## **CENG 455 – Homework 1** (Solutions)

(Deadline: Wednesday 25th Jan 2019)

1- [5 points] Calculate and report the *Release time and Relative deadline* as well as your *Response time, Execution time, Completion time* and *Slack time* for this homework. [A sample solution]

Release time: Wed 18<sup>th</sup> 8:30am Relative Deadline: 7 Days
Completion time: Friday 20<sup>th</sup> 8:30pm Execution time: 1 hour
Response time: 2.5 Days Slack time: 4.5 days

2- [10 points] Name three different types of redundancies and provide an example for each.

[Three out of the following four]

- Hardware redundancy: Triple Modular Redundancy (TMR), Duplication with Comparison (DwC), etc.
- Software redundancy: n-Version Programming (nVP)
- Information redundancy: Parity bits, Cyclic Redundancy Check (CRC)
- Time redundancy: Sending multiple packets over the network, Multiple execution of the same function
- 3- [15 points] A hard real-time system comprises two independent tasks:
  - Task A with Period of 100ms and Execution time of 40ms
  - Task B with Period of 150ms and Execution time of 30ms

(Provide your full solution as well as the final answer)

a. [5] In a time period of **3 Seconds**, how much **idle time** is available to the system?

The hyper-period is the least common multiple of all periods. i.e. Hyper-period = LCM(100,150) = 300ms

In the 300ms interval, task A runs three times (resulting in 3\*40=120ms total execution time for task A), while task B runs twice (resulting in 2\*30=60ms execution time for task B). Therefore, the total execution time for all tasks is 180ms, resulting in 300-180=120ms of idle time in a 300ms interval.

Total idle time in 3 seconds = 10\*120ms = 1.2 seconds

b. [10] Assuming we add another task (i.e. Task C) with **50ms** period, what is the maximum allowed execution time for Task C in order to have feasible scheduling (i.e. all tasks meet their deadlines)?

As the period for task C is 50ms, it executes 6 times in the 300ms interval. The idle time available in the 300ms interval is 120 ms, therefore the maximum allowed execution time for each instance of Task C is 120/6=20ms.

[Additionally, assuming Earliest-Deadline-First scheduling policy with no pre-emption, the following is the Gantt chart after the addition of task C] (not required)

\[
\begin{bmatrix} C & A & C & B & C & A & C \\
0 & 20 & 60 & 80 & 110 & 130 & 170 & 190 & 220 & 240 & 280 & 300 \end{bmatrix}
\]

- 4- [20 points] In a RT System, the tasks become ready in the following order. Assuming Priority-based scheduling (where lower numbers mean higher priority levels with **0** being the highest priority task), Draw the scheduling Gantt chart for this example.
  - Time 0: **Task A** (Priority: 1, Execution time: 30)

Task B (Priority: 2, Execution time: 20)

- Time 40: Task C (Priority: 1, Execution time: 20)
- Time 100: **Task D** (Priority: 0, Execution time: 40)
- Time 120: Task E (Priority: 0, Execution time: 50)
- Time 130: Task B (Priority: 2, Execution time: 30)

Assumption: Scheduling using MQX policies (i.e. no pre-emption for same priority tasks becoming ready + pre-empted tasks stay at the front of the ready queue) - (other solutions accepted as long as needed assumptions are made clear)

