University of Victoria Department of Computer Science CSC 355 Digital Logic and Computer Design

ASSIGNMENT 1 DUE Thursday September 24 AT BEGINNING OF CLASS

Neatness Counts!

It is expected that answers to assignments are either typed or written *extremely* neatly. In all cases, the Karnaugh Maps formats below *must* be used, either copied and edited to add the required bits and circles or printed and written on.

1. Determine the radix r given that $(257)_r = (11010110)_2$ (show all your work).

$$(11010110)_2 = 128+64+16+4+2 = 214_{10}$$

Note: It is clear that r is less than 10 because 214 is smaller than 257.
Using a trial and error method, guess 9:
 $2x9^2+5x9+7 = 162+45+7 = 214_{10}$ \therefore base 9 is the correct answer!

2. Simplify the following expression, using Boolean algebra, into minimum sum of products form:

$$(B+C)(\overline{B}+D)(\overline{A}+C)(\overline{A}+\overline{D})$$

Show each Boolean algebra rule used in the simplification.

$$(B+C)(\overline{B}+D)(\overline{A}+C)(\overline{A}+\overline{D})$$

$$= (B\overline{B}+BD+\overline{B}C+CD)(\overline{A}\overline{A}+\overline{A}C+\overline{A}\overline{D}+C\overline{D}) \quad \text{, distributive}$$

$$= (BD+\overline{B}C+CD)(\overline{A}+\overline{A}C+\overline{A}\overline{D}+C\overline{D}) \quad \text{, complement, idempotent}$$

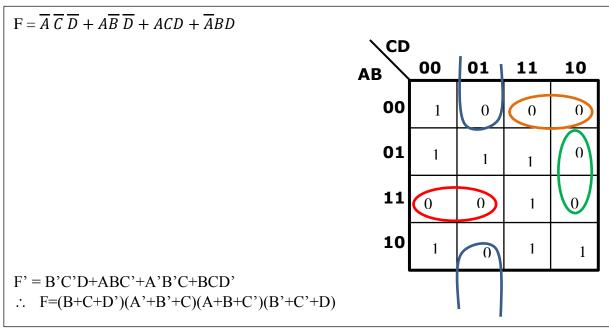
$$= (BD+\overline{B}C)(\overline{A}+C\overline{D}) \quad \text{, consensus, absorption}$$

$$= \overline{A}BD+\overline{A}\overline{B}C+BCD\overline{D}+\overline{B}CC\overline{D} \quad \text{, distributive}$$

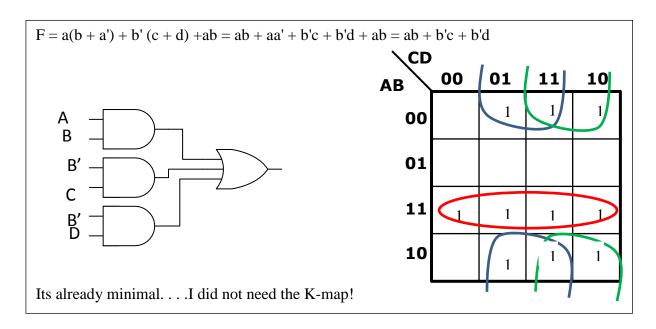
$$= \overline{A}BD+\overline{A}\overline{B}C+\overline{B}C\overline{D} \quad \text{, complement, idempotent}$$

3. Convert the following expression into minimum product of sums form:

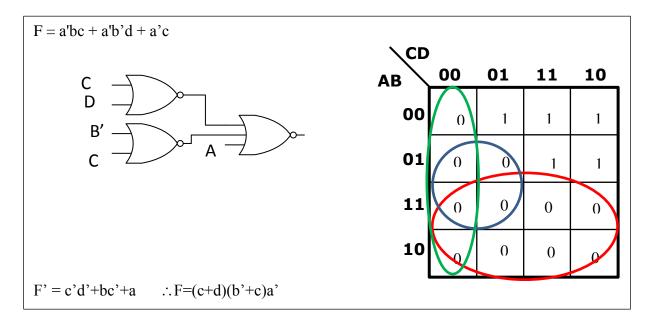
$$\overline{A} \overline{C} \overline{D} + A \overline{B} \overline{D} + A C D + \overline{A} B D$$



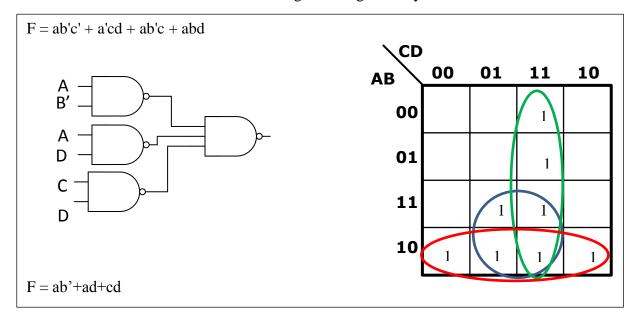
- 4. Design circuits as specified below. In each case assume that all variables are available in both true and inverted form. Gates may have any fan-in up to 4. Marks will be awarded for keeping the total number of gates as small as possible.
 - a. a two level circuit for a(b + a') + b'(c + d) + ab using only AND, OR gates;



b. a circuit for a'bc + a'b'd + a'c using NOR gates only



c. a circuit for ab'c' + a'cd + ab'c + abd using NAND gates only.



5. Simplify the following Boolean expressions (to the simplest sum of products form) using three variable maps.

a.
$$F(A,B,C) = (\overline{A} \overline{C} + \overline{A} BC + \overline{B}C)$$

$$F(A,B,C) = \left(\overline{A} \ \overline{C} + \overline{A} \ BC + \overline{B}C\right)$$

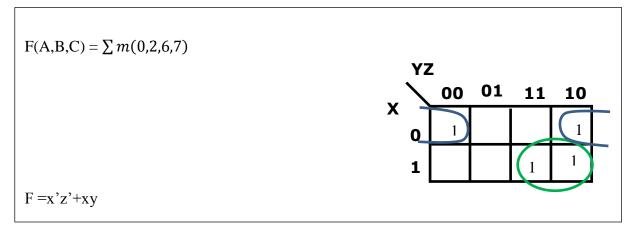
$$bc$$

$$a 00 01 11 10$$

$$1 1 1 1$$

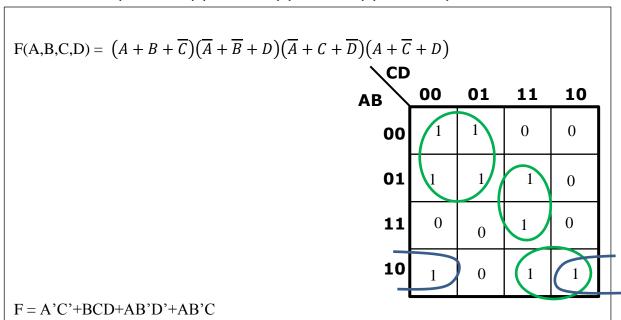
$$F = a + b c$$

b. $F(X,Y,Z) = \sum m(0,2,6,7)$

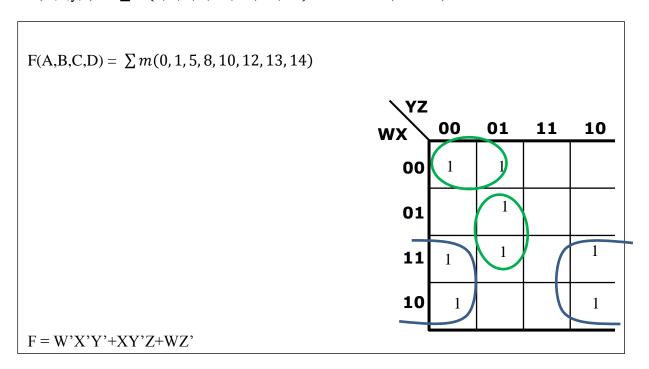


6. Simplify the following Boolean expressions (to the simplest sum of products form) using four variable maps:

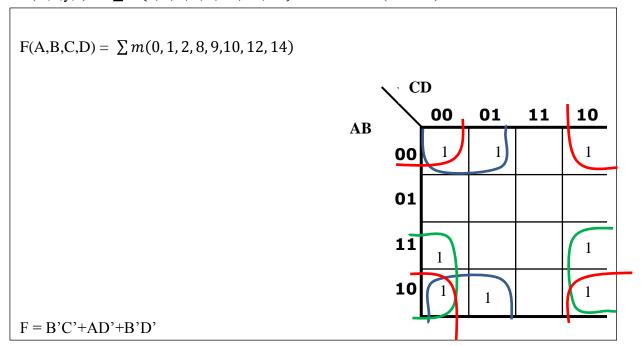
a.
$$\mathrm{F}(\mathrm{A},\mathrm{B},\mathrm{C},\mathrm{D}) = \, \left(A+B+\overline{C}\right) \left(\overline{A}+\overline{B}+D\right) \left(\overline{A}+C+\overline{D}\right) \left(A+\overline{C}+D\right)$$



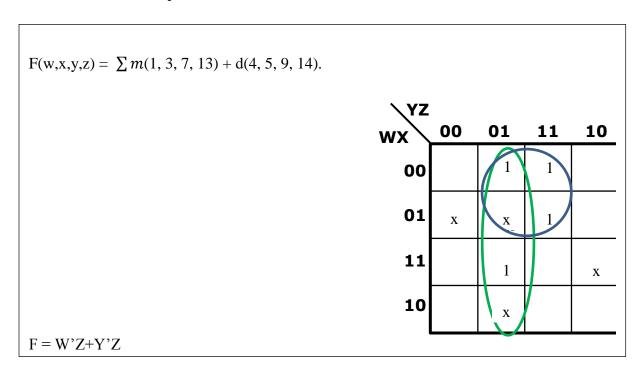
b.
$$F(w,x,y,z) = \sum m(0,1,5,8,10,12,13,14)$$
 (3 terms)



c.
$$F(w,x,y,z) = \sum m(0,1,2,8,9,10,12,14)$$
 (3 terms)

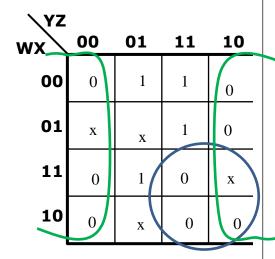


- 7. Given the function $F(w,x,y,z) = \sum m(1, 3, 7, 13) + d(4, 5, 9, 14)$. Find:
 - a. the minimum sum of products form for F



b. the minimum product of sums form for F.

$$F(w,x,y,z) = \sum m(1, 3, 7, 13) + d(4, 5, 9, 14).$$



F' = Z' + WY $\therefore F = Z(W' + Y')$

- 8. A switching network has 3 inputs and 2 outputs. The output variables, a and b, represent the first and second bits, respectively of a binary number, N. N equals the number of inputs which are "1". For example, if w=1, x=0. y=1, then a=1, b=0.
 - a. Find the minterm expansion for a and b.
 - b. Find the maxterm expansion for a and for b.

Express each answer in abbreviated notation (with Σ or π).

W	X	y	a	b
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

a.
$$a = \Sigma m(3, 5, 6, 7)$$
 $b = \Sigma m(1, 2, 4, 7)$

$$b = \sum m(1, 2, 4, 7)$$

b.
$$a = \pi M(0, 1, 2, 4)$$

$$b = \pi M(0, 3, 5, 6)$$