# thornado-Hydro (xCFC)

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#### thornado

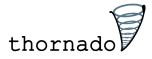
https://github.com/endeve/thornado



My Website

https://www.samueljdunham.com





### toolkit for high-order neutrino-radiation hydrodynamics

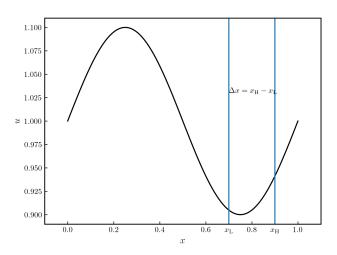
- DG
- SSPRK/IMEX
- GR (xCFC)
- Hydro<sup>a</sup> (Valencia)
- Neutrino transport<sup>b</sup> (M1)
- Interfaces to tabulated EoS/Opacities (weaklib: https://github.com/ starkiller-astro/weaklib)

- GPUs via OpenACC or OpenMP pragmas
- MPI parallelism and AMR via AMReX: https://github. com/AMReX-Codes/amrex

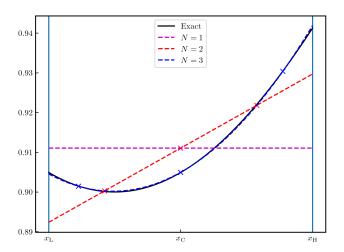
Fluid self-gravity via Poseidon: https://github.com/ jrober50/Poseidon

<sup>&</sup>lt;sup>a</sup>Endeve et al. (2019); Dunham et al. (2020); Pochik et al. (2021) <sup>b</sup>Laiu et al. (2021)

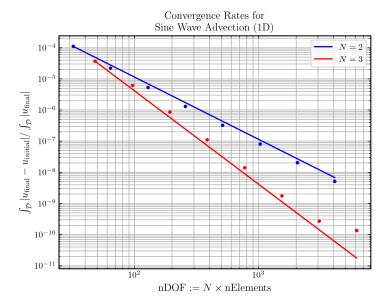
$$u\left(x\right) = 1 + 0.1\sin\left(2\pi x\right)$$



$$u_{h}\left(x,t\right):=\sum_{i=1}^{N}u_{i}\left(t\right)\,\ell_{i}\left(x\right)$$

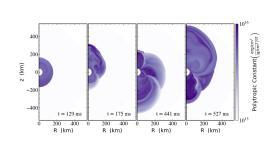


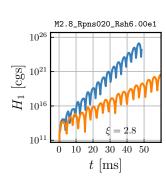
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# Standing Accretion Shock Instability

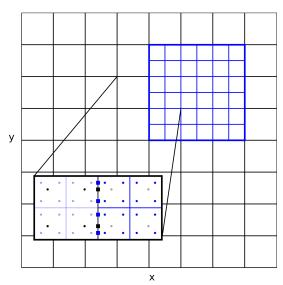
Used thornado to investigate the role of GR on the SASI<sup>1</sup>





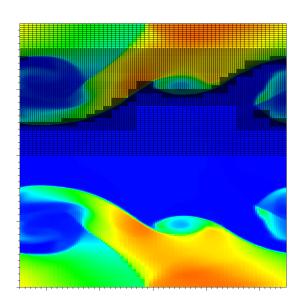
<sup>&</sup>lt;sup>1</sup>Dunham et al. (2020, 2023)

# Mesh Refinement

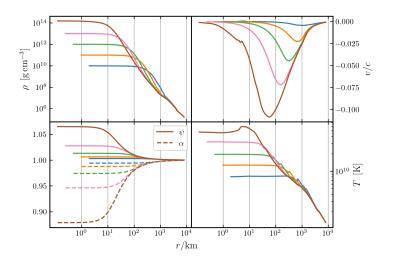


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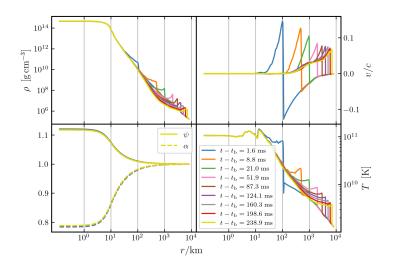
# Kelvin–Helmholtz Instability



# Adiabatic Collapse (AMR, Collapse Phase)



# Adiabatic Collapse (AMR, Post-Bounce Phase)



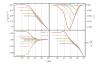
## Bibliography

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# Summary

### Can run pure hydro problems in GR with AMR



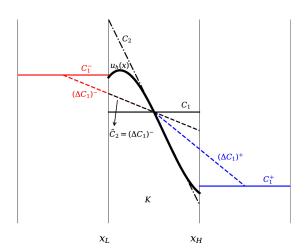


Can run hydro+self-gravity problems in GR with  $\ensuremath{\mathsf{AMR}}$ 

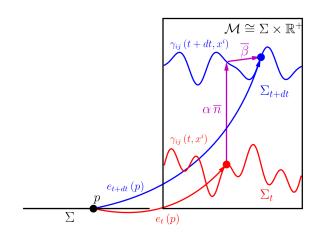
Working on coupling GR transport to existing hydro+gravity modules  $\ensuremath{\mathsf{GR}}$ 



$$u_h(x,t) = \sum_{n=1}^{N} C_n(t) P_n(x) \implies \tilde{u}_h(x,t) = C_1(t) P_1(x) + \tilde{C}_2(t) P_2(x)$$



# 3+1 Decomposition



$$ds^{2} = g_{\mu\nu} dx^{\mu} dx^{\nu} = -\alpha^{2} dt^{2} + \gamma_{ij} \left( dx^{i} + \beta^{i} dt \right) \left( dx^{j} + \beta^{j} dt \right)$$

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# Conformally-Flat Condition

Developed by Wilson et al. (1996), extended by Cordero-Carrión et al. (2009)

$$\gamma_{ij}(x) = \psi^{4}(x) \,\overline{\gamma}_{ij}(x^{i})$$

$$K = 0, \,\partial_{t}K = 0$$
(Always and everywhere)

- Exact in spherical symmetry!
- Hyperbolic → Elliptic equations
- Good for long-time simulations

Special case: Schwarzchild spacetime in isotropic coordinates (G=c=1)

$$\alpha = \left(1 + \frac{1}{2}\Phi\right)\left(1 - \frac{1}{2}\Phi\right)^{-1}$$

$$\psi = 1 - \frac{1}{2}\Phi$$

$$\beta^{i} = 0,$$

with

$$\Phi\left(r\right) := -\frac{M}{r}$$