contour matcher solution shift=-0.5053889751434326 CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (42.407913, 0.153422) (98, 136) (91, 143) CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.802428) (81, 91) (92, 92) CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.508830) (46, 140) (45, 129) offsetImgX1=10 offsetImgY1=10 offsetImgX2=14 offsetImgY2=61 rotationInRadians=2.4194849 rotationInDegrees=138.6262707153875 scale=1.3252375





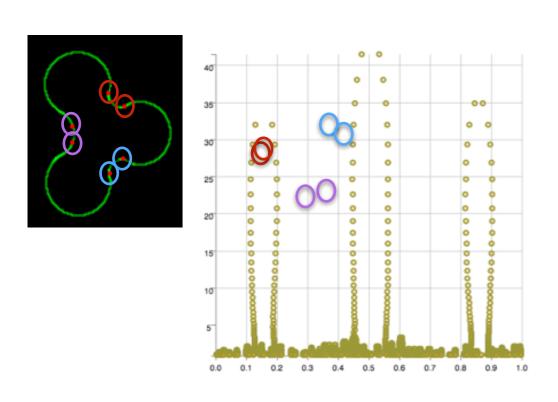
offsetImgX1=10 offsetImgY1=10 offsetImgX2=14 offsetImgY2=61 rotationInRadians=2.4194849 rotationInDegrees=138.6262707153875 scale=1.3252375 translationX=-5.8268623 translationY=25.13414

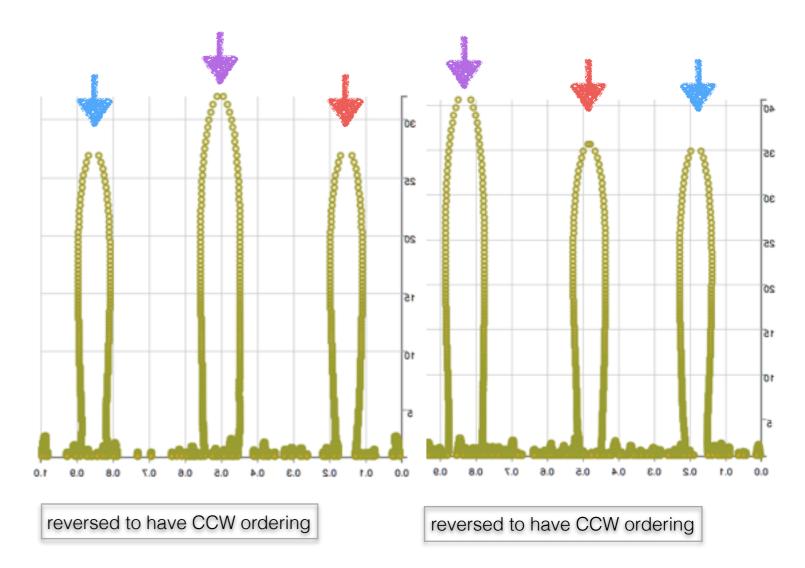
scale should be 1.3 rotation should be 360 - 225



#### **After Refinement**

rotationInRadians=2.3322184
rotationInDegrees=133.6262717146147
scale=1.2752376
translationX=-3.0
translationY=27.0



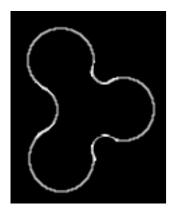


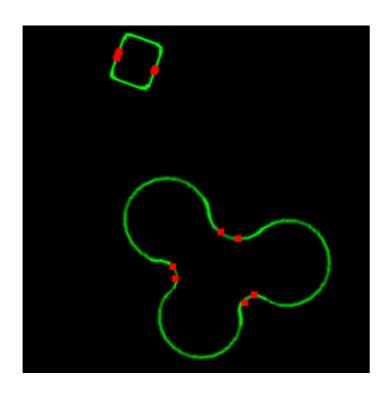
scale should be 1.3 rotation should be 360 - 255

translationY=-1.6037707

CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (40.609955, 0.168514) (98, 115) (82, 118) CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.817073) (101, 65) (113, 73) CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (35.660648, 0.517738) (49, 89) (51, 86)

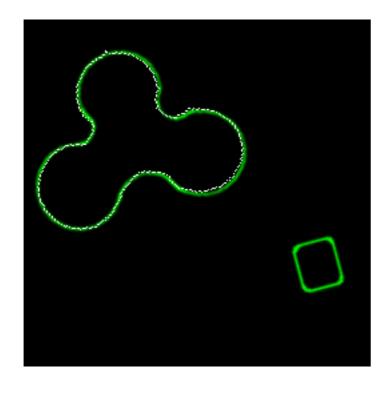
offsetImgX1=10 offsetImgY1=10 offsetImgX2=5 offsetImgY2=20 rotationInRadians=1.8595577 rotationInDegrees=106.54481071213507 scale=1.2690517 translationX=3.6613295





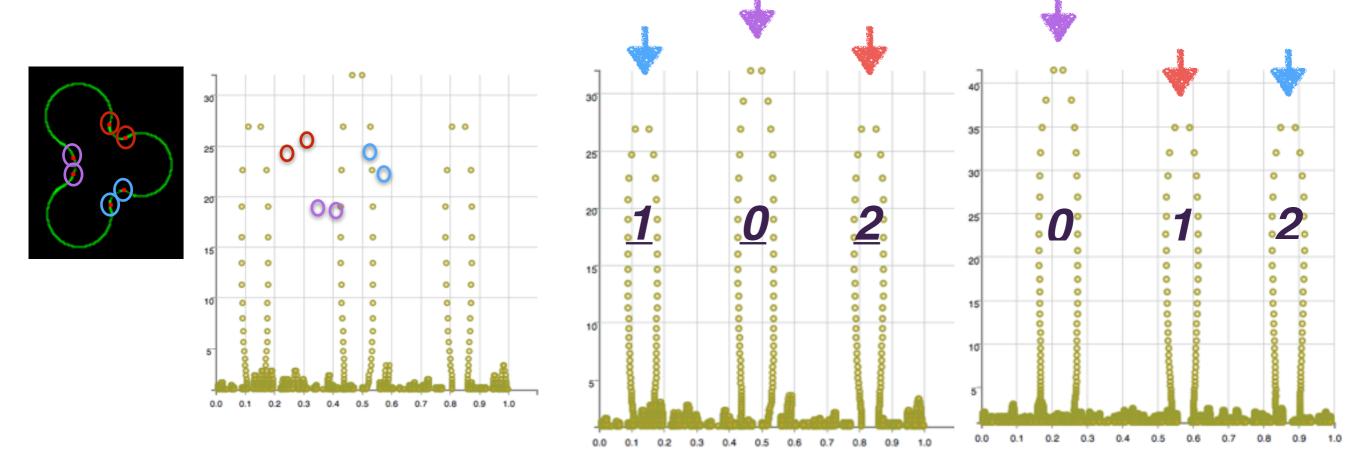
rotationInRadians=1.8595577
rotationInDegrees=106.54481071213507
scale=1.2690517
translationX=3.6613295
translationY=-1.6037707

scale should be 1.3 rotation should be 360 - 255



### **After Refinement**

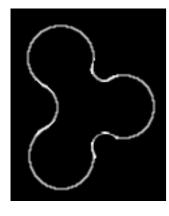
rotationInRadians=1.8558925
rotationInDegrees=106.33480971591386
scale=1.2845517
translationX=4.0
translationY=-6.0



scale should be 1.3 rotation should be 360 - 280

translationY=-16.518988

```
Contour matcher solution scale=1.2968404293060303
Contour matcher solution shift=-0.4310373365879059
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (41.499199, 0.213656) (106, 108) (96, 106)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (35.660648, 0.865639) (134, 70) (137, 76)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (35.660648, 0.566079) (74, 67) (82, 60)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=19 offsetImgY2=9
rotationInRadians=1.4486057
rotationInDegrees=82.9989903033234
scale=1.2968404
translationX=28.18638
```



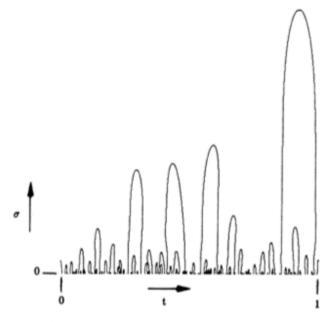
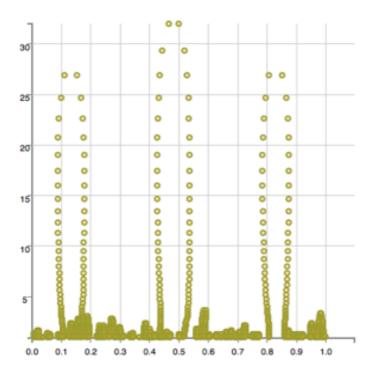


Fig. 3. Generalized scale space image of Africa.

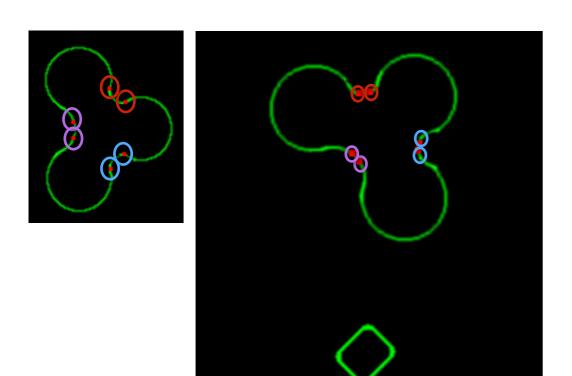
offsetImgX1=10 offsetImgY1=10 offsetImgX2=19 offsetImgY2=9 rotationInRadians=1.4486057 rotationInDegrees=82.9989903033234 scale=1.2968404 translationX=28.18638 translationY=-16.518988

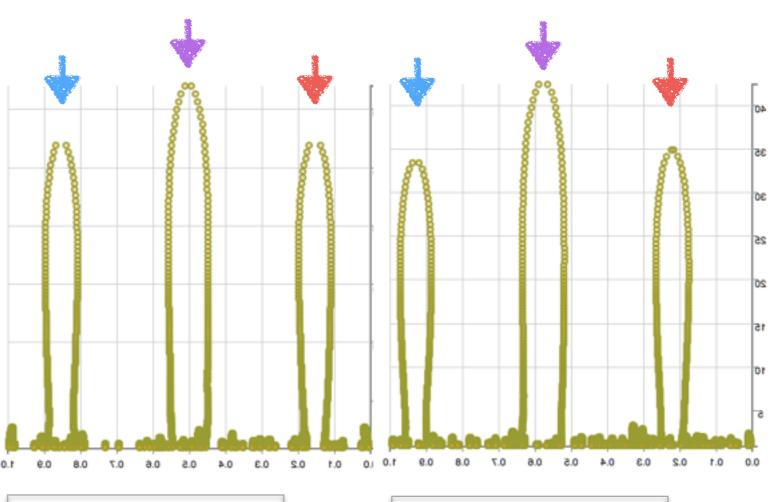
scale should be 1.3 rotation should be 360 - 280



#### **After Refinement**

rotationInRadians=1.4049724
rotationInDegrees=80.49899080293699
scale=1.2968404
translationX=29.0
translationY=-17.0





reversed to have CCW ordering

reversed to have CCW ordering

scale should be 1.3 rotation should be 360 - 315

Contour matcher solution scale=1.325237512588501 Contour matcher solution shift=-0.2311936765909195

Contour matcher solution cost=89.0

CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (42.407913, 0.427617) (125, 102) (112, 89) CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (33.417011, 0.074610) (169, 80) (168, 93) CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.148750, 0.783964) (120, 45) (132, 45)

offsetImgX1=10 offsetImgY1=10 offsetImgX2=52 offsetImgY2=14

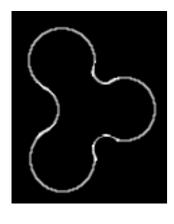
rotationInRadians=0.7365556

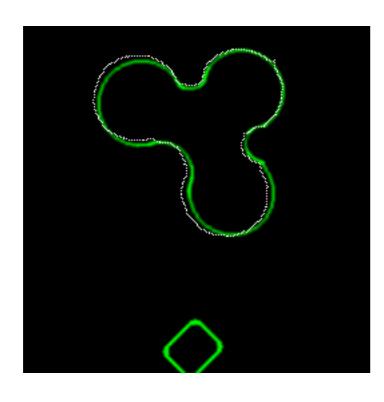
rotationInDegrees=42.2015259002177

scale=1.3252375

translationX=60.744064

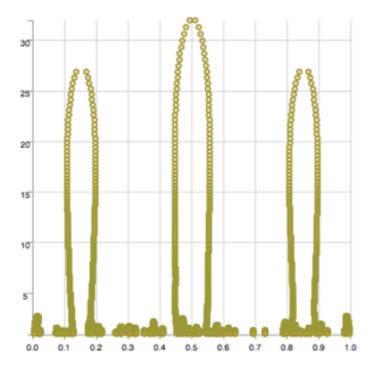
translationY=-25.366236





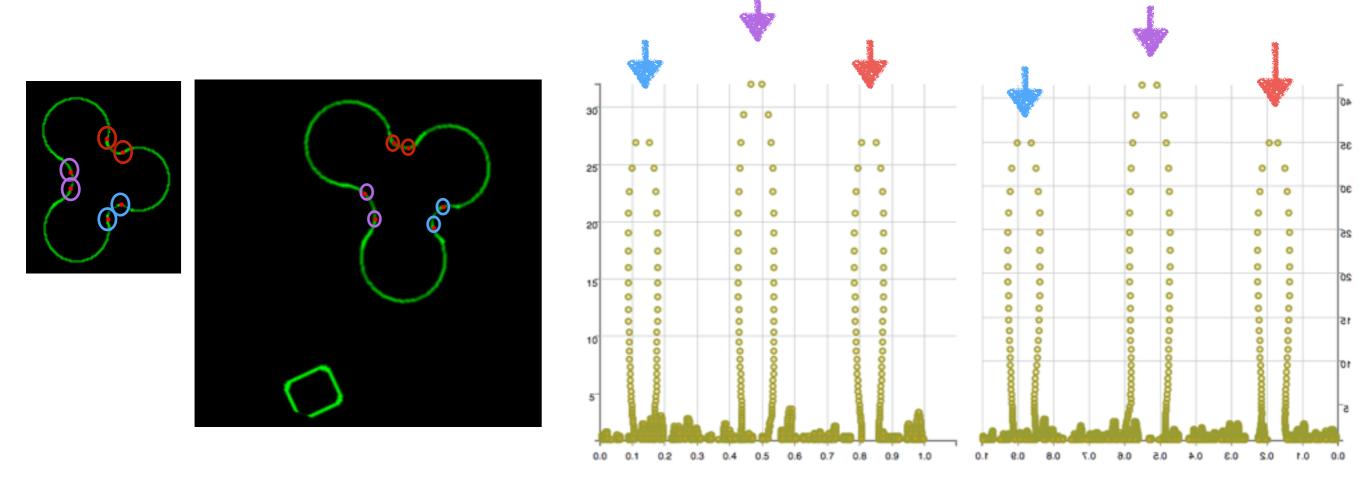
offsetImgX1=10 offsetImgY1=10 offsetImgX2=52 offsetImgY2=14 rotationInRadians=0.7365556 rotationInDegrees=42.2015259002177 scale=1.3252375 translationX=60.744064 translationY=-25.366236

scale should be 1.3 rotation should be 360 - 315



#### **After Refinement**

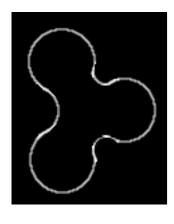
rotationInRadians=0.7801888
rotationInDegrees=44.70152540060411
scale=1.2752376
translationX=65.0
translationY=-21.0

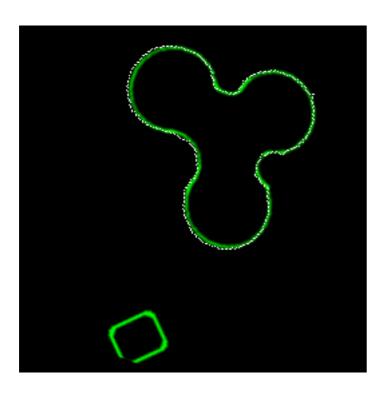


scale should be 1.3 rotation should be 360 - 335

Contour matcher solution scale=1.325237512588501
Contour matcher solution shift=-0.19089026749134064
CONTOUR PEAK1: (32.000237, 0.497126) (34, 78) (35, 72) CONTOUR PEAK2: (42.407913, 0.467920) (134, 99) (131, 90)
CONTOUR PEAK1: (26.908875, 0.146552) (70, 93) (61, 99) CONTOUR PEAK2: (34.896511, 0.115044) (182, 98) (178, 106)
CONTOUR PEAK1: (26.908875, 0.846264) (60, 45) (69, 54) CONTOUR PEAK2: (34.896511, 0.818584) (150, 48) (158, 51)
offsetImgX1=10 offsetImgY1=10
offsetImgX2=63 offsetImgY2=12
rotationInRadians=0.43239865
rotationInDegrees=24.77461754427387
scale=1.3252375

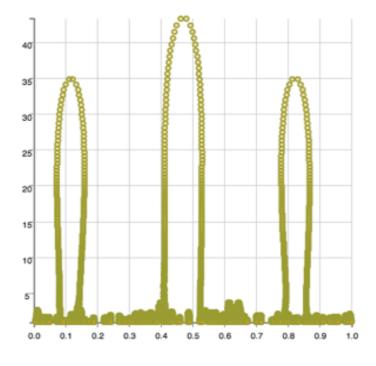
translationX=81.613556 translationY=-16.98058





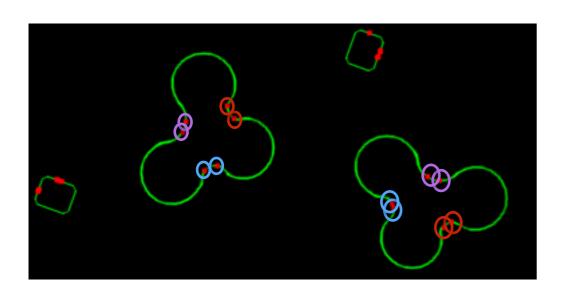
offsetImgX1=10 offsetImgY1=10 offsetImgX2=63 offsetImgY2=12 rotationInRadians=0.43239865 rotationInDegrees=24.77461754427387 scale=1.3252375 translationX=81.613556 translationY=-16.98058

scale should be 1.3 rotation should be 360 - 335



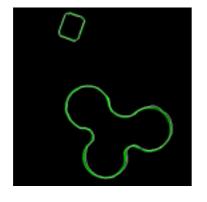
### **After Refinement**

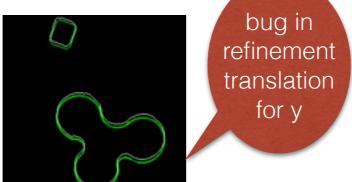
rotationInRadians=0.43239865
rotationInDegrees=24.77461754427387
scale=1.2752376
translationX=85.0
translationY=-14.0

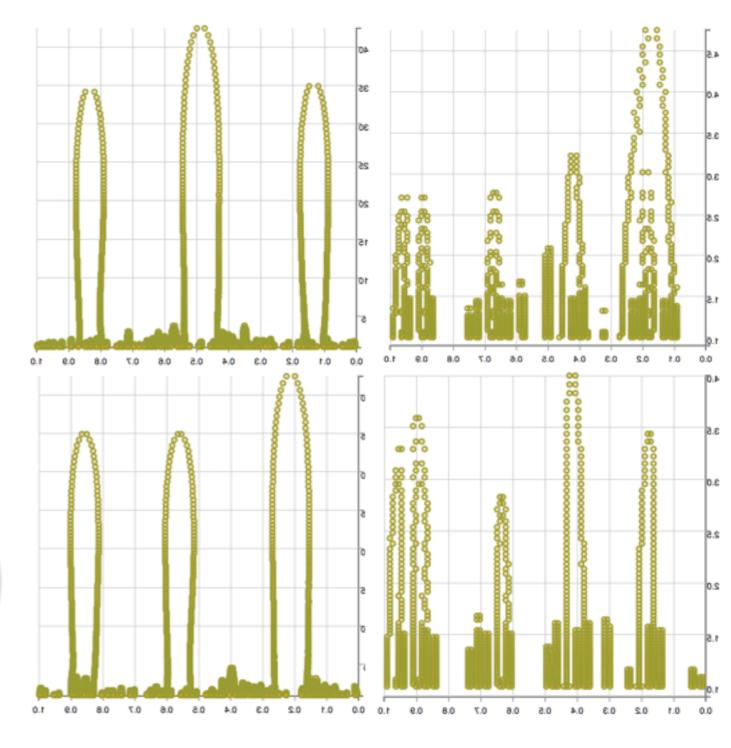


rotationInRadians=4.7316465
rotationInDegrees
=271.1033767625259
scale=1.0
translationX=0.5612701
translationY=0.34837633

rotationInRadians=4.7141933 rotationInDegrees =270.10338242652267 scale=1.0 translationX=-0.8046181 translationY=-4.0230904







```
Contour matcher solution scale=1.0
```

Contour matcher solution shift=0.27483445405960083

Contour matcher solution cost=14.0

CONTOUR PEAK1: (42.407913, 0.513245) (156, 110) (159, 99) CONTOUR PEAK2: (42.407913, 0.788080) (149, 155) (161, 159)

CONTOUR PEAK1: (34.896511, 0.866446) (201, 83) (208, 96) CONTOUR PEAK2: (34.896511, 0.142384) (173, 201) (166, 207)

CONTOUR PEAK1: (4.756843, 0.845455) (33, 160) (33, 160) CONTOUR PEAK2: (3.589427, 0.103604) (99, 33) (98, 34)

CONTOUR PEAK1: (34.148750, 0.166667) (191, 144) (178, 149) CONTOUR PEAK2: (34.896511, 0.440397) (115, 187) (113, 182)

CONTOUR PEAK1: (3.220988, 0.581818) (9, 170) (10, 168) CONTOUR PEAK2: (3.437247, 0.828829) (90, 9) (90, 9)

CONTOUR PEAK1: (3.018335, 0.809091) (28, 158) (30, 159) CONTOUR PEAK2: (3.291518, 0.049550) (101, 27) (101, 28)