

Probability

Q1. A bag contains 25 cards, numbered through 1 to 25. A card is drawn at random. What is the probability that the number on the card drawn is:

- (a) multiple of 5
- (b) a perfect square
- (c) a prime number? [2023]

Solution: (a) $1/5$ (b) $1/5$ (c) $9/25$

Step-by-step Explanation:

Let S be the sample space i.e bag contains cards numbered from 1 to 25.

$$n(S) = 25 .$$

(a) A event of getting the number on this card multiple of 5 is

$$n(A) = \{ 5, 10, 15, 20, 25 \} = 5$$

$$P(A) = 5/25 = 1/5$$

(b) Number of perfect squares between 1 to 25 = 5. The perfect squares are 1, 4, 9, 16, 25.

$$\text{Hence } P(\text{a perfect square}) = 5/25 = 1/5$$

(c) number of prime number between 1 to 25 = 9 (2, 3, 5, 7, 11, 13, 17, 19, 23)

$$\text{Hence } P(\text{a prime number}) = 9/25$$

Q2. A letter is chosen at random from all the letters of the English alphabets. The probability that the letter chosen is a vowel, is:

- (a) $4/26$
- (b) $5/26$
- (c) $21/26$
- (d) $5/24$ [2023]

Solution: (b) $5/26$

Step-by-step Explanation: Total number of English Alphabets are 26, namely, A,B,C,D,E,F,G,H,I,J,K,L,M,N,O,P,Q,R,S,T,U,V,W,X,Y,Z.

Let S be the sample space i.e. $n(S) = 26$

Vowels in English alphabets are 5- A, E, I, O, U.

Hence, $P(\text{a vowel}) = 5/26$ (Option b)

Q3. A letter of the word 'SECONDARY' is selected at random. What is the probability that the letter selected is not a vowel? [2022 Semester-2]

Solution: $2/3$

Step-by-step Explanation: Number of letters in the word SECONDARY = 9.

Let S be the sample space. Hence, $n(S) = 9$.

letters which are not vowel are S, C, N, D, R, Y = 6

Hence, $P(\text{not a vowel}) = 6/9 = 2/3$

Q4. The bag contains 5 white, 2 red and 3 black balls. A ball is drawn at random. What is the probability that the ball drawn is a red ball? [2022 Semester-2]

Solution: $1/5$

Step-by-step Explanation: Total number of balls in the bag = $5 + 2 + 3 = 10$

Let S be the sample space. Hence, $n(S) = 10$

Number of red balls = 2.

Hence, $P(\text{a red ball}) = 2/10 = 1/5$

Q5. The Probability of getting a number divisible by 3 in throwing a dice is:

- (a) $1/6$
- (b) $1/3$
- (c) $1/2$
- (d) $2/3$ [2022 Semester-2]

Solution: (b) $1/3$

Step-by-step Explanation: The numbers in a dice are 1, 2, 3, 4, 5, 6 = 6.

Let S be the sample space. Hence, $n(S) = 6$.

Numbers divisible by 3 in a dice are = 3 and 6 = 2

Hence $P(\text{getting a number divisible by 3}) = 2/6 = 1/3$

Hence option (b) is correct.

Q6. Each of the letters of the word 'AUTHORIZES' is written on identical circular discs and put in a bag. They are well shuffled. If a disc is drawn at random from the bag, what is the probability that the letter is: [2020]

- (i) a vowel
- (ii) one of the first 9 letters of the English alphabet which appears

in the given word.

(iii) one of the last 9 letters of the English alphabet which appears in the given word.

Solution: (i) $1/2$ (ii) $2/5$ (iii) $1/2$

Step-by-step Explanation:

Number of letters in the word 'AUTHORIZES' is 10.

Let S be the sample space. Hence $n(S) = 10$.

(i) Vowels in the word AUTHORIZES = A, U, O, I, E = 5

Hence $P(\text{a vowel}) = 5/10 = 1/2$

(ii) One of the first 9 letters of the English alphabet which appears in the word AUTHORIZES are = A, H, I, E = 4

Hence $P(\text{one of the first 9 letters of the English alphabet which appears in the word}) = 4/10 = 2/5$

(iii) One of the last 9 letters of the English alphabet which appears in the word AUTHORIZES are = U, T, R, Z, S = 5

Hence, $P(\text{One of the last 9 letters of the English alphabet which appears in the word}) = 5/10 = 1/2$

Q7. There are 25 discs numbered 1 to 25. They are put in a closed box and shaken thoroughly. A disc is drawn at random from the box. Find the probability that the number on the disc is: [3]

(i) an odd number

(ii) divisible by 2 and 3 both

(iii) a number less than 16. [2019]

Solution: (i) $13/25$ (ii) $4/25$ (iii) $3/5$

Step-by-step Explanation: There are 25 discs numbered 1 to 25.
Let S be the sample space.

Hence, $n(S) = 25$.

(i) odd numbers = 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25 = 13

Hence, $P(\text{odd number}) = 13/25$.

(ii) Numbers divisible by 2 and 3 both are = 6, 12, 18, 24 = 4

Hence, $P(\text{Number divisible by 2 and 3 both}) = 4/25$.

(iii) Numbers less than 16 are 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15 = 15

Hence, $P(\text{Number less than 16}) = 15/25 = 3/5$.

Q8. Cards bearing numbers 2, 4, 6, 8, 10, 12, 14, 16, 18 and 20 are kept in a bag. A card is drawn at random from the bag. Find the probability of getting a card which is :

(i) a prime number.

(ii) a number divisible by 4.

(iii) a number that is a multiple of 6.

(iv) an odd number [4] [2018]

Solution: (i) $1/10$ (ii) $1/2$ (iii) $3/10$ (iv) 0

Step-by-step Explanation: Total number of cards bearing numbers 2, 4, 6, 8, 10, 12, 14, 16, 18 and 20 = 10.

Let S be the sample space. Hence $n(S) = 10$.

(i) Prime numbers in the cards is only number 2. Hence total number of cards having prime number = 1

Hence, $P(\text{a prime number}) = 1/10$

(ii) numbers divisible by 4 in cards are 4, 8, 12, 16, 20 = 5.

Hence, $P(\text{number divisible by 4}) = 5/10 = 1/2$.

(iii) numbers multiple of 6 in the cards are 6, 12, 18 = 3

Hence, $P(\text{a number that is a multiple of 6}) = 3/10$.

(iv) odd numbers in the cards are 0.

Hence, $P(\text{an odd number}) = 0/10 = 0$.

Q9. Sixteen cards are labelled as a, b, c ... m, n, o, p. They are put in a box and shuffled. A boy is asked to draw a card from the box. What is the probability that the card drawn is : [3]

(i) a vowel

(ii) a consonant

(iii) none of the letters of the word median [3] [2017]

Solution: (i) $1/4$ (ii) $3/4$ (iii) $5/8$

Step-by-step Explanation: Sixteen cards are labelled as a, b, c ... m, n, o, p.

Let S be the sample space. Hence $n(S) = 16$.

(i) Vowels in the cards are a, e, i, o = 4

Hence, $P(\text{a vowel}) = 4/16 = 1/4$.

(ii) consonants in the cards are b, c, d, f, g, h, j, k, l, m, n, p = 12

Hence, $P(\text{a consonant}) = 12/16 = 3/4$.

(iii) none of the letters of the word 'median' in the cards are b, c, f, g, h, j, k, l, o, p = 10.

Hence, $P(\text{none of the letters of the word median}) = 10/16 = 5/8$.

Q10. A game of number has cards marked with 11, 12, 13, 40. A card is drawn at random. Find the Probability that the number on the card drawn is:

- (i) A perfect square
- (ii) Divisible by 7. [3] [2016]

Solution: (i) 0 (ii) 0

Step-by-step Explanation: A game of number has cards marked with 11, 12, 13, 40.

Let S be the sample space. Hence, $n(S) = 4$

(i) Perfect squares in the numbers 11, 12, 13 40 are = 0.

Hence $P(\text{a perfect square}) = 0/4 = 0$.

(ii) Numbers divisible by 7 in the numbers 11, 12, 13 40 are = 0.

Hence $P(\text{divisible by 7}) = 0/4 = 0$.

Q11. A bag contains 5 white balls, 6 red balls and 9 green balls. A ball is drawn at random from the bag. Find the probability that the ball drawn is:

- (i) a green ball.
- (ii) a white or a red ball
- (iii) is neither a green ball nor a white ball. [2015]

Solution: (i) $9/20$ (ii) $11/20$ (iii) $3/10$

Step-by-step Explanation: Let S be the sample space. Total number of balls in the bag = $5 + 6 + 9 = 20$.

Hence, $n(S) = 20$

(i) Number of green balls = 9.

Hence, $P(\text{a green ball}) = 9/20$.

(ii) Number of white and red balls = $5 + 6 = 11$.

Hence, $P(\text{a white or a red ball}) = 11/20$.

(iii) Neither green ball or white balls mean red balls. Number of red balls = 6.

Hence, $P(\text{neither a green ball nor a white ball}) = 6/20 = 3/10$.

Q12. A die has 6 faces marked by the given numbers shown below:



The die is thrown once. What is the probability of getting

(i) a positive integer.

(ii) an integer greater than -3.

(iii) the smallest integer. [2014]

Solution: (i) $1/2$ (ii) $5/6$ (iii) $1/6$

Step-by-step Explanation: Numbers in a die are 6 (1, 2, 3, -1, -2, -3).

Let S be the sample space. Therefore, $n(S) = 6$.

(i) Number of positive integers in the die is 3 (1, 2, 3).

Hence, $P(\text{a positive integer}) = 3/6 = 1/2$.

(ii) Number of integers in a die which are greater than -3 is 5 (1, 2, 3, -1, -2).

Hence, $P(\text{an integer greater than } -3) = 5/6$.

(iii) the smallest integer is -3.

Hence $P(\text{smallest integer}) = 1/6$.

Q13. A box contains some black balls and 30 white balls. If the probability of drawing a black ball is two-fifths of a white ball, find the number of black balls in the box. [3] [2013]

Solution: 12

Step-by-step Explanation: Let the number of Black balls be x .
Therefore, total number of balls = $x + 30$.

Let S be the sample space. Hence, $n(S) = x + 30$.

Number of white balls = 30.

Hence, $P(\text{a white ball}) = 30 / (x+30)$

Number of black balls = x .

Hence, $P(\text{a black ball}) = x / (x+30)$

Given,

$$\begin{aligned}\frac{x}{x+30} &= \frac{2}{5} \times \frac{30}{x+30} \\ \Rightarrow x &= \frac{2 \times 30}{5} \\ \Rightarrow x &= 12\end{aligned}$$

Hence, number of black balls is 12.

Q14. Two coins are tossed once. Find the probability of getting:

(i) 2 heads

(ii) At least 1 tail. [2012]

Solution: (i) $\frac{1}{4}$ (ii) $\frac{3}{4}$

Step-by-step Explanation:

Two coins are tossed. The sample set S will be $\{HH, HT, TH, TT\}$.

Hence, $n(S) = 4$

(i) Let A be the event of getting two heads. Then event A will contain the outcome $\{HH\} = 1$

Hence, $P(A) = \frac{1}{4}$.

(ii) Let B be the event of getting at least 1 tail. Then, B will contain the outcomes $\{HT, TH, TT\} = 3$

$P(B) = \frac{3}{4}$.

Q15. From a pack of 52 playing cards all cards whose numbers are multiples of 3 are removed. A card is now drawn at random. What is the probability that the card drawn is:

(i) a face card (King, Jack or Queen)

(ii) an even-numbered red card? [3] [2011]

Solution: (i) $\frac{3}{10}$ (ii) $\frac{1}{4}$

Step-by-step Explanation: From a pack of 52 playing cards all cards whose numbers are multiples of 3 are removed.

So, 3, 6, 9 are removed from each set. Hence total cards removed $= 3 \times 4 = 12$.

Total number of cards left $= 52 - 12 = 40$.

Let S be the sample space. Hence, $n(S) = 40$.

(i) Total face cards = 4 kings, 4 queens and 4 Jacks = 12

Hence, $P(\text{a face card}) = 12/40 = 3/10$.

(ii) even-numbered red cards (i.e from Hearts and diamonds) =
 $2(2, 4, 6, 8, 10) = 2(5) = 2 \times 5 = 10$.

Hence, $P(\text{an even-numbered red card}) = 10/40 = 1/4$.

Q16. Cards marked with numbers 1, 2, 3, 4 ... 20 are well shuffled and a card is drawn at random. What is the probability that the number of the cards is

(i) a prime number

(ii) divisible by 3

(iii) a perfect square? [3] [2010]

Solution: (i) $2/5$ (ii) $3/10$ (iii) $1/5$

Step-by-step Explanation: Cards are marked with numbers 1, 2, 3, 4 ... 20. Therefore, total number of cards = 20.

Let S be the sample space. Hence, $n(S) = 20$.

(i) Prime numbers are 2, 3, 5, 7, 11, 13, 17, 19 = 8.

Hence, $P(\text{a prime number}) = 8/20 = 2/5$.

(ii) numbers divisible by 3 are 3, 6, 9, 12, 15, 18 = 6.

Hence, $P(\text{divisible by 3}) = 6/20 = 3/10$.

(iii) Perfect squares are 1, 4, 9, 16 = 4.

Hence, $P(\text{a perfect square}) = 4/20 = 1/5$.