

# Bags

- A bag is like a set, but an element may appear more than once.
  - Multiset is another name for "bag."
- Example:
  - $\{1,2,1,3\}$  is a bag.
  - {1,2,3} is also a bag that happens to be a set.
- Bags also resemble lists, but order in a bag is unimportant.
  - Example:
    - $\{1,2,1\} = \{1,1,2\}$  as bags, but
    - [1,2,1] != [1,1,2] as lists.

### Why bags?

- SQL is actually a bag language.
- SQL will eliminate duplicates, but usually only if you ask it to do so explicitly
  - except for union, intersection, and difference where the default is "set mode".

# **Bag Union**

- Union, intersection, and difference need new definitions for bags.
- An element appears in the union of two bags the sum of the number of times it appears in each bag.
- Example:

```
\{1,2,1\} \cup \{1,1,2,3,1\}
= \{1,1,1,1,1,2,2,3\}
```

### **Bag Intersection**

 An element appears in the intersection of two bags the minimum of the number of times it appears in either.

Example:

```
\{1,2,1\} \cap \{1,2,3\}
= \{1,2\}.
```

### Bag Difference

- An element appears in difference A B of bags as many times as it appears in A, minus the number of times it appears in B.
  - But never less than 0 times.

```
• Example: \{1,2,1\} - \{1,2,3\}
= \{1\}.
```

# Examples of Union, Intersection, Difference in SQL

 Remember, we need to have the same schema for the relations that we union, intersect, or take difference.

```
(SELECT * FROM R)
UNION
(SELECT * FROM S);

(SELECT * FROM R)
INTERSECT
(SELECT * FROM S);

(SELECT * FROM R)
EXCEPT ---MINUS in Oracle
(SELECT * FROM S);
```

- Add "ALL" for bag version of these operators. Only UNION ALL exists in Oracle.
- These are the only operators that work in 'set mode' by default. All the others work in 'bag mode' by default.

### The Extended Algebra

- **1.**  $\delta$ : eliminates duplicates from bags.
- 2.  $\tau$ : sorts tuples.
- **3. Extended projection**: arithmetic, duplication of columns.
- **4.**  $\gamma$ : grouping and aggregation.
- **5. OUTERJOIN**: includes "dangling tuples" = tuples that do not join with anything.

# **Example: Duplicate Elimination**

$$R_1 := \delta(R_2)$$

 R<sub>1</sub> consists of one copy of each tuple that appears in R<sub>2</sub> one or more times.

SELECT **DISTINCT** \* FROM R;

$$\delta(R) = \begin{array}{c|c} A & B \\ 1 & 2 \\ 3 & 4 \end{array}$$

# Sorting

$$\mathsf{R}_1 := \mathsf{\tau}_{\mathsf{L}} \; (\mathsf{R}_2).$$

- -L is a list of some of the attributes of  $R_2$ .
- R<sub>1</sub> is the list of tuples of R<sub>2</sub> sorted first on the value of the first attribute on L, then on the second attribute of L, and so on.
- τ is the only operator whose result is neither a set nor a bag.

Example:

SELECT \*
FROM R
ORDER BY A, B;

# **Example: Extended Projection**

Using the same  $\pi_L$  operator, we allow the list L to contain arbitrary expressions involving attributes, for example:

- 1. Arithmetic on attributes, e.g., A+B.
- 2. Duplicate occurrences of the same attribute.

SELECT A+B AS C, A AS A1, A AS A2 FROM R;

# **Aggregation Operators**

- They apply to entire columns of a table and produce a single result.
- The most important examples:
  - SUM
  - AVG
  - COUNT
  - MIN
  - MAX

# **Example: Aggregation**

$$SUM(A) = 7$$

$$COUNT(A) = 3$$

$$MAX(B) = 4$$

$$MIN(B) = 2$$

$$AVG(B) = 3$$

SELECT SUM(A), COUNT(A), MAX(B), MIN(B), AVG(B) FROM R;

# **Grouping Operator**

$$R_1 := \gamma_L (R_2)$$

- L is a list of elements that are either:
  - 1. Individual (grouping) attributes.
  - 2. AGG(*A*), where AGG is one of the aggregation operators and *A* is an attribute.

# Example: Grouping/Aggregation

$$\gamma_{A,B,AVG(C)}(R) = ??$$

First, group *R*:

<u> </u>		
Α	В	C
1	2	3
1	2	5
4	5	6

Then, average *C* within groups:

Α	В	AVG(C)
1	2	4
4	5	6

SELECT A,B,AVG(C) FROM R GROUP BY A,B;

# $\gamma_L(R)$ - Formally

- Group R according to all the grouping attributes on list L.
  - That is, form one group for each distinct list of values for those attributes in R.
- Within each group, compute AGG(A) for each aggregation on list L.
- Result has grouping attributes and aggregations as attributes.
- One tuple for each list of values for the grouping attributes and their group's aggregations.

# Example: Grouping/Aggregation

#### StarsIn(title, year, starName)

- For each star who has appeared in at least three movies give the earliest year in which he or she appeared.
  - First we group, using starName as a grouping attribute.
  - Then, we compute the MIN(year) for each group.
  - Also, we need to compute the COUNT(title) aggregate for each group, for filtering out those stars with less than three movies.
- $\pi_{\text{starName,minYear}}(\sigma_{\text{ctTitle}\geq 3}(\gamma_{\text{starName,MIN(year)}\rightarrow \text{minYear,COUNT(title)}\rightarrow \text{ctTitle}}(\text{StarsIn})))$

# Example: Grouping/Aggregation

```
SELECT starName, miny
FROM (SELECT starname, COUNT(title) AS cnt, MIN(year) AS miny
       FROM StarsIn
       GROUP BY starname)
WHERE cnt>=3:
Or (more concisely):
SELECT starname, MIN(year) AS miny
FROM StarsIn
GROUP BY starname
HAVING COUNT(title)>=3;
```

#### **Problems**

Product(maker, model, type)

**PC**(model, speed, ram, hd, rd, price)

Laptop(model, speed, ram, hd, screen, price)

Printer(model, color, type, price)

Find the manufacturers who sell exactly three different models of PC.

Find those manufacturers of at least two different computers (PC or Laptops) with speed of at least 700.

### Outerjoin

#### **Motivation**

- Suppose we join  $R \bowtie S$ .
- A tuple of R which doesn't join with any tuple of S is said to be dangling.
  - Similarly for a tuple of S.
  - Problem: We loose dangling tuples.

#### **Outerjoin**

 Preserves dangling tuples by padding them with a special NULL symbol in the result.

# **Example: Outerjoin**

$$S = \begin{bmatrix} B & C \\ 2 & 3 \\ 6 & 7 \end{bmatrix}$$

(1,2) joins with (2,3), but the other two tuples are dangling.

Α	В	С
1	2	3
4	5	NULL
NULL	6	7

SELECT \*
FROM R FULL OUTER JOIN S USING(B);

#### **Problems**

- $R(A,B) = \{(0,1), (2,3), (0,1), (2,4), (3,4)\}$
- $S(B,C) = \{(0,1), (2,4), (2,5), (3,4), (0,2), (3,4)\}$
- $\gamma_{A,SUM(B)}(R)$
- R № S
- R \(\sigma\_L\)S -- This left outerjoin: Only pad dangling tuples from the left table.
- R R S -- -- This right outerjoin: Only pad dangling tuples from the right table.